

Parallelized Flight Path Prediction using a Graphics Processing Unit

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Abstract: Summarized under the term Transport-by-Throwing, robotic arms throwing objects to each other are a visionary system intended to complement the conventional, static conveyor belt. Despite much research and many novel approaches, no fully satisfactory solution to catch a ball with a robotic arm has been developed so far. A new approach based on memorized trajectories is currently being researched. This paper presents an algorithm for real-time image processing and flight prediction. Object detection and flight path prediction can be done fast enough for visual input data with a frame rate of 130 FPS (frames per second). Our experiments show that the average execution time for all necessary calculations on an NVidia GTX 560 TI platform is less than 7.7ms. The maximum times of up to 11.7ms require a small buffer for frame rates over 85 FPS. The results demonstrate that the use of a GPU (Graphics Processing Unit) considerably accelerates the entire procedure and can lead to execution rates of $3.5\times$ to $7.2\times$ faster than on a CPU. Prediction, which was the main focus of this research, is accelerated by a factor of 9.5 by executing the devised parallel algorithm on a GPU. Based on these results, further research could be carried out to examine the prediction system's reliability and limitations (compare (Pongratz, 2016)).

1 INTRODUCTION

Customer needs and requirements are becoming increasingly personalized in almost all product fields. Manufacturers have to produce a large number of products that are similar, but not completely identical. As not every personalized product has to pass through the same production stages, the currently used static conveyor belt no longer matches the application profile; more flexible types of product lines are needed.

Transport-by-Throwing (Pongratz et al., 2012) describes an alternative solution whereby robot arms pass on their payload: one throws it, and another one catches it. Just as with communication networks with hop-by-hop routing, passing is repeated until the transport good reaches its final destination in the production process. Despite many novel approaches, a fully satisfactory solution to catch an object has not yet been developed. In the last 25 years, many other studies (Bäumel et al., 2011; Hong et al., 1995) have been concerned with the topic of catching a thrown ball, but the best results achieved a success rate of about 80% or less. All of these studies has one fact

in common; the predictions are based on a model of the involved physical laws. Pongratz *et al.* propose a strategy based on memorized trajectories (Pongratz et al., 2010; Pongratz, 2016).

The hypothesis is that humans learn object-catching based on experience, for example, the way a child learns to catch a ball. It does not contemplate about physics when trying to catch. A child only learns from its experiences: after numerous failed attempts, it is able to catch an object in the right way based on memorized previous experience. By analogy, in the approach proposed by Pongratz *et al.* the ball's flight is captured and compared with a set of stored reference (Figure 1) throws to enable prediction of the trajectory and the location where the object can be caught (Pongratz et al., 2012). Although the execution time of the prediction is as important as its accuracy, its real-time constraints have not been examined until now (Pongratz et al., 2010). If the estimation algorithm takes up too much of the processor's capacity, the computation time will interfere with the camera's sample rates (Hong et al., 1995). Image processing, as well as the comparison of the determined

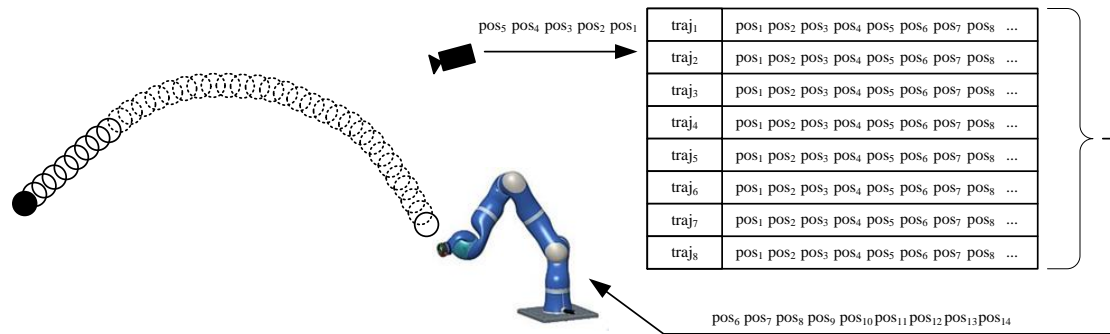


Figure 1: The Transport-by-Throwing approach deals with a robot arm that catches thrown objects with the help of a prediction based on stored trajectories.

data with all the numerous database entries, require a huge number of calculation steps. Managing the massive amount of computation in a short period leads to the necessity of employing high-performance hardware/accelerators. An FPGA (Field Programmable Gate Array) based implementation can accelerate the procedure (Pongratz, 2009), but this would result in higher development costs. A GPU (Graphics Processing Unit) can speed up the software wholly or partially by parallelizing the operations (Fung et al., 2005).

