Linear Discriminant Analysis for Zero-shot Learning Image Retrieval

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Abstract: This paper introduces a new distance function for comparing images in the context of content-based image retrieval. Given a query and a large dataset to be searched, the system has to provide the user – as efficiently as possible – with a list of images ranked according to their distance to the query. Because of computational issues, traditional image search systems are generally based on conventional distance function such as the Euclidian distance or the dot product, avoiding the use of any training data nor expensive online metric learning algorithms. The drawback is that, in this case, the system can hardly cope with the variability of image contents. This paper proposes a simple yet efficient zero-shot learning algorithm that can learn a query-adapted distance function from a single image (the query) or from a few images (e.g. some user-selected images in a relevance feedback iteration), hence improving the quality of the retrieved images. This allows our system to work with any object categories without requiring any training data, and is hence more applicable in real world use cases. More interestingly, our system can learn the metric on the fly, at almost no cost, and the cost of the ranking function is as low as the dot product distance. By allowing the system to learn to rank the images, significantly and consistently improved results (over the conventional approaches) have been observed on the Oxford5k, Paris6k and Holiday1k datasets.

1 INTRODUCTION

Content-based image retrieval (CBIR) consists in finding the visually closest images with regards to the content of an input query. State-of-the art CBIR systems have been dominated for a while by the bag of visual words (BoVW) representation (Sivic and Zisserman, 2003; Philbin et al., 2007) and its derivatives (Perronnin et al., 2010; Jégou et al., 2012). The BoVW approach involves quantizing local descriptors (usually SIFT) into visual words and representing images by the frequencies of visual words. Approaches based on BoVW derivatives differ from the BoVW approach in that they replace the frequency of visual words with the aggregated version of the difference between image local descriptors and their closest visual words. This aggregation can be done using either Fisher Vector (Perronnin et al., 2010) or Vector of Local Aggregated Descriptor (VLAD) (Jégou et al., 2012). These recent works have been shown to perform significantly better than BoVW approaches.

Recently, researchers have been trying to scale such systems up to large scale datasets, e.g. datasets including a hundred of millions of images (Jégou et al., 2012). In this latest trend, the efficiency becomes more and more important. The ranking must be able to retrieve the images from hundreds of millions of images, almost in real time. An effective retrieval system must be able to obtain high recall using relatively low number of candidates (high precision). Thus, the ranking function plays an important role in effective and efficient retrieval algorithms. Ranking functions used in image retrieval systems can be broadly grouped into two categories: (i) those based on conventional distance measures, and (ii) those based on machine learning algorithms. Conventional ranking, such as dot product, is very often the first choice of many researchers in the field, owing to its simplicity, straightforward interpretation and low computational cost. The second category is employed to better capture the variability in the images and to retrieve semantically related images. A typical scenario of this approach can be: retrieve all the sunset images from the image database by feeding into the system a “sunset” query. This approach is typically more robust when dealing with, semantically related, largely-varying visual content. However, this second approach may need hundreds (or even thousands) of training samples to produce meaningful models. More importantly, they are limited to
a few object categories due to the needed resources.

In this paper, we aim at bridging these two approaches together by means of the zero-shot learning paradigm, in which no training images are available for test categories. We assume indeed no annotation data nor predefined classes are available for learning a classifier/manifold. Given a query image and without any prior knowledge of the data/classes the system should be able to learn a ranking function, adapted to the query, that costs as less as possible and rank the images on a visual-similarity basis. The proposed system, based on Linear Discriminant Analysis (LDA), needs as low as one single sample (the query) to learn a new model for every single query. The cost of learning new query-adapted model is negligible and the ranking is as fast as the dot product distance. This allows us to achieve the highest efficiency comparing to other supervised learning, yet the results can be significantly and consistently improved.

Linear Discriminant Analysis has been a rich source of inspiration in the literature, giving birth to many different variations of the original LDA. For instance, (You et al., 2011) proposed a kernel based LDA algorithm. Differently, (Zhu and Martínez, 2006) extended the original LDA framework by the use of subclasses in compelling complex within-class variations. We claim that those variations of LDA might produce better results over the original version, but would need much more samples to train the model and would require doing a lot of online computations. This would limit the system to work only on those annotation-available objects. In contrast, we show that the original LDA, albeit its simplicity, allows to learn a model without using any annotation data and yet produces meaningful improvement over traditional distance measure.

