Denoising of Noisy and Compressed Video Sequences

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Abstract: A novel denoising algorithm is presented for video sequences. The proposed approach takes advantage of the self similarity and redundancy of adjacent frames. The algorithm automatically estimates a signal dependent noise model for each level of a multi-scale pyramid. A variance stabilization transform is applied at each scale and a novel sequence denoising algorithm is used. Experiments show that the new algorithm is able to correctly remove highly correlated noise from dark and compressed movie sequences. Particularly, we illustrate the performance with indoor and lowlight scenes acquired with mobile phones.

1 INTRODUCTION

Techniques for noise removal in digital images comprise transform thresholding, local averaging, patch based methods and variational techniques. Nowadays, state of the art methods actually combine two or three of these techniques. For example, variational and patch based techniques were combined for both denoising and deblurring (Lou et al., 2010). BM3D (Dabov et al., 2007) combined patch based grouping and thresholding methods, using a 3D DCT transform. Several methods appeared combining the grouping of similar patches and the learning of an adapted basis via PCA or SVD decomposition (Zhang et al., 2010; Orchard et al., 2008). State of the art results are obtained using Gaussian models for groups of similar patches (Lebrun et al., 2013) or adapting the shape of the patch before learning a PCA model (Dabov et al., 2009).

Local average methods, as the bilateral filter (Tomasi and Manduchi, 1998), or patch based methods as NL-means (Buades et al., 2011) or BM3D (Dabov et al., 2009) and NLBayes (Lebrun et al., 2013) can be easily adapted to video just by extending the neighboring area to the adjacent frames. The performance of local average methods is improved by introducing motion compensation. These compensated filters estimate explicitly the motion of the sequence and compensate the neighborhoods yielding stationary data. Kervrann and Boulanger (Boulanger et al., 2007) extended the NL-means to video by growing adaptively the spatio-temporal neighborhood. VBM4D (Maggioni et al., 2011) exploits the mutual similarity between 3-D spatio-temporal volumes constructed by tracking blocks along trajectories defined by the motion vectors.

In (Buades et al., 2016) the authors proposed to combine optical flow estimation algorithms and patch based methods for denoising. The algorithm was inspired by image fusion algorithms in the sense that it tends to a fusion algorithm as the temporal sampling of the sequence gets dense and the motion estimation or global registration is able to perfectly register the frames and no occlusions are present. As this is an ideal scenario, the algorithm in (Buades et al., 2016) compensates the failure of these requirements by introducing spatiotemporal patch comparison and denoising in an adapted PCA based transform.

It must be noted that the previous techniques are able to deal only with uniform white noise. They are usually tested on simulated data, by adding a Gaussian noise of fixed and known variance to a noise-free image or video. In this paper we propose a new algorithm for the denoising of real (i.e. not simulated) noisy video sequences. No noise model is assumed in order to deal with any type of video sequence. The noise amplitude is estimated at each level of a multi-scale pyramid. A noise amplitude is estimated for each color channel assuming the noise is signal dependent. This is a realistic assumption since the noise actually follows a signal dependent model at the sensor (Colom et al., 2014) which is modified through the imaging chain. The proposed algorithm removes noise at each scale by using the white noise removal strategy proposed in (Buades et al., 2016). Since this strategy applies only for uniform standard deviation
noise, a variance stabilization transform is applied at each scale using the estimated noise amplitude values. The whole algorithm is illustrated in Figure 1. For the best of our knowledge, this is the first algorithm attempting to join all necessary tools for denoising real video data.

We shall proceed as follows: Section 2 summarizes the method proposed in (Buades et al., 2016) for white noise removal. Section 3 deals with the estimation of noise in real image sequences. The whole denoising chain is described in Section 4 and experimental results are shown in Section 5. Finally some conclusions are presented in Section 6.

2 IMAGE SEQUENCE WHITE NOISE REMOVAL

In this section we briefly review the image sequence denoising algorithm proposed in (Buades et al., 2016). A complete description and discussion of the algorithm can be found in the paper. The proposed algorithm deals only with white and uniform noise.

