Effect of Displaying Uncertainty in Line and Bar Charts

Presentation and Interpretation

D. Jan van der Laan, Edwin de Jonge and Jessica Solcer

Statistics Netherlands, Henri Faasdreef 312, The Hague, The Netherlands

Keywords: Uncertainty Visualization.

Abstract: This paper investigates the effect of presenting uncertainty in bar and line charts in trend-finding and comparison tasks. Different options for presenting uncertainty were investigated in a carefully designed user evaluation that was conducted on statistical analysts, policy makers and journalists (N = 108). The study includes exploring several options for displaying interval estimates with and without point estimates in line and bar charts. We discuss the results for all options and derive presentation suggestions. Our study indicates that showing uncertainty improves the validity of user statements and that data without point estimates have different display needs.

1 INTRODUCTION

In scientific publications experimental results are usually presented with a measure of uncertainty. Surprisingly, this is seldom the case for statistical figures presented by national statistical offices and other statistical agencies. When a measure of uncertainty is known, it is usually not presented or little communicated. (Manski, 2014) argues that by not presenting uncertainty measures users may think that the data is error-free or that they conjecture wrong error magnitudes. Census data, inflation, GDP are shown in tables, bar and line charts without an indication of their precision, although important policy decisions are made based on these data (Reckhow, 1994; Spiegelhalter et al., 2011). Setting aside that calculating uncertainty measures users may think that the data is error-free or that they conjecture wrong error magnitudes. Census data, inflation, GDP are shown in tables, bar and line charts without an indication of their precision, although important policy decisions are made based on these data (Reckhow, 1994; Spiegelhalter et al., 2011).

There is a limited body of literature on visualization methods for uncertainty especially for basic chart types such as the line and bar chart. A number of papers give an overview of possible encodings for uncertainty (Thomson et al., 2005; Pang et al., 1997; Pang et al., 2001; Griethe and Schumann, 2006; Griethe and Schumann, 2005; Zuk, 2008). However, most are applied to more complex graphs such as 3D scientific visualizations and maps. Several papers stress the importance of visualizing uncertainty and give examples and guidelines. (Spiegelhalter et al., 2011).
226

2011) focuses on the interpretation of probabilistic uncertainty in predictions and introduces methods such as shading and uncertainty areas to visualize this uncertainty. (Cleveland and McGill, 1984; Cleveland and McGill, 1985) show how statistical data can be analysed using visualizations. They introduce error bars in scatter plots and bar charts. (Cumming and Finch, 2005) argue that confidence intervals should be used more and offers guidelines for using and displaying confidence intervals to increase their readability. (Olston and Mackinlay, 2002) differentiate between statistical and bounded uncertainty providing different visualization methods for these types of uncertainty. They reserve error bars for statistical uncertainty and use area graphs for bounded uncertainty. The paper visualizes multiple chart types with both types of uncertainty, but does not test these in a user study. (Sanyal et al., 2009) provides a user study on the effectiveness of uncertainty on 1D and 2D data. The paper compares error bars, glyph sizes, glyph color and surface color for displaying uncertainty in dense data and tests for correctness of the size of the uncertainty using an evaluation framework. The focus is on assessing uncertainty and letting users find regions of high uncertainty. Noteworthy is that error bars performed worse than the other methods that were tested. (Tak et al., 2013) describe research on the perception of uncertainty by non-experts, which is similar to our paper, but test user certainty to assess the likelihood of several \( \hat{y} \) given different uncertainty visualizations. Most papers, except the last two do not include an user study to test the effectiveness of their suggestions. More importantly, while previous papers describe how uncertainty should be displayed so a user can accurately assess the amount of uncertainty (e.g. \([\hat{y}_i, \hat{y}_u] \)) or the likelihood of \( \hat{y} \), we focus on the effect of displaying uncertainty on the interpretation and usage of the line and bar chart.

2 CHARTS

We discuss below the methods used to show uncertainty intervals in line and bar charts. For bar charts it is necessary to introduce new variants, as the existing method is not suitable for showing interval estimates without a point estimate.