The remaining of the paper is organized as follows. In section 2, we begin by presenting some related work of LDA in the context of image retrieval system. Then we go gently to various variations of LDA in literature and zero shot learning in general. In Section 3, we present our retrieval approach in the framework of zero-shot learning approach. In section 4, we describe the experimentation protocol followed by our experimental results and discussion. Finally, we conclude the paper in Section 5.

2 RELATED WORKS

LDA has been long used in the context of image retrieval but are targeted for different tasks. For instance, (Tao et al., 2006) used LDA in relevance feedback step to select a subset of image features to construct a suitable dissimilarity measure. (Lu and He, 2005), instead of learning subspace of the image feature, use LDA to obtain the semantic subspace by learning on a large number of user’s feedback information. (Swets and Weng, 1996) used LDA for dimensionality reduction to select the most discriminant features then performed image similarity measure based on euclidean distance. We are interested, in this paper, in using LDA as a query-adapted function for similarity measure (as we will detail in the next section).

LDA has been widely used in literature for classification problems. A number of variations of LDA has been largely studied (Kim et al., 2007; Zhao et al., 2014; You et al., 2011). In (Zhao et al., 2014) a new way to combine the unlabelled data and labelled data together is proposed to enhance the performance of LDA. (Kim et al., 2007) suggested an incremental LDA which is accurate as well as efficient in both time and memory, and could be targeted for online learning tasks. (You et al., 2011) suggested an approach to map the original class (or subclass) distributions into a kernel space where they are best separated by a hyperplane. Experimental results in a large variety of datasets have demonstrated that this approach achieves higher recognition rates than most of other methods based on LDA. In the latest work related to LDA (Deng et al., 2014), the idea is to extend the classical LDA technique to linear ranking analysis, by considering the ranking order of class centroids on the projected subspace. This technique, even if targeted for zero-shot learning, would require annotation data to optimize two criteria: (1) the minimization of the classification errors with the assumption that each class is gaussianly distributed; (2) the maximization of the sum (average) of the k minimum distances of all neighbouring-class (centroids) pairs.

However, these improved versions of LDA contrast with our motivation where we assume no annotation data is available and the system should be able to retrieve any object without prior knowledge of it. To the best of our knowledge, we are the first to propose this ranking strategy based on one-shot learning approach for image retrieval.

Unlike LDA, zero-shot learning is relatively new in the domain. Zero-shot learning is useful to predict a new class label whose training data is not available for learning. For example, (Larochelle et al., 2008) experimented and reported to be able to uncover the novel classes of digits that were not presented in the training set. The motivation comes from the fact that no training data can cover all the possible objects in real world, but only some sort of description is available for that object category. Zero-shot learning
makes use of those descriptions to uncover the hidden category. In (Palatucci et al., 2009), the authors proposed a semantic knowledge (concept) to extrapolate to novel classes. The observation \( x \) is first described in the feature space, then the model will map \( x \) in the feature space to a semantic space of \( p \) dimensions, then map this semantic encoding to a class label. (Lampert et al., 2009), however, introduced a binary attribute layer to describe various object instances and detect unseen object classes based on these attributes. (Parikh and Grauman, 2011) worked on the same “attribute based” principle, but in a relative way via a trained ranking function. Interestingly, (Hoo and Chan, 2013) used probabilistic latent semantic analysis to discover attributes (topic) in an unsupervised manner and use it in zero-shot learning approach.

3 OUR APPROACH

Let \( q \) be a query image and \( q = \{q_1, q_2, \ldots, q_D\} \in \mathbb{R}^D \) a set of visual features representing the image. We address the question of how to represent images by \( D \)-dimensional features later in this section.

On the other hand, we assume having a large collection of images, denoted as \( X = \{x_1, x_2, \ldots, x_n\} \), \( x_j \in \mathbb{R}^D, \forall j \in [1 \cdots n] \). These images are represented using the same type of visual features as the query. The retrieval system has to be able to retrieve, as efficiently as possible, the set of the most similar images, based on their distance to the query. This is to say that we have to rank the images of the dataset according to their distance to the query, i.e. we have to compute \( X' = \{x_{r(1)}, x_{r(2)}, \ldots, x_{r(n)}\} \) such that \( S(q,x_{r(i)}) < S(q,x_{r(j)}) \iff i < j \), where \( i, j \in [1 \cdots n] \). \( S \) is a function measuring the visual similarity between two images.

