Improved Representation of Dependencies in Feature-based Parametric CAD Models using Acyclic Digraphs

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Abstract: In an engineering design context, the process of modeling complex 3D parts with feature-based parametric software systems often produces a large number of dependencies between geometric features that are difficult to manage. The resulting network of feature interdependencies can be understood as an alternative representation of the CAD model that can help identify the most important aspects of the geometry, its critical features, and understand the overall complexity and interconnectedness of the model. Being able to visualize and process this information efficiently can significantly enhance design activities and facilitate model reuse, which can ultimately lead to cost and time savings, and better quality models. In this paper, we identify some of the simplifications and elements that are overlooked by current representation techniques and describe the negative consequences of not taking these elements into consideration. We describe a new method and a software solution to generate a simplified, intuitive, and more accurate visualization of a parametric model as an acyclic digraph. Finally, to validate our approach, the proposed representation is compared to existing techniques using a group of CAD models.

1 INTRODUCTION

Over the years, feature-based parametric Computer-Aided Design (CAD) technology has steadily progressed to become a mature and commonly deployed technology for the creation of 3D CAD models and assemblies. In a parametric model, a series of variable parameters and geometric relations control the geometry of the object so it can be modified easily to create different design variants. These elements can be defined by dimensional, geometric, and algebraic constraints (Shah, 1991).

Feature-based parametric modeling systems rely on data structures that maintain geometric information of specific aspects of the model (features) in an associative manner, specifically in the form of parent/child relationships. Therefore, all individual features in the CAD model are connected hierarchically, creating a network structure where every node represents a feature and every connection represents a dependency between two features (Hanratty, 1995). This structure is commonly known as design tree, feature tree, or history tree.

Because of the adaptable nature of the design tree, parametric 3D CAD systems allow the incorporation of design semantics to the model, which facilitates the modification of the geometry by simply changing the values of the parameters and dependencies. In this regard, a parametric model can be considered an intelligent representation of a part.

When dependencies are properly defined, alterations to a parent node will automatically propagate downstream to all its child nodes and the CAD model will adjust and react to changes in a predictable manner (Bodein, Rose, and Caillaud, 2014). Therefore, from a designer’s perspective, it is important to plan the modeling procedure beforehand to determine the most efficient sequence of features, as poor modeling strategies often result in parts that take longer to create and are more difficult or impossible to modify (Hartman, 2005).

Unfortunately, parent/child interdependencies are also the root of many regeneration problems in parametric modeling. As the size and complexity of a parametric model grows, so do the number of dependencies and the degree of interconnectedness of its design tree, which can severely impact maintainability and model reuse (Salehi and McMahon, 2009).
From a user’s standpoint, modeling complex parts requires using and managing large amounts of parametric information and dependencies efficiently, which can be overwhelming and confusing, even for the most experienced designers (Baxter et al., 2007; Mohammed, May, and Alavi, 2008). For this reason, many design firms claim they have difficulties visualizing parametric information, which often has a negative impact on the documentation of design knowledge (Myung and Han, 2001).

Although some tools have been developed to improve the visualization of a CAD model structure (some of which will be discussed in the next section), there are currently no tools that can automatically generate a simple and intuitive representation of all the dependencies in a parametric model for visualization and documentation purposes (Marchenko et al., 2011). In fact, most commercial CAD tools only provide tree views to navigate the model features in a linear manner, which often hinders the understanding of complex relations. Furthermore, the simplifications and assumptions made by these representations are frequently inaccurate and ambiguous, making them impractical and unreliable in production environments.

In this paper, the problems with current representations of parametric model structures are identified and discussed. An improved representation method based on directed acyclic graphs (DAG) is proposed that eliminates ambiguity and simplifies inherited dependencies between features at multiple levels. Additionally, a prototype of our method is presented along with examples of achieved results.

2 RELEVANT LITERATURE

A general description of the hierarchical structure of a parametric CAD model was provided by (Marchenko et al., 2011). According to the authors, a parametric model can be understood as a monohierarchical, tree-like structure consisting of general assemblies, subassemblies, parts, features, dependencies, and parameters, where all elements stand in relation to exactly one parent.

If individual CAD elements are isolated and studied independently, additional dependencies can be added on separate hierarchical layers, resulting in a directed acyclic graph structure, also called polyhierarchy, in which multiple parents are possible for any given node. Consequently, a more complex network structure is produced (Marchenko et al., 2011).

