

Mathematical Backdoors in Symmetric Encryption Systems

Proposal for a Backdoored AES-like Block Cipher

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Abstract: Recent years have shown that more than ever governments and intelligence agencies try to control and bypass the cryptographic means used for the protection of data. Backdooring encryption algorithms is considered as the best way to enforce cryptographic control. Until now, only implementation backdoors (at the protocol/implementation/management level) are generally considered. In this paper we propose to address the most critical issue of backdoors: mathematical backdoors or by-design backdoors, which are put directly at the mathematical design of the encryption algorithm. While the algorithm may be totally public, proving that there is a backdoor, identifying it and exploiting it, may be an intractable problem. We intend to explain that it is probably possible to design and put such backdoors. Considering a particular family (among all the possible ones), we present BEA-1, a block cipher algorithm which is similar to the AES and which contains a mathematical backdoor enabling an operational and effective cryptanalysis. The BEA-1 algorithm (80-bit block size, 120-bit key, 11 rounds) is designed to resist to linear and differential cryptanalyses. A challenge will be proposed to the cryptography community soon. Its aim is to assess whether our backdoor is easily detectable and exploitable or not.

1 INTRODUCTION

Despite the fact that in the late 90s/early 2000s, citizens have partially obtained the freedom for using cryptography, the recent years have shown that more than ever, governments and intelligence agencies still try to control and bypass the cryptographic means used for the protection of data and of private life. Snowden's leaks were a first upheaval. A tremendous number of secret projects (from NSA, GCHQ) have been revealed to the public opinion which proves this situation.

While the need for the security of everyday life activities (for companies, for citizens) requires more and more cryptography, recent bothering initiatives by political decision-makers ask for an even stronger control over cryptography not to say preparing the simple prohibition or ban of cryptographic application such as telegram. At the same time, the EU as well as a number of security agencies (such as French ANSSI, German BSI) confirmed that it was nonsense and militate for the mandatory use of end-to-end encryption.

The recurring approaches and attempts consist in making the implementation of backdoors mandatory. The simplest and naive approach consists in enforc-

ing key escrowing at the operators' level. But point-to-point encryption solutions (which are not equal to end-to-end encryption) like Telegram or Proton mail enable to prevent it. A number of different backdoor techniques are regularly mentioned or proposed.

The most critical aspect in implementation backdoors lies on the fact that hackers or analysts may find them more or less easily and worse may exploit them. This is the reason why it is likely that IT operators or developers are very reluctant to accept backdoors until now. In case of leak, they will inevitably lose users' confidence and favor the development of trusted services abroad. In fact, the backdoor issue arises due to the fact that only implementation backdoors (at the protocol/implementation/management level) are generally considered.

In this paper we address the most critical issue of backdoors: mathematical or by-design backdoors. In other words, the backdoor is put directly at the mathematical design of the encryption algorithm. While the algorithm may be totally public, proving that there is a backdoor, identifying it and exploiting it, may be an intractable problem, unless you know the backdoor. To some extent, the RSA's Dual_EC_DRBG standard case falls within this category (Shumow and Fergu-

son, 2007). Other non-public examples are known within the military cryptanalysis community, and partially revealed to the public thanks to the 1995 Hans Buehler case (Strehle, 1994). This kind of backdoor is the most difficult one to address and there is quite no public work on that topic. It is generally the technical realm of a few among the most eminent intelligence agencies (namely NSA, GCHQ, SVR/GRU) which moreover have the ability and power to step in and to influence the international standardization processes.

We intend to explain that it is probably possible to design and put such backdoors. Considering a particular case of mathematical backdoors (among all the possible ones) based on our previous work (Bannier et al., 2016), we present a block cipher algorithm which is similar to the AES and which contains a mathematical backdoor enabling an operational and effective cryptanalysis (in other words in a limited time on a modern desktop computer and with a limited number of plaintext/ciphertext pairs). This block cipher algorithm (80-bit block, 120-bit key size, 11 rounds) is designed to resist to linear and differential cryptanalyses.

This paper is organized as follows. In Section 2 we explore the concept of backdoors and trapdoors and we identify two main categories, each containing itself subcategories depending on the nature of the cipher (stream or block ciphers). This observation is backed by the personal experience of the second author as a military cryptanalyst. We also present the state-of-the-art, history and previous work regarding backdoors, mostly in symmetric cryptography. In Section 3, we present our backdoored block cipher algorithm BEA-1 (standing for *Backdoored Encryption Algorithm 1*), based on our work (Bannier et al., 2016). This is a particular family of trapdoors using a suitable partition of the plaintext and ciphertext spaces. In Section 4, we discuss the cryptographic security of this cipher, with respect to linear and differential cryptanalyses. We also propose a cryptographic challenge to the cryptography community¹, regarding the backdoor identification and exploitation. We suppose that this backdoor is likely to be detected. Such a challenge should enable to prove or disprove this claim. Lastly we conclude in Section 5 and explore future work.

¹This challenge will be launched on the Arxiv repository right after the conference, at the end of February.

2 THE CONCEPT OF BACKDOOR

2.1 Definition and Classification Proposal

Trapdoors are a two-face, key concept in modern cryptography. It is primarily related to the concept of “*trapdoor function*” — a function that is easy to compute in one direction, yet difficult to compute in the opposite direction without special information, called the “*trapdoor*”. This first “face” relates most of the time to asymmetric cryptography algorithms. It is a necessary condition to get reversibility between the sender/receiver (encryption) or the signer/verifier (digital signature). The trapdoor mechanism is always fully public and detailed. The security and the core principle is based on the existence of a secret information (the private key) which is essentially part of the trapdoor. In other words, the private key can be seen as *the trapdoor*.

The second “face” of the concept of trapdoor relates to the more subtle and perverse concept of “mathematical backdoor” and is a key issue in symmetric cryptography (even if the issue of backdoors may be extended to asymmetric cryptography; see for example the case of the DUAL EC_DRBG (Shumow and Ferguson, 2007), or the case of trapdoored primes addresses recently in (Fried et al., 2016)).

In this case, the aim is to insert hidden mathematical weaknesses which enable one who knows them to break the cipher. If possible, these weaknesses should be independent of the secret key. Somehow, it consists to create a hidden asymmetry to the detriment of the legitimate users of the communication and to the benefit of the eavesdropper. In this context, the existence of a backdoor is a strongly undesirable property.

In the rest of the present section, we will oppose the term of trapdoor (desirable property) to that of backdoor (undesirable property). While the term of trapdoor has been already used in the very few literature covering this second face of this problem, we suggest however to use the term of backdoor to describe the issue of hidden mathematical weaknesses. This would avoid ambiguity and maybe would favor the research work around a topic which is nowadays mostly addressed by governmental entities in the context of cryptography control and regulations.

Inserting backdoors in encryption algorithms underlies quite systematically the choice of cryptographic standards (DES, AES...). The reason is that the testing, validation and selection process is always conducted by governmental entities (NIST or equivalent) with the technical support of secret entities (NSA or equivalent). So an interesting and critical

research area is: “how easy and feasible is it to design and to insert backdoors (at the mathematical level) in encryption algorithms?”. In this paper, we intend to address one very particular case of this question. It is important to keep in mind that a backdoor may be itself defined in the following two ways.

- As a “natural weakness” known — but non disclosed — only by the tester/validator/final decision-maker (e.g. the NSA as it could have been the case for the AES challenge). The best historic example is that of the differential cryptanalysis. Following Biham and Shamir’s seminal work in 1991 (Biham and Shamir, 1993), NSA acknowledged that it was aware of that cryptanalysis years ago (Schneier, 2000). Most of experts estimate that it was nearly 20 years ahead. However a number of non public, commercial block ciphers in the early 90s may be weak with respect to differential cryptanalysis.
- As an intended design weakness put by the author of the algorithm. To the authors knowledge, there is no known cases for public algorithms yet.

As far as symmetric cryptography is concerned, there are two major families of cipher systems for which the issue of backdoor must be considered differently.

