Predicting Stock Market Movement: An Evolutionary Approach

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Abstract: Social Networks are becoming very popular sources of all kind of data. They allow a wide range of users to interact, socialize and express spontaneous opinions. The overwhelming amount of exchanged data on businesses, companies and governments make it possible to perform predictions and discover trends in many domains. In this paper we propose a new prediction model for the stock market movement problem based on collective classification. The model is using a number of public mood states as inputs to predict Up and Down movement of stock market. The proposed approach to build such a model is simultaneously promoting performance and interpretability. By interpretability, we mean the ability of a model to explain its predictions. A particular implementation of our approach is based on Ant Colony Optimization algorithm and customized for individual Bayesian classifiers. Our approach is validated with data collected from social media on the stock of a prestigious company. Promising results of our approach are compared with four alternative prediction methods namely, bagging, Adaboost, best expert, and expert trained on all the available data.

1 INTRODUCTION

Social networks and portable devices have made exchange and sharing a huge amount of personal experiences possible. More than 500 million tweets are shared daily. In particular, tweets on stock markets are taking part in the everyday traffic on these social networks. Mining such social behavior of users in social networks, like Twitter and Facebook, has become a hot research topic. In social data mining, the behavior of users can be used in predicting global phenomenon (Asur and Huberman, 2010) such as stock market (Bollen et al., 2011), disease epidemic (Ginsberg et al., 2008), elections (Gayo-Avello, 2012), movie box office (Liu, 2006), and marketing (Yu and Kak, 2012). In order to mine social data, we need to consider standard measures of human behavior. The Profile of Mood States (POMS) and its variations (e.g., GPOMS), quoted from psychology, are used to measure individuals mood (Ginsberg et al., 2008). The combination of these moods can represent individual sentiment. Doubtlessly understanding the user behavior and relating it to stock market index can affect positively traders behaviors. However, unlike other works (Ginsberg et al., 2008; Asur and Huberman, 2010; Gayo-Avello, 2012; Yu and Kak, 2012; Liu, 2006), our focus is to build an ensemble prediction model that preserves two properties, namely, interpretability and performance. In the context of financial market, one would like to predict the stock market movement not only accurately but also with an easy understanding of the causality relationship that leads a particular direction of the stock values. For example, one wants to know how specific public mood states are related to stock changes. Different mining techniques, in social engineering, have been used in order to obtain highest prediction performance (Yu and Kak, 2012). Examples of such techniques include ANN, Regression, Decision Trees, Rule Mining, and SVM (Michalski et al., 1986; Goebel and Grunwald, 1999). However, some of these techniques suffer from interpretability shortcomings. Interpretability is the ability for an expert to interpret prediction model by analyzing/examining the causality relationship between input features and prediction outcome. Such quality is of a critically important; especially when the user wants to focus her effort to improve input features to prevent undesirable outcomes. Decision Trees, Bayesian classifiers, rule set systems, and fuzzy rules are examples of interpretable techniques because we can visualize the effect of input features on the final prediction outcome (Lavrač, 1999). Examples of non-interpretable techniques include SVM, Regression, ANN, and ensemble techniques such as Bagging and Boosting. Although some of the non-interpretable techniques feature high performance and strong mathematical background, they are still unacceptable by experts in many domains (Kim et al.,
In this paper, we propose an ensemble classifiers technique to build prediction model that is more interpretable and accurate. The model is based on Ant Colony Optimization (ACO) to combine Bayesian classifiers. We show that our model preserves the interpretability of individual Bayesian classifiers and attains higher performance. We apply such model in the stock market prediction because it is essential to have highly accurate and interpretable prediction model according to the market dynamics.

The rest of this paper is organized as follows: Section 2 summarizes the related work. Section 3 describes the problem we are addressing and gives an overview of the proposed solution. Background techniques are introduced in Section 4. A customization of Ant Colony Optimization to our problem is presented in Section 5. A validating experiment is described in Section 6. Conclusions and future work are drawn in Section 7.

