

# Analysis of the Evolution of the UML Metamodel

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**Abstract:** UML has been widely used for modeling applications and it changes continuously. In this situation, it is reasonable to analyze its evolution. This paper presents an approach to analyzing the evolution of the UML metamodel by using complex network and information entropy technologies. The approach can provide insight into the constructive mechanism and future trends of UML, and potentially form the basis for eliciting improved or novel laws of UML evolution. The study is a contribution for analyzing the evolution of not only the UML metamodel but also other metamodels like the UML metamodel.

## 1 INTRODUCTION

Unified Modeling Language (UML) has been widely used for modeling applications in various fields and has been improving all along.

Each version of UML has several metaclasses and a large number of relations between the metaclass, and thus UML is a complex body of knowledge.

It is inevitable that the complex language has quality defects, because the design for UML is closely related to the cognitive ability of designers. The practice has proved that it is much harder to design good quality complex diagrammatic languages (such as UML).

The defects result in a big trouble for building, understanding, and applying UML. Therefore, a quality assurance mechanism is necessary for solving the problems. The key part of the work is making certain the UML's structure mechanism.

There is little research on what is the well-ordered structure of the UML metamodel. It is an important approach to analyzing the structure mechanism of the UML metamodel from an evolutionary point of view.

In this paper, we use information entropy to analyze the evolution of the UML metamodel, since information entropy can provide theoretical underpinnings for software engineering in general (Clark et al, 2015).

Currently, the crossover study of software engineering and complex network has obtained some achievements, and we also explore to use the achievements to analyze the evolution of the UML metamodel.

The paper is structured as follows. Section 2 presents our analyzing approach. Section 3 analyzes data calculated from the 11 versions of UML and our preliminary observed results. Section 4 further discusses the preliminary results and the problems needing to be solved further. Section 5 analyzes related work. Section 6 draws conclusions.

## 2 ANALYZING APPROACH

### 2.1 Structure of the UML Metamodel

The UML metamodel is a complex body of knowledge. Typically, it consists of hundreds of metaclasses, a metaclass may have many properties, and there are complex relationships between metaclasses. Therefore, packages are used to organize the metamodel since the packages provide namespaces for the grouped elements.

According to the UML XMI document, we unfold the package structure of the UML metamodel into a directed graph by parsing merge, include, and import relations between the packages, and obtain

one metaclass diagram (i.e. one directed graph) for calculating the UML metamodel.

Moreover, we need to find an approach to analyzing in detail the distribution of the features of metaclasses (i.e. property, operation, and OCL expression) and the distribution of the relations between the metaclasses, and to exploring the evolution of the UML metamodel by using statistics, complex network, and information entropy technologies.

## 2.2 Complex Network

We obtain the directed graphs of the 11 versions of the UML metamodel, and each of them is a network, which consists of nodes (metaclasses) and directed edges (inheritances, and compositions, unidirectional and bidirectional associations).

Each version of the UML metamodel all has several hundreds or even more than one thousand of features, and so is relations. Therefore, such a directed graph from the metamodel is complex, and it is complex network (Wang et al. 2013).

Using network and statistical methods to analyze software helps to reveal the essential characteristics of software, and lay a foundation for quantizing the complexity of software (He et al. 2008). Barabási think that complex network is an efficient tool for handling complex systems and that network topology (including calculated statistical properties) is closely related to the evolution of networks (Barabási,2009). We mainly apply degree distribution, network density, and average path length to analyze the UML metamodel and evolution, along with information entropy.

## 2.3 Analysis of Entropies

There are some relations between microstates of a system and its components: the number of microstates of a system increases with the number and complex of the components of the system (Silviu, 1977).

Information theory uses an amount of information of a system to measure the degree of its structuralization or systematization, and advocates that increasing information can order chaotic systems, in contrast, loss of information can bring chaos of systems. Moreover, the structure of a system affects its efficiency of information flow.

One calculates an amount of information of a system by using information entropy, which is a measurement of the micro-disorder degree or the uncertain degree of the information of a system. Let

$p(x_i)$  be a probability of  $x_i$  occurring in a whole distribution for a system, and the information entropy of the system is

$$-\sum p(x_i)\log_2 p(x_i), \quad i=1,2,..n.$$

One takes the UML metamodel as a system and continually modifies its structure or order degree. While modifying, it receive negentropy or positive entropy from outside. Therefore, it is far away balance and its growth is not irreversible, since UML strives to model as many application fields as possible and such fields develop continuously. Moreover, the interaction between the components of the UML metamodel is nonlinear, i.e. not simply overlaying the functions of the components.

