

CONTROL OF AN ASYMMETRICAL OMNI DIRECTIONAL MOBILE ROBOT

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Keywords: Holonomic Omnidirectional mobile robot; Asymmetrical Structure.

Abstract: This paper describes how to control an asymmetric wheeled mobile robot with omnidirectional wheels, considering the sample of a robot with three wheels. When flexible motion capabilities are required this robot must be designed to meet the related requirements, namely fast and agile motions as well as robust navigation. This paper provides an overview for the design of kinematics and dynamics of the robot, as well as the motion and velocities equations. In addition to the above, a control method to obtain a proper control model is explained. Simulation example is presented to demonstrate the ability of this control method. The implementation and test of the controller on the real robot gives the results compatible with the simulation. It was learned that the discontinuities between omnidirectional wheels' rollers play an important role in decreasing the accuracy of motion.

1 INTRODUCTION

Omnidirectional vehicles provide superior maneuvering capability compared to the more common car-like vehicles. The ability to move along any direction, irrespective of the orientation of the vehicle, makes it an attractive option in dynamic environments. The annual RoboCup competition, where teams of fully autonomous robots engage in soccer matches, is an example of where omnidirectional vehicles have been used in computationally intensive dynamic environments (Kalmár-Nagy et al., 2004) (Veloso et al., 1999) (Kitano et al., 1998).

Among omnidirectional mobile robots, the one with three or more wheels is more powerful. A holonomic system is one in which the number of degrees of freedom (DOF) is equal to the number of coordinates needed to specify the configuration of the system. In the field of mobile robots, the term holonomic mobile robot is applied to the abstraction called the robot, or base, without regard to the rigid bodies which make up the actual mechanism. Thus, any mobile robot with three degrees of freedom of motion in the plane has become known as a holonomic mobile robot (Holmberg et al., 1999). Many different control mechanisms have been

created to achieve holonomic motion (Jung et al., 1999) (Moore et al., 1999). In addition, these systems have symmetric mechanisms. The symmetric mobile robots with 3 DOF mostly have 120-degree angles between the wheels and the full structure includes 3 actuators as well as 3 wheels (Kalmár-Nagy et al., 2004). The control procedure of such robots has been the subject of discussion in several research papers. However in small robots (18 cm diameter of base) there is not enough space to accommodate other components and the change in angles between the wheels would partially overcome this problem. The angle between front wheels is 140° and the two other angles are 110°, which causes asymmetric problem in robot and its control system. The objective of this paper is to establish a real time control strategy that could move the asymmetrical robot to a given location with zero final velocity as quickly as possible based on measurement of the vehicle position and orientation.

The paper is ordered in such a way to describe the Persia Robot system followed by the kinematics and dynamic model of asymmetric omnidirectional robot vehicle. Then Simulations and PD control method are presented. The paper ends with the concluding remarks.

2 ROBOPERSIA SYSTEM OVERVIEW

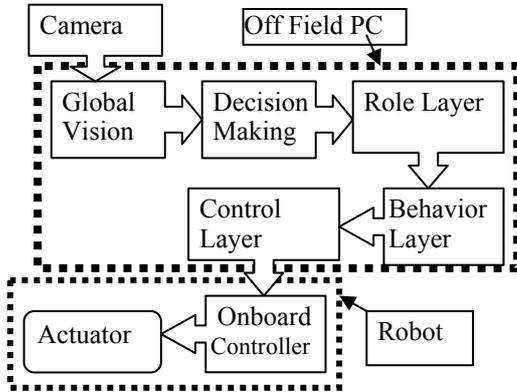


Figure 1: Complete RoboPersia System

The complete RoboPersia system is a layered set of subsystems which is shown in Figure 1. Figure 2 shows a photograph of the RoboPersia. An overhead camera captures global images of the field. The vision software processes the images to identify the location and the velocity of robots and the ball. This state of the field is passed to the Decision-Making System (DMS). DMS is the highest level planner in the system, responsible for distributing the overall goal of the team amongst the individual robots. DMS is responsible for the multi-robot coordination and cooperation by selecting a role for each robot. Some example roles include ATTACK and DEFEND. The DMS roles and role parameters with the field state are sent to the Role Layer which is responsible for executing roles by selecting behaviour for each robot. Some example behaviours include KICK and MOVE. Behaviours and behaviour parameters with the field state are passed to Behaviour Layer. The Behaviour Layer attempts to execute the desired behaviour by dedicating the proper motion while avoiding obstacles. This layer determines the immediate desired heading and distance for the control layer. The Control Layer, based on PD controller, controls the position and head of the robots by changing the actuators duty cycles. The feedback comes from the state of the field.