- *Stream ciphers*. Their design complexity is rather low since they mostly rely on algebraic primitives (LFSRs and Boolean functions which have intensely been studied in the open literature). Until the late 70s, backdoors relied on the fact that quite all algorithms were proprietary and hence secret. It was then easy to hide non primitive polynomials, weak combining Boolean functions. The Hans Buehler case in 1995 (Strehle, 1994) shed light on that particular case.
- *Block ciphers*. This class of encryption algorithms is rather recent (end of the 70s for the public part). They exhibit so a huge combinatorial complexity that it is reasonable to think to backdoors. As described in (Daemen and Rijmen, 2002) for a k -bit secret key and a m -bit input/output block cipher there are $((2^m)!)^{2^k}$ possible such block ciphers. For such an algorithm, the number of possible internal states is so huge that we are condemned to have only a local view of the system, that is, the round function or the basic cryptographic primitives. We cannot be sure that there is no degeneration effect at a higher level. This point has been addressed in (Daemen and Rijmen, 2002) when considering linear cryptanalysis. Therefore, it seems reasonable to think that this combinatorial richness of block cipher may be used to hide

backdoors.

Since block ciphers are the most widely used encryption algorithms nowadays by the general public and the industry, we will focus on them in the rest of the paper. Backdoors in stream ciphers have quite never been exposed to the public.

2.2 Previous Work

One of the first trapdoor cipher was proposed in 1997 by Rijmen and Preneel (Rijmen and Preneel, 1997). The S-boxes are selected randomly and then modified to be weak to the linear cryptanalysis. They are finally applied to a Feistel cipher such as CAST or LOKI91. But because of the big size of the S-boxes, the linear table of such an S-box cannot be computed. However the knowledge of the trapdoor gives a good linear approximation of the S-boxes which is then used in a linear cryptanalysis. As an example, the authors created a 64-bit block cipher based on CAST cipher, and four 8×32 S-boxes. If the parameters of the trapdoors are known, a probabilistic algorithm allows to recover the key easily. Such a family of trapdoor ciphers leads to recover only a part of the key, and the authors claim that the trapdoor is undetectable. But in (Wu et al., 1998), Wu and al. discovered a way to recover the trapdoor if the attacker knows its global design but not the parameters. They also showed that there exists no parameter allowing to hide the trapdoor. Nevertheless, it is worthwhile to mention that in practice, if a real cipher containing a trapdoor is given, the presence of the trapdoor will certainly not be revealed.

In (Paterson, 1999), a DES-like trapdoor cipher exploiting a weakness induced by the round functions is presented. The group generated by the round functions acts imprimitively on the message space to allow the design of the trapdoor. In other words, this group preserves a partition of the message space between input and output of the round function. Such a construction leads to the design of a trapdoor cipher composed of 32 rounds and using a 80 bits key. The knowledge of the trapdoor allows to recover the key using 2^{41} operations and 2^{32} plaintexts. Even if the mathematical material to build the trapdoor is given, no general algorithm is detailed to construct such S-boxes. Furthermore, as the author says, S-boxes using these principles are incomplete (half of the cipher text bits are independent of half of the plaintext bits). Finally, the security against the differential attack is said *not as high as one might expect*.

More recently in (Angelova and Borissov, 2013), the authors created non-surjective S-boxes embedding a parity check to create a trapdoor cipher. The mes-

sage space is thus divided into cosets and leads to create an attack on this DES-like cipher in less than 2^{23} operations. The security of the whole algorithm, particularly against linear and differential cryptanalyses is not given and the authors admit that their attack is dependent on the first and last permutation of the cipher. Finally, the non-surjective S-boxes may lead to detect easily the trapdoor by simply calculating the image of each input vector. This problem is naturally avoided in a Substitution-Permutation Network (SPN) in which S-boxes are bijective by definition.

In a slightly different context, Caranti and al. answer to Patterson's question by the affirmative in (Caranti et al., 2006), by proving that the imprimitivity of the group generated by round functions is actually related to the cosets of a linear subspace. They also give some conditions to create such a primitive group to design a secure cipher that cannot contain such trapdoor, and finally show that the AES respects these conditions. They add in (Caranti et al., 2009) an algorithm to verify this last condition simply and show that AES and Serpent S-boxes verify this property.

3 DESCRIPTION OF BEA-1

The algorithm BEA-1 (standing for *Backdoored Encryption Algorithm version 1*) is based on our research work on partition-based trapdoors (Bannier et al., 2016). This section is intended to describe this cipher precisely. The cipher operates on 80-bit data blocks using a 120-bit master key. Our algorithm is directly inspired by Rijndael (Daemen and Rijmen, 2002), the block cipher designed by Joan Daemen and Vincent Rijmen which is now known as the AES (the encryption standard proposed by the USA, under the auspices of NIST and NSA (NIST, 2000)). Consequently, our cipher is a Substitution-Permutation Network.

The encryption consists in applying eleven times a simple keyed operation called *round function* to the data block. A different 80-bit round key is used for each iteration of the round function. Since the last round is slightly different and uses two round keys, the encryption requires twelve 80-bit round keys. These round keys are derived from the 120-bit master key using an algorithm called *key schedule* (depicted in Figure 1).

The round function in Figure 2 is made up of three distinct stages: a *key addition*, a *substitution layer* and a *diffusion layer*. The key addition is just a bitwise XOR between the data block and the round key. The substitution layer consists in the parallel evaluation of four different S-boxes and is the only part of the

cipher which is not linear or affine. Following the design principles of the AES, the diffusion layer comes in two parts: the *ShiftRows* and the *MixColumns* operations.

The decryption is straightforward from the encryption since all the components are bijective. Thus, to decrypt, we just have to apply the inverse operations in the reverse order. Remark that the key addition and the *ShiftRows* are involutions, therefore the same operations are used in the decryption process. In contrast to the AES, the algorithm works with bundles of 10 bits instead of 8 bits. Let \mathbb{F}_2 denote the Galois Field of order 2. Any $10n$ -bit block x is seen as n -tuple of 10-bit bundles (x_0, \dots, x_{n-1}) , thus as an element of $(\mathbb{F}_2^{10})^n$. The hexadecimal notation is used to denote any 10-bit bundle. For example, $37A$ stands for 1101111010 in \mathbb{F}_2^{10} .

The S-boxes S_0 , S_1 , S_2 and S_3 are four permutations of \mathbb{F}_2^{10} given in Appendix. The linear map $M : (\mathbb{F}_2^{10})^4 \rightarrow (\mathbb{F}_2^{10})^4$ processes four 10-bit bundles. Because of the linearity of this map, M is only defined on the standard basis of $(\mathbb{F}_2^{10})^4$. For convenience, its inverse M^{-1} is also given in Appendix.

A pseudo-code for the key schedule is given in Algorithm 1. To provide an overview of its structure, the first step is represented in Figure 1. This representation also emphasizes the similarities between our key schedule and the AES one. The pseudo-code for the encryption and decryption functions are respectively given in Algorithms 2 and 3. The notation $[a \parallel b]$ denotes the concatenation of the vectors a and b . Again, an overview of the round function is given in Figure 2.

4 CRYPTOGRAPHIC SECURITY ANALYSIS OF BEA-1

4.1 Differential and Linear Cryptanalyses

In (Daemen and Rijmen, 2002), Daemen and Rijmen introduced the differential and the linear branch numbers of a linear transformation. With an exhaustive search, it can be checked that the differential and linear branch numbers of M are both equal to 5, which is the maximum. This implies that any 2-round trail has at least 5 active S-boxes. Thus, a 10-round trail involves at least 25 active S-boxes.