As said in the introduction, the most commonly used similarity function is the dot product, i.e.

\[
S(q,x_i) = q^T \cdot x_i
\]  

(1)

because of its simplicity and efficiency (Sivic and Zisserman, 2003; Jagou et al., 2012; Perronnin et al., 2010)). However, as the dataset becomes larger, having a better similarity function becomes crucial to avoid overwhelming the user with irrelevant images. The conventional ranking function is very fast but does not cope well with variations of the images. Metric learning is efficient and better captures the variations, but requires too much training data and can only be applied to those data-available object categories (implying that some categories must be pre-defined, which is not the case in general).

Our approach consists in defining the similarity function based on Linear Discriminant Analysis in the context of zero-shot learning to overcome this limitation. The goal of zero-shot learning is to map the observations to an object class even if the direct mapping function is not available (the model of this class could not be trained). A general paradigm to achieve this is first by mapping the observation into another space (e.g. semantic space or attribute space). Next, another mapper will map the observation from the mid-level feature to the class label. Unlike other zero-shot learning systems that mostly operate on mid-level features (attribute or semantic layer) and for which there are some available training data (on the seen category) to derive unseen objects, our approach works on almost no seen object category. The only knowledge we have to know lies in the two matrices \( \mu \) and \( \Sigma \), which are the mean and covariance of the distribution of \( X \). The interesting point is that these matrices can be pre-computed once for all and do not depend on the query.

Let us start by assuming that the images of \( X \) can either be relevant or non relevant to the query \( q \). The distributions of these two classes can be approximated by multivariate normal distributions characterized by their means and the covariance matrices \( (\mu_y=1, \Sigma_y=1) \) and \( (\mu_y=0, \Sigma_y=0) \).

**LDA based Similarity Function.** In LDA, an observation is labeled as relevant if \( P(y=1|x) > P(y=0|x) \) where \( P(y=k|x) \) is represented by a multivariate normal distribution \( f \):

\[
P(y=k|x) = \frac{f(x;\mu_k,\Sigma_k)}{\sum_{l=0,1} f(x;\mu_l,\Sigma_l)} P(y=l)
\]

(2)

where \( \Sigma_{l=0,1} P(y=l) = 1 \) and \( P(y=l) \) is the prior probability of the class \( l \). Using the log of the likelihood ratios, the previous equation becomes:

\[
\log \left( \frac{P(y=1|x)}{P(y=0|x)} \right) = \log \left( \frac{f(x;\mu_1,\Sigma_1)}{f(x;\mu_0,\Sigma_0)} \right) + \log \left( \frac{P(y=1)}{P(y=0)} \right) > 0
\]

(3)

However, we do not assume having any training image at all to explicitly define the two classes. The idea is hence to approximate the values of \( (\mu_y=1, \Sigma_y=1) \) and \( (\mu_y=0, \Sigma_y=0) \). The dataset \( X \) where the non-relevant images are generally dominant is a good distribution to approximate the non-relevant class. Hence, let \( \mu_y=0 \) and \( \Sigma_y=0 \) denote the mean and covariance of the distribution of \( X \). Even if this assumption does not hold because it might contain some relevant images, we will show that the achieved results are significantly improved in the experimentation section. To approximate the relevant class, we employed...
the query image \( q \) as a single known vector. The query image will be used as the center of the distribution \((\mu_q, y_q = q)\). As we do not have enough images to approximate the value of \( \Sigma_{i=1} \), we make the assumption that the two classes share the same covariance matrix \((\Sigma_{i=0} = \Sigma_{i=1} = \Sigma)\). Hence, the equation (3) can be rewritten as:

\[
\log \left( \frac{P(y = 1|x)}{P(y = 0|x)} \right) = \log \left( \frac{P(y = 1)}{P(y = 0)} \right) - \frac{1}{2} (q - \mu_y = 0) \Sigma^{-1} (q - \mu_x = 0) + x^t \Sigma^{-1} (q - \mu_x = 0) > 0
\]

(4)

The ranking of the images can be obtained by simply using \( w^t x > C \) where \( w = \Sigma^{-1} (q - \mu_x = 0) \) and \( C \) is a constant based on prior probability, mean and covariance. As we are interested by ranking the dataset and not detecting relevant/non relevant images, \( C \) can be ignored as it does not depend on \( x \). By replacing this new similarity function in the Eq. (1), we obtain:

\[
S(q,x_i) = w^t . x_i
\]

(5)

where \( w = \Sigma^{-1} (q - \mu_x = 0) \). This is particularly useful because the \( w \) can be obtained at almost no cost (simple products/sums) for each iteration and the value of \((\mu_x = 0, \Sigma)\) can be calculated offline.