We describe the complete algorithm for denoising a frame \( I_k \) from a sequence \( \{I_1, I_2, \ldots, I_k\} \) (Algorithm 1). The same procedure is applied sequentially to all the frames of the sequence. First, the optical flow between \( I_k \) and adjacent frames in a temporal neighborhood is computed and used for warping these frames onto \( I_k \). If registration were accurate and the sequence free of occlusions, a temporal average in this static data would be optimal, even if the noise reduction would slowly decrease as \( 1/M \), being \( M \) the number of adjacent frames involved in the process. Generally, this will not be the case, inaccuracies and errors in the computed flow and the presence of occlusions make this temporal average likely to blur the sequence and have artifacts near occlusions. The proposed approach tends to solve these limitations.

Oclusions are detected depending on the divergence of the computed flow: negative divergence values indicate occlusions. Additionally, the color difference is checked after flow compensation. A large difference indicates occlusion, or at least failure of the color constancy assumption.

Once the neighboring frames have been warped, the algorithm uses a 3D volumetric approach to search for similar patches, while still 2D image patches are used for denoising. For each patch \( P \) of the reference frame \( I_k \), the patch \( \hat{P} \) referring to its extension to the temporal dimension is considered, having \( M \) times more pixels than the original one (assuming \( M \) patches in the temporal neighborhood). Since the images have been resampled according to the estimated flow, the data is supposed to be static. The algorithm looks for the \( K \) extended patches closest to \( \hat{P} \). As each extended patch contains \( M \) 2D image patches, the group contains \( K \cdot M \) selected patches. The Principal Component Analysis (PCA) of these patches is computed and their denoised counterparts are obtained by thresholding of the coefficients. As proposed in (Zhang et al., 2010), the decision of canceling a coefficient is not taken depending on its magnitude, but the magnitude of the associated principal value. A more robust thresholding is obtained by comparing the principal values to the noise standard deviation and canceling or maintaining the coefficients of all the patches associated to a certain principal direction. The whole patch is restored in order to obtain the final estimate by aggregation.

A second iteration of the algorithm is performed using the “oracle” strategy. Once the whole sequence has been restored, the algorithm is re-applied on the initial noisy sequence, but motion estimation and patch selection are performed on the result of the first iteration. In the same way, the PCA is computed in the set of already denoised patches while the coefficients of noisy patches in the computed basis are modified by a Wiener filter strategy. In the present paper this “oracle” strategy is not applied on the result of Algorithm 1 but on the result of the whole denoising chain (Algorithm 4).

Color images are denoised directly without the use of any color decorrelating transform. Each color patch is considered as a vector with three times more components than in the single channel case. The use of several frames makes the number of patches available much larger, relaxing the conditions on the length of the patch vector for learning an adapted model. This permits the use of PCA with color patches. That is, the color decorrelation of PCA is adapted for each group of patches, thus increasing the effectiveness of the model.

Some results of this algorithm, applied on simulated noisy sequences (with added white Gaussian noise of known variance) are displayed in Figure 2. This figure compares the performance of the proposed algorithm SPTWO (Buades et al., 2016) and the state of the art algorithm VBM4D (Maggioni et al., 2011). Both methods are designed to deal with white uniform noise. We display the noisy and denoised central frames for two image sequences of 8 frames. Both algorithms are able to remove the noise, while the algorithm SPTWO (Buades et al., 2016) better preserves details and texture. The title of the book in the gray sequence and the background texture for the color sequence are better recovered by SPTWO. The root mean squared errors (RMSE) between the original
3 NOISE ESTIMATION

In real video sequences (such as the ones displayed in Figure 3) the results of the denoising algorithm proposed in the previous section are far from optimal. One reason is that in real scenes the uniform noise model does not hold. In general, the level of noise depends on the level of the signal. Moreover, even in the case of uniform noise, the noise standard deviation is unknown.

In the case of uniform noise, the problem can be overcome by estimating the noise level. If the noise is signal dependent it is also possible to estimate a “noise curve”, that associates a noise level to each intensity value of the images. Both issues are discussed in the following subsections.

3.1 Uniform Noise

Ponomarenko et al. (Ponomarenko et al., 2007) method estimates the noise standard deviation from the DCT of image blocks. The DCT of each block is computed and denoted by \( D_m(i, j) \) where \( m \) is the index of the block, \( w \) its size and \( 0 \leq i, j < w \) is the frequency pair associated to that coefficient.

The algorithm labels coefficients of the transformed blocks as belonging to low \((i + j < T)\) or medium/high frequencies \((i + j \geq T)\), where \( T \) is a given threshold. For each block, an (empirical) variance associated to the low-frequency coefficients of the block \( m \) is defined \( V^L_m \).