2 RELATED WORK

Prediction in social media context has generally gone three main streams, namely, marketing (Bollen et al., 2011), movie box-office (Liu, 2006), and information dissemination (Yu and Kak, 2012). In marketing, Bollen et al. (Bollen et al., 2011) analyzed the text content of daily Twitter feeds to measure positive vs. negative mood in terms of 6 dimensions, namely, Calm, Alert, Sure, Vital, Kind, and Happy. The main conclusion is that mood states can improve the accuracy of predictions of the Dow Jones Industrial Average (DJIA). Trasov et al. (Trusov et al., 2009) employ Word of the Mouth (WOM) in marketing and link it with the number of new members joining the site (sign-ups). Liu et al. (Liu, 2006) analyzed data collected from yahoo/movies to show that WOM activities are very informative during pre-release and the opening week, and the movie viewers tend to hold relatively high anticipation before release, but become more critical in the opening week. Other social mining applications include election prediction using Twitter data (Gayo-Avello, 2012), measuring flu spread using Google search queries (Ginsberg et al., 2008), analyzing and measuring athletic success based on POMS (Yu and Kak, 2012), and others. Although, Bollen’s proposed model is accurate, it cannot explain precisely how some mood indexes are related to Dow Jones Industrial Average. In prediction models, the trade-off between interpretability and performance is gaining an increasing interest. Generally, researchers have gone in one of the following two directions to build quality models. First, in order to improve prediction accuracy, selected models are combined composing a wisdom council which makes the final decision. Prediction is done by consulting all models in the council. The methods known as Ensemble Classifiers Methods (ECM) dominate this strategy. They have demonstrated an out-performance of classifiers combination on the individual ones when it is applied to unseen data sets. Namely, averaging, boosting, bagging, and voting (Moerland and Mayraz, 1999; Oza and Tumer, 2008; Galar et al., 2012) are the most commonly used techniques of classifiers combination. The second strategy aims at preserving an easy understanding of the causality buried in the classification models. This is what we refer to as interpretability of the classifiers. Such a property is preserved by employing modeling techniques that outcome white boxy classifiers able to explain the causal relationship between inputs and outputs. Examples include the use of decision tree, Networks and Bayesian classifier, rule set system, fuzzy rule, etc. In particular, Bayesian classifiers and networks have been proposed as solution of lack of interpretability in several domains such as clinical diagnosis (Van Genven et al., 2007), text and mail classification (Chen et al., 2009), and software engineering (Fenton and Neil, 1999; Bouktif et al., 2006).

With respect to the problem of stock market prediction, company managers would like prediction models to explain precisely how some user mood states are related to the stock movement direction. Hence, we propose a high performance and interpretable model for stock market prediction problem. We build such a model using Ant Colony Optimization that combines classifiers structures while preserving the interpretability and increasing the accuracy. Our approach is customized for the case of individual Bayesian Classifiers (BC) used for stock market movement prediction and validated using empirical experiment.

3 PROBLEM STATEMENT AND SOLUTION PRINCIPLE

3.1 Problem Statement

Our goal in this work is to construct a prediction model that maps public mood states collected from social media to stock market movement. Such a model is generally built/validated using a representative data set on the problem being predicted. Particularly, in the problem of stock market movement prediction, the data set $D_c$ is assumed to be descriptive of the particular context of a stock market changes.
Accordingly, if we want to be representative of all the possible world-wide stock markets contexts, we have to consider collecting data from all the world, which is infeasible. A compromising solution is to reuse learned patterns from different contexts as an attempt to approximate more representative data. As an opinion of experts (Bouktif et al., 2002; Bouktif et al., 2010; Bouktif and Awad, 2013), adopted by our approach, a high quality prediction model should be a mixture of domain common knowledge and context specific knowledge. On the one hand, the reuse of existing experiences of prediction, allows to integrate the common domain knowledge represented by a diversity of contexts. On the other hand, the adaptation of the models driven by the specific context data takes into account the specific knowledge represented by the available context data \( D_c \). In other words, more generalizable prediction model is attained by covering more contexts and building higher performance expert is achieved by adapting and reusing multiple expertise. For evaluating our proposed solution and validating our approach assumption, the best expert among others, used as a benchmark.

Our problem can be seen as a problem of reusing \( N \) predefined prediction classifiers \( f_1, \ldots, f_N \) called experts. The objective of our solution is how to improve performance of stock market prediction while preserving interpretability. Therefore, the challenging question is how to produce a new optimal BC that inherits the "white-boxy" property (i.e., interpretability) of BCs, while improving the prediction performance on the available context represented by \( D_c \).