The dot product in Eq. (5) between the hyperplan \( w \) and the observation \( x_i \) can thus be seen as the difference between two mahalanobis distances, with the same covariance matrix, of \( x_i \) to the centers of the two normal distributions. This can be illustrated by the toy example shown in Fig.1. Unlike the conventional similarity measures that compute the distance between the observation \( x_i \) and the query only, our LDA-based similarity function allows one step further by considering also the distance between the observation \( x_i \) and the non relevant distribution \((d(x_i, \mu_0))\).

Computation of the Mean\((\mu_x = 1)\) using Subqueries. In practice, it is generally better to insert more input images to produce a statistically stable mean of the relevant class, so that the model can be more robust to image variations. We introduce here, some additional relevant images by computing sub-windows on the original query (shown in Fig. 2). The additional images are generated with at least 70% of the original size to guarantee that the system is not introducing noise into the model. The mean query \( \hat{q} \) is then calculated on this small set of generated images. \( \hat{q} \) is then used in Eq. (5) in replacement of \( q \). Hence, we obtain:

\[
S(q,x_i) = w^t . x_i, w = \Sigma^{-1} (\hat{q} - \mu_x = 0).
\]

(6)

Image Representation. To better assess the behaviour of our zero-shot learning approach, we employed two image representations namely Fisher Vector (Sánchez et al., 2013) and VLAD (Jégou et al., 2012). The image is first described by a dense SIFT descriptor of 128 dimension which is later reduced to a 64 dimensional vector, thanks to a PCA and whitening, following (Jégou and Chum, 2012). Now, Let \( P = \{p_i, i = 1...T\} \) denotes the set of \( d \) dimensional local descriptors extracted from the image \((d = 64)\). A codebook of size \( K \) is built with a kmeans on these descriptors. We will next calculate the VLAD and Fisher Vector representations as follows:

VLAD. The VLAD descriptor associates each local descriptor to the nearest neighbour visual words (cluster) \( c_i \). Then the differences between each local descriptor \( p_i \) and its nearest visual words are accumulared:

\[
v_i = \sum_{p:NN(p_i) = i} p_i - c_i \text{ for all } i = 1..K
\]

(7)

Figure 1: The black and the red circles represent \( \mu_0 \) (mean of the non relevant distribution) and \( \mu_1 \) (mean of the relevant distribution) respectively. \( x_1 \) and \( x_2 \) represent two particular instances in the dataset. At each iteration, LDA is not only looking for the direct similarity between the query to the observation, but also take into account the non relevant instance and make a comparison whether the observation is closer to the query or to the non relevant distribution.

Figure 2: Example of an original query (first left image) and its associated positive samples generated by extracting sub-windows on the original query (from Oxford Dataset).
The VLAD vector is the aggregated version of all $v_i$. Thus it contains $Kd$ dimensions where $d$ is the dimension of the local SIFT-based descriptor.

**Fisher Vectors.** Let us assume that the samples are independent and can be modeled as a mixture of $K$ Gaussian distributions. Let $\Lambda = \{\omega_k, \mu_k, \Sigma_k, k = 1...K\}$ be the parameters of the mixture of $K$ Gaussians, where $\omega_k, \mu_k, \Sigma_k$ are respectively the mixture weight, mean vector and covariance matrix. Each vector $p_i$ is associated to the Gaussian $k$ with a soft assignment $\gamma_i(k)$ also known as the posterior probability, and defined as:

$$\gamma_i(k) = \frac{\omega_k u_k(p_i)}{\sum_j \omega_j u_j(p_i)} \quad (8)$$

where $u_k(p)$ denotes the $k$-th Gaussian and is defined as:

$$u_k(p) = \frac{1}{(2\pi)^d \sqrt{\det \Sigma_k}} e^{-\frac{1}{2} (p - \mu_k)^T \Sigma_k^{-1} (p - \mu_k)} \quad (9)$$