In this paper, we deal with such real-time constraints and deploy GPUs for performing both object detection as well as flight path prediction. The here stated results shall enable examination of the system's accuracy in future works.

The rest of the paper is organized as follows. The concepts and the setup are described in Section 2. Section 3 shows our implementation of the RANSAC algorithm and the flight path prediction. In Section 4, we present and discuss the results from our experiments. Finally, Section 5 concludes the paper.

2 SETUP AND CONCEPT

The ability to catch a thrown object requires knowledge about the trajectory and other attributes of the motion of the object (Barteit et al., 2009), which we gather with cameras. The thrown object is a tennis ball with a velocity from $4.6 \frac{m}{s}$ to $5.4 \frac{m}{s}$. The light system consists of multiple floodlights and results in a sufficient illumination of the whole scene. Changing light intensity is compensated by a light profile for the algorithm which influences the thresholds of the detection algorithms. The distance of the ball to each camera is in the range of 0.6m to 3.2m. Figures 2 and 3 show the experimental setup that is briefly explained here in this section.



Figure 2: The Throwing-and-Catching test environment consists in a robot arm, multiple LED floodlights, two parallel aligned cameras, and a throwing device that accelerates a tennis ball to overcome the distance of about 2.5m.

2.1 Capturing the Scene

Obtaining a 3D view of a scene using only one camera potentially results in low-level accuracy and robustness (Bäumel et al., 2011). Therefore, we opted to use two cameras (IDS uEye UI-3370CP) working synchronously and manually aligned in parallel with a baseline distance of approximately 0.92m. These two cameras support a resolution of 2048-by-2048 pixels at a frame rate of 75FPS (frames per second) and 2048-by-800 pixels at 110FPS. To predict the flight path in time while still having the advantages of this high resolution, a cropping system based on Binary Large Objects (BLOBs) detection was used that provides output images with only 300-by-300 pixels where the ball is roughly in the center.

The following hardware was used for image processing and flight path prediction: a computer with an i7-4770S CPU clocked at 3.10GHz, 8GB main memory clocked at 667MHz and an NVidia GeForce GTX 560 Ti graphics card (NVidia, 2015) with 384 cores (with compute capability 2.1). This GPU fam-

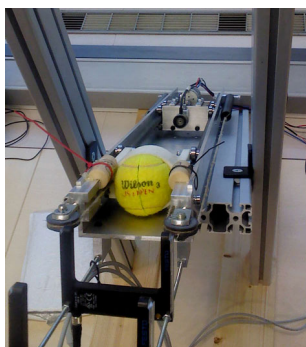


Figure 3: This coil-based throwing device accelerates a tennis ball to overcome the distance of about 2.5m.

ily was used as it is a rather standard representative of GPUs in general. Other - more up to date - GPUs would change the specific figures but not the general trend and conclusion. Besides, Intel claims that its integrated GPUs are starting to get equal with discrete graphics cards¹. To have also some results for Catching-and-Throwing devices based on embedded system, we chose this - weak - graphics processor.

2.2 Detecting the Flying Object

After a coil-based throwing device (Figure 3) accelerated the tennis ball, it appears on both camera images. Various methods for detecting circles exist (D'Orazio et al., 2002) but two of them are well-known, distinguished by their accuracy, and often used for object detection: the Hough Transformation and the RANSAC algorithm. Both procedures perform efficiently when images are not noisy, but the Hough Transformation was highlighted as being more accurate when detecting objects in the presence of noise (Jacobs et al., 2013). On the other hand, the duration of this algorithm depends on the number of pixels in the edge image (Wu et al., 2012). One circle is drawn in the Hough Space for each possible radius around each edge pixel. Therefore, the more pixels present, the more time is needed. In comparison, the time required by the RANSAC algorithm only depends on the number of iterations. The algorithm chooses randomly three points to span a possible circle. In other words, only one circle is drawn per iteration; not for every possible radius as it was for the Hough Transformation. Since the number of iterations needed is much less than the number of edge pixel multiplied by possible radii, the RANSAC algorithm performs typically faster.

