A Notation for Discrimination Network Analysis

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Abstract: Because of their ability to store, access, and process large amounts of data, Database Management Systems and Rule-based Systems are used in many information systems as information processing units. A basic function of a Rule-based System and a function of many Database Management Systems is to match conditions on the available data. To improve performance intermediate results are stored in Discrimination Networks. The resulting memory consumption and runtime cost depend on the structure of the Discrimination Network. A lot of research has been done in the area of optimising Discrimination Networks. In this paper we focus on re-using of network parts by multiple rule conditions. We introduce the block notation as a first step to enhance optimisation. The block notation allows for the identification of meaningful sharing constructs.

1 INTRODUCTION

Because of their ability to store, access, and process large amounts of data, Database Management Systems and Rule-based Systems are used in many information systems as information processing units (Brownston et al., 1985; Forgy, 1981). A basic function of a Rule-based System and a function of many Database Management Systems is to match conditions on the available data. Checking all data repeatedly every time some data changes performs badly. It is possible to improve performance by saving intermediate results in memory introducing the method of dynamic programming. A common example for this approach is the Discrimination Network. Different Discrimination Network optimization techniques are discussed in (Forgy, 1982), (Miranker, 1987), and (Hanson and Hasan, 1993). These approaches only address optimisations limited to single rules. Further improvement is possible by optimising the full rule set of a Rule-based System. In this paper we will introduce a visualisable notation as a first step to enhance optimisation of rule sets.

This paper is organized as follows: In Section 2 we introduce Discrimination Networks and in Section 3 we explain the concept of re-using network parts for different rules. In Section 4 we discuss the arising problems in the field of node sharing. Those problems are then addressed in Section 5 and the notation is presented. Section 6 comprises the conclusion and gives an outlook on future work.

2 DISCRIMINATION NETWORKS

Rules in Rule-based Systems and Database Management Systems both comprise a condition and actions. The actions of a rule must only be executed, if the data in the system matches the condition of the rule.

Discrimination Networks are an efficient method of identifying rules to be executed employing dynamic programming trading memory consumption for runtime improvements. Rule conditions are split into their atomic (w.r.t. conjunction) sub-conditions. In the following, such sub-conditions are called filters.

Discrimination Networks apply these filters successively joining only the required data. Intermediate

![Discrimination Network example](image)

Figure 1: Discrimination Network example.
results are saved to be reused in case of data changes. Each filter is represented by a node in the Discrimination Network. Additionally, every node has a memory, at least one input, and one output. The memory of a node contains the data received via its inputs matching its filter. The output is used by successor nodes to access the memory and receive notifications about memory changes. Data changes are propagated through the network along the edges. Changed data reaching a node is joined with the data saved in nodes connected to all other inputs of the node. So only the memories of affected nodes have to be adjusted. Each rule condition is represented by a terminal node collecting all data matching the complete rule condition. An example Discrimination Network is shown in Figure 1.

**data input nodes** serve as entry points for specific types of data into the Discrimination Network. They are represented as diamond shaped nodes.

**filter nodes** join the data from all their inputs and check if the results match their filters. They are represented as inverted triangle shaped nodes.

**terminal nodes** collect all data matching the conditions of the corresponding rules. They are represented as triangle shaped nodes. The action part of a rule should be executed for each data set in its terminal node.

### 3 NODE SHARING

The construction of a Discrimination Network that exploits the structure of the rules and the facts to be expected in the system is critical for the resulting runtime and memory consumption of the Rule-based System. To avoid unnecessary re-evaluations of partial results, an optimal network construction algorithm has to identify common subsets of rule conditions. In the corresponding Discrimination Network, these common subsets may be able to use the output of the same network nodes. This is called node sharing.

Despite the fact, that there is a lot of potential to save runtime and memory costs, current Discrimination Network construction algorithms mostly work rule by rule. According to (The CLIPS Team, 1992) the Rule-based System CLIPS tries to identify condition parts already present in the network for sharing. The concept used in (Hanson and Hasan, 1993) also mentions node sharing and the rating function used to identify the best possible network assigns costs of zero to network parts already present because of earlier rules constructions. Taking the sharing of network parts already constructed into consideration is a good first step, but it will not always be possible to exploit node sharing to its full extent. This is the case e.g. if the nodes were constructed in a way, that the network is (locally) optimal for the single rule it was constructed for, but prevents node-sharing w.r.t. further rules and might therefore thwart finding the (globally) optimal Discrimination Network for all rules in case sharing the nodes would have reduced costs (cf. Example 3.1).