The set of transformed blocks is rewritten with respect to the corresponding value of \( V^L_m \) in ascending order. Given the list of sorted blocks \( \{D_{(m)}\} \), the noise variance estimate associated with the high-frequency coefficient at \((i, j)\) is defined by

\[
V^H(i, j) = \frac{1}{K} \sum_{k=0}^{K-1} |D_{(k)}(i, j)|^2,
\]
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Algorithm 1: Video Denoising (with uniform \( \sigma \)) (SPTWO).

**Input:** noisy video sequence.

**Input:** noise standard deviation (\( \sigma \)).

**Output:** denoised sequence.

1: for each frame \( I_k \) in input sequence do
2: \( N_k \)=temporal neighborhood (\( M \) adjacent frames)
3: Compute optical flow from \( I_k \) to all \( I_j \in N_k \).
4: Warp all \( I_j \in N_k \) using this flow.
5: for each pixel \( x \) do
6: \( P_x \)=patches centered at \( x \) for all frames in \( S_k \).
7: Remove from \( P_x \) patches with occluded pixels.
8: for each pixel \( y \) do
9: \( P_y \)=patches centered at \( y \) for frames in \( S_k \).
10: Remove from \( P_y \) patches with occlusions.
11: end for
12: \( S_k \)=\( K \) closest sets \( P_y \) to \( P_x \).
13: Get denoised patch \( \tilde{P}_x \) centered at \( x \):
14: PCA analysis of patches in \( S_k \).
15: \( \tilde{P}_x \)=reconstruction from thresholded coefficients in PCA basis (thresholds depend upon \( \sigma \)).
16: end for
17: Get denoised frame by aggregation of denoised patches.

where \( i+j \geq T \) and \( K = \lfloor pM \rfloor \), \( p < 1 \) is the position of the \( p \)-quantile in the list \( \{D_{(m)}\}_{m=0}^{M-1} \). Note that this empirical variance estimate is made with the list of the \( K \) transformed blocks whose empirical variance as measured in their low-frequencies is lowest. It is understood that these blocks are likely to contain only noise. Thus their high frequencies are good candidates to estimate the noise. The high and low frequencies are uncorrelated and since most of the energy of the ideal image is concentrated in the low and medium frequency coefficients (because of the sparsity of most natural images), one can assume that \( V^H(i, j) \) gives an accurate estimation of the noise variance.

The final noise estimation is given by the median of the variance estimates. However, the values in the list \( \{V^H(i, j)\} \) depend on the value of the quantile \( K \). This is fixed to a small percentile equal to 0.5%. The algorithm is summarized in Algorithm 2.

Algorithm 2: Ponomarenko noise estimation.

**Input:** \( W \)=Set of \( 8 \times 8 \) image blocs (1 channel).

**Output:** noise level \( \sigma \).

1: \( D = \text{DCT}(W) \). 2D orthonormal DCT-II.
2: Compute \( V^L \)=low-frequency variances of \( D \).
3: Compute \( V^H \)=high-frequency variances of high-frequency blocks in \( D \) with small value in \( V^L \).
4: Compute \( \sigma^2 \) as median of variances in \( V^H \).

3.2 Signal Dependent Noise

In (Colom et al., 2014) it is proposed an adaptation of the Ponomarenko noise estimation method to the case of non-uniform noise (summarized in Algorithm 3). For a signal dependent noise, a “noise curve” must be established. This noise curve associates with each image value \( U(x, y) \) an estimation of the standard deviation of the noise. Thus, for each block in the image, its mean is computed and gives an estimation of a value in \( U \).

The means of these blocks are classified into a disjoint union of variable intervals or bins, in such a way that each interval contains a large enough number of elements. That is, the gray level range is not divided.
into uniform length intervals, but these intervals are adapted to the image itself. This way, if the image is dark, most part of the intervals will be of short length and belonging to dark values while none or very few bins will be in the lighter part of the gray level range. These measurements allow for the construction of a list of block standard deviations whose corresponding means belong to the given bin.

Algorithm 3: Signal-dependent noise estimation.

Input: noisy video sequence.
Output: noise curves (for each color channel).