Both algorithms require an edge image for detecting objects in an accurate way. We use the Canny

¹<http://www.extremetech.com/extreme/221322-intel-claims-its-integrated-gpus-now-equal-to-discrete-cards>

Edge Detector algorithm since it achieves good results and is commonly used (Luo et al., 2008). Its implementation is carried out in four steps: Gaussian filtering, Sobel filtering, non-maximum suppression, and hysteresis thresholding (Ogawa et al., 2010). The first three procedures are linearly separated in x- and y-direction so that they run efficiently on parallel hardware (Luo et al., 2008). In contrast to these steps, the hysteresis thresholding is an iterative algorithm. Therefore, this step is not parallelizable and limits the performance of edge detection.

To improve the quality of the edge images, the images' backgrounds can be subtracted as an additional step. Changing lighting conditions may lead to a non-perfect background subtraction, but the edge images and consequently the detection is still more accurate.

2.3 Flight Path Prediction

After the ball's center point has been detected in both images, the triangulation step converts these two positions to one 3D position. Due to the imperfect alignment of the stereo vision system, the distortion of the cameras, and other effects, the vision system has been calibrated with the help of a Matlab toolbox². The result of the calibration process are the intrinsic parameters of the individual cameras (e.g., focal length, distortion coefficients) and the extrinsic parameters of the stereo system (baseline and orientation).

Since every pair of frames offer a new position of the thrown ball, its movement in space and time is known. From that moment, we can start the prediction of the ball's further flight path. Figure 4 shows two different approaches for estimating a flight path based on this technique: either comparing the ball's positions with their counterparts in the database directly or comparing the rates of change from one position to the next. Because of the high similarity of both versions, we introduce only the former. To find the most similar trajectory, the Euclidean distances between each position of the actual flight and its counterpart in the database are calculated. Afterwards all these distances are added up to a total distance, which gives information on how well the actual flight matches a database trajectory. The database trajectory that leads to the smallest sum of distances is the most similar trajectory and is, therefore, selected to predict the flight path of the thrown tennis ball. One challenge of this algorithm lies in the enormous number of possibilities to fit the actual flight in a reference trajectory. Four examples of possible flight paths compared with one and the same trajectory of the database are shown

²Available at: http://www.vision.caltech.edu/bouguetj/calib_doc/

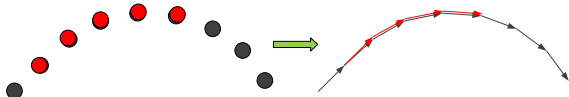


Figure 4: The two prediction approaches: comparing directly the balls positions, or comparing its rates of change from one position to the next.

in Figure 5. While the first example represents a fairly good match, the second example shows a lack of congruence between the two flight paths. However, the reason might be that the actual flight's positions are not present in the database trajectory which still fits best (examples 3 and 4 of Figure 5).

2.4 Software Development Environment

Two options for programming a GPU exist: CUDA (Compute Unified Device Architecture) (NVidia, 2014), which was developed by NVidia in 2006 and OpenCL (Open Computer Language) by the Khronos Group (Khronos, 2015). We selected CUDA as development environment because of its better performance (Karimi et al., 2010), and a more comprehensive documentation.

3 IMPLEMENTING PARALLELIZED FLIGHT PATH PREDICTION

Based on the edge image object detection is performed. Because the background subtraction is simple to implement and parallelized algorithms for the Canny Edge Detector (Luo et al., 2008), the Hough Circle Transformation (Askari et al., 2013; Chen et al., 2011), and the RANSAC algorithm (Wang et al., 2011) have been reported before, we do not describe their implementation in detail. Instead, we focus on the flight path prediction. We show the performance differences of all algorithms in Section 4; also the comparison of the straight-forward and inverse-checking version of the Hough Circle Transformation (Askari et al., 2013; Chen et al., 2011).

To enable database access as fast as possible, an initializing function loads all reference trajectories and stores the data in the GPU's memory in a 3D array as a first step (similar to (Gowanlock et al., 2015)). These three dimensions are needed for the different trajectories, the trajectories' various positions, and the positions' various coordinates. The size of the GPU's memory limits the number of reference throws, but as has been shown (Pongratz, 2016), small databases also lead to acceptable catching results.