### 3.2 Solution Overview

To achieve our goal, we propose to reuse existing classifiers to derive new accurate and interpretable ones. Our proposed approach is founded on three operations (1) expertise identification (2) expertise pooling and (3) expertise adaptation. In the former operation, each expert is decomposed into chunks of expertise. Each chunk is a subset of the entire input domain. The decomposition of a Bayesian classifier, leads to expertise chunks expressed as a set of prior probabilities attached to each range (interval) of attribute values (See details in Section 5.1). The rational behind the decomposition is to give more flexibility to the process of combination, specially when selecting the appropriate chunk of expertise. Moreover, the derived expert which is a collection of chunks of expertise, is intended to be interpretable since we know the particular chunks responsible for the final decision. The expertise pooling operation consists in reusing the chunks of expertise coming from different experts to progressively build more accurate combinations of these experts using \( D_c \) to guide the search. The expertise adaptation operation consists in modifying some expertise chunks in order to obtain more refined expertise combinations to a particular context \( D_c \).

Our proposed solution can be seen as a searching problem where the goal is to select and generate the best set of expertise suitable for performing well in the context \( D_c \). Therefore, several existing experts will be decomposed into chunks of expertise. However, searching an optimal combination of these chunks will degenerate combinatorial explosion. This situation makes the problem an NP-complete one. Typically, such a problem can be circumvented by using search-based techniques in a large search space (Bouktif et al., 2010) (Ahmed et al., 2008). In this work, we propose a customization of the Ant Colony Optimization to combine Bayesian Classifier based experts.

### 4 BACKGROUND

#### 4.1 Naive Bayesian Classifier

A Bayesian classifier (BC) is a classification method, that assigns the most probable class \( c \) to a \( d \)-dimensional observation \( \mathbf{x} \), by determining its computed as:

\[
c = \arg \max_{c_m} p(c_m|a_1, \ldots, a_d),
\]

where \( c_m \) ranges of the set of possible classes \( \mathcal{C} = \{c_1, \ldots, c_q\} \) and the observation \( \mathbf{x} \) is written as generic attribute vector. Assuming that all attributes are conditionally independent, BC degenerates to a Naive Bayes. An attribute domain is divided into \( m \) intervals \( I_{j_1} \) and \( p(I_{j_1}|c_m) \) will be the prior conditional probability of a value of the \( j^{th} \) attribute to be in the interval \( I_{j_1} \), when the class is \( c_m \); \( t_j \in \mathbb{N} \) is the rank of the interval in the attribute domain. To classify a new observation \( \mathbf{x} \), a BC with continuous attributes applies Bayes rule to determine the \( a posteriori \) probability \( p(c_m|a_1, \ldots, a_d) \). as:

\[
p(c_m|I_{t_1}, \ldots, I_{t_d}) = \frac{\prod_{i=1}^m p(I_{j_i}|c_m) \prod_{h=1}^q p(I_{j_h}|c_h) p(c_h)}{\sum_{h=1}^q \prod_{j=1}^m p(I_{j_i}|c_h) p(c_h)} p(c_m),
\]

where \( a_j \in I_{j_1} \).

#### 4.2 ACO Metaheuristic

Ant Colony Optimization (ACO) is an algorithm inspired by the efficient process by which ants look
for food and carry it back to their nest (Deneubourg et al., 1990). Throughout its trip, an ant deposits a chemical substance called pheromone which constitutes a mean of indirect communication between species members (Dorigo et al., 2006). The amount of pheromone deposited by an ant reflects the quantity of food as well as the optimality of the traversed path. Investigations show that at the beginning of the food search, the ants randomly choose their paths. Nevertheless, after some time and based on their communications through pheromone trails, the ants tend to follow the same optimal path. A static graph modeling all the possible paths followed by the ants is used to represent an optimization problem. Based on this representation, an artificial ant builds a solution by moving along the graph and selecting the suitable edges towards the optimal path. The deposited amount of pheromone mirrors the optimality of the traversed path.

5 CUSTOMIZATION OF ANT COLONY APPROACH

Customizing ACO algorithm for Bayesian classifiers combination needs the definition of the following elements: a solution representation, a graph on which the artificial ants will progressively construct the solutions, a measure of solution quality, a suitable strategy for the ants communication via pheromone update and finally a moving rule that decides for an ant to move from one node to the next in the graph.