2.1 Line Chart

A line chart connects individual data points with a line. Almost always the order in which they are connected is time, so line charts are most often used to display time series, with time projected on the \( x \)-axis and the statistic \( y \) of interest on the \( y \)-axis. In this paper we restrict the use of a line chart to time series and assume that its intention is to reveal change of statistic \( y \) over a period of time \([t_1, t_n]\): is the phenomenon visualized in the chart increasing, stable or decreasing? Each \( \hat{y}(t_i) \) in a line chart is uncertain so the (overall) change of the statistic can be noisy and difficult to assess. Since reading and interpreting this trend is its most important goal, we focus on how displaying the uncertainty interval affects the perception of the trend in the series \( \hat{y}(t_1), \cdots, \hat{y}(t_n) \). It is assumed that the uncertainty in a line chart is one dimensional: it is in the \( \hat{y} \) but not in time.

There are two popular ways of displaying uncertain data in line charts: error bars and ribbon charts (see figure 1). Error bars are used mostly in academic literature while ribbon charts were popularized in weather forecasts. Both error bars and ribbon charts are able to show the uncertainty interval and optionally the point estimate. Note that line chart types ribbon and error bar allow for investigating the perception of interval estimates when no point estimate is available.

2.2 Bar Chart

Bar charts plot data points by encoding the estimated value \( \hat{y} \) for group \( i \) in the length of bar \( b_i \). Bar charts are typically used for comparing the absolute values of \( \hat{y} \) between different groups. Is the population of Berlin larger than that of Paris? Is drug \( a \) more effective than drug \( b \)? Comparing absolute values explains for a large part the popularity of the bar chart in the sciences and communication of official statis-
tics. We focus on the more difficult and ambiguous task of comparing absolute values when uncertainty intervals are displayed. For displaying uncertainty intervals $[\hat{y}_l, \hat{y}_u]$ in a bar chart almost always the error bar is used. Research (Sanyal et al., 2009) indicates that error bars are not the most readable type of charts.

A bar chart with error bars has several perceptual problems. First, the bar chart puts a visual focus on the point estimate. Since $\hat{y}$ is encoded in a color filled rectangle and $[\hat{y}_l, \hat{y}_u]$ in an error bar, the point estimate $\hat{y}$ visually dominates. Second, the upper bound $\hat{y}_u$ gets more visual attention than the lower bound $\hat{y}_l$. Since the bar has a color fill and the background of a chart usually has no fill, the contrast of the upper and lower boundary of the error bar is very different. Finally, in a bar chart it is not possible to present an interval estimate without a point estimate.

There are some other visualization methods found in literature used for comparing distributions, most notably the boxplot (Tukey, 1977), dotplot, stripchart (Cleveland, 1993) and violin plot (Hintze and Nelson, 1998). However, none of these is very suitable for presenting statistical estimates. All of them except the dotplot present distributions and some display individual values, which is not possible for statistical estimates. Furthermore, none of them use length to encode the absolute value of the data as they focus on the differences between the measured points.

To account for the perceptual problems of the bar chart we created two alternatives: the chisel and cigarette chart. These had the following requirements:

- They should be closely related to the bar chart: use length for encoding $\hat{y}$
- They should put the same visual attention on $[\hat{y}_l, \hat{y}_u]$ and $\hat{y}$.
- They should support plotting $[\hat{y}_l, \hat{y}_u]$ without $\hat{y}$.
- Lower bound $\hat{y}_l$ and upper bound $\hat{y}_u$ should be equally visible.

### 2.2.1 The Chisel and Cigarette Chart

The chisel and cigarette chart are based on the boxplot in which the most probable interval is visualized using a box and the most likely value with a line in this box. For the chisel and cigarette chart, this was translated into drawing a rectangle from $\hat{y}_l$ to $\hat{y}_u$ and a (optional) line at $\hat{y}$. The charts differ in the way the total length of the bar is drawn. Both variants are shown in figure 2.

The chisel chart is a bar chart in which $[\hat{y}_l, \hat{y}_u]$ is encoded with a rectangle with increased width, hence its name. The optional $\hat{y}$ is drawn with a line. The cigarette chart shows the uncertainty interval clearly and allows to omit $\hat{y}$. However it is to be expected that since the chisel chart is very similar to a bar chart that visual attention is drawn to the upper boundary. A user might think that the upper bound $\hat{y}_u$ is the point estimate $\hat{y}$.

The cigarette chart is a bar chart in which $[\hat{y}_l, \hat{y}_u]$ is encoded with a lighter colored rectangle enclosed in the bar. The optional $\hat{y}$ is indicated with a line. The cigarette chart shows the uncertainty interval clearly and allows to omit $\hat{y}$. A possible disadvantage of the cigarette chart is the same as for the chisel chart: a user could mistake the upper bound for the point estimate.