Visualizing the CAD model structure is problematic, particularly for complex models. Efforts include the use of modeling languages such as UML (Wang and Li, 2012) and SysML (Peak et al., 2007; Wölk and Shea, 2009) to help designers define structures that can be implemented in a CAD model, or the application of entity-relationship diagrams borrowed from database technologies (Zhou, 2011). These methods, however, were developed to describe models during the early stages of the design process, not as tools to generate visualizations of existing structures.

The standard method to visualize the model structure implemented by most commercial systems such as SolidWorks®, Catia®, or PTC Creo®, is the design tree (see Figure 1).

Figure 1: Sample design tree in SolidWorks®.

The design tree is not a tool itself, but a chronological representation of all the steps and operations performed to create a specific model. As new features are created, they are sequentially inserted at the bottom of the model’s design tree. The design tree allows the user to go back to any specific point in the design and edit a particular feature or sketch. Nevertheless, it is difficult to visualize and analyze feature interdependencies. Although CAD packages allow designers to select node from the design tree and query their dependencies (the result is typically two lists of nodes with parent and child features), an overall view of the model’s structure is often not available.

Various methods for modeling dependencies in engineering processes have been applied to the visualization of parametric models. For example, feature dependencies can be represented as design structure matrices. A Design Structure Matrix, or Dependency Structure Matrix, (DSM), is a method originally introduced by Steward (1981) for representing and analyzing interdependencies between elements and has become a common modeling tool in a variety of application areas (Eppinger, 1991).
A DSM is a square matrix (i.e., it has an equal number of rows and columns) that shows relationships between elements in a system. In the context of parametric models, a binary matrix is used because it can represent the presence or absence of a relationship between pairs of features in a model. This matrix is described as follows:

- Features of the model are placed down the left side of the matrix as row headings and across the top as column headings in the same order.
- If there exists a parent-child relation from node \( i \) to node \( j \), then the value of element \( i,j \) (row \( i \), column \( j \)) is 1. Otherwise, the value of the element is zero.

The diagonal elements of the matrix do not have any interpretation in describing the system, so they are usually either left empty or blacked out. An example of a DSM is shown in Figure 2.

![Table: DSM showing model dependencies.](image)

Authors Tang et al. (2010) used DSM structures to capture and reuse past design knowledge. Specifically, they use DSM to record information such as interaction levels and design parameters. Researchers Lai and Gershenson (2008) applied DSM techniques based on design features to the representation of dependencies for assembly modularity. Karniel, Belsky, and Reich (2005) used DSM to decompose complex 3D-surface fitting reengineering problems from geometry constraints. In terms of CAD model visualization, Bhaskara (2011) suggested a novel approach to analyze and restructure complex CAD models using DSM techniques. In his work, once all the dependencies were identified and represented as a DSM, he applied partitioning and clustering algorithms to restructure and optimize the final matrix (and, thus, the original model structure). For instance, heavily used features and their closely related dependencies were automatically moved to the bottom of the DSM, and closely connected features were grouped together to form clusters. For his study, he developed the DSMs manually, but he recognized the need for software systems that can automatically generate accurate DSMs for large and complex CAD models. He also acknowledged the need to represent dependencies from auxiliary features and sketches (Bhaskara, 2011).

A more visual, intuitive, and common method to represent dependencies in parametric models is provided by graph-based tools. Generally speaking, a graph \( G \) can be defined as a pair \( G = (V, E) \) where \( V \) is a set of nodes (or vertices) and \( E \), the links (or edges) between two connected nodes. When the edges have a direction associated with them, then the graph is called a directed graph, or digraph.

Graphs have been used to model a variety of problems in many disciplines such as mathematics (Bondy and Murty, 1976), engineering and computer science (Deo, 2004), and economics (Michael and Battiston, 2009). In the context of parametric CAD, models can be understood as directed graph structures where every feature is represented as a node, and every parent-child relation is represented with a directed edge from the parent to the child node, as shown in Figure 3: Furthermore, because the nature of parent-child relations prevents the appearance of directed cycles of loops in the structure, the directed graph is always acyclic.

![Figure 3: Directed graph showing model dependencies.](image)

Graph-based tools have been used to define the relationships and dependencies among the geometric features of parts in mechanical assemblies (Srikanth and Turner, 1990) and more recently, to check tolerance specifications assigned to a CAD model (Franciosa, Patalano, and Riviere, 2010). Researchers Marchenko et al. (2011) proposed a method that uses graphs to visualize and document parametric information of 3D CAD models. Their system is limited to assemblies in the area of sheet metal forming tools, although the authors claim that...
their visualizations and tools can be generalized for design tasks in other branches.