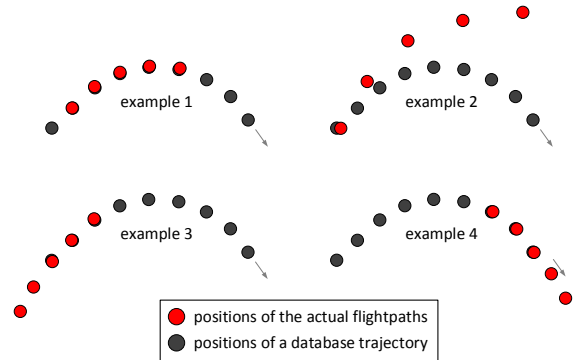


Figure 5: Four examples comparing actual flight paths with the same database trajectory.

The challenge of the flight path prediction algorithm lies in the enormous number of possibilities to fit the actual flight in all reference trajectories. On the one hand, many reference trajectories exist that have to be compared with the actual flight, and on the contrary, many different possibilities exist on how to fit the actual flight in a reference trajectory (Figure 5). Next we describe our algorithm which makes use of the parallel architecture of a GPU.

To examine every possibility, the actual flight's positions are shifted over the various trajectories of the database. Additionally, the possibility must be included that not all the actual positions are aligned with their counterpart in the database trajectory. Figure 6 shows such a shift of one actual flight over one database trajectory. However, since the focus is on a parallelized algorithm, the term "shift" is not completely correct. Each database trajectory is examined in a separate block, and each possible alignment of the actual flight with a database trajectory is examined in a separate thread. Therefore, for each of the database's trajectories one block exists, and for each possibility to fit the actual flight, a thread is needed and created. Since all blocks have to have the same number of threads, the number of required threads depends on the longest database trajectory. Separating the examinations of the various alignments in different threads is equal to parallelizing the act of shifting the actual flight over a database trajectory.

To speed up the whole procedure, all positions of the actual flight and database trajectories are moved from the global- to the shared memory before the distance calculation begins. This step accelerates the procedure because accessing GPU's global memory consumes much more time than accessing its shared memory (NVidia, 2014). However, it should be noted that this extra step may lead to a demand for more threads than alignments of the actual flight that are possible in the database trajectories. This requirement

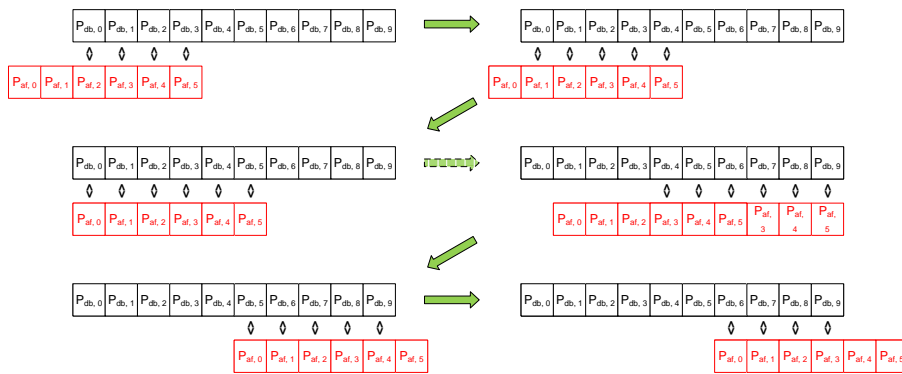


Figure 6: An actual flight path is shifted over a database trajectory to find the place where the sum of all Euclidian distances is the smallest. A predefined parameter decides how many of the actual flight positions (paf) are allowed to be outside of the database trajectory.

is caused by the fact that all points of all trajectories and the actual flight have to be moved to the shared memory to guarantee correct calculations of all Euclidean Distances. So, if there are trajectories with more points than possible alignments, more threads are needed.

Additionally, there is a fact that has to be noted when allowing some positions of the actual flight to be outside of the database trajectory’s boundaries. Distances of an actual flight’s positions that are not in alignment with a database position are not included in further calculations. The fact that the sum consists of fewer addends leads to a smaller total distance. As a result, it might occur that a trial that examines fewer positions, results in a smaller distance, although it fits less well than the one that examines more positions. Therefore, all results have to be normalized meaning that the sum of total distances d_{total} has to be divided by the number of positions that have been considered in the calculation.