### 3 METHODS

#### 3.1 Experimental Design

The goal of present research is to investigate how displaying uncertainty effects a user to find a trend in a line chart and how it affects the comparison of values in a bar chart. Note that it was not investigated how well $[\hat{y}_l, \hat{y}_u]$ could be estimated by the respondents or how certain a user is about reading a value from a chart.

The variants of the two chart types were tested using an online survey in which respondents were asked to perform regular tasks with these charts. The target population of the research are statistical analysts, policy makers and journalists. Therefore, crowd source testing (Heer and Bostock, 2010) was not a viable option for the survey. The large number of questions also made this difficult. Therefore the charts were tested using an online survey. Emails were sent to a list of contacts we had in government departments, government institutes and some data journalists with the request to pass the message on to relevant contacts. The survey started with a few background questions (education level, type of occupation, previous experience) which were followed by five groups of questions on line graphs, six groups of questions on...
bar charts and finally two groups of questions on preferences.

As line charts are used to show trends, respondents were asked if there was a trend visible in the graph, which they could answer in five certainty levels. Bar charts are used to compare figures and read figures from the graphs. Therefore, respondents were asked to do just that and again could answer this in 5 different certainty degrees.

Five possible types of line charts were tested: line, ribbon + line, error bar + line, ribbon and error bar. To test the difference in perception for each type, five data sets were created. Two of these have no trend (high and low uncertainty), two have an increasing trend (high and low uncertainty) and one has a decrease followed by an increase. To exclude learning effects each respondent was randomly assigned to one of five groups that was shown each line chart type with a different data set. Furthermore, each line chart type was tested with each of the data sets which should largely correct for any effects of the data set on the interpretation of the graph.

The same design was used for the bar chart. There, six types were tested: each of the three types (error bar, cigarette and chisel) with and without showing the point estimate. Therefore, six data sets were generated and the respondents were divided into six groups.

For the line chart, each respondent was asked 4 different questions for each chart type. In the first question the respondent had to answer if the trend was increasing or not (5 possible answers), the second was to assess if value $\hat{y}_t$ was probably higher than $\hat{y}_{t-1}$ in previous year, the third to approve a detailed statement on the data and the last one was to read a specific value from the chart. The last three questions should be straightforward for a normal line chart, but were included to see how they perform in the other chart types.

For the bar chart, the respondents were asked four different questions for each graph. In the first three the respondents had to answer for a combination of two bars which of the two was higher (5 possible answers). In the final question they were asked to read a figure from the graph (open answer). The last question was included to assess the chisel and cigarette plot and to find out what users do when point estimate $\hat{y}$ is not available.

### 3.2 Analysis

Most of the answer categories could be recoded to dichotomous variables. In principle the design should be-balanced. However, because of the large number of combinations of graphs and data sets (25 and 36 for the line and bar charts respectively) and the limited number of respondents, some unbalance remained. Therefore, in order to test for a significant effect of the graph type on the results a logistics model was fitted that predicts the variable under investigation. This model contained the interaction of the data set and the question (in case of multiple questions), and the graph type. A significant effect of graph type indicates that even when correcting for question and data set, the graph type has an effect on the response.

For brevity, the results of the logistic regressions are not presented in the results section. Only tables and figures are presented. However, significant effects (following from the logistic model) are indicated in the text. A confidence of 95% was used for the tests.

### 4 RESULTS

When the survey was closed, we had 108 complete responses of which 78 came from our statistical office. We had quite a large number of incomplete surveys (98) which were not used in the final analysis. The probable reason for this is that respondents found the survey harder to fill in than anticipated (it was pre-tested on a few colleagues) and, therefore, took more time than anticipated. Table 1 gives an overview of the response and shows that the respondents are highly educated and most have a job in which they work regularly with data: our target group.

#### 4.1 Line Chart

In the first question for each of the line charts the respondents had to assess if the trend in the chart was increasing with the following answer options: certainly
Table 3: Types of given answers when asked to read a value from a line chart with uncertainty (estimated standard deviations omitted for space).