1: Extract all $8 \times 8$ (overlapping) blocks from all the frames in input sequence.
2: for each color channel do
3: Compute average value of each block.
4: Classify blocks in bins according to average value. Adapt number of bins such that every bin contains at least 42000 blocks.
5: for each bin $i$ do
6: Get set of points $(\lambda_i, \sigma_i)$ where $\sigma_i=$Ponomarenko(bins$_i$) (Algorithm 2) and $\lambda_i=$average value bin $i$.
7: end for
8: Interpolate $(\lambda_i, \sigma_i)$ values.
9: Filter noise curve.
10: end for

Therefore, it is possible to apply the noise estimation algorithm described in the previous section to each set of blocks associated with a given bin. In this way, an estimation of the noise for the intensities inside the limits of the bin is obtained. This noise estimation algorithm will be applied at each level of the multi-scale pyramid. Figure 4 displays the noise curves estimated for some of the video sequences used in this paper and three scales, the original fine scale and two more. In order to compute these curves we have used a pyramid with a subsampling of factor two at each scale, obtained by simple averaging of four pixels. We do not apply any convolution since we want our algorithm to work also with white noise. If the noise at the finest scale is white, this ensures that it stays white during the whole pyramid and the noise standard deviation is divided by two at each scale. This is not the case for the curves displayed in the figure since the initial noise was not white.

We must emphasize that these curves are not exactly the same ones that will be obtained during the denoising process explained in the next section. During the denoising process, at a certain scale, lower ones are already denoised, and therefore the images for which the noise curves are estimated are different from the ones in this experiment. The figure displays the noise pairs $(u_i, \sigma(u_i))$ for each channel and the interpolated ones by using a polynomial of degree 2. The polynomial fits well with the estimated noise pairs. These curves are quite similar to the ones proposed by (Liu et al., 2008) even if the methods are quite different since this latter algorithm estimates actually a noise model taking into account the demosaicking, tone curve and color corrections applied by the camera.

4 Proposed Algorithm

The noise being nearly white at the CFA sensor gets correlated by the demosaicking process. The rest of the imaging chain consisting mainly in color and gamma correction enhances the noise in dark parts of the image leading to colored spots of several pixels. The size of these spots depends on the demosaicking method applied. In order to remove such noise we use a multi-scale strategy aiming at denoising each of these spots at the correct scale where they look like white noise.

4.1 Multi-scale

The proposed algorithm decomposes the image in a multi-scale pyramid and, at each level, the noise is estimated, the variance stabilized and the noise removed by the white noise removal algorithm detailed in Section 2. Once the lowest scale is denoised, the result is up-sampled and the details added back. Down-sampling at each scale is performed by averaging groups of four pixels (factor 2 down-sampling) while up-sampling is done using cubic splines interpolation. The procedure is repeated until the finest scale is attained. The multi-scale strategy is illustrated in Figure 1.

4.2 Noise Standard Deviation Stabilization

As commented in the previous section, the denoising algorithm proposed in Section 2 (Algorithm 1) fails to denoise a real video sequence due to the fact that, in general, the noise level is not uniform but depends on the intensity level of the images. However, the noise curve relating intensity values and noise levels can be learnt from the video sequence (Algorithm 3) and the original video sequence can be manipulated in order to achieve a uniform noise distribution with arbitrary noise level. This manipulation is known as the Anscombe transform (described in the next para-
Figure 4: Display of noise curves for different image sequences and three scales. The algorithm is applied at each scale obtained from the previous one by subsampling of factor two, obtained by agglomeration of four pixels. The noise pairs \((u_i, \sigma(u_i))\) obtained by the algorithm proposed in Section 3.2 are displayed for each channel and interpolated by using a polynomial of degree 2. The polynomial fits well with the estimated noise pairs.

Algorithm 4: Multi-scale Blind Video Denoising.

**Input:** noisy video sequence \(\tilde{u}_0\).

**Output:** denoised sequence \(\hat{u}_0\).

1: for \(s = 1 \cdots N - 1\) do
2:  Noisy sequence (scale \(s\)): \(\tilde{u}_s = \text{downsample}(\tilde{u}_{s-1})\)
3:  Details: \(d_{s-1} = \tilde{u}_{s-1} - \text{upsample}(\tilde{u}_s)\)
4: end for
5: Set \(\tilde{u}_{N-1} = \tilde{u}_{N-1}\).
6: for \(s = N - 1 \cdots 1\) do
7:  Denoise: \(\hat{u}_s = \text{denoise}(\tilde{u}_s)\) (with Algorithm 5).
8:  Add details: \(\tilde{u}_{s-1} = \text{upsample}(\hat{u}_s) + d_{s-1}\)
9: end for
10: Set \(\hat{u}_0 = \tilde{u}_0\).