Note that all the S-boxes are (at most) differentially 40-uniform and linearly 128-uniform. Therefore, the probability of any 10-round differential trail is upper bounded by $(\frac{40}{1024})^{25} \approx 2^{-116.9}$ and the absolute bias of a 10-round linear trail is upper bounded

Algorithm 1 – ExpandKey
Input. The 120-bit master key $K = (K_0, \dots, K_{11}) \in (\mathbb{F}_2^{10})^{12}$.
Output. The twelve 80-bit round keys $k^0, \dots, k^{11} \in (\mathbb{F}_2^{10})^8$.

```

1    $(k_0, \dots, k_{11}) \leftarrow (K_0, \dots, K_{11})$ 
2   For  $i$  from 0 to 6 do
3      $x \leftarrow M(k_{12i+8}, \dots, k_{12i+11})$ 
4      $x \leftarrow (S_j(x_j))_{0 \leq j \leq 3}$ 
5      $x \leftarrow (x_0 \oplus (3^i \bmod 2^{10}), x_1, x_2, x_3)$ 
6      $(k_{12i+12}, \dots, k_{12i+15}) \leftarrow (k_{12i+0}, \dots, k_{12i+3}) \oplus x$ 
7      $(k_{12i+16}, \dots, k_{12i+19}) \leftarrow (k_{12i+4}, \dots, k_{12i+7}) \oplus (k_{12i+12}, \dots, k_{12i+15})$ 
8      $(k_{12i+20}, \dots, k_{12i+23}) \leftarrow (k_{12i+8}, \dots, k_{12i+11}) \oplus (k_{12i+16}, \dots, k_{12i+19})$ 
9   For  $r$  from 0 to 11 do
10     $k^r \leftarrow (k_{8r+i})_{0 \leq i \leq 7}$ 
```

Algorithm 2 – Encrypt
Input. The 120-bit master key $K \in (\mathbb{F}_2^{10})^{12}$ and the 80-bit plaintext block $p \in (\mathbb{F}_2^{10})^8$.
Output. The 80-bit ciphertext block $c \in (\mathbb{F}_2^{10})^8$.

```

1    $k^0, \dots, k^{11} \leftarrow \text{ExpandKey}(K)$ 
2    $x \leftarrow p$ 
3   For  $r$  from 0 to 9 do
4      $x \leftarrow x \oplus k^r$ 
5      $x \leftarrow (S_i \bmod 4(x_i))_{0 \leq i \leq 7}$ 
6      $x \leftarrow (x_0, x_5, x_2, x_7, x_4, x_1, x_6, x_3)$ 
7      $x \leftarrow [M(x_0, x_1, x_2, x_3) \parallel M(x_4, x_5, x_6, x_7)]$ 
8      $x \leftarrow x \oplus k^{10}$ 
9      $x \leftarrow (S_i \bmod 4(x_i))_{0 \leq i \leq 7}$ 
10     $x \leftarrow (x_0, x_5, x_2, x_7, x_4, x_1, x_6, x_3)$ 
11     $x \leftarrow x \oplus k^{11}$ 
12     $c \leftarrow x$ 
```

Algorithm 3 – Decrypt
Input. The 120-bit master key $K \in (\mathbb{F}_2^{10})^{12}$ and the 80-bit ciphertext block $c \in (\mathbb{F}_2^{10})^8$.
Output. The 80-bit plaintext block $p \in (\mathbb{F}_2^{10})^8$.

```

1    $k^0, \dots, k^{11} \leftarrow \text{ExpandKey}(K)$ 
2    $x \leftarrow c$ 
3    $x \leftarrow x \oplus k^{11}$ 
4    $x \leftarrow (x_0, x_5, x_2, x_7, x_4, x_1, x_6, x_3)$ 
5    $x \leftarrow (S_i^{-1} \bmod 4(x_i))_{0 \leq i \leq 7}$ 
6    $x \leftarrow x \oplus k^{10}$ 
7   For  $r$  from 9 to 0 do
8      $x \leftarrow [M^{-1}(x_0, x_1, x_2, x_3) \parallel M^{-1}(x_4, x_5, x_6, x_7)]$ 
9      $x \leftarrow (x_0, x_5, x_2, x_7, x_4, x_1, x_6, x_3)$ 
10     $x \leftarrow (S_i^{-1} \bmod 4(x_i))_{0 \leq i \leq 7}$ 
11     $x \leftarrow x \oplus k^r$ 
12     $p \leftarrow x$ 
```

by $(\frac{128}{512})^{25} = 2^{-50}$. Consequently, a differential cryptanalysis of the 10-round version of our cipher would require at least 2^{117} chosen plaintext/ciphertext pairs and a linear cryptanalysis would require 2^{100} known plaintext/ciphertext pairs.

Even if this is a rough approximation since it does not take into account the inter-column diffusion provided by the ShiftRows operation, it suffices to prove the cipher practical resistance against classical differential and linear cryptanalyses. In fact, there is only 2^{80} different plaintext/ciphertext pairs for a fixed master key.

4.2 Statistical Analysis of BEA-1

Any cryptographic algorithm must behave as a random generator or at least must exhibit enough randomness properties. Therefore, its outputs for differ-



ent classes of inputs must pass all the reference statistical testings. The most widely used is the NIST's Statistical Test Suite (STS) (Rukhin et al., 2001).

We have performed the statistical analysis for BEA-1 with respect to all the tests which are implemented in STS. Our encryption has passed all the tests successfully. This result is of rather high importance since

- STS is the tool recommended by the US government to evaluate statistical properties of any secure encryption algorithm. It is explicitly mandatory to consider it in the industry.
- The presence of our backdoor remains statistically undetectable which proves that if statistical properties are a necessary condition for cryptographic security it is absolutely not a sufficient property. It may be bypassed by considering statistical simulation techniques (Filiol and Josse, 2007). Alge-

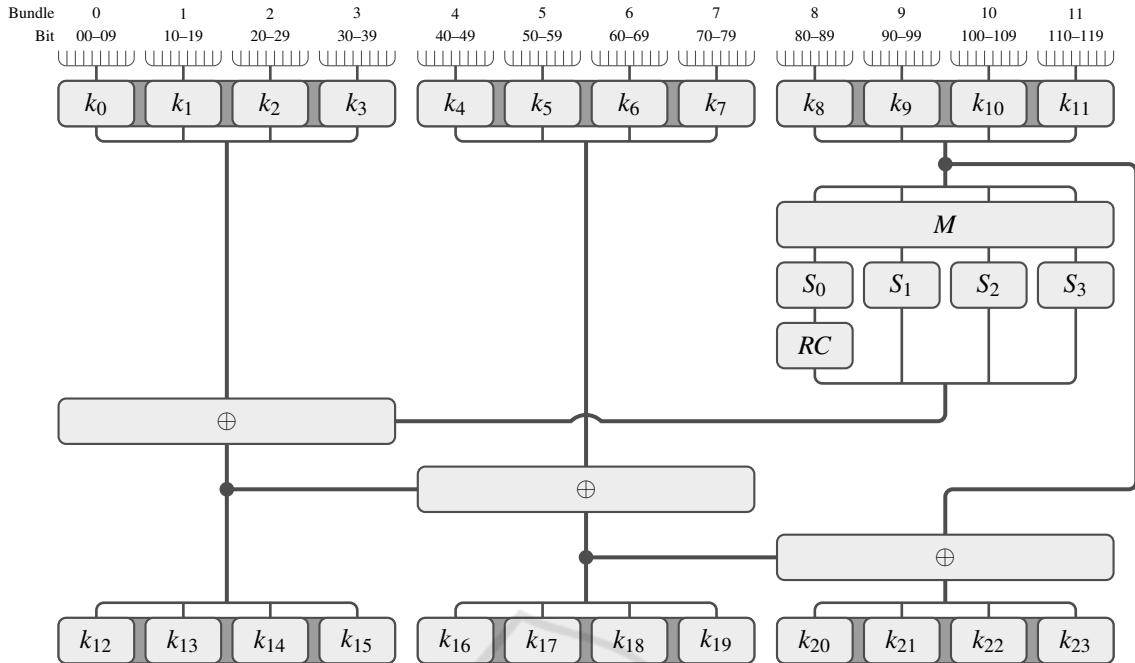
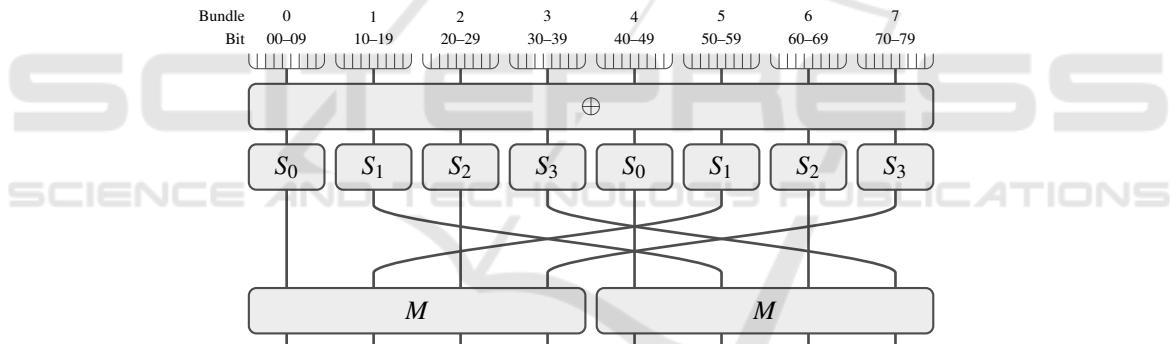

 Figure 1: A diagrammatic representation of the key schedule `ExpandKey`.