2.1 Optimizing the Omni Directional Wheel

The holonomic and non-holonomic omnidirectional mobile robot has been studied by using a variety of mechanism. Several omnidirectional platforms have



Figure 2: RoboPersia

been known to be realized by developing a specialized wheel or mobile mechanisms (Holmberg et al., 1999). These include various arrangements of universal or omni wheels (La 1979; Carlisle 1983), double universal wheels (Bradbury 1977), Swedish or Mecanum wheels (Ilon 1971), chains of spherical wheels (West and Asada 1992) or cylindrical wheels (Hirose and Amano 1993), orthogonal wheels (Killough and Pin 1992), ball wheels (West and Asada 1994) and omni directional poly roller wheel (Asama, 1995, Watanaba, 1998). All of these mechanisms, except for some types with ball wheels, have discontinuous wheel contact points which are a great source of vibration; primarily because of the changing support provided; and often additionally because of the discontinuous changes in wheel velocity needed to maintain smooth base motion (Watanabe, 1998) (Williams et al., 2002) (Pin et al., 1994) (Diegel et al., 2002). In order to decrease the vibration of the platform, the number of little rollers was increased from 12 per wheel, which was used in the previous design to 22 with the constant diameter (Fig. 3). The run-out is decreased nearly 0.08-0.1mm. It's where the previous run out was 1mm. An equation was derived for determining the run out, namely to find how much a given wheel design will bounce up and down as it rotates (run-out). The derivation is relatively straightforward procedure by using trigonometry, and the resulting formula is shown below in which n is the number of the rollers and R is radius of the wheel (Fig. 4).

$$Run-out_{Max} = \overline{OC} - \overline{OD} = R(1 - \cos \phi) \quad (1)$$

$$\angle \phi = \angle BOC - \angle BOM \quad (2)$$

$$\angle BOC = \frac{1}{2} * (2\pi/n) \quad (3)$$

$$R * \angle BOM = 2 \Rightarrow \angle BOM = \frac{2}{R} \quad (4)$$

$$\therefore \angle \phi = \left(\frac{\pi}{n} - \frac{2}{R} \right) \quad (5)$$

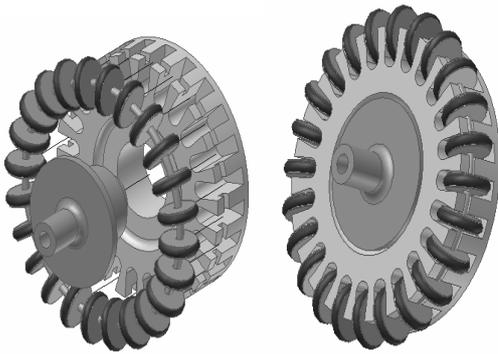


Figure 3: The explosive view of new omnidirectional wheel and Omnidirectional Wheel

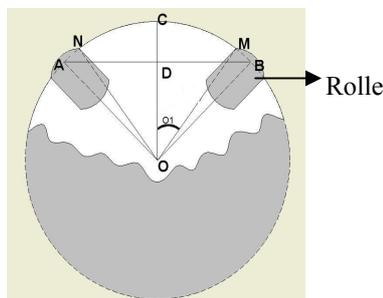


Figure 4: Schematic of Omnidirectional.

3 ROBOT KINEMATIC

Omnidirectional robots usually use special wheels, which were described in the preceding section. The body of each wheel is connected to the preceding section. Therefore, a robot with three omnidirectional wheels can equilibrate on plane easily and follow any trajectory. Our robot structure includes three special omnidirectional wheels for the motion system as shown in Fig.3.