5.1 Solution Structure

The decomposition of BC into expertise chunks is critical to our based approach. This operation facilitates the exploration of the search space defined by all the combinations of expertise chunks. Consequently, it makes the steps of reusing and adapting the existing BC expert is easy and efficacious. According to the description of Naive BCs in Section 4.1, two BC parameters can represent an expertise chunk, namely, marginal probabilities of classes, and prior conditional probabilities of attributes. Since prior conditional probabilities are more determinant in the BC structure, we use them to characterize a chunk of expertise.

For a given attribute $j$, there are $m_j$ chunks of expertise. An expertise chunk can be coded as a triplet made up of one interval and two conditional probabilities. To elaborate on expertise chunk, let us consider the prediction of stock market movement problem. The used BCs are binary and each of them predicts the stock price movement directions. The set of used class labels is $C = \{c_1, c_2\}$, with $c_1 = up$ and $c_2 = down$. In this example a chunk of expertise is a triplet, denoted by $(I_{p_j}, p(I_{p_j} | c_1), p(I_{p_j} | c_2))$. It can be interpreted as follows: the probability of a value of the $j^{th}$ attribute to be within the interval $I_{p_j}$ when the class is set to $c_1$, is equal to $p(I_{p_j} | c_1)$ and is equal to $p(I_{p_j} | c_2)$ when the class is set to $c_2$. The index $t_j \in \mathbb{N}$ is the rank of the interval in the attribute domain that contains $N$ intervals. In this illustrative prediction problem, a mood state attribute $j$ in a BC will be encoded by the following vector:

$$
\begin{bmatrix}
(0, 11), 0.241, 0.296 \\
(11, 19), 0.303, 0.192 \\
(19, 44), 0.209, 0.254 \\
(44, 96), 0.253, 0.258
\end{bmatrix}
$$

where each line encodes a vector of expertise chunks. An expertise chunk is defined by the triplet $(interval, cond.\ probability|c_1, cond.\ probability|c_2)$. For example, the stock market chunk of expertise $([0, 11], 0.241, 0.296)$ means that the conditional probability of a mood state score to be in the interval $[0, 11]$ when the class is $c_1 = up$, is equal to 0.241 and 0.296 when the class is $c_2 = down$. In this particular example, the mood state attribute is divided into 4 intervals.

5.2 Solution Construction Mechanism

5.2.1 Possible Strategies

There are two candidate strategies of modeling BCs combination. The first one considers the modular structure of BC, in which, ACO is applied on each single attribute. In other words, the artificial ants will progressively construct, for each attribute, a new composition until obtaining a near optimal set of expertise chunks. On each attribute, the ants work to derive a new decomposition (i.e., new slicing) of the attribute domain, and a new distribution of conditional probabilities. Then a final classifier is built-up by grouping all the near optimal derived compositions for all the attributes, respectively.

The second strategy considers all the attributes, simultaneously. A new BC solutions is built-up from expertise chunks that contain knowledge from all the attributes. In this paper, we adopt the first strategy, however, we will empirically study both in future work. Therefore, we focus on constructing a solution at the BC attribute level. The solution construction mechanism aims at searching the optimal path in a directed graph $G(V, E)$ where $V$ is a set of nodes and $E$ is a set of edges that will map a BC-attribute structure.
5.2.2 Graph Construction

The first step of the ACO customization is to construct the graph to model the possible paths for the ants moves. To construct the attribute graph \( G(V,E) \), we first consider all attribute compositions throughout all the BCs and create a new slicing of the domain attribute. The new slicing is defined by considering all the boundaries of the attribute intervals in all the BCs. The list of all these boundaries sorted in an ascending order, denoted by \( B \), is used to create the new slicing such that each interval is bounded by two adjacent values from \( B \). Therefore, each node \( v \) in \( V \) represents a boundary from the list \( B \) of boundaries of the attribute being processed. The nodes of an attribute graph are then ordered by value \( v \) of the attribute coming from the \( k^{th} \) BC. For example, the conditional probabilities associated with the edge \( e_{11} \) are computed in the following way:

\[
p(e_{11}|c_m) = p((v_1^1,v_1^2]|c_m) * (v_2 - v_1),
\]

where, \( m = 1,2 \) and \( [v_1^1,v_2^1] \) is the interval containing the interval \([v_1,v_2]\) in the original composition of the attribute \( j \) in the BC number 1. Figure 1 shows two nodes from the graph constructed for an attribute \( j \). As described above, the solution construction mechanism assumes that the used graph is static, built on quantized pairs of conditional probabilities; all possible values of conditional probabilities are predetermined, listed, and used to build the static graph. Thus, attribute compositions that form the candidate solutions are derived from simple combinations of edges.