The Fisher Vector of $P$ can be expressed as the concatenation of the three main components:

$$s_k^P = \frac{1}{\sqrt{w_k}} \sum_{i=1}^T (\gamma_i(k) - w_k) \quad (10)$$

$$s_{\mu_k}^P = \frac{1}{\sqrt{w_k}} \sum_{i=1}^T \gamma_i(k) (p_i - \mu_k) / \Sigma_k \quad (11)$$

$$s_{\Sigma_k}^P = \frac{1}{\sqrt{w_k}} \sum_{i=1}^T \gamma_i(k) \frac{(p_i - \mu_k)^2}{\Sigma_k} - 1 \quad (12)$$

where the division and exponentiation of vectors should be understood as term-by-term operations. The final dimension after aggregation is $(2d + 1)K$ where $K$ is the number of Gaussians and $d$ is the dimension of the local descriptors. To simplify the process, we will follow the same direction as in (Jégou et al., 2012), where it is suggested to keep only the mean component (Eq. 10) and ignore other components. In this case, the Fisher Vector will have only $Kd$ dimensions as in the case of VLAD.

## 4 EXPERIMENTAL RESULTS

In this section, we first introduce our experimentation protocol. Then, we present the experimental results with various settings to show how LDA performs comparing to dot product. Finally, we present the experimental results based on LDA with product quantization and asymmetric distance computation in larger scale retrieval system.

### 4.1 Experimentation Protocol

**Parameters.** The dense SIFT extractor is set to extract 128 features from $24 \times 24$ patches, every 8 pixels. The 128D vectors are reduced to 64D using PCA whitening, which has been reported to improve the performance (Jégou and Chum, 2012). Regarding the size of the codebook, we follow the same protocol as in (Jégou et al., 2012) where $K$ is between 16 and 64. A second PCA is used to reduce the number of features of the VLAD/Fisher Vector; the reduced dimension is in the range 16 to 1024.

**Baseline System.** As baseline system, we choose to employ dot product as similarity measure; all other things being equal. The image representation is the same as the one used in our retrieval system.

**Datasets.** To test the proposed technique, we employed three public datasets (see Table 1): Oxford5k, Paris6k and Holiday1k. Since LDA needs more samples to produce a good covariance matrix, we employed also Flickr1M dataset as a distractor to form Oxford1M, Paris1M and Holiday1M. The retrieval result is measured by the Mean Average Precision (mAP) as in (Philbin et al., 2007).

### 4.2 Results

In this section, we first investigate our approximation of the mean and covariance matrices. We first identify a good trade-off between the number of sub-queries to be used and the computational time to generate them. Then we present the effect of the approximation of the shared covariance matrices. Finally, we present the comparison results between our zero-shot ranking system and the baseline.

### Approximation of the Mean of the Relevant Class.

As shown in Section 3, our motivation is to approximate the two distributions on the fly and to allow the system to learn a new ranking function (Eq. 12). Let us recall that the mean of the relevant class can be approximated by one (the query) or a small set of sub-queries. Fig. 3 shows the mAP vs an increasing size of sub-queries from 1 to 100

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1http://press.liacs.nl/mirflickr/dlform.php
Figure 3: Approximation of the mean of the relevant class using the query or with additional sub-queries from 1 to 100 (abscissa). The ordinate shows the retrieval results measure in mAP learnt with $k = 64$ Oxford dataset. $D'$ refers to the dimension after PCA of Vlad and Fisher vector.

Figure 4: Influence of the approximation of the shared covariance matrix for LDA-based retrieval system. The tested datasets are Oxford5k and Paris6k with different covariance matrices approximated with the images in the dataset itself with flickr1M. (abscissa), with $K = 64$ and the dimension after PCA $D' \in \{16, 32, 64, 128, 256, 512, 1024\}$. The slope of the curves appears to be null when the number of positive samples is superior to 10. The same behaviour is also observed with different codebook sizes ($K = 16$) and other datasets (Holiday and Paris). Interestingly, this suggests that we need only 10 samples to approximate a stable value of the mean. This number is negligible comparing to the size of the dataset. For the rest of the paper, we will fix the number of positive samples to 10.

Approximation of the Covariance Matrices. Because the data set might contain some relevant instances and thus it might affect the covariance matrices, we are interested in this section in the size of the image used to approximate the covariance matrices. We present in Fig. 4, the retrieval results on Oxford5k and Paris6k by employing different numbers of additional sub-queries to generate the covariance matrices ranging from 5k (the original size) to 1M by using the images from flickr1M. When using approximately 5k to calculate the covariance matrices, we observed some unexpected behaviour when the dimension of the vector becomes larger. This effect might be the problem of having no enough observations to produce statistically stable covariance matrices. As shown in Fig. 4, our approximation technique, even if simple yet achieves significant improvement over the results provided by the baseline technique. In the following experiment, we will use the covariance matrices calculated from 1M vectors.