Figure 2: A diagrammatic representation of the round function.

braic or combinatorial weaknesses moreover remains out of reach from statistical analysis.

4.3 Cryptographic Challenge

We propose a cryptographic challenge whose aims is twofold:

- identifying and explaining what our backdoor consists in,
- exploiting this backdoor in the most efficient way (in terms of computing time, memory requirements, the number of required plaintext/ciphertext pairs).

We have run our own full cryptanalysis implementation several times. Each time, we retrieve the 120-bit key successfully.

This challenge will be officially launched right after the presentation of the present paper, on the arxiv.org. To take part, participants must send the following data to both authors (prior to any publication):

- the description of the backdoor,
- the description of the attack to exploit the backdoor successfully.
- the relevant source codes. They will help us to sort the different proposals with respect to, first the number of required plaintext/ciphertext pairs, second the computing time on our reference computer.

Incentive (non monetary) awards will be awarded to the three best attacks. Our attack as the reference solution will be presented in at the RusCrypto 2017 con-

ference around end of March 2017. Consequently, the challenge holds until this date. Moreover the best attack will be considered for publication in the Journal in Computer Virology and Hacking Techniques.

5 CONCLUSION AND FUTURE WORK

In this paper, we have proposed an AES-like encryption algorithm which contains a backdoor at its design level. This algorithm, named BEA-1, exhibits many of the desirable properties that any secure algorithm should. However, it is absolutely unsuitable for actually protection information. Indeed, we manage to break it with a rather limited amount of resources successfully.

While it is a humble, first step in a larger research work, it illustrates the issue of using foreign encryption algorithms which may contain such hidden weaknesses. The very final aim of our work is to prove that it is feasible to embed such undetectable intended weaknesses. It is consequently a critical issue to have a broader work conducted in this research area and we hope that other people will also consider it as such.

The next step will be to consider more sophisticated combinatorial structures.

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APPENDIX

The present appendix contains the different tables for the S-boxes (Figures 5, 6, 7 and 8), the linear map M (Figure 3) and its inverse M^{-1} (Figure 4). They can be copied and pasted for a practical implementation of the encryption algorithm.

x	\mapsto	$M(x)$
(001,000,000,000)	\mapsto	(112,1BC,36C,0C5)
(002,000,000,000)	\mapsto	(344,394,342,165)
(004,000,000,000)	\mapsto	(23F,15B,0C7,0A7)
(008,000,000,000)	\mapsto	(215,11F,1E0,2E7)
(010,000,000,000)	\mapsto	(2D9,10A,0C4,095)
(020,000,000,000)	\mapsto	(231,120,322,016)
(040,000,000,000)	\mapsto	(3C6,010,0EC,261)
(080,000,000,000)	\mapsto	(32C,199,2C5,07A)
(100,000,000,000)	\mapsto	(35C,13E,212,110)
(200,000,000,000)	\mapsto	(13E,20F,253,0BC)
(000,001,000,000)	\mapsto	(237,252,004,0F8)
(000,002,000,000)	\mapsto	(0CC,32A,01A,2DB)
(000,004,000,000)	\mapsto	(13B,2FA,328,38C)
(000,008,000,000)	\mapsto	(022,37D,08D,3D4)
(000,010,000,000)	\mapsto	(1F4,1C5,1FF,31D)
(000,020,000,000)	\mapsto	(39A,062,38C,2EB)
(000,040,000,000)	\mapsto	(006,131,32E,12B)
(000,080,000,000)	\mapsto	(15E,0BF,1E2,04F)
(000,100,000,000)	\mapsto	(17E,011,198,3C5)
(000,200,000,000)	\mapsto	(0E6,0ED,314,289)
(000,000,001,000)	\mapsto	(075,380,371,2E9)
(000,000,002,000)	\mapsto	(38B,1A6,221,260)
(000,000,004,000)	\mapsto	(019,08E,280,1A7)
(000,000,008,000)	\mapsto	(0DC,0B1,061,3DE)
(000,000,010,000)	\mapsto	(189,2AB,1A6,39D)
(000,000,020,000)	\mapsto	(1B2,0A7,178,208)
(000,000,040,000)	\mapsto	(269,2CC,27E,1CD)
(000,000,080,000)	\mapsto	(09A,1DD,336,34B)
(000,000,100,000)	\mapsto	(2D5,29F,072,04D)
(000,000,200,000)	\mapsto	(009,175,254,3ED)
(000,000,000,001)	\mapsto	(28D,172,3EA,24E)
(000,000,000,002)	\mapsto	(058,044,3A0,281)
(000,000,000,004)	\mapsto	(22D,1C8,221,18B)
(000,000,000,008)	\mapsto	(370,1D0,3CD,07F)
(000,000,000,010)	\mapsto	(256,130,382,067)
(000,000,000,020)	\mapsto	(37F,282,3A4,3D8)
(000,000,000,040)	\mapsto	(165,3BA,19B,0F7)
(000,000,000,080)	\mapsto	(1C7,259,17E,0BE)
(000,000,000,100)	\mapsto	(38E,3D2,2CD,21C)
(000,000,000,200)	\mapsto	(099,176,3BC,031)

 Figure 3: Specification of M .

x	\mapsto	$M^{-1}(x)$
(001,000,000,000)	\mapsto	(10B,221,09D,398)
(002,000,000,000)	\mapsto	(1AE,1E9,2CB,245)
(004,000,000,000)	\mapsto	(1AB,11E,05F,3A4)
(008,000,000,000)	\mapsto	(08D,04D,016,34C)
(010,000,000,000)	\mapsto	(0AD,337,3C5,2D4)
(020,000,000,000)	\mapsto	(322,3FD,3D5,0E5)
(040,000,000,000)	\mapsto	(002,246,2E2,380)
(080,000,000,000)	\mapsto	(1E9,3FE,238,329)
(100,000,000,000)	\mapsto	(0F5,1BD,210,210)
(200,000,000,000)	\mapsto	(2D8,209,353,243)
(000,001,000,000)	\mapsto	(07D,2BB,037,3C8)
(000,002,000,000)	\mapsto	(055,128,25A,17F)
(000,004,000,000)	\mapsto	(0EB,2FD,3C3,176)
(000,008,000,000)	\mapsto	(3D1,236,09D,2F1)
(000,010,000,000)	\mapsto	(06D,1BE,3EB,0BE)
(000,020,000,000)	\mapsto	(3D9,069,21B,11B)
(000,040,000,000)	\mapsto	(3AA,29E,239,1C0)
(000,080,000,000)	\mapsto	(0BD,1B1,18E,2AB)
(000,100,000,000)	\mapsto	(2D7,1F4,378,157)
(000,200,000,000)	\mapsto	(395,295,38D,129)
(000,000,001,000)	\mapsto	(15E,23B,378,376)
(000,000,002,000)	\mapsto	(0D0,34D,18C,354)
(000,000,004,000)	\mapsto	(084,128,167,20B)
(000,000,008,000)	\mapsto	(1C7,3F1,063,33C)
(000,000,010,000)	\mapsto	(141,222,031,28A)
(000,000,020,000)	\mapsto	(009,1D9,3CC,131)
(000,000,040,000)	\mapsto	(169,1A1,02D,39B)
(000,000,080,000)	\mapsto	(0C8,111,34B,38E)
(000,000,100,000)	\mapsto	(263,36C,361,369)
(000,000,200,000)	\mapsto	(0A6,050,36D,016)
(000,000,000,001)	\mapsto	(015,371,2DC,0E2)
(000,000,000,002)	\mapsto	(04A,1EC,1B6,3B4)
(000,000,000,004)	\mapsto	(2BE,1DD,223,1FA)
(000,000,000,008)	\mapsto	(322,319,244,300)
(000,000,000,010)	\mapsto	(19A,0E6,364,0F2)
(000,000,000,020)	\mapsto	(13C,355,058,07F)
(000,000,000,040)	\mapsto	(211,2D9,1B2,362)
(000,000,000,080)	\mapsto	(14F,3D2,0E2,1C7)
(000,000,000,100)	\mapsto	(005,38F,215,2DF)
(000,000,000,200)	\mapsto	(03D,208,27E,249)

 Figure 4: Specification of M^{-1} .