![Figure 2: Simple node sharing example network](image)

**Example 3.1.** Assume there are two filters: filter $f_1$ uses facts of type $a$ and $b$, filter $f_2$ uses facts of type $b$ and $c$. Furthermore there are two rules: rule $r_1$ using $f_1$ and rule $r_2$ using $f_1$ and $f_2$. Then filter $f_1$ is used in both rules and we can construct a Discrimination Network where both rules use the same node to apply $f_1$ to the input (see Figure 2). If we were to construct rule $r_2$ first and would have decided to construct the node $f_2$ as an input for $f_1$, sharing $f_1$ with $r_1$ afterwards would have been impossible, since the output of the node for $f_1$ is also already filtered by $f_2$.

It is therefore advisable to construct the Discrimination Network, taking into account the set of rules as a whole.

### 4 CHALLENGES

Since node sharing is beneficial in most situations, Discrimination Network construction algorithms should be presented the necessary data to maximise the potential savings in runtime cost and mem-
Assume there is an additional third rule $r_3$ using only the filter $f_2$. Now $f_1$ is part of $r_1$ and $r_2$ 

![Diagram Figure 3: $f_1$ shared, twofold materialisation of $f_2$.](image)

**Example 4.1.** Assume there is an additional third rule $r_3$ using only the filter $f_2$. Now $f_1$ is part of $r_1$ and $r_2$ 

![Diagram Figure 4: $f_2$ shared, twofold materialisation of $f_1$.](image)

while $f_2$ is part of $r_2$ and $r_3$. Despite the fact that there are two non-trivial rule condition subsets, we can’t share both filters between the three rules in an intuitive way. The rule $r_2$ requires a network that applies the filters $f_1$ and $f_2$ successively. Yet, the rule $r_1$ ($r_3$) needs the output of a node applying nothing but $f_1$ ($f_2$), meaning the corresponding nodes receive unfiltered input. Thus, we need two nodes for the two filters side by side at the beginning of the network and some additional node to satisfy the chained application of the two filters. There are three result networks 

![Diagram Figure 5: Sharing conflict solved using a special join.](image)

still applying node sharing to some extent: We can either share $f_1$ and duplicate $f_2$ (Figure 3), share $f_2$ and duplicate $f_1$ (Figure 4), or re-use both nodes for $r_2$ by introducing an additional node that selects only those pairs of facts that contain identical $b$-typed facts in both inputs (Figure 5).

Formalising the phenomenon just observed, we say that two filters are in conflict if they use the same facts.

Employing the rating algorithm for discrimination networks presented in (Ohler et al., 2013), we compare the costs of the networks in Figure 5 and Figure 3. The memory consumption is the same in all situations, as the additional node always stores the same data. To simplify matters, we ignored the effect of paging and only inspected costs introduced by the insertion of additional facts. The costs of fact deletions look similar. Let $c(b = b')$ be the runtime cost for the additional node in Figure 5 regarding insertions and let $c(f_1)$ be the runtime cost for the additional $f_1$ node in Figure 4. Then

$$c(b = b') - c(f_1) = F_1(b) \cdot |c| \cdot |a \times_{f_1} b \times_{f_2} c| \geq 0$$

determines the additional costs needed for the node $b = b'$ not necessary for an additional $f_1$ node regarding fact insertions. $|c|$ represent the estimated fact count in the node $c$. $F_1(b)$ is an estimate for
the frequency of fact insertions into the node $b$. $|a \triangleleft f_1 b \triangleleft f_2 c|$ is an estimate for the number of facts that match the two join predicates $f_1$ and $f_2$. So, it is never beneficial to use the network shown in Figure 5. The result looks analogue for an additional $f_2$ node. The choice between an additional $f_1$ or $f_2$ node depends on the expected data, though.