5.3 Solution Quality Measure

The mission of our ACO based approach is to maximize the performance of derived BC containing the attribute composed by the ants. Our approach can be seen as a learning process where the data set \( D_c \), the particular context data, is used to guide the ants in their trails to construct solutions. Therefore, the set \( D_c \) is used as evaluation data to compute the predictive accuracy of the derived classifier.

The predictive accuracy of a BC can be evaluated with different measures as discussed in (Bouktif et al., 2010). In order to avoid falling in either constant or guessing classifiers, we decided to use Youden’s \( J \)-index (Youden, 1961), defined as

\[
J(f) = \frac{1}{2} \sum_{i=1}^{2} \frac{n_{ii}}{\sum_{j=1}^{2} n_{ij}}.
\]

where \( n_{ij} \) is the number of cases in the evaluation data set with real label \( c_i \) classified as \( c_j \). Intuitively, \( J(f) \) is the average correctness per label. In statistical terms, \( J(f) \) measures the correctness assuming that the a-priori probability of each label is the same.

5.4 Ant Walk, Attractiveness and Visibility

When an ant on a node \( v_i \) moves to the next node \( v_{i+1} \), it chooses an edge \( e_{ik} \) representing the \( k^{th} \) couple of conditional probabilities associated to the interval \([v_i,v_{i+1}]\) and originally copied from the \( k^{th} \) BC. Hence, the ant’s task after each move, is to assign a pair of conditional probabilities to the attribute interval \([v_i,v_{i+1}]\).

Initially, the ants start by moving randomly from one node to the following one. After some iterations, the ants become guided by a transition strategy. Such a strategy consists in choosing the edge to be traversed based on the amount of pheromone deposited on that edge. The higher the amount, the higher the probability of choosing that edge. This probability is computed by the following equation:

\[
p(choosing(e_{ik})) = \frac{\tau(e_{ik})^\alpha * \eta(e_{ik})^\beta}{\sum_{h=1}^{N} \tau(e_{ih})^\alpha * \eta(e_{ih})^\beta}, \tag{2}
\]

where \( \tau(e_{ik}) \) and \( \eta(e_{ik}) \) are respectively the attractiveness and the visibility of the edge \( e_{ik} \) to be chosen. The attractiveness function is based on the quality of the previous solutions. It is modeling the amount of pheromone accumulated on the trail of ants and defined by the Equation 3. However, the visibility function is defined as the sum of conditional probabilities associated with the edge \( e_{ik} \). The two parameters \( \alpha \) and \( \beta \) are parameters of the visibility function.
and β are used to balance the impact of attractiveness (i.e., pheromone) versus visibility. These are two parameters of the ACO Algorithm and have to be tuned empirically after several runs. After computing the probability of choosing every edge \( e_{ik}, k = 1..N \), a Casino wheel method is used to select an edge.

### 5.5 Pheromone Update Strategy

An ant deposits a quantity of pheromone on every edge it traverses. The accumulated quantity of pheromone constitutes the attractiveness of an edge. It can also be considered as long-term memory of the ant colony. In our proposed ACO algorithm, this long-term memory is updated after an ant finishes one tour. The schema of updating the deposited pheromone amount during the iteration \( t \) on an edge \( e_{ik}, k = 1..N \), is given by the following equation:

\[
\tau(e_{ik}) = \begin{cases} 
(1 - \rho) * \tau(e_{ik})^{t-1}, & \text{if edge is not traversed} \\
(1 - \rho) * \tau(e_{ik})^{t-1} + Q * J(f), & \text{otherwise,} 
\end{cases}
\]

where \( 0 \leq \rho \leq 1 \) is a parameter of the ACO algorithm representing the evaporation rate of the pheromone substance. This parameter indicates low evaporation at small values and vice-versa. The quantity of the newly deposited pheromone, \( \Delta \tau = Q * J(f) \), is proportional to both the base attractiveness constant \( Q \) and the quality measure \( J(f) \) that has to be maximized.