S_0	.0 .1 .2 .3 .4 .5 .6 .7 .8 .9 .A .B .C .D .E .F
00.	0BA 026 0AO 1E1 183 3DB 1A4 083 110 350 085 2E5 3B4 195 359 286
01.	33A 26B 209 217 1CE 2E3 0C0 136 129 0C8 3D6 054 040 3F2 09F 322
02.	11B 07F 139 07D 2CF 02A 268 227 246 1C5 12B 3B6 16C 20D 1E7 35B
03.	313 0CD 11E 1E6 117 355 182 0E6 094 1B9 19C 2B9 336 0A9 19D
04.	2BC 1A9 31B 02E 282 2AE 272 2B9 3AA 1DD 013 2D3 30F 35A 159 1BB
05.	11C 12A 248 3C7 28B 191 025 173 018 38D 1A1 185 007 156 378 312
06.	0C9 143 05D 3FA 038 3DE 081 0F9 2D1 3FB 1C7 3E0 1DC 16A 2D8 23F
07.	030 1EB 3AF 311 36D 3BD 3C9 348 261 1AF 071 3EE 3BA 3AB 1B8 3CA
08.	22B 11B 279 0F6 3FF 122 1B2 360 1D6 1B6 3D4 3B3 3B3 0EA 097 308
09.	3A9 086 0AE 15A 253 058 0BD 3D5 01D 1A3 23E 053 35D 277 384 0E2
0A.	233 2B8 0BF 0D0 1B1 105 0B3 215 2A2 27F 2DB 17E 12C 3A2 18E 2AC
0B.	321 09C 294 0AC 036 2F1 3D2 18D 349 128 069 198 2F4 3DC 370
0C.	138 324 23C 1FD 082 247 005 0A3 0F0 273 152 178 1A0 1C8 04E 34C
0D.	12F 0CC 075 10E 290 021 1AE 211 3E6 17A 276 289 3B5 123 01F 048
0E.	201 08F 29A 002 179 32E 120 1AC 1E3 109 079 37C 297 096 12B 323
0F.	165 0AC 1B8 0AB 1FF 230 25B 3D3 111 07E 21C 1B8 187 30E 3A4 318
10.	269 343 29F 395 1AD 1D2 023 2DE 1B3 35E 2D7 044 206 3F1 310 0A7
11.	287 3C3 2A5 213 3E4 3DA 0FD 140 3E8 2C2 154 254 15F 02C 1FB 1ED
12.	1C6 051 062 090 214 1B4 190 15D 0A1 186 032 0B9 1DA 239 3D1 383
13.	331 06D 02D 009 2FC 3AD 2AA 363 1EF 38F 39A 2DC 3BF 106 39B 31F
14.	03E 0DE 1BC 067 0CF 155 2CE 240 05E 0E8 0C4 149 08C 3E5 2A1 150
15.	1D1 22B 3DF 0E0 3F3 193 19B 27D 2B0 35C 0E3 171 180 022 008 358
16.	161 0EE 365 15B 0C3 2CD 3E1 06C 119 283 0F1 3B9 212 226 076 382
17.	38C 1D3 15C 0B2 22C 314 056 216 364 3DD 1E9 020 176 389 2F2 073
18.	06F 27B 027 14E 177 26D 1B8 0EC 25A 194 3C6 2F9 221 0E1 3F4 087
19.	14F 293 144 0FB 2F0 3ED 0F4 1CC 0C6 065 028 315 3E2 2DD 274 0FA
1A.	0D3 041 080 2C5 072 08D 339 2A3 1F1 1DF 2F5 267 015 0B1 275 21B
1B.	091 03F 259 18F 1C3 27B 319 153 0D2 0BD 2B0 064 000 379 2F6 2A9
1C.	142 0F5 3EF 03B 3F8 344 3BC 265 0E7 334 238 08E 347 174 18C 162
1D.	112 1D0 01C 292 2C0 0E9 2B6 301 0C1 30D 369 1C0 1E4 1F7 08A 2FA
1E.	3CB 34D 2BE 28F 09A 3D2 293 262 333 2F8 397 2C4 06E 27A 317 017
1F.	327 26C 325 167 05B 36C 362 004 3F7 0F7 20B 22D 222 2D0 0CA 196
20.	33F 3B2 17D 302 146 170 367 18A 1DE 0B5 099 3B2 2C1 0BC 2A0 01B
21.	11D 010 342 169 366 2BC 088 361 291 131 2FF 199 1CA 3B0 008 24F
22.	287 063 3EB 281 0A5 070 1CB 07B 270 2CC 398 32B 1C1 396 278 39E
23.	160 0FF 1A2 0D4 024 24B 178 1BD 326 2EF 28D 392 21F 24A 10B 042
24.	141 256 229 21B 0E8 260 145 050 035 0E5 300 3AE 1E2 34E 223 20A
25.	164 02F 0C5 210 1A6 258 3F5 32D 184 2EA 1C4 3D0 381 371 2D9 101
26.	3C8 3F3 1F2 10F 0D1 1BF 2D6 320 390 25E 249 341 33B 203 087 23A
27.	09E 095 2C8 3A6 0F2 263 108 307 3E8 3C4 2B8 14C 36E 13E 2C9 37E
28.	014 00F 0DA 133 163 05C 0AA 1E5 019 37D 043 1FC 184 07A 3FE 03D
29.	0FE 25F 26E 3B7 135 2E8 3B1 1B7 012 2C0 02 113 001 271 1D8 01A
2A.	16F 1C9 0AD 236 299 3CF 3EC 24E 3F0 1D4 3CC 2B7 203 338 1B5 25C
2B.	181 052 243 1F3 11F 2EE 332 034 03A 284 34F 031 305 006 124
2C.	13F 13C 19E 3A0 17C 2E2 3C6 345 3CD 0EF 205 31A 23D 06B 059 19F
2D.	1B0 3D8 3F9 103 337 0BD 14D 353 127 0CE 385 114 107 307 057 288
2E.	04F 2B2 2CB 039 234 285 2E1 32A 1B5 111 116 37B 3A5 092 333 373 17F
2F.	21E 2AB 37F 2F2 2ED 2B8 1EA 125 208 16E 33C 0A9 2F3 3C2 3C1 21D
30.	11A 0A4 3EA 047 157 25D 1D9 10A 16D 20E 098 2B1 340 22E 241 078
31.	1F5 0ED 31E 298 3A7 30C 1CF 051 351 0E4 335 046 151 24C 1EE 235
32.	12E 2A6 1A5 061 3A1 29C 011 066 093 03A 38A 1F8 1P0 084 134 356
33.	225 20C 3D9 2E4 0A8 0BE 1F6 0C7 377 2F7 07C 074 045 1E8 05A
34.	36B 36F 3TE 375 04F 1FA 257 13B 089 220 399 00B 158 2D5 068 280
35.	357 0DD 0BF 1B0 2A7 23B 255 3FC 00A 330 240 200 016 008 126 0A6
36.	09B 37A 284 2D4 0F3 28E 237 31D 0DF 368 386 060 374 31C 033 26A
37.	100 394 1F9 04B 391 39F 30B 00C 077 2EB 3E3 231 29B 049 202 224
38.	132 2DA 2A8 286 06A 189 130 13D 1EC 29D 104 387 32F 316 207 137
39.	0DC 02B 1D7 21A 354 39C 0B6 329 285 3A4 0D9 245 2B3 0D6 33E 252
3A.	0CB 1DB 172 296 192 04A 244 250 1F6 2AD 2C6 346 09D 388 328 3A3
3B.	2C7 3E7 29E 3C0 0D5 22A 1F4 168 3FD 242 102 3C5 0F8 251 264 2DF
3C.	27C 029 003 38B 10C 380 10D 295 303 197 1CD 219 13A 306 166 304
3D.	175 19A 0D8 2B8 0A2 26F 3B8 1C2 148 30A 08B 24D 1A7 121 156 372
3E.	0B4 266 22F 2FE 0B0 055 01E 3AC 1A4 2E0 34B 1D5 3E9 393 2E7 037
3F.	20F 0D7 1A8 1AB 16B 36A 352 204 2BD 08B 147 1AA 35F 03C 309 33D

 Figure 5: Specification of the S-box S_0 .