3.1 Kinematics Modeling

Using omnidirectional wheels, the schematic view of robot kinematics can be shown in Fig. 5 (Kalmar-Nagy, T., 1998), where O is the robot center of mass, P_o is defined as the vector connecting O to the origin and D is the drive direction vector of each wheel and θ is the angle of counter clockwise rotation. Unitary rotation matrix, $[R(\theta)]$ is defined as:

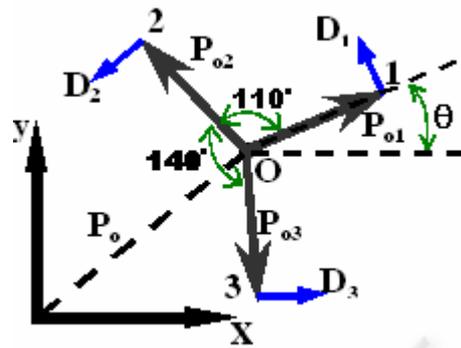


Figure 5: Omnidirectional Robot Model, Top View.

$$[R(\theta)] = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \quad (6)$$

The position vectors $\{P_{o1}\}, \dots, \{P_{o3}\}$ with respect to the local coordinates centered at the robot center of mass are given as:

$$P_{o1} = L \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad (7)$$

$$\angle P_{o1}, P_{o2} = 110^\circ$$

$$P_{o2} = R\left(\frac{11\pi}{18}\right)P_{o1} = L \begin{bmatrix} \cos\left(\frac{11\pi}{18}\right) \\ \sin\left(\frac{11\pi}{18}\right) \end{bmatrix} \quad (8)$$

$$\angle P_{o1}, P_{o3} = -110^\circ$$

$$P_{o3} = R\left(\frac{-11\pi}{18}\right)P_{o1} = L \begin{bmatrix} \cos\left(\frac{11\pi}{18}\right) \\ -\sin\left(\frac{11\pi}{18}\right) \end{bmatrix} \quad (9)$$

Where, L is the distance of wheels from the robot center of mass (O).

$$D_i = \frac{1}{L} R\left(\frac{\pi}{2}\right) P_{oi} \quad (10)$$

$$D_1 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, D_2 = \begin{bmatrix} -\sin\left(\frac{11\pi}{18}\right) \\ \cos\left(\frac{11\pi}{18}\right) \end{bmatrix}, D_3 = \begin{bmatrix} \sin\left(\frac{11\pi}{18}\right) \\ \cos\left(\frac{11\pi}{18}\right) \end{bmatrix} \quad (11)$$

3.2 Equation of motion and velocities

Using the above notations, the wheel position and velocity vectors can be expressed using rotation matrix $[\mathbf{R}(\theta)]$ as:

$$\mathbf{r}_i = \mathbf{P}_0 + \mathbf{R}(\theta)\mathbf{P}_{oi} \quad (12)$$

$$\mathbf{v}_i = \dot{\mathbf{P}}_0 + \dot{\mathbf{R}}(\theta)\mathbf{P}_{oi} \quad (13)$$

The vector $\mathbf{P}_0 = (x \ y)^T$ is the position of the center of mass with respect to Cartesian coordinates. The individual wheel velocities are

$$\mathbf{v}_i = [\mathbf{v}_i^T (\mathbf{R}(\theta)\mathbf{D}_i)] \quad (14)$$

Substituting equation (13) into equation (14) results in:

$$\mathbf{v}_i = \dot{\mathbf{P}}_0^T \mathbf{R}(\theta)\mathbf{D}_i + \mathbf{P}_{oi}^T \dot{\mathbf{R}}(\theta)\mathbf{R}(\theta)\mathbf{D}_i \quad (15)$$

Note that the second term in the right hand side is the tangential velocity of the wheel. This tangential velocity could be also written as:

$$L\dot{\theta} = \mathbf{P}_{oi}^T \dot{\mathbf{R}}(\theta)\mathbf{R}(\theta)\mathbf{D}_i \quad (16)$$

From the kinematics model of the robot, it is clear that the wheel velocity is a function of linear and angular velocities of robot center of mass, i.e.:

$$\begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix} = \begin{pmatrix} -\sin\theta & \cos\theta & L \\ -\sin(\frac{7\pi}{18}-\theta) & -\cos(\frac{7\pi}{18}-\theta) & L \\ \sin(\frac{7\pi}{18}+\theta) & -\cos(\frac{7\pi}{18}+\theta) & L \end{pmatrix} \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} \quad (17)$$

4 DYNAMIC EQUATIONS

Linear and angular momentum balance can be written as;

$$\sum_{i=1}^3 f_i \mathbf{R}(\theta)\mathbf{D}_i = m \ddot{\mathbf{P}}_0 \quad (18)$$

$$L \sum_{i=1}^3 f_i = J \ddot{\theta} \quad (19)$$

Where f_i is the magnitude of the force produced by the i th motor, m is the mass of the robot and J is its moment of inertia.

$$f = \alpha U - \beta v \quad (20)$$

Where f is the magnitude of the force generated by a wheel attached to the motor, and v (m/s) is the velocity of the wheel. The constants α (N/V) and β (kg/s) can readily be determined from experiment or from motor catalogue.