Comparison between LDA and Dot Product. Fig. 5 shows that the results based on LDA are significantly higher than the ones from the dot product. The three left and the three right columns show the retrieval results on (Paris6k, Oxford5k, Holiday1k) and (Paris1M, Oxford1M, Holiday1M). The abscissa represents the dimension of the vector after PCA and the ordinate represent the retrieval results measured in mAP. At almost every dimension and for each dataset, the mAP of LDA is significantly higher than the results based on dot product. In addition, when injecting more images (flickr1M) into the system, the dot product distance seems not to capture well the different variations in the image and thus results in decreasing a lot of mAP while LDA-based retrieval seems to better maintain the retrieval results. The average time for retrieving a single query on a dataset of 1M images based on dot product is around 3.9 seconds while with LDA, it takes around 3.95 seconds.

4.3 Product Quantization

Product Quantization (PQ) and Asymetric Distance Computation (ADC) have been proven to be an effective compression and approximation technique for image retrieval (Jégou et al., 2012). We are interested in this section on how Product Quantization (PQ) and Asymetric Distance Computation (ADC) perform by adapting them to our similarity ranking function. Let $q_r \in \mathbb{R}^D$ be the query vector and $X = \{x_1, x_2, \ldots, x_n\}$, $x_j \in \mathbb{R}^D, \forall j \in [1 \cdot \cdot \cdot n]$, a set of vectors representing the images in the data set. The ADC approximates the distance between the query $q_r$ with $x_i \in X$ by:

$$d(q_r, x_i) = d(q_r, q(x_i))$$ (13)

where $q(x_i)$ is the quantized version (closest cluster vector) of $x_i$ learnt prior to the search. In practice, the size of the cluster should be large enough to better approximate the distance. However, making the
codebook size higher is not favourable due to the cost of complexity at approximation time. Another simple solution is to construct a large set of sub-centroids by splitting the feature vector into \( m \) segments and each segment is encoded in the same manner with a cluster Id number. Hence, the approximate distance can be rewritten as:

\[
d(q_r, q(x_i)) = \sqrt{\sum_{j=1}^{m} d(u_j(q_r), q_j(u_j(x_i))))^2}
\]  

(14)

where \( j = 1..m \) and \( u_j(q_r) \in \mathbb{R}^{D/m} \) corresponds to the \( j^{th} \) segment of the vector \( q_r \). Supposing the vector \( q_r \) has 128 dimensions and \( m \) is set to be 16, each quantizer \( q_j(.) \) has 256 clusters (and thus can be coded with 1 byte), the total number of approximation vector is \( 255^{16} \). During the processing phase, the calculation can be accelerated by using a look-up table.

Although, this technique has been applied on Euclidean distance (see Eq. 14), we aim at adapting this technique with our ranking function where the distance is a simple dot product distance. Recalling our similarity function (Eq. 5), and by splitting the vector into \( m \) segments:

\[
S(q,r) = w^T \cdot x_i = \sum_{j=1}^{m} S(w_j, x_{i,j})
\]  

(15)

Note that, in the previous ADC calculation, the approximation introduced two errors. One by replacing the actual vector with the cluster center, another one occurs when calculating the distance by the sum of distances between each segment. In our dot product, however, the second approximation error is eliminated thanks to the nature of the dot product distance.

We present in Table. 2, the results of PQ + ADC adapted to our ranking function. The experimentation is again running on the three dataset with Flickr1M. The dimension after PCA used are 128 and 1024 coded with 16 and and 64 bytes respectively for each image. At every dimension \( D' \), the retrieval results based on LDA are higher than the one provided by the Dot product ranking. Furthermore, even with PQ, our LDA-based ranking still achieves higher result comparing to the dot product approach. This make our system more robust even if used with high compression technique.

5 CONCLUSION

We have introduced linear discriminant analysis as a ranking approach for image search system in the context of zero-shot learning. By allowing the system
to learn to rank the image, significant and consistent improvement has been validated on several datasets. More interestingly, our approach is able to learn a new query-adapted ranking function at almost no cost and rank the images at the minimum cost as conventional ranking functions. Furthermore, our query-adapted function can be transformed into a single dot product distance and is thus suitable for the state of the art techniques for compression and fast distance calculation. This makes our ranking system suitable even for the context of large-scale retrieval.

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