S_1	.0 .1 .2 .3 .4 .5 .6 .7 .8 .9 .A .B .C .D .E .F
00.	021 09B 37A 3AB 0DF 016 1FE 004 07C 3BE 141 397 300 185 00C 1A7
01.	2FA 3AA 235 0B9 003 3CF 14A 18F 356 363 173 2E4 168 0CF 373 379
02.	2CA 326 16B 393 283 2E0 2B9 3E9 12F 247 3D8 07B 288 146 30F 267
03.	15C 01B 22C 0F8 10F 35D 367 343 1EC 047 008 062 2CF 3D6 36B 148
04.	0B4 2E3 25E 234 0D2 1F8 184 2FF 2EB 2BB 3A1 34F 312 10B 2EA 04D
05.	1B1 2FE 084 229 216 337 0D4 08D 21F 035 164 32A 1AA 182 24B 1BF
06.	245 257 01E 34E 375 197 292 1DD 14D 190 27E 13B 137 3A3 228 392
07.	010 34C 389 114 3B9 2B8 325 210 1E7 30B 388 1A1 094 088 038 1C2
08.	305 38E 112 0AA 01B 260 3C1 104 30E 3D4 0EF 079 347 382 22E 09D
09.	186 087 278 20D 2B5 060 215 2C6 3E0 055 3F9 179 252 1B5 105 368
0A.	029 1E9 2C4 2C5 037 233 204 133 3BD 20B 37D 1AE 03D 116 1B2 2F3
0B.	266 333 08F 050 1B9 328 26F 1EA 1A9 0E6 291 2ED 05E 162 1EE 362
0C.	15B 351 20F 17D 085 2D5 259 271 14F 2F5 011 3E7 14B 391 248 082
0D.	119 3CD 160 23B 06A 0D0 3C3 01C 171 3D3 349 061 16F 0FB 1DF 342
0E.	082 068 218 2B9 3B3 225 2F9 230 020 223 151 0C5 2A9 0FE 096 045
0F.	0F2 0D4 03A 015 049 370 14C 255 369 193 3B8 20E 0B1 3A6 039 387
10.	24C 030 315 3CA 0A1 0C6 02C 203 107 115 3F8 244 26C 264 1C6 1C9
11.	123 090 36F 28F 1A3 19D 0E6 317 19B 25C 117 0ED 395 0BF 37E 3E4
12.	04C 3FB 103 2E6 3C8 11E 3D1 279 316 38C 277 286 081 074 213 1F7
13.	3C5 095 2FC 09F 2B5 332 05C 31F 324 09E 2DD 3FC 19F 111 2A7 2B0
14.	091 329 106 10E 012 273 2E4 080 174 2DB 1C7 102 2D3 2EE 1B0
15.	03F 2D4 364 131 0A6 275 004 386 052 3DC 339 11A 211 02A 27F 0DD
16.	318 27B 17B 2D7 1E4 285 0AC 265 2B9 3F4 1EF 093 3BB 307 08E 3B0 0EB
17.	209 2CB 0B8 3A5 129 1CA 027 028 3E6 064 221 125 159 2B7 0F9 37C
18.	054 32D 3F6 031 053 29F 23C 2A1 0D9 237 336 232 1B3 1C1 380 2C1
19.	1DA 360 30C 265 34A 17F 296 3E1 20C 0A2 1F6 207 0F1 040 1D5 026
1A.	200 121 134 2AB 2F2 27D 07E 001 262 27A 1FF 299 3EB 1FA 39F
1B.	253 006 128 3E6 14B 289 0F6 3A8 3D2 261 178 3E5 2C0 0B7 303 181
1C.	097 22A 32E 166 306 0FC 139 138 3BF 1AC 1FD 29B 0AF 041 2CC 0CA
1D.	23B 1F2 25D 0EC 314 20A 03C 120 3C6 0C0 158 28C 3E8 21E 06E 263
1E.	0C4 085 1BD 051 3E2 153 013 0F3 2B6 1A8 17C 2DC 3B7 33C 29E
1F.	0B5 27C 3F2 398 194 099 0A9 320 35A 366 2C2 05D 1F9 226 098 04E
20.	05A 3AC 33E 0E8 0A7 186 1D8 17E 126 32B 110 05F 1A5 390 3CE 1FC
21.	11F 019 3D5 13C 2B2 251 355 065 1F5 3D8 152 07A 086 1B6 308 188
22.	0DC 124 15F 075 2E7 39E 046 302 3ZC 2CE 3CC 3AF 208 066 394 12B
23.	06D 371 2A2 12A 378 319 24D 1D7 3F7 3A2 21D 157 31A 3FF 3B2 2DA
24.	071 318 256 3F3 33D 280 144 08C 21C 058 1CD 2D6 165 3A0 077 354
25.	022 32F 359 28C 374 1EB 30A 192 1CF 1BA 06B 0AO 177 183 28E 2A8
26.	29C 130 323 122 331 201 3B1 0BC 25A 0D8 34B 11B 24F 2E8 1F1 3F5
27.	31C 254 346 376 11C 000 243 0C8 381 0E9 22D 01A 161 3D0 07F 1B0
28.	295 175 04F 3C4 1AA 2B1 191 2F7 34D 36C 2E2 3D7 0F7 18B 0F5 2F6
29.	0C1 30D 02D 1F3 01D 1D3 0D3 1C8 109 2DF 3B8 2E5 18C 0E1 231 10D
2A.	36D 3D8 377 1ID 16D 09C 024 242 072 39B 31D 2C9 149 0F0 089 0A3
2B.	0EA 057 250 2CD 38F 2B0 0A3 169 12D 309 2D8 2A0 358 3F1 1C8 043
2C.	268 2A3 1D6 28A 3EC 18D 2A2 0F8 1D8 037 0D3 274 147 219 02B 2B2
2D.	0CC 13F 383 3D4 3D6 26A 0AB 1D0 301 2A4 350 2F2 0AB 2A6 39A 014
2E.	2D2 352 108 0E3 270 3E3 028 29B 1D8 06E 002 059 0A4 198 23A 044
2F.	0CB 258 348 39C 176 2B4 007 3C2 33F 217 297 073 238 15E 03B 167
30.	288 2D0 340 0F4 0BD 2F0 353 100 18A 29A 399 246 1CB 02B 1A2 2E1
31.	3F0 212 1B7 032 281 357 3A8 048 322 3A9 3B6 33A 196 1BB 1FB 19A
32.	1E2 0A0 101 033 22F 227 0B6 345 0C2 220 07D 298 3EF 0B8 2F1 0DE
33.	304 0E4 202 0D1 21B 005 12C 0EE 13A 0C7 092 00B 05B 009 37B 365
34.	0DB 2AC 27D 39D 3A7 214 338 1A1 335 2DE 1D9 1E5 1C0 3DE 140 24A
35.	2B3 26B 1F0 3C0 3A4 0A4 0A8 2C3 0BA 078 1D4 1E3 16A 145 170 2C8
36.	00B 35B 1AB 127 2BF 16E 2B8 241 1E1 063 334 2B1 136 3EE 3B8 1C5
37.	23D 2D1 042 372 3B4 1E0 0FA 327 0C9 018 1C3 396 3F8 26E 1BC 187
38.	034 3F3 310 118 1D1 076 22B 143 38D 33B 0E5 0D5 3B4 199 3C9 3B5
39.	0E2 195 10A 284 156 150 11D 155 3D 15D 0CD 163 1A0 0C3 10C 35C
3A.	180 1A6 321 00E 276 03E 25F 0D6 189 206 1D0 1C2 26D 205 17A 3FA
3B.	35E 036 35F 2F8 067 2B4 2A5 16C 3D9 2FD 297 18E 113 0FD 313 0E7
3C.	15A 1B8 08A 239 04B 384 083 385 2F4 19C 12E 017 3B 224 135 290
3D.	09A 311 240 13B 0A5 24E 069 3CB 0FF 236 36A 1A4 344 3AB 1E8 31E
3E.	132 23F 222 070 2A8 3EA 249 023 293 0B0 330 21A 28D 1C8 154 172
3F.	1F4 056 00F 2E9 361 1D2 0E0 1C4 19E 282 1B4 3F7 294 142 2D9 0CE

 Figure 6: Specification of the S-box S_1 .