According to the aforementioned characteristics of the UML metamodel, it is a dissipative structure system (Zhang and Vijay, 2012) and is evolutionary, and thus we measure it with information entropy. In the paper, the information entropy is a measurement of the space distribution and randomness of the structural components of the UML metamodel since the UML metamodel can be transformed into a size and complex directed graph. Ideally, the UML metamodel is well-formed and well-order, i.e. its entropy is as small as possible.

According to information theory based on microscopic states, the microstates of the UML metamodel are its possible existing structural forms, and the number of the microstates of the metamodel is a key factor for the entropy of the metamodel. Therefore, the paper uses microstates to evaluate the order degree of the UML metamodel. Moreover, for multi-versions of the UML metamodel, it is necessary to analyze the change of the entropy of the property, operation, inheritance, association, composition, OCL expression, feature, and relation in the metamodel.

### 2.3.1 Calculating the Entropy of Basic Components

The features and relations between the metaclasses in the UML metamodel are basic components calculated, and the following algorithm is used to calculate their entropy:

1. For a given component C,  $C \in \{\text{property, operation, OCL expression, generalization, association, composition}\}$ , and the UML metamodel M
2. Set the total number of metaclasses of M be N
3. num-set:= {}
4. FOR i:= 1 to N
  - num-set:= num-set  $\cup$  {the number of C of metaclass  $c_i$ } //calculating the distribution of the number of C (e.g. property) of metaclasses of M

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5. FOR each j ∈ num-set {
5.1. f[j]:=0 // recording the number of the
    metaclasses which the number of C of is j
5.2. FOR i:= 1 to N {
    IF the number of C of metaclass ci = j THEN
    f[j]:=f[j]+1
    ci.C.absolute-frequency:=f[j] // set absolute
    frequency on C of ci be f[j]
    ci.C.self-information:=-log2(ci.C.absolute-
    requery/N) //calculating self-information of ci
    on C
    }
    }
6. The entropy on C of M is
    - ∑in ((ci.C.absolute-frequency/N) × ci.C.self-
    information)
    