<table>
<thead>
<tr>
<th>Answer type</th>
<th>With line</th>
<th>Without line</th>
<th>Tot.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Line</td>
<td>Ribbon</td>
<td>Error bar</td>
</tr>
<tr>
<td>No answer</td>
<td>1%</td>
<td>2%</td>
<td>3%</td>
</tr>
<tr>
<td>Point</td>
<td>90%</td>
<td>65%</td>
<td>54%</td>
</tr>
<tr>
<td>LB</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>Point+LB</td>
<td>1%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>UB</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>Point+UB</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>LB+UB</td>
<td>6%</td>
<td>19%</td>
<td>28%</td>
</tr>
<tr>
<td>Point+LB+UB</td>
<td>3%</td>
<td>15%</td>
<td>16%</td>
</tr>
<tr>
<td>Total</td>
<td>108</td>
<td>108</td>
<td>108</td>
</tr>
</tbody>
</table>

Table 2: Correctness of trend assessment and correctness of assessment of year to year change in line charts for different chart types. In brackets the estimated standard deviation.

<table>
<thead>
<tr>
<th>Type</th>
<th>Answers</th>
<th>Trend Correct</th>
<th>Change Correct</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ribbon + line</td>
<td>90</td>
<td>85.9(3.3)%</td>
<td>67.6(4.9)%</td>
</tr>
<tr>
<td>Error bar</td>
<td>83</td>
<td>85.5(3.9)%</td>
<td>82.4(4.2)%</td>
</tr>
<tr>
<td>Error bar + line</td>
<td>82</td>
<td>81.7(4.3)%</td>
<td>66.7(5.2)%</td>
</tr>
<tr>
<td>Ribbon</td>
<td>86</td>
<td>80.2(4.3)%</td>
<td>79.6(4.4)%</td>
</tr>
<tr>
<td>Line</td>
<td>91</td>
<td>74.7(4.6)%</td>
<td>67.6(4.9)%</td>
</tr>
</tbody>
</table>

Increasing, probably increasing, probably not increasing, certainly not increasing. The answers of the respondents on the different types were compared with the statistical significance of the trends in the data. Data sets 1 and 2 had no significant trend but data sets 3 and 4 did have a trend. Data set 5 had a decrease followed by an increase and was included in the analysis of this question. The answers of the respondents were split into two variables: correctness and certainty. An answer is considered correct when the respondent sees an increase when there is a significant trend and seeing no increase when there is no increase. An answer is considered certain when an answer category is chosen without the word ‘probably’ in it. As discussed in section 3.2, a logistic regression regression was applied to test for significance in both correctness and certainty.

The results for correctness (table 2) show that line without indication of uncertainty scores lowest on correctness. The ribbon + line chart scores best, which may be due to its frequent use in media. Remarkable is that error bar is second and scores considerably better than the other options, including ribbon. Error bar may emphasize the uncertainty in the value leading to better assessment of the significance of the trend, while in other options the direction of the line or ribbon may influence user perception.

Unsurprisingly respondents get more uncertain in their answers for chart types where uncertainty is shown and even more cautious when no line is shown.

For error bar this is most clear and statistically significant ($p < 0.001$).

In the second question respondents had to answer whether $y(t_i)$ was probably higher than $y(t_{i-1})$, with two answer options: ‘Yes’ or ‘No’. Their answers were recorded in correct and incorrect: when the uncertainty interval of $y(t_i)$ overlapped more than 50% with the uncertainty interval of $y(t_{i-1})$ (or vice versa), the correct answer for each question was considered ‘No’ and ‘Yes’ otherwise. Notice that this correctness criterion could be unfair to line, since that chart does not show uncertainty intervals. However since the time series contained noise, respondents were aware that the values of the line were not exact. Furthermore in ambiguous cases line might induce a more clear decision. The criterion stresses the point that users need an indication of uncertainty for a valid reading of a line chart. The correctness of the answers for year to year change over all the data is shown in table 2.

The scores show two groups: with and without point estimate (i.e., line). The figure indicates that in general adding a line deteriorates the validity assessment of a year to year change. It should be noted that the scores for the different line charts differ over the data sets and in specific cases (e.g., data set 2), line scores among the best. This can be explained by the fact that in those cases the overlap of the uncertainty intervals was considerable but less than 50%. Line shows a clear change, expressed in the slope of the line segment $[y_{i-1}, y_i]$, while the interval methods are more ambiguous to the respondents.