S_2	$\dots .0 \dots .1 \dots .2 \dots .3 \dots .4 \dots .5 \dots .6 \dots .7 \dots .8 \dots .9 \dots .A \dots .B \dots .C \dots .D \dots .E \dots .F$
00.	12E 38B 18E 131 039 10D 2DE 246 286 2BE 315 384 21D 142 06D 0CA
01.	2A2 2CE 264 085 374 3B9 1B7 3E6 3BC 207 002 392 185 0BA 318
02.	39C 2EE 1DA 125 019 063 27E 126 19A 082 305 0E3 206 0AO 009 3C6
03.	100 3F3 2AD 199 102 108 1DB 2F0 310 245 0A8 116 022 3C1 028 332
04.	1E1 2E7 0DA 2B7 0CB 07C 2A0 240 150 165 258 2C8 0C4 334 36B 2D1
05.	1E0 138 39A 0FF 1A7 10C 353 19B 171 038 3BD 000 3A2 1B8 282 2EB
06.	1D4 3D4 20F 23C 0D7 154 012 0DF 3A8 237 09E 155 2E2 189 2F2 136
07.	1B4 381 273 123 052 12C 158 033 2D2 3D3 23B 3B8 2F7 160 341 124
08.	337 1E6 3BE 327 1D3 045 2E4 107 1C2 263 2A4 2CF 244 196 36A 16D
09.	0A1 2C3 004 049 209 3A3 221 361 01E 1B0 05D 319 21B 249 2B2 399
0A.	198 26A 080 1B1 340 28A 33C 316 0FC 37F 1A8 134 17F 3DF 34F 3E5
0B.	2D9 32A 34A 1D1 09D 3FB 0BE 3EA 383 036 3B6 222 22E 286 3A6 0FA
0C.	1C1 0B2 113 3E8 129 34C 153 333 07E 01F 01D 213 299 0F8 130 1B9
0D.	1B2 0A2 1A1 3D5 119 10F 24C 020 097 3F0 280 112 04C 14D 1EB 307
0E.	386 0AE 322 2FE 053 3D7 1AF 345 05B 2F5 110 1C8 03C 1C5 35A 0CO
0F.	3F1 15B 338 1CB 0F4 284 00F 3A1 242 03D 29D 1B3 003 114 3FA 313
10.	35F 217 261 2C1 15D 28F 390 1C9 1DD 3C7 14F 11D 066 04D 03B 0E9
11.	2B4 2FD 347 191 044 0B8 194 256 360 326 257 1A4 396 098 2CD
12.	1E7 3CD 1FF 269 040 3E7 08A 216 0C9 33B 3D9 1BC 2B1 325 11B 16F
13.	053 22A 186 180 27D 11F 2A9 13E 3E1 0D4 24E 1D2 2FC 3C9 1FB 31A
14.	3DE 1D7 025 372 339 2C7 2ED 2F5 0A7 098 2EF 247 0E8 2D3 105 09F
15.	2CC 36D 31F 24B 1D8 241 068 211 20F 0AA 355 35C 026 2BD 238 0EF
16.	35B 233 05A 1B8 291 368 137 035 298 140 26B 1E4 379 07F 3EB 164
17.	20B 12D 375 1BF 12F 1AA 18B 268 3F4 364 0F7 1CC 0B9 3C5 060 19D
18.	22B 17C 11C 0B1 23A 3B4 05F 2F5 219 224 0E5 042 06F 39D 218 023
19.	1DE 177 190 395 274 359 0E2 2B9 397 0F1 010 099 17D 08E 314 317
1A.	0DC 03F 1AC 1A6 132 152 195 3AD 3E9 3C2 1BB 0F0 0CD 074 178 174
1B.	184 3E0 389 2F2 1A8 087 250 27B 06C 13B 0FB 296 297 30F 350 14E
1C.	007 10E 19C 055 351 034 175 103 272 02D 2C0 21C 047 20D 0EA 29B
1D.	13F 1DF 162 376 0BF 1CA 3EC 2B9 3FE 388 133 0A9 33A 304 1FE 059
1E.	13D 0BD 294 02B 127 18B 275 07B 1C4 018 031 0C6 0A3 0E2 27C 087
1F.	38D 3B0 284 1FA 1F5 00A 3E2 02E 228 285 34B 311 075 2F1 1C4 094
20.	3FF 202 27F 2F9 30B 135 3F1 301 3B8 2C6 3D2 309 057 073 1F1 289
21.	3B5 3C5 111 0B4 20B 18A 1F7 24A 394 157 366 336 39B 017 25C 3C4
22.	1EC 2BC 144 1E9 193 16A 33D 344 295 079 027 2D4 38A 17A 292 0AC
23.	0F2 35E 1EF 0BB 106 071 2DA 3F7 084 037 2AB 330 0B0 2DB 0TA 22D
24.	00C 149 0AF 290 2E0 122 283 32E 3AE 3C3 1D9 2E5 3B7 0BC 265 32D
25.	089 2CB 115 081 18A 255 05C 1A3 287 0D0 276 32C 0C3 30B 226 1C0
26.	2F3 0A5 121 2AA 210 091 20B 3EE 230 320 385 2B1 21E 3F9 11E 05E
27.	159 281 0C8 37C 0DD 188 04F 26E 33E 2F8 3A0 3B3 3C8 227 1A2 3AA
28.	302 36B 3F8 19E 212 13C 24D 0B3 141 3EF 1CE 262 145 362 346 176
29.	1E3 14B 3A9 3DD 093 3F8 070 0D3 1EA 3B4 248 146 201 243 1F6 205
2A.	1CD 20A 2F6 00E 267 26D 2A7 1FC 2D0 0D1 38E 006 30A 3E3 2C5 28B
2B.	2D5 3A1 7D5 3A4 101 2D7 34B 2B5 072 26C 090 1F8 1F9 3AF 1FO 0C2
2C.	2C2 21A 06A 0AB 109 16B 156 161 38C 156 271 279 369 342 1D6
2D.	01A 016 352 173 34D 354 181 185 1A5 23F 16C 030 215 1C3 2EA 0CF
2E.	0DE 078 1B0 01B 117 393 3F2 39E 37D 1B2 24F 18C 29A 04A 08D 187
2F.	015 065 0C1 251 00D 348 014 21F 001 008 2CA 321 1B2 186 043 147
30.	223 0B6 054 1AB 0FD 373 31E 323 20C 151 1OB 288 2DF 041 349 2E3
31.	32F 0ED 277 179 27B 3F6 23B 252 077 0A4 120 200 308 300 312 04B
32.	1ED 048 30C 183 0D2 39F 3B7 0AD 3FD 204 050 1C7 197 3B7 046 04E
33.	1F3 343 051 1F2 169 266 25A 26F 0F3 2B0 095 17B 31B 0F6 0E6 2DC
34.	225 36C 377 253 058 0E1 021 31C 3D6 1AD 167 2AC 06B 23D 398 032
35.	35D 2FA 00B 391 239 0F5 335 02C 083 143 02A 29E 36F 214 104 14A
36.	0E4 096 19F 2E1 1FD 30E 28D 07D 11A 0EE 0EB 370 358 1DC 163 056
37.	367 03A 2D6 363 229 3DA 08B 1E5 270 2E8 2FF 168 10A 2AE 170 28C
38.	2A3 08C 1CF 076 3D1 32B 2EC 2A5 2C9 2A6 29C 3ED 09C 0CC 2A8 203
39.	0FE 293 29F 2F4 0E7 232 0CE 3AB 13A 011 3DB 220 0D8 1F4 22F 236
3A.	062 1A4 27A 128 329 324 067 365 024 2B8 3E4 0D6 3AC 3A5 172 306
3B.	16B 0DB 3C0 25B 088 2D8 303 380 259 2A1 1E2 0B5 02F 029 356 2BF
3C.	2C4 03E 2BB 3B1 17E 3CC 01C 25E 2B3 069 0A6 15C 0D5 3DC 118 2E6
3D.	2DD 235 18F 371 064 260 0C7 0EO 0C6 1D0 254 0D9 37A 387 3CB 234
3E.	3D0 15F 3B2 08F 15A 013 331 328 0E6 25D 0F9 092 166 378 31D 139
3F.	005 09A 12B 061 231 1A0 3CF 3CA 382 192 086 357 22C 12A 3FC 37E

 Figure 7: Specification of the S-box S_2 .