```

### 2.3.2 Calculating the Utility of the UML Metamodel

The utility of the UML metamodel is the efficiency of the directed graph. Here, the paper focuses on the communication efficiency validity and communication quality validity of the directed graph since both indexes can figure the utility (Zhang and Vijay,2012).

By the aid of information entropy theory based on microscopic states (Zhang and Vijay,2012), the structure validity of a system

$$R = 1 - H/H^*$$

Where H and H\* is the structure entropy and the max structure entropy of the system, respectively. The bigger R is, the better the structure of the system is, since H should be as small as possible according to the aforementioned information entropy theory.

Concretely, here H is classified to communication efficiency entropy and communication quality entropy.

The communication efficient validity of a system indicates the velocity of information communication between all components of the system, and it is related to the distance of propagation. The measure of the uncertainty of communication efficient validity is the communication efficiency entropy of the system.

The communication quality validity of a system indicates the accuracy of information communication between all components of the system, and it is related to the number of these components (i.e. the more the components are, the more the chance of the introduction of communication error is) and to the

affinity within components (i.e. connectivity of relations between components). The measure of the uncertainty of communication quality validity of a system is the communication quality entropy of the system.

According to aforementioned definitions, we can see that communication efficiency entropy and communication quality entropy can be used to evaluate the manageability and understandability of the UML metamodel.

(a) Calculating communication efficient validity

According to the definition of communication efficient validity, the greater the path length between two metaclasses is, the more difficult the understanding their relation is.

Communication efficient validity of the UML metamodel

$$R_t = 1 - H_t/H_t^*$$

where H<sub>t</sub> is communication efficient entropy of the UML metamodel, and H<sub>t</sub>\* is its max communication efficient entropy.

Set the UML metamodel have n metaclasses, L<sub>ij</sub> be the sum of path lengths between metaclasses i and j, and then the total efficient microstates of the UML metamodel

$$L = \sum_{i=1}^n \sum_{j=1}^n L_{ij}, \text{ and } H_t^* = \log_2 L.$$

The probability of occurring efficient microstates between metaclasses i and j

$$p_{ij} = L_{ij} / L, \text{ and } H_t = \sum_{i=1}^n \sum_{j=1}^n -p_{ij} \log_2 p_{ij}.$$

(b) Calculating communication quality validity

The more the number of needed metaclasses for defining a metaclass is, the bigger the error possibility for defining the metaclass is.

Communication quality validity of the UML metamodel

$$R_q = 1 - H_q/H_q^*,$$

where H<sub>q</sub> is communication quality entropy of the UML metamodel, and H<sub>q</sub>\* is max communication quality entropy.

Set the UML metamodel have n metaclasses, D<sub>i</sub> be the out degree of metaclass i (i.e. the number of needed direct metaclasses for defining i), and then the total communication quality microstates (interconnection) between all metaclasses of the UML metamodel

$$D = \sum_{i=1}^n D_i, \text{ and } H_q^* = \log_2 D.$$

The probability of occurring quality microstates of metaclasses  $i$

$$p_i = D_i/D, \text{ and } H_q = \sum_{i=1}^n -p_i \log_2 p_i.$$

(c) Calculating the utility of the UML metamodel

The utility of the UML metamodel  $= \alpha R_t + \beta R_q$  where  $\alpha$  and  $\beta$  are weights, and  $\alpha + \beta = 1$ . The bigger the utility is, the better the ordering degree of the UML metamodel is.

### 3 PRELIMINARY RESULTS

We obtain basic data from 11 versions of UML and analyze the data by using statistics, complex network, and entropy technologies.

#### 3.1 Statistical Analysis of Basic Components

##### 3.1.1 Scale

The UML metamodel contains basic components: class, property, operation, OCL expression, association, inheritance, and composition. The previous four basic components are collectively called feature, and latter three are collectively called relation. One usually concerns the number of them and the trend of their evolutions, see Figure 1.

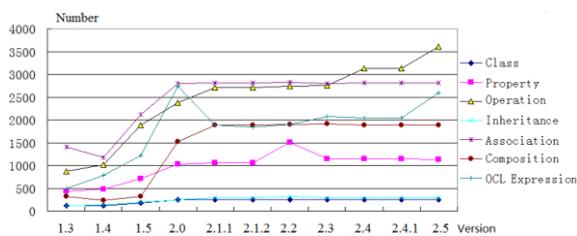


Figure 1: Evolution of basic elements of 11 versions of the UML metamodel.

The scales of almost all basic components of early versions of the UML metamodel are increasing, and the scales of class, associations, inheritances, property, and composition all trend toward leveling out after UML 2.1.1 except for scale of property in UML 2.2.