In the final question respondents had to read a value from the graph which was an open question. Although for charts with a point estimate (i.e., line) this should be straightforward, for the charts without line this task is ambiguous. The answers ranged from “don’t know”, to point estimates, the upper and lower bound and a combination thereof.

Table 3 shows the percentages in answers for each line chart type and answer type. Most respondents...
give a point estimate (62%) even for the chart types that do not have a line. These participants derive a point estimate by choosing a value in the middle of the interval. Apparently most users expect that this question has one and only one answer, namely the point estimate. In 25% of the answers an interval is given, which is the second most popular answer type. While this answer is natural for chart types without line, it is remarkable for the other charts, such as line. Those respondents are more confident in giving an interval estimation and chose to exclude the point estimate. 10% of the answers try to give a complete answer, both point and interval estimates.

A final question in the line chart part of the survey was a preference question. Which of the line chart types did the respondents prefer? The answers to this question shown in table 4. When a line is shown, most users prefer ribbon + line, when no line is shown, they prefer error bar.

Table 4: Preferences for each of line chart types depending on whether or not the line is shown. In brackets the estimated standard deviation.

<table>
<thead>
<tr>
<th>Chart type</th>
<th>With line</th>
<th>Without line</th>
</tr>
</thead>
<tbody>
<tr>
<td>Line chart</td>
<td>24</td>
<td>22.2(4.0)%</td>
</tr>
<tr>
<td>Ribbon chart</td>
<td>56</td>
<td>51.9(4.8)%</td>
</tr>
<tr>
<td>Error bar</td>
<td>28</td>
<td>25.9(4.2)%</td>
</tr>
</tbody>
</table>

4.2 Bar Chart

In the first three questions for each bar chart, the respondents were asked to compare two bars to each other with answer options: A is larger than B, A is probably larger than B, they are approximately equal, B is probably larger than A, B is larger than A. Afterwards the answers have been ordered in such a way that the point estimate of B is always larger than that of A. Figure 3 shows the distribution of the answers of the respondents.

Since $\hat{y}_B$ is always larger than $\hat{y}_A$, the answer categories ‘A is (probably) larger than B’ are wrong. The answer ‘approximately equal’ was also considered wrong when the confidence intervals of the two bars do no overlap. The figure shows that number of wrong answers are larger when no point estimates are shown, especially for the error bars. Tests confirmed both effects as significant. The figure furthermore shows that the answer category ‘approximately equal’ is more frequently chosen when the point estimate is not shown. It is less frequently chosen for the cigarette chart. Users seem to be more confident when $\hat{y}$ is shown especially for the cigarette chart.

In the final question respondents were asked to

read information from the table with the following question: ‘According to you, what is the turnover in (X)?’ The respondent had a input box where they could type in their answers. These answers were then recoded into three variables: the lower bound, the upper point and the point estimate. Each of these variables were left missing when missing from the answer. Therefore, for an answer containing only a point estimate only the point estimate is coded, the lower and upper bound are coded missing.

Table 5 shows the types of answers given by the respondents. Most respondents (approx. 60%) only give a point estimate even for the graphs that do not show a point estimate. However, for these graph types this number is slightly lower. Also, a large number of respondents (approx. 30%) only give a lower and upper bound. This number is slightly higher for the graph types that do not show the point estimate. The differences between the different graph types are small and except for the aforementioned slightly smaller number of point estimates for the graph types without point estimate, other differences (probability of lower bound, upper bound, no answer) are not significant.

Figure 4 shows the distribution of the point estimates given by the respondents. The true values of the point estimates and lower and upper bounds are shown by the vertical lines. Each column of graphs shows the distribution for one data set for the different types of graphs investigated. The first thing that can be noted from the figure is that the answers of the respondents are influenced by the position of the tick marks. For example in the third data set (third column in the figure) the true point estimate is 16.6. Since this is between the tick marks 15 and 20, respondents have to interpolate and values of 16 and 17 are reported.

As was mentioned earlier, when the point estimate is not shown most respondents will still report a point estimate. When doing so, they will report a value that
Table 5: Types of answers given when asked to read a bar chart showing uncertainty (estimated standard deviations omitted for space).