4 RESULTS AND DISCUSSION

This chapter provides information about execution times, the detection’s accuracy, and the real-time behavior of the entire program. All presented figures of execution time include the time for processing both images of the stereo-camera-system.

4.1 Canny Edge Detector

We have studied and compared the edge detection with and without background subtraction and found that it significantly improves the quality of an edge image (Figure 7).

The background subtraction does affect not only the accuracy of the edge images but also the ex-

ecution times of the Canny Edge Detector. Figure 8 shows the execution times of background subtraction plus Canny Edge Detector and the Canny Edge Detector without a background subtraction. Performing the background subtraction and the Canny Edge Detector takes slightly more time than creating edge images without subtracting the background when there are no other objects present in the images. In the case of other objects displayed in the image, the Canny Edge Detector without a background subtraction takes up to $1.6\times$ more time than performing both steps combined. This situation is caused by the hysteresis step of the Canny Edge detector which leads to a higher processing time when more pixels are in the image.

The slight slope of the graphs is caused by the ball approaching the cameras from frame to frame. The more the flight advances, the larger the ball is displayed in the images. The more edge pixels in the frames, the more time is taken by the hysteresis procedure. One flight was processed 1000 times in a row to obtain reliable measurements and to capture information about variances in the computation time. Figure 8 shows the minimum, maximum, and average execution times of the 92 frames of a flight.

4.2 Object Detection

Two different approaches of the Hough Circle Transformation have been implemented and compared with each other: the straightforward strategy and the inverse-checking strategy. While threads of the former strategy that are assigned to an edge point have to start a loop to draw a circle, each thread of the latter strategy must start a loop to draw a circle. Therefore, performing the inverse-checking strategy results in an execution time 9.4 to 17 times longer compared with straightforward strategy. The data obtained do not confirm the statements made in the studies (Askari

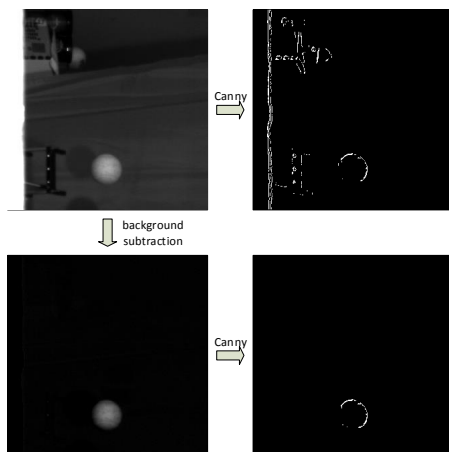


Figure 7: The additional step of background subtraction improves an edge image's quality.

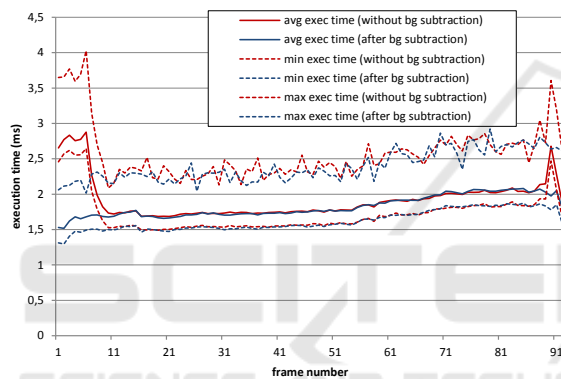


Figure 8: Execution times of background subtraction plus Canny Edge Detector and of the Canny Edge Detector without a background subtraction.

et al., 2013; Chen et al., 2011). Possibly, they included images with a huge amount of edge points, in which case it might be better to perform the inverse-checking strategy. The background subtraction affected the Hough Circle Transformation's execution times as well: detecting the ball with an untouched background took up to $2.7\times$ more time than doing this after the background subtraction step.

Besides, Figure 9 shows that the execution times of both the Hough Circle Transformation and the RANSAC algorithm are almost the same at the beginning of the flight when the ball's image consists in only a few pixels. Afterward, the RANSAC algorithm is executing up to 3.4 times faster than the Hough Circle Transformation.