5 BLOCK NOTATION

To ease the visualisation of conflict situations such as the one described above and to allow for a straightforward network construction, we introduce a graphical representation called the block notation. A block in this notation consists of conflicting filters and rules sharing those filters (i.e., the corresponding nodes). Blocks are thus sets that are consistent in that all filters in a block are contained in all rules of the block and all rules of the block contain all filters of the block. As a start, we will only consider filters that are in conflict with at most two other filters to allow for two-dimensional diagrams.

Figure 6: Block diagram for Exemple 3.1.

Figure 6 shows the block diagram for Exemple 3.1. The conflicting filters are shown as columns in the grid and the conflicts are emphasised by the $\oplus$. A dot on the grid indicates that a rule uses the corresponding filter. The depicted block contains filter $f_1$ and the rules $r_1$ and $r_2$ suggesting the possibility to share the filter between the two rules.

Figure 7: Block diagram for Exemple 4.1.

Figure 7 shows the block diagram for Exemple 4.1. There are two blocks corresponding to the previously identified common subsets of the rules. The grey marker highlights the fact, that the blocks touch each other implying that node sharing will require some form of special treatment.

We say that two blocks are in conflict if they touch each other vertically or even overlap and it is not the case that all filters of one of the blocks are contained in the other block. Furthermore, a block set is complete if no block is contained in another block and for every rule there is one block containing all filters of the rule. A block is maximal, if we can not add another rule (because no further rule contains all the filters in the block) or filter (because no further filter is contained in all the rules in the block) to it. To further illustrate the block notation, we give another, more complex example.

Example 5.1. Assume there are five filters $f_1, \ldots, f_5$ and three rules $r_1, r_2, r_3$. Rule $r_1$ uses the first three filters, $r_2$ uses all filters, $r_3$ uses the last three filters. The filters $f_i$ and $f_{i+1}$ are in conflict for $i = 1, \ldots, 4$. This information is represented in Exemple 5.1. Additionally, all blocks of maximal size are depicted. The given block set is complete, but there is one conflict in this block diagram: the top left $2 \times 3$ block is in conflict with the bottom right $2 \times 3$ block.

Figure 8: Block diagram for Exemple 5.1 with maximal blocks.

Figure 9: Block diagram for Exemple 5.1 without conflicts.

A different (complete) set of blocks for the same situation is shown in Figure 9. Choosing this partitioning produces no conflicts. Thus we can easily translate it into a Discrimination Network. Figure 10 shows a possible result Discrimination Network leaving out the nodes providing the facts for simplicity.
Constructing the Discrimination Network for a complete, conflict-free block set can be done by materialising the filters in the blocks starting with the blocks containing the fewest filters. Within the set of blocks containing an equal number of filters the order is arbitrary, since none of these blocks can be the input of another block in that set (otherwise they would overlap and would have been in conflict).

The construction order is relevant only if blocks contain the same filter-rule-combinations. Since the blocks are conflict-free and the block set is complete, if one block overlaps with another block, the filters of one of the blocks are a subset of the filters of the other block. As the one with fewer filters is constructed first, its output can be used to construct the larger (w.r.t. filter count) block.

In Example 5.1, we start by constructing the filters $f_1$ and $f_3$ for the $2 \times 1$ and the $3 \times 1$ block, respectively. The next step is to add the filters $f_2$ using the output of $f_1$ and $f_3$ for the $1 \times 3$ block and the filters $f_4$ and $f_5$ in an arbitrary manner using the output of $f_3$ for the $2 \times 3$ block. Finally, we add another $f_2$ for the $1 \times 5$ block using the output of $f_1$ and the network constructed for the $2 \times 3$ block.

Block diagrams become hard to draw and interpret when filters are in conflict with more than two other filters. The concept of blocks and conflicts remains valid, though.

6 CONCLUSION AND FUTURE WORK

We presented the block notation as an abstraction to share nodes and network parts. Using this notation we defined the structure of meaningful sharing constructions. The abstraction can be visualised in block diagrams (in a restricted form) easing the development of algorithms to optimise node sharing.

Based on the notation presented, we are currently developing optimisation algorithms considering several rules at once. The output of such an algorithm should be complete, conflict-free blocks. An optimising Discrimination Network construction algorithm can then use this information to decide, whether node-sharing is beneficial w.r.t. runtime cost and memory consumption for the data to be expected. Developing such an algorithm with acceptable runtime costs although it has to look at a set of rules instead of a single one is pending.

REFERENCES