Figure 5: Comparison of the application of the chain with a single scale (top-right) or three scales (bottom) as used by our method. The original image is displayed in the top-left corner of the figure. The images have been enhanced (Drago et al., 2003) in order to better illustrate the differences between the two methods. The single scale algorithm actually removes noise but only noise values of slightly more than one pixel but not large spots. Large colored spots are removed only by the multi-scale algorithm, which removes them at the scale for which they become almost white noise.

**The Anscombe Transform.** We usually refer to the Anscombe transform as to the transformation \(f(u) = 2\sqrt{u + \frac{3}{8}}\) which is known to stabilize the variance of a Poisson noise model. However, any signal dependent additive noise can be stabilized by a simple transform. Let \(v = u + g(u)n\) be the noisy signal, we search for a function \(f\) such that \(f(v)\) has uniform standard deviation. When the noise is small compared to the signal we can apply the decomposition \(f(v) = f(u) + f'(u)g(u)n\). Forcing the noise term to be constant, \(f'(u)g(u) = c\), and integrating we obtain \(f(u) = \int_0^u c dt / g(t)\).

When a linear variance noise model is taken, this transformation gives back the known Anscombe transform.

We apply this transformation with the curve obtained at each scale in order to stabilize the noise variance. The inverse transform is applied back after denoising to get the original range.
Algorithm 5: Video Denoising (with signal-dependent unknown noise).

**Input:** noisy video sequence.

**Output:** denoised sequence.

1. Compute noise curves for the input sequence (Algorithm 3).
2. Apply Anscombe transform to the input sequence, based on the previous noise curves.
3. Denoise video (Algorithm 1).
4. Apply inverse Anscombe transform to obtain the final denoised sequence.

4.3 Denoising Algorithm and the Second Iteration Question

The denoising algorithm in (Buades et al., 2016) has originally two steps as explained in Section 2. In the second step the already denoised image is used in order to compute the patch distances and learn the PCA model.

A straightforward extension of the method to the multi-scale video algorithm would apply the two steps for each particular image at each scale. Instead, we apply only the first step at each scale and after the image sequence or video has been completely denoised, a second step is applied. The second step takes as input the completely filtered sequence, and for the denoising of a particular image and scale, the already denoised image at that scale is used for selecting the similar patches and learn the PCA model.

5 EXPERIMENTATION

In this section we illustrate the performance of the proposed method and the importance of each stage. All experiments use exactly the same parameters which mainly are the number of scales, the window size and the filtering parameter. We used three scales, a $5 \times 5$ window and a filtering parameter equal to $4\sigma$ at each scale. The denoising stage is applied after the variance stabilization transform for which the standard deviation curve is estimated automatically. We used the proposed method in Algorithm 3 with 10 bins and the curve was approximated by a polynomial of degree 2.

We first illustrate the need of a multi scale algorithm. Figure 5 compares the application of the chain with a single scale or three scales as proposed. The denoised images are afterwards enhanced (with the tone mapping algorithm described in (Drago et al., 2003)) in order to better illustrate the differences between the two methods. The single scale algorithm actually removes noise but only noise values of slightly more than one pixel but not large spots. Large colored spots are removed only by the multi-scale algorithm, which removes them at the scale for which they become almost white noise.

Figure 6 compares our method with state of the
art algorithm VBM4D (Maggioni et al., 2011). It must be remarked that this algorithm is not designed for real image noise but for the denoising of white and uniform noise. Moreover, an estimation of the noise variance must be provided. In our examples we tested with different noise variances ($\sigma = \{10, 15, 20, 25, 30\}$). We display the best results for each video sequence. The figure also displays the images after enhancement. This enhancement permits a better visualization of the noise removal but is not part of the proposed chain. These examples show that the proposed denoising method outperforms state of the art techniques and illustrates the need of such a complex chain with multi-scale and signal dependent noise estimation and stabilization.

One short movie displaying the results of the denoising chain can be found in the supplementary materials accompanying this paper.

6 CONCLUSIONS

We have proposed a denoising algorithm for real video comprising all stages, multi-scale, noise estimation and denoising. The proposed algorithm has shown to effectively remove highly correlated noise from dark and compressed movie sequences with weak signal-to-noise ratio.

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