OCL expression and operation help to formalize the semantics of UML, their scales also are increasing except that the scale of OCL expressions jumps in UML 2.0.

##### 3.1.2 Distribution of Basic Components

In the UML metamodel, for a given feature or relation (e.g. property or composition), the number of the metaclasses that have the feature or relation may be 0, 1, 2, ..., and these numbers seems like it should follow a skewed distribution, because the probability distributions of structural components of OO software tends to follow skewed distributions with long tails (Valverde and Sol'e, 2007), since the basic components of the UML metamodel is similar to ones of OO software. In fact, the obtained distributions of each kind of components are irregular. This indicates that UML designers do not use the smaller numbers of properties and relations to define the metaclasses.

Figure 2 shows the evolution trend of the means of the basic components of 11 versions of UML.

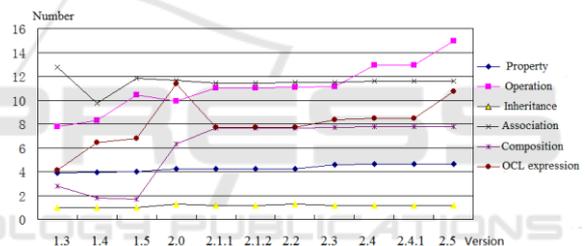


Figure 2: Evolution trend of means of the basic components.

The scales of the basic components all trend toward leveling out after UML 2.0 except for scales of operations and OCL expressions in UML 2.5. Indeed, UML 2.5 designers increase the operations and OCL expressions in order to enhance UML static semantics.

Figure 2 shows that the average scale of the properties and inheritances in all versions remain stable and the values are small. The reason for this should be that UML designers usually follow that a metaclass is defined with a few properties and inheritances for the sake of reusability and understanding.

##### 3.1.3 Information Entropy

According to the algorithm for calculating entropy (See Section 2.3.2), we obtain the curves for entropy evolutions of the basic components from 11 versions of the UML metamodel in Figure 3.

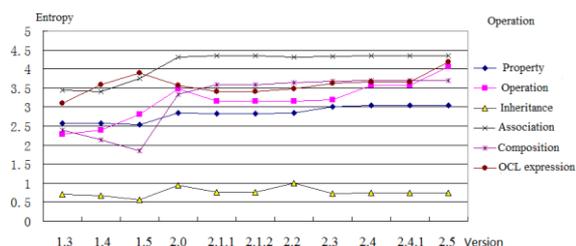


Figure 3: Entropy evolutions of the basic components.

In Figure 3, the entropy of the basic components since UML 2.0 all tends to changes little except for the entropy of operations and OCL expressions in UML 2.5. In practice, UML 2.5 increases the operations and OCL expressions. The observed result is compatible with that in Figure 2.

### 3.2 Structural Analysis of Metamodels

#### 3.2.1 Degree Distribution

Here, we discuss the in-degrees and out-degrees of the metaclasses. Obviously, the larger the degree of a metaclass is, the higher the influence of the metaclass. Therefore, we focus on the degree distribution of the graph.

Because early 3 version of UML metamodel is small scales and undergo a great deal of change, Figure 4 shows the distribution of in-degrees of the metaclasses of the UML metamodel from version 2.0 to version 2.5.

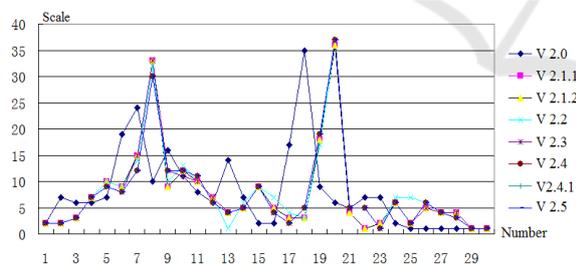


Figure 4: The distribution curves of the in-degrees of metaclasses from later 8 versions.

The distribution curve of the in-degrees of metaclasses in UML 2.0 is obviously different with the others. The reason for this is that UML 2.0 has structural problems, and OMG (Object Management Group) declared the issue.

The distribution curves of the in-degrees of the metaclasses of the other UML versions are bimodal, and are almost the same. This means the distribution probability of the in-degrees concentrated on two areas.

Figure 5 show the distribution of out-degrees of the metaclasses from 11 versions of the UML metamodel.

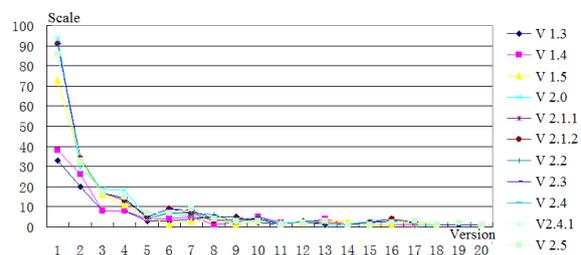


Figure 5: The distribution curves of the out-degrees of metaclasses.

In Figure 5, the degrees of the previous three versions are obviously smaller than degrees of the later ones.

Many of the metaclasses in each version of the UML metamodel devote themselves to define a very few other metaclasses, and the curves follow long tail distribution.

#### 3.2.2 Network Density

Network density characterizes the complexity of a network structure. The greater network density is, the more difficult understanding and maintaining it is.

Set a version of the UML metamodel (i.e. a directed graph) have  $N$  nodes and  $M$  edges, its network density  $\rho = M / (N * (N - 1))$ , i.e. the ratio of the number of its actual edges to the largest possible edges. Figure 7 shows the evolution trend of network densities of 11 versions of the UML metamodel.

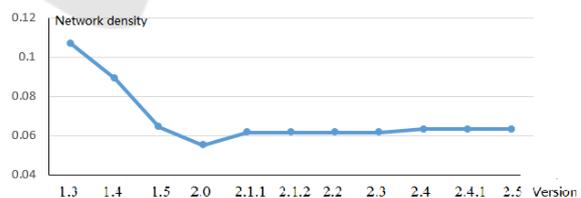


Figure 6: Evolution trend of network densities of 11 versions of the UML metamodel.

In the current trend, since UML 2.0, network densities stabilize,  $M \approx 0.0054N * (N - 1)$ , i.e.  $M(t) \sim N^\alpha(t)$ ,  $1 < \alpha < 2$ , where  $t$  is time. This means that the evolution of the networks follows densification power law.

The densification power law means that, on the one hand, a directed graph will become more and more densification, but on the other hand, the graph