Substituting equation (20) into equation (18) and (19) yields:

$$\sum_{i=1}^3 (\alpha U_i - \beta v_i) \mathbf{R}(\theta)\mathbf{D}_i = m \ddot{\mathbf{P}}_0 \quad (21)$$

$$L \sum_{i=1}^3 (\alpha U_i - \beta v_i) = J \ddot{\theta} \quad (22)$$

This system of differential equations can be written in the following form (Kalmár-Nagy et al., 2004):

$$\begin{pmatrix} m \ddot{x} \\ m \ddot{y} \\ J \ddot{\theta} \end{pmatrix} = \hat{\mathbf{P}}(\theta) \mathbf{U}(t) - \frac{3\beta}{2} \begin{pmatrix} \dot{x} \\ \dot{y} \\ 2L^2 \dot{\theta} \end{pmatrix} \quad (23)$$

With

$$\hat{\mathbf{P}}(\theta) = \begin{pmatrix} -\sin\theta & \cos\theta & L \\ -\sin(\frac{7\pi}{18}-\theta) & -\cos(\frac{7\pi}{18}-\theta) & L \\ \sin(\frac{7\pi}{18}+\theta) & -\cos(\frac{7\pi}{18}+\theta) & L \end{pmatrix}^T \quad (24)$$

And

$$\mathbf{U}(t) = \begin{pmatrix} U_1(t) \\ U_2(t) \\ U_3(t) \end{pmatrix} \quad (25)$$

So that the non-dimensional equations of motion become (Kalmár-Nagy et al., 2004):

$$\begin{pmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{\theta} \end{pmatrix} + \begin{pmatrix} \dot{x} \\ \dot{y} \\ \frac{2mL^2 \dot{\theta}}{J} \end{pmatrix} = \mathbf{q}(\theta, t) \quad (26)$$

Where $\mathbf{q}(\theta, t)$ is the control action (Kalmár-Nagy et al., 2004):

$$\mathbf{q}(\theta, t) = \mathbf{P}(\theta)\mathbf{U}(t) \quad (27)$$

5 POSITION CONTROL AND IMPLEMENTATION

In order to control the position and head angle of robot a PD controller is employed. Mathematically a PD controller can be expressed as

$$K = K_p e + T_d \frac{de}{dt} \quad (28)$$

By increasing K_p the rise time becomes faster, but on the other hand the overshoot increases too, which is undesired. Furthermore the stability gets worse. Derivative control improves system performance in two ways. Firstly, it adds positive phase angles to increase the open-loop frequency response so as to improve system stability and to increase close-loop system bandwidth to increase the speed of response. Secondly, it provides braking when the response is getting closing to the new set point. This braking action not only helps to reduce overshoot but also tends to reduce steady-state error. Influence of derivative control on the system is proportional to K_d , but increasing derivative feedback will slow the system response and magnify any noise that may be present. It is important to note that derivative control has no influence on the accuracy of the system, but just on the response time.

A problem that can occur with derivative control is that in a real control system, the set point is usually stepped up or down in discrete steps. A step change has an infinitely positive slope, which will saturate the derivative function. A solution to this problem is to base the derivative control on the feedback signal alone instead of the error because the controlled variable can never actually change instantaneously, even if the set point does. The effect of proportional and derivative action is summarized in table 1.