<table>
<thead>
<tr>
<th>Answer type</th>
<th>With point estimate</th>
<th>Without point estimate</th>
<th>Tot.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Err. b.</td>
<td>Chis.</td>
<td>Cig.</td>
</tr>
<tr>
<td>No answer</td>
<td>2%</td>
<td>6%</td>
<td>3%</td>
</tr>
<tr>
<td>Point</td>
<td>59%</td>
<td>66%</td>
<td>63%</td>
</tr>
<tr>
<td>LB</td>
<td>2%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>Point+LB</td>
<td>0%</td>
<td>1%</td>
<td>1%</td>
</tr>
<tr>
<td>UB</td>
<td>0%</td>
<td>0%</td>
<td>0%</td>
</tr>
<tr>
<td>Point+UB</td>
<td>0%</td>
<td>1%</td>
<td>1%</td>
</tr>
<tr>
<td>LB+UB</td>
<td>31%</td>
<td>22%</td>
<td>24%</td>
</tr>
<tr>
<td>Point+LB+UB</td>
<td>6%</td>
<td>5%</td>
<td>9%</td>
</tr>
</tbody>
</table>

is midway between the lower bound and upper bound, i.e., they assume symmetric confidence intervals although in practice this need not be the case. Furthermore, when the point estimate is not shown there is a group of respondents that give the lower bound as point estimate for the graph using error bars. This results in a significantly lower point estimate for this graph type.

The data from figure 4 was recoded to show whether the answer was closest to the lower bound, point value, center of the confidence interval, upper bound. When answer is exactly midway between the lower bound and point estimate or between the point estimate and the center, it is assumed that the respondent tried to give the value of the point estimate. This data can be used to test the effects visible in the figure. These tests were performed using separate logistic regressions for each of the four categories. In all models except for the upper bound the effect of the type of graph was significant. A number of observations can be drawn from these results. First, respondents give more correct answers for cigarette and chisel chart compared to error bars. When confronted with a bar graph with error bars respondents seem to have a tendency to give the center of the confidence interval as point estimate. The reason for this is unclear. Second, when the point estimates are not available respondents give the center of the confidence interval as their estimate except for the error bars where they give the lower bound as their estimate. Finally, respondents hardly ever give the upper bound as estimate. Even for the cigarette and chisel chart where this was expected.

Finally, respondents were asked which of the chart types was clearest to them. Table 6 shows the preferences of the respondents. When the point estimate is shown most respondents prefer the bar chart with error bars. When point estimates are not available this changes to the cigarette chart. Surprisingly, in this case the bar chart is still preferred by many respondents, even though this user study shows that many of them have trouble interpreting it. The chisel chart is less preferred in both cases.

Table 6: Preferences for each of graph types depending on whether or not the point estimate is shown. In brackets the estimated standard deviation.

<table>
<thead>
<tr>
<th>Graph type</th>
<th>With point estimate</th>
<th>Without point estimate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bar chart</td>
<td>70</td>
<td>64.8(4.6)%</td>
</tr>
<tr>
<td>Chisel chart</td>
<td>8</td>
<td>7.4(2.5)%</td>
</tr>
<tr>
<td>Cigarette chart</td>
<td>30</td>
<td>27.8(4.3)%</td>
</tr>
</tbody>
</table>

5 CONCLUSIONS

We found that showing uncertainty in line charts improves the validity of the statements users make on the depicted data. When omitting the display of uncertainty, respondents are overconfident in spotting a trend, even though the increase is not statistically significant. They are more cautious when a line chart contains an indication of its uncertainty. When a point estimate is available and shown, a ribbon+line chart scores best in our test. However when is not available, error bar without a line generates the most accurate user statements. Error bars are to be preferred for interval estimates. When a point estimate is shown most users prefer the regular bar chart with error bars over the new chisel and cigarette charts. However, these last two chart types score slightly better in the task of comparing two bars in length. When data does not contain a point estimate, most users prefer the cigarette chart. The results also show that the data in a bar chart with error bars without point estimate is often wrongly interpreted. There are no differences in interpretation between the chisel chart and cigarette chart. Most important to us, against common opin-
Figure 4: Density plots of the answers given by the respondents for the position of the point estimate for each of the data sets (columns) and bar chart types (rows). The true lower bound, point estimate and upper bound are indicated by the vertical lines. The tick marks correspond to the tick marks shown to the respondents.

ion, is that users of official government statistics appreciate the appearance of uncertainty intervals and are able to interpret graphs showing uncertainty. This opens up the possibility to start publishing uncertainty for more output tables as presentation of this extra information is possible in a usable way.

REFERENCES