still is actually sparse with comparing a unity coupling network for the graph (Wang et al. 2013). With increase of modeling requirements, N should increase, and M should increase even more. This will result in that the UML metamodells are larger and more complex, and seriously impact that one learns and maintains it, etc. Therefore, it is necessary to build UML profiles as required, instead of complicating the basic UML metamodel, i.e. restraining the increase of N, just like what OMG advocates.

### 3.2.3 Average Path Length of Network

UML metaclasses are defined step-by-step, and each modeling element (i.e. a metaclass which in-degree is 0), which are used by end-modelers, depends on the metaclasses locating to one or several directed paths. Obviously, the long dependency paths increase the degree of difficulty to manage and understand the whole UML metamodel. Therefore, we use the average path length of network to assess the efficiency for learning the UML metamodel.

For a directed graph for a version of the UML metamodel, we take the sum of path lengths of a given modeling element to all end metaclasses as the path length for defining the modeling element. Figure 7. shows the average path lengths of 11 versions of the UML metamodel.

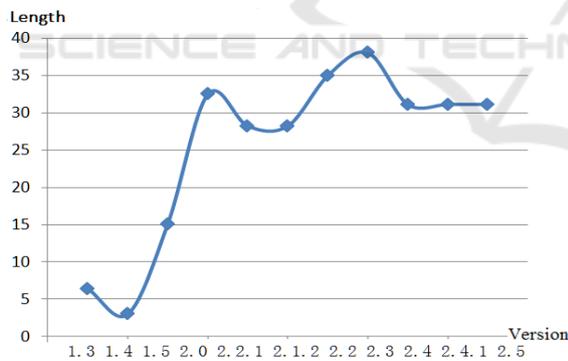


Figure 7: The average path lengths of 11 versions of the UML metamodel.

Figure 7 shows that the average path lengths of early UML metamodells increase since the sizes of the metamodells become bigger, and ones of the other UML metamodells are bigger since the metamodells all are big in size. It is worthwhile to note that the average path lengths of the last several metamodells almost changes a little since the metamodells hold steady.

This means that learning a modeling element needs learning about dozens of metaclasses.

According to the “Seven, Plus or Minus Two” rule (George, 1956), which is instructive to understand a concept with reasonable sizes to a certain extent, current the UML metamodel is obviously not easy to learn.

### 3.2.4 Utility of an UML Metamodel

According to the algorithm in Section 2.3.2, we obtain the utility of 11 versions of the UML metamodel by setting  $\alpha$  and  $\beta$  all be 0.5, see Figure 9.

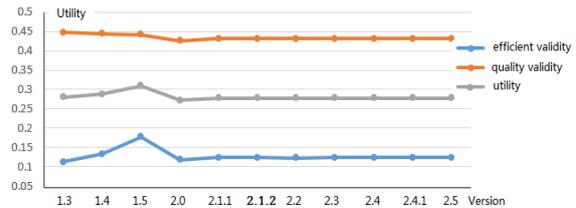


Figure 8: Curves for the utility of 11 versions of the UML metamodel.

In Figure 8, the communication quality validity, communication efficient validity, and utility of early versions of UML metamodel are almost higher than ones of later versions. The reason for this is that the early versions far away from user requirements, even after they are to come into the service, they still have defects on correctness, precision, conciseness, consistency, and understandability.

Since UML 2.0, the communication quality validity, communication efficient validity, and utility converge to a relatively small range of values (i.e. have cohesiveness to large extent), respectively. This indicates that these versions all are mature and stable to a large extent, since they have been applied and improved for a long time. On the other hand, for the later versions, their communication quality validity and communication efficient validity all are small, and so is their utility. Such small values indicate that these versions of UML metamodel are still less than satisfactory, and they need to be further improved since the bigger the three values is, the better the structure of the UML metamodel is.

For other values for  $\alpha$  and  $\beta$ , the values of the related utilities all are in the interval [0.08,0.22] since UML 2.0, and the related trend lines are the same as that in Figure 9 in essence. Therefore, the above conclusion still is true.

## 4 DISCUSSION

Figures 1 to 3 show that the scale of the metamodel

of UML 2.0 swells first, the later versions have a little change. For basic components except for the operations and OCL expressions in UML 2.5, their scales and entropies from UML 2.0 to UML 2.4.1 change slightly, see Figures 2 and 3. As mentioned, the explanation for the increases of the operations and OCL expressions in UML 2.5 is that formal OCL expressions can enrich UML static semantics and reduce ambiguity.

The current evolution trend of network densities in Figure 6 is stable, and this is the effort of OMG on using profiles as soon as possible instead of extending UML, i.e. the OMG has benefitted from the pursuit.

The current the communication quality validities, communication efficient validities, and utilities of the UML metamodel all change slightly, and the result accords with the aforementioned results. However, their values all are small, and such small values indicate that these versions of the UML metamodel still need to be further improved.

In figure 4, the distribution curves of the in-degrees of the metaclasses of the other UML versions are bimodal, that is, the distribution probability of the in-degrees concentrated on two areas. The reason needs to be further explored.