To obtain reliable statements about the average tracking error of the determined center point to the real one, the results of the Hough Circle Transformation and the RANSAC algorithm were additionally analyzed with the help of the Rauch-Tung-Striebel

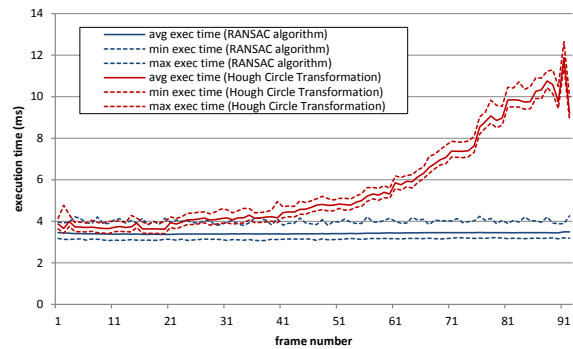


Figure 9: Execution times of the Hough Circle Transformation and the RANSAC algorithm for each frame of an entire flight.

Table 1: Tracking error of ball positioning.

Detection algorithm	Background	avg. tracking error
Hough Circle	subtracted	2.73 mm
Hough Circle	untouched	25.81 mm
RANSAC	subtracted	2.78 mm
RANSAC	untouched	25.96 mm

smoother³. This filter examines the recorded flight path from front to back and reverse, to create a smoothed flight path. This smoothing process corrects physically impossible trajectories. Table 1 shows what Figure 7 had already suggested: Subtracting the background considerably improves the detection's accuracy as well. In this case, the localized position is only about 2 to 3mm away from the Rauch-Tung-Striebel smoother estimated one.

4.3 Prediction

While the accuracy of both prediction algorithms has been examined earlier (Pongratz, 2016), their execution times are presented here. Figure 10 shows the temporal behavior of both methods as functions of the number of reference trajectories. The average and minimum time rise fairly linearly as the number of reference trajectories in the database increases. While the minimum execution time increases very slowly, the average time's graph definitely illustrates the impact of including a higher number of reference throws. This behavior is caused by a larger number of blocks when more trajectories are in the database. The temporal behavior of the two approaches is almost even, but the time required is slightly different. While a database with up to 120 trajectories leads to

³Available at: <http://becs.aalto.fi/en/research/bayes/ekfukf/>

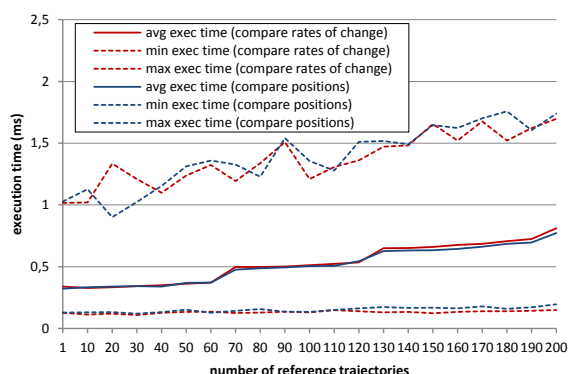


Figure 10: The predictions execution time as a function of the number of reference trajectories for the comparison of positions and rates of change.

nearly identical execution times, a small difference is observed when the number of reference throws increases. For this purpose, the database was filled with 200 dummy trajectories, all with a length of 92, which is equivalent to the longest trajectories of an already existing database. A comparison of the various trials with different database sizes would not be fair.

4.4 Entire Procedure

The best solution for each step was selected to examine the execution time of the entire procedure. Each pair of frames had to run through the following tasks: clearing the GPU storage, background subtraction, Canny Edge Detector, RANSAC algorithm, triangulation, coordinate translation, and prediction.

Figure 11 shows the combined execution times of five different flights that have been processed 1000 times in a row. The shorter time, as well as the rapid increase of the time at the beginning of the flight, is caused by the throwing device, which partially covered the ball. The slight slope of the graphs is due by the ball approaching the cameras from frame to frame. Without our good light profile⁴, which changes the Canny Edge Detector’s thresholds in the course of the ball’s flight, the execution times would significantly increase, and the detection would not work that well. The average maximum time of the different flights was about 7.69ms and enables a frame rate of 130FPS. Because of maximum execution times that were, in rare cases, over 10ms, a small buffer is required for compensation. Without such a buffer, there would not be sufficient computational power for the frame rate of 110FPS of the camera system used.

⁴To counteract the heterogeneity of the room’s illumination (to improve the detection of the ball), we created a light profile by trial and error.