### 6 EXPERIMENTAL RESULTS

In this section, we present the empirical results to validate our proposed approach. We focus on evaluating the accuracy of the obtained model for stock market movement prediction derived by combining Bayesian classifiers. Two inputs are needed for such an evaluation. (1) A set of “existing” models, called stock market experts that predict stock price movement. In our case, these prediction models are Bayesian Classifiers. (2) A representative data set that serves as a guidance for the classifiers combination process.

#### 6.1 Data Description

Inspired by Bollen’s work (Bollen et al., 2011) and for the sake of a future comparison with the results obtained in our previous work (Bouktif and Awad, 2013), we have decided to use public mood scores collected on Twitter as input attributes for the individual classifiers. A set of 18 mood states is used by a prestigious company (i.e., IBM). These 18 mood state attributes are used to track the negative and positive mood sentiments during the 9 days preceding the closing price of a particular stock. Precisely, two mood state attributes are used to capture, respectively, the score of negative mood sentiments and the score of positive mood sentiments of one day. The stock movement data (i.e., up or down) of the IBM company is obtained from Google Finance. Let \( PM_j \) and \( NM_j \) be respectively, the number of positive and the number of negative mood sentiments for the IBM company stock \( j \) days before closing price, \( j = 1..9 \). A sample of data row could be \((16, 32, 43, 13, 28, 10, \ldots, 15, 36, \text{Down})\), where for example, the score of positive public mood sentiments one day before closing price is 16 (i.e., \( PM_1 = 16 \)) and the score of negative public mood sentiments one day before closing price is 32 (i.e., \( NM_1 = 32 \)). Besides, the stock movement direction (i.e., Up or Down) as well as the mood scores are tracked for a period of more than 20 months. The collected data set contains 462 data points capturing each 18 mood scores followed by the stock movement direction.

#### 6.2 Building Individual Stock Market Experts

For the sake of performing a controlled experiment, the individual stock market experts are built “in-house”. Therefore, we use random combinations of attributes from the 18 stock mood states (i.e., of two, three,..., and nine days). By these combinations, we imitate different opinions of stock market experts that may predict the direction of the particular stock value based on different set of mood states about the stock of the studied company. Randomly, we formed 20 subsets of mood states, and subsequently 20 training data sets were created. Therefrom, one classifier is built on each data set by using the RoC machine learning tool (Ramoni and Sebastiani, 1999).

#### 6.3 Experimental Context Data Set

A data sample called particular context consists of 154 records of mood states about IBM company extracted randomly from the whole data set (i.e., from the 462 data points). Also, each record is described by the 18 mood state attributes and labeled by the stock movement direction (i.e., up or down). We recall that the context data set \( D_c \) is supposed to represent stock market movement prediction circumstances.
6.4 ACO Algorithm Setting

After several runs, the termination criterion is determined by the maximum number of iterations (i.e., number of tours performed by each ant) which was set to 150 and the number of artificial ants used to select the conditional probabilities was set to 100. The pheromone update is conducted by two parameters, namely, the pheromone variation that was set to 2.0 and the pheromone evaporation rate $\rho$ that was set to 1%. In order to balance between the impacts of pheromone and visibility, $\alpha$ and $\beta$ were fixed at 1.0 and 1.0, respectively.