In figure 5, the distribution curves of the out-degrees of the metaclasses of each version of the UML metamodel follow long tail distribution, and the distribution results from structure of the UML metamodel. First the UML defines a great many of the simple foundational language constructs required, then the constructs are used to define the user level constructs required for UML step by step. OMG always follows the principle: the incrementally defining the UML metamodel and reusing the foundational language constructs for defining the modeling elements of UML and other modeling languages.

The average path lengths since UML 2.0 are more than 25 (see Figure 7), and this means that current versions of the UML metamodel are obviously not easy to learn. How to increase the comprehensibility of UML is a big challenge. Enriching a metaclass with information (e.g. adding the number of basic components) to a certain extent may be a measure.

The results in Section 3 also obviously shows that, with the evolution of the UML metamodel, the number of their components swells and their structure gets complicated during early evolution, and the degree of their change becomes small during later evolution.

The UML metamodel is used to define modeling elements. Specifically, a modeling element, out-degree of which is 0, is defined with a series of subsequent metaclasses up to end-metaclasses, in-degree of which all are 0, and there may be several definition paths for the modeling element. Therefore, it is improper to calculate average shortest path lengths of the directed graph for the UML metamodel. Since average shortest path length is a property of the small world network (Valverde and Solé, 2007), the directed graphs are different with the small world network.

## 5 RELATED WORK

To some degree, the UML metamodel is similar to ordinary OO class models, and some of the measure technologies for the class models can be used to measure the UML metamodel. Bansiya and Davis (2002) collect data from class models of some software frameworks with successive versions according to their nine OO metrics, and then calculate the change between different versions of a framework. Mattsson and Bosch present a method (1999), which is similar to Bansiya's method, that can measure the change between different versions of a framework, and includes six hypotheses for assessing stability of a framework. Valverde and Solé deeply study hierarchical small-worlds in OO software architecture based on complex network theory (2007). However, indeed the UML metamodel, as a new kind of the body of knowledge, is different from ordinary class models, and these studies involve few characteristics of the UML metamodel.

For the studies on the quality of metamodels, typical some focus on UML. The existing studies focus on the design expectations of UML (Weigert,2000; Douglass,1998; Siau and Cao, 2002). However, these design expectations have not explicit definitions, without concrete solutions. Ma et al. (2013) define a quality model and present an operable measuring mechanism to assess the quality of metamodels, without a main focus on evolutionary.

Some studies use entropies to assess software. The studies help to our work, but are not direct related to the UML metamodel. Hassan and Holt (2003) use information entropy to deeply research the chaos phenomenon of software, and find that the information entropy of software becomes bigger and bigger in the evolution process of the software; this makes the increases of the difficulty in that

developers maintain the software. Using entropy principle, Gaudan, et al (2008) present a measure method of OO software reliability, and the method misses important OO concepts such as associations. Moreover, Yu, et al (2008) present an approach to measuring the component cohesion based on structure entropy and Zhang, et al (2011) analyze system coupling by measuring the entropy of modules. The later two works apply entropy to measure systems, but they aim at component and entity respectively, not metaclass.

## 6 CONCLUSIONS

For large and complex the UML metamodel, the paper presents an approach to analyzing its evolution to make certain its structure mechanism by using statistics, complex network, and information entropy technologies.

The study of the paper can provide the guides to develop, measure, and refactor not only the UML metamodel but also other metamodels like the UML metamodel, and lays a foundation for further exploring the structure mechanisms of large and complex the metamodels like the UML metamodel with good quality.

The paper analyses the basic components and structure of the UML metamodel, and reveal only some structural properties. This means that further analysis is needed.

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