Table 1: Controller properties

Action	Rise Time	Overshoot	Stability
Increasing K_p	Faster	Increases	Gets worse
Increasing K_d	Slower	Decreases	Improves

A digital controller is used for our purpose. For digital filter differentiation of a function $e(t)$ the following technique is used. The slope of $e(t)$ at the $t = kT$ is approximated to be slope of the straight line connecting $e[(k-1)T]$ with $e(kT)$. Numerical derivative of $e(t)$ at $t=kT$ can be written as

$$D = \frac{e(kT) - e[(k-1)T]}{T} \quad (29)$$

The z-transform of this equation yields

$$D(z) = \frac{z-1}{z} \quad (30)$$

So the digital PD controller can be written as

$$K = K_p + K_d \left[\frac{z-1}{z} \right] \quad (31)$$

We use this equation to implement the controller. As depicted in Fig.6, the position and the angle of the robot is obtained by using a camera.

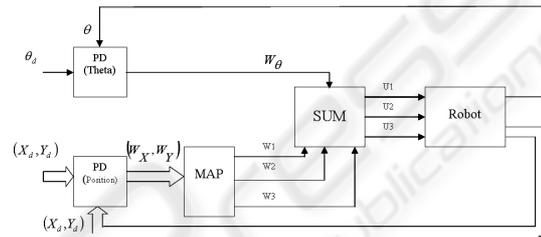


Figure 6: Control Diagram

These measurements are compared with the desired set-point values and the calculated errors. The camera also gives the derivative of output values. The error in position is fed to a digital PD (position PD). Position PD output is applied to a limiter and then mapped to direction of each wheel by an appropriate function block (W_1, W_2, W_3). Error in robot angle is fed to another PD (head angle PD). Head angle PD output (W_θ) is limited and then added to the outputs of mapping block.

$$\begin{cases} U1 = W1 + W_\theta \\ U2 = W2 + W_\theta \\ U3 = W3 + W_\theta \end{cases} \quad (32)$$

These signals determine the duty cycle of each robot motor.

To tune the PDs, the following procedure is pursued. The derivative action removed by setting $K_d=0$, the gain K_p is tuned to give the desired response and K_d is adjusted to damp the overshoot. The above steps are repeated until an acceptable response is achieved.

To demonstrate the computational efficiency and robustness of the algorithm, simulations were performed (with $m=3\text{kg}$, $j=0.014 \text{ Kg m}^2$, $L=0.07\text{m}$). Position and velocity of the vehicle are assumed to be measured 50 times per second. The inputs to the algorithm are initial and desired positions and head angle.

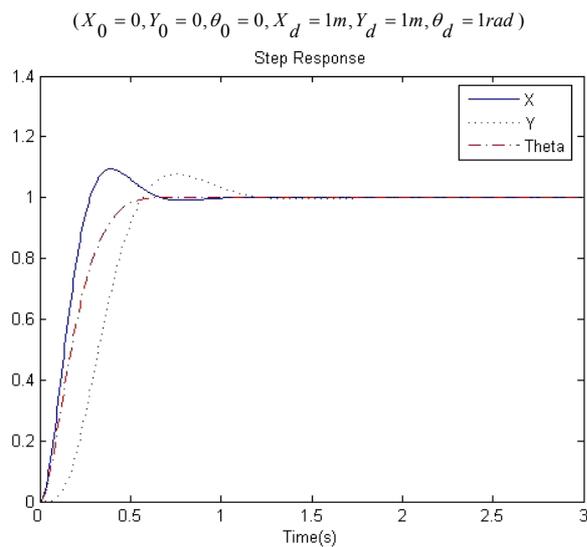


Figure 7: Step Response

The results are shown in Fig. 7. As depicted, the robots head angle overshoot is smaller than X overshoot and y overshoot.

6 CONCLUSIONS

Wheeled mobile robots (WMRs) are increasingly present in industrial and service robotics, particularly when flexible motion capabilities are required on reasonably smooth ground and surface (Schraft et al., 1998). Several mobility configurations (wheel number and type, their location and actuation, single or multi-body structure) can be found in the applications (Jones et al., 1993), which can lead to designing and implementing an asymmetric robot.

This paper has presented a control model for a specific kind of asymmetric omnidirectional wheeled mobile robot. During initial modelling and experimental works, it was supposed that asymmetric feature could be a limitation for robot to meet the requirements. While this is true, it was however learned that if we derive proper control model for robot we can overcome this limitation to some extent. Since our objective was to model the control of a specific kind of an asymmetric omnidirectional wheeled mobile robot, this paper did not develop a method for a large variety of asymmetric robots. A control method that depends on the angles between robot wheels, and includes motion and velocity equations are supposed to be developed in the future studies as extension of this work.

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