6.5 Experimental Design and Results

Four alternative approaches are used as benchmarks to evaluate the performance of our proposed ACO-based model construction; the "best expert selection" approach, the "data combination" approach, and two other methods from the ECM, namely, the bagging and boosting algorithms. The "best expert selection" approach consists in analyzing the performance of the existing expert across a spectrum of available data ($D_c$), in order to choose the one having the best performance, referred to as $f_{\text{Best}}$. The "data combination" approach takes advantages of the availability of data sets that served in building the "simulated" existing experts in this controlled experiment. With the latter approach an expert, $f_{\text{AllData}}$, is trained on the combination of all the available data sets. With respect to the ECM, the bagging is a voting based method that consists in assigning the class that collects the higher number of votes among the individual experts (Merz, 1998). In our experiment, it is denoted $f_{\text{Bagg}}$. Finally the boosting approach implemented by the well-known Adaboost algorithm, a sophisticated weighted sum of individual classifiers outputs (Freund and Schapire, 1997). It is referred to as $f_{\text{Boost}}$. Table 1 compares the accuracy of the resulting expert $f_{\text{ACO}}$ to those of $f_{\text{Best}}, f_{\text{AllData}}, f_{\text{Bagg}}$ and $f_{\text{Boost}}$, respectively. The accuracies of the obtained classifiers are evaluated using J-index of Youden and estimated with 10-fold cross validation. The process of deriving the new BC is guided by the union of 9 folds from the context data $D_c$. A new classifier is then trained on the union of 9 folds, and tested on the one remaining fold. The process is repeated 10 times for all 10 possible combinations. The mean and standard deviation of accuracies J-index are computed on both the training and the test data.

When compared to the best expert $f_{\text{Best}}$, the generated BC $f_{\text{ACO}}$ has gained 15.90% in predictive accuracy on the training data set and 7.41% on the testing data. On both training and testing data, the performance improvement is significantly greater than each of the standard deviations computed respectively for $f_{\text{Best}}$ accuracy (e.g., 1.22 or 14.25) and for $f_{\text{ACO}}$ accuracy (1.28 or 2.6). The null hypothesis $H_01$, assuming that no differences exist between $f_{\text{Best}}$ and $f_{\text{ACO}}$, is rejected by the statistical testing t-test, with very strong evidence (Two-tailed t-test, p-value <1%). Thus a result shows a significant improvement in the accuracy of stock market expert derived by our approach. Moreover, the accuracy of the derived BC $f_{\text{ACO}}$ is compared to that of the BC trained on all the available data denoted $f_{\text{AllData}}$ and the result shows a significant difference in performance (i.e., 13.16% on training data and about 9.00% on testing data) on the favor of $f_{\text{ACO}}$. T-test statistical analysis shows a significant accuracy difference between $f_{\text{ACO}}$ and $f_{\text{AllData}}$. The null hypothesis $H_02$, assuming that no differences exist between $f_{\text{AllData}}$ and $f_{\text{ACO}}$, is rejected with very strong evidence (Two-tailed t-test, p-value <1%).

In order to compare our approach to similar ones, two ensemble classifiers methods are implemented, namely, bagging (i.e., $f_{\text{Bagg}}$) and boosting (i.e., $f_{\text{Boost}}$). The performance of the derived model $f_{\text{ACO}}$, shown in Table 1, is not only comparable to $f_{\text{Bagg}}$ and $f_{\text{Boost}}$ but surprisingly higher. A t-test statistics reject with high significance of more than 95% both the the null hypothesis $H_{03}$, assuming that the accuracy of $f_{\text{ACO}}$ is significantly lower than that of the bagging $f_{\text{Bagg}}$ and the null hypothesis $H_{04}$, assuming that $f_{\text{ACO}}$ is significantly more better than $f_{\text{Boost}}$ obtained by boosting technique. Figure 2 shows a summary of the performance achieved by the prediction model derived by our approach ($J(f_{\text{ACO}})$).

7 CONCLUSION

In this paper, we have applied our previously proposed approach of mixture of experts to the problem of stock market movement prediction. Ant Colony Optimization was tailored and improved to combine stock market experts. A data driven combination was
performed and new expert is learned on public mood data collected from social networks. The novelty of the proposed models combination resides in the reuse of the structural elements of individual models rather than their outputs. This way of combining models does not only improve the performance of the composite model but it also promotes model interpretability. The latter model property is very critical in the context of stock market decision making. In particular it is very useful in discovering which mood states attributes and which mood scores are responsible for a particular movement of the stock value. The high complexity of combining expert chunks was resolved by the application of a metaheuristic, namely, ACO algorithm. Bayesian Classifiers are used as interpretable type of prediction models. The results obtained on data of a particular company in the stock market, show the higher performance of the derived model when compared to four alternative approaches including bagging and boosting. Other types of prediction models are to be considered in our future works. Besides, we will continue collecting more representative data from social media. In particular, for maturing the problem of stock market prediction and discovering better predictors.

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