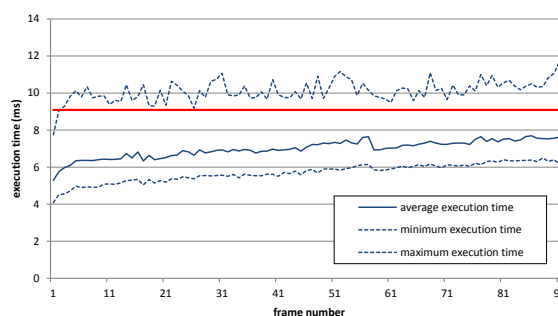


Figure 11: The execution times of five flights were processed, examined, and combined for this chart.

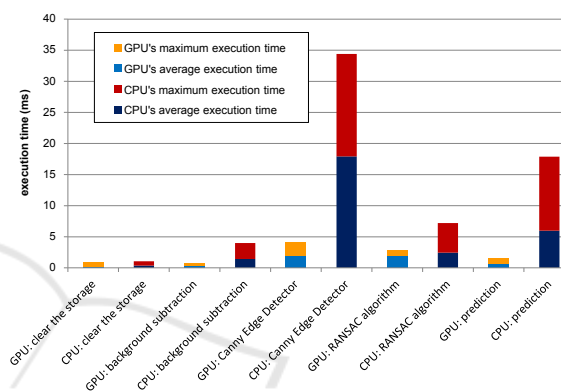


Figure 12: Average and maximum times of the various tasks when performing it on a GPU and on a CPU.

For examining the speed-up achieved by using a GPU instead of a CPU, the entire program was rewritten to a purely sequential approach on a CPU to be executable on a CPU. To compare execution times, one flight was processed 1000 times in a row and the required times for the various steps were measured. Figure 12 shows that the largest increase in speed was measured for the Canny Edge Detector (9.74×) and the prediction (9.55×), followed by background subtraction (5.35×), storage clearing (2.04×), and the RANSAC algorithm (1.26×). In short, a single frame was processed 3.46 to 7.17 faster on a GPU than on a CPU. Hence, this demonstrates that the selected GPU is a viable platform for this application as it gives a significant performance improvement compared with the CPU based reference implementation.

Besides the real-time requirement also the tracking accuracy of the algorithms is a major concern for the application. The achieved tracking error, compared to the Rauch-Tung-Striebel smoothed trajectory, was well below 4 cm for 99 % of the tracked balls over a distance from 0.7 to 3m (Pongratz, 2016).

5 CONCLUSION

One of the main questions here was whether a GPU can perform the ball detection and flight path prediction fast enough to achieve a high frame rate. The results of the NVidia GTX 560 Ti GPU show execution times that enable data processing at 130FPS. Moreover, using a GPU for the required calculations proved to be a beneficial idea. The implemented program was 3.46 to 7.17 faster when running on a GPU than on a CPU; Intel i7-4770S. Using a newer GPU would - most probably - accelerate the whole procedure. However, using this five years old GPU is representative of GPUs in general. Additionally, as earlier mentioned, integrated GPUs also offer computation possibilities. The performance we reached by using the GPU shows that processing this flight path prediction will most probably be possible also on an embedded system with an onboard GPU.

We performed numerous optimizations to enable such high-speed computation on the GPU used. Well-thought-out algorithms and letting some data make a detour over the fast shared memory were the keys to success. However, some constraints still have to be considered to achieve an execution time short enough for this frame rate. Firstly, a small buffer is needed to compensate for the maximum execution times, which can be slightly too high for 110FPS (the two cameras captured the scene with 110FPS). Secondly, the Hough Circle Transformation turned out to be computationally too costly and time-consuming. Therefore, the RANSAC algorithm had to be used to achieve the desired execution time.

Additionally, the background subtraction step and the adapting threshold profile used for the Canny Edge Detector were necessary for achieving these execution times. Otherwise, a considerably higher number of edge points would be in the images, which would lead to an execution time that is too high for 110FPS. These additional computational steps also enable a more precise detection. For the future, we plan to consider an approach similar to (Tang et al., 2015) to use more than one trajectory for the prediction and examine the influences on the prediction accuracy.

Detecting other - more complex - objects than a ball will require both more computational power and more convoluted algorithms. The detection will be more complicated, and the prediction would have to take also into account the object's orientation with its three degrees of freedom.

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