S_3	$\dots .0 \dots .1 \dots .2 \dots .3 \dots .4 \dots .5 \dots .6 \dots .7 \dots .8 \dots .9 \dots .A \dots .B \dots .C \dots .D \dots .E \dots .F$
00.	200 084 1B5 30A 25A 151 174 3F9 113 3B4 35B 291 332 170 021 31E
01.	00E 2FC 023 0B0 3A9 259 2BC 378 031 050 0D0 1FF 26C 0D5 214 23E
02.	1AB 0AB 3AC 036 0E2 2F6 07A 0EA 2CB 0FF 24E 280 138 073 219 3EA
03.	2B2 27C 032 162 285 13C 0B6 1ED 0B3 2F5 2C6 34B 335 1EF 26E 37A
04.	273 17E 30F 2E7 14B 3BC 1CE 039 315 01A 144 1C4 20A 17B 362 10D
05.	235 1D9 2F9 0A4 052 0E3 0BD 061 02C 140 0E1 156 10E 250 288 1BE
06.	07C 2B8 05D 242 192 0A8 3B0 0DB 129 2AF 063 3AF 3D1 0C8 0A6 029
07.	2B9 3B8 0D2 078 2A2 0E6 2CF 3CF 0EF 0E7 019 1F1 07E 1BB 2C7 251
08.	36A 2CA 076 216 2E5 0E6 1DD 2F2 390 277 1D2 394 2C5 022 05A 096
09.	0F4 265 0FD 150 057 111 2E6 29C 3DF 11F 13A 158 388 1D3 3C8 386
0A.	3B8 279 064 1A4 028 22F 1D5 352 2C8 257 3C4 355 104 322 2C1 382
0B.	1DF 1A9 137 3DC 015 096 2AA 2A4 3F6 1A3 3DA 086 2E8 343 233 11A
0C.	0A5 38B 328 348 292 132 3F4 059 31C 1AC 16C 3BF 1C2 36D 1B8 0ED
0D.	191 3D3 3D4 3DE 0E8 373 034 23C 224 3C5 11E 393 00B 308 2DA 0OF
0E.	209 230 19D 184 1B8 339 360 2D7 011 305 17A 324 344 128 3F0 0F3
0F.	317 0B4 08D 1B8 035 0C9 345 0D3 37D 3CA 284 3EF 0D0 197 36B 06B
10.	0B8 10B 1B8 218 046 32A 2CC 08E 0A6 254 3FC 066 246 24D 232 0A2 145
11.	2DB 199 37F 1E1 392 3F3 1C8 1CD 136 2D0 325 27B 068 1F5 077 22D
12.	12F 2F4 0B2 2E9 3FC 296 2E6 2A16 30D 276 02D 266 09C 255 157 195
13.	3A1 3F2 3D7 130 258 227 0D4 26B 027 1EA 379 329 179 2D5 0C4 09F
14.	39E 09E 1FD 15B 126 2B3 158 012 21A 372 356 154 042 017 217 19B
15.	1F8 261 3ED 14A 1FB 110 037 1B7 079 045 3C9 0EE 2B6 107 3C 302
16.	19E 21D 1E5 205 25F 3BD 196 189 337 069 32E 0DF 3EE 201 0BC 3C2
17.	01D 37B 3C0 0A3 22E 123 2A9 0DE 2A7 2FF 3A5 05B 38F 047 1B4 350
18.	0CB 0A1 29D 1FC 024 29B 3A2 2A1 3B8 215 09A 37E 2A0 0C2 377 0B1
19.	149 33B 323 365 3D6 2E3 082 35A 38C 0D7 134 3D0 36E 336 334 1F6
1A.	1DC 3B2 2B1 213 3F1 1FA 380 0E6 020 211 033 28D 0DA 34C 20C 1A8
1B.	28F 369 349 3F5 2B1 1FC 383 387 35B 08E 29A 135 3A7 2B0 346 30E
1C.	163 33C 32F 093 0FA 125 244 226 1C1 1EE 1A2 252 189 3A0 146 3D8
1D.	148 353 0FF 37C 09D 2C0 268 048 117 1E3 2A6 003 11B 0AD 1D7 313
1E.	072 18D 297 39A 0CT 12D 18B 016 222 056 1CB 287 095 366 293 3E0 354
1F.	13E 299 190 10F 2B3 183 080 186 361 3AA 3E1 318 2B4 15C 0D8 1DB
20.	342 2EE 1AE 04F 1A7 2CD 2F8 03A 06A 0BA 188 090 2B7 1E4 16F 0C5
21.	1B0 2D2 1CC 3B9 267 153 24B 1E7 20B 0FC 266 0F7 3B8 376 1C7 0D9
22.	00C 271 0A1 1C5 357 1E8 01E 3FE 081 245 314 294 164 13F 212 340
23.	141 1B9 120 02E 34F 0E4 092 26A 171 249 22B 206 0CO 001 0AO 23F
24.	02B 2B6 06F 05B 27C 20E 3B3 12A 28A 100 2AC 22A 263 0F9 1C0 21B
25.	203 303 35C 295 088 008 3E5 0DD 307 105 121 185 0A7 3EC 11C 347
26.	094 39D 1B2 02A 3B1 204 114 312 167 131 304 290 231 3E7 2D3 3D2
27.	2C2 32C 3E6 04A 009 10C 327 1B7 2D1 1BA 2FD 35B 253 2EF 2B2 3D9
28.	338 14F 1B1 2B8 330 2F0 18C 175 12B 169 2D9 223 2F3 255 0C3 13D
29.	398 15F 16D 2DC 2BD 0FB 3FA 2ED 147 161 01B 04B 17D 28C 058 3C1
2A.	146 21F 1DA 0E9 124 2BF 39C 005 054 35F 143 3CE 19A 043 36F 1F3
2B.	0CF 28E 1B8 243 006 106 333 152 1BF 3F 3B7 1EC 30B 098 0BE 1D1
2C.	089 3CD 1F0 210 2B9 30F 2F7 1B3 20D 3AD 02F 0EC 11D 06D 3AB 38E
2D.	311 1E6 3F8 0AF 2E1 1ZB 220 03D 0F1 2FA 208 16C 28E 181 33A 119
2E.	109 10A 0CA 2A5 010 31F 3B8 0F7 3B5 2D2 193 2A2 283 085 0OA 32B
2F.	2A8 3AB 1D0 2F1 0EB 2DF 298 1DE 065 17C 18F 364 33E 0B8 2C6 1F2
30.	289 142 1B2 0D6 3E2 24C 101 2A4 39B 09B 097 1A0 229 375 320 062
31.	33D 118 3EB 03C 15A 281 1A1 207 3C7 331 319 274 127 34E 07B 239
32.	23A 300 0B5 01C 2B5 1E0 3F9 180 321 133 26F 371 1B3 363 26D 0F5
33.	0C6 165 0F6 19C 070 0E0 367 002 247 389 053 27F 2D6 2B4 3D9 29E
34.	30C 1AD 0E5 22C 15D 2E0 013 236 2A3 228 0BB 14D 018 278 155 1C9
35.	178 0CD 370 07D 3A6 23B 2F4 049 2D4 397 0BF 1B8 21E 399 3F8 0AC 004
36.	34A 055 04D 14C 33F 1F7 301 05C 3A2 112 2DE 075 3F7 391 040 326
37.	2D8 000 0DC 001 041 14E 067 160 166 168 051 0A9 31B 0CC 16E 172
38.	1CA 2C4 3C3 1E2 03F 173 27E 08A 25D 1F9 014 17F 044 16B 2F2 176
39.	31D 3E9 108 139 2C9 04C 187 071 29F 381 316 038 0CE 2C3 34D 1AA
3A.	122 225 1C3 04E 368 351 202 38A 102 189 194 304 026 0F0 248 08C
3B.	05F 19F 2B8 270 060 083 186 3D3 2A6 0C1 23D 272 241 0F8 1EB 01F
3C.	374 177 3E4 358 1FE 099 2AB 1D4 3A4 310 030 1AF 1F4 0BE 074 16A
3D.	274 1D6 21C 3FD 3C6 238 234 262 3D5 31A 395 27D 3E8 240 1A5 087
3E.	32D 359 341 25C 0B9 115 237 0F2 2E4 12C 103 025 20F 260 3AE 269
3F.	07F 03B 03E 007 182 159 091 3B6 3E3 384 264 385 36C 256 221 24F

 Figure 8: Specification of the S-box S_3 .