More recently, Patalano, Vitolo, and Lanzotti (2013) presented a software tool that uses graph theory to generate the geometric modeling of mechanical assemblies. Similarly to the previous authors, Patalano, Vitolo, and Lanzotti (2013) also limited their study to assemblies and did not consider the representation of individual parts.

Graphs are also used by Owensby and Summers (2014) to estimate assembly times of products. In their work, the authors generate the connectivity graph of an assembly from assembly constraint information and analyze the structural complexity of the graph using a variety of metrics. Once again, only assemblies are considered.

Some high-end commercial CAD packages such as Catia® and UG-NX® provide tools to explore the structure of CAD models and the links between assembled parts in the form of graphs (Tickoo, 2014).

In the next section, some of the visualization problems with current representation tools are discussed, focusing on the ambiguity of the representations when certain simplifications are made.

3 PROBLEMS WITH CURRENT GRAPH-BASED VISUALIZATION METHODS

Some of the problems with current graph visualization techniques in the area of parametric modeling were identified by Marchenko et al. (2011). The problems described by the authors, however, are mainly concerned with the descriptiveness, readability, and clarity of the graph, i.e., the challenges that need to be overcome to make the graph representation more expressive and understandable. The problems they identified as well as some of their recommendations can be summarized as the following:

- In many models, especially those with a large number of relations, some dependencies cannot be drawn without intersections, which can result in a confusing visualization. Objects and lines in the graph should be drawn without overlapping.
- In large graphs, it is often difficult to track down the hierarchy of individual CAD elements, particularly if the graph is not clearly organized by levels. Connections should be easy to follow, with minimum crossings and bends.
- The designation of certain parameters is not unique. In some cases, to reduce the number of intersections, some graph representations show the same feature as multiple nodes.
- The representation of specific input and output parameters related to a dependency is not shown, which hinders the tracking of information flows. In fact, these specific elements cannot be efficiently displayed by a static visualization, as the large number of dependencies would overwhelm the viewer. Instead, an interactive approach is needed to control the number of elements that are displayed at any given time.
- There is a lack of standardization in terms of the graphical language (icons) used to represent individual CAD elements, which can be confusing due to the abundance of CAD elements and the variety of CAD systems.

Although the previous recommendations can certainly improve the graph representation of the parametric CAD model, they do not consider some of the specific relations that may result in ambiguous representations or incorrect graphs. In the following subsections, two of these specific problems are described.

3.1 Multi-level Relations

An ambiguous graph can be generated if multi-level relations (grandparent-parent-child) are ignored, simplified, or not carefully analyzed. As part of this research, the authors of this paper evaluated this situation using two popular parametric modeling packages, SolidWorks® and Autodesk Inventor®.

To illustrate the problem, two versions (A and B) of a CAD model were used. Both versions are identical in terms of geometry, but different in terms of the parameters used to control the features. The geometry of the models is shown in Figure 4.

The two models differ slightly in the way step 6 ("cut hole") was performed. This 3D operation takes the two-dimensional profile of the circle as input and removes material up to a specified depth, which can be parameterized. Since the design of the part requires the hole to pierce through the top horizontal block, which is 0.5” thick, the depth of the hole must also be 0.5” deep.

In version A of the model, the depth of the cut operation was indicated as a fixed value of 0.5” which goes through the entire top block. In version B, however, the depth of the cut was indicated by
using an existing point as a reference (one of the corners on the base block). This way, if the thickness of the horizontal block needs to be increased, the depth of the cut does not have to be manually adjusted. The two approaches are shown in Figure 5. Both of them will successfully perform the cut and deliver the desired result.

When asked to display the feature dependencies for both models, the CAD packages return the exact same information. The dependency graph for both versions of the model is shown in Figure 6. The node “Extrude1” represents the first extrusion of the original sketch (step 2), node “Extrude2” represents the extrusion of the horizontal block (step 4), and node “Cut” represents the circular hole (step 6).

The dependency between the first node (“Extrude1”) and the third (“Cut”) is problematic. Even though the dependency is displayed in the graph in both versions of the model, its meaning differs greatly.

In the first case (version A), the link between “Extrude1” and “Cut” represents an inherited dependency. “Cut” depends on “Extrude2” and “Extrude2” depends on “Extrude1”, therefore “Cut” depends on “Extrude1.” In other words, “Extrude1” is the grandparent node of “Cut.” This relation indicates that the node “Cut” will be affected by changes in either “Extrude1” or “Extrude2.”

In the second case (version B), the same link represents a direct dependency between “Extrude1” and “Cut.” The geometry of the cut is partially dictated by a geometric element (point P1) that belongs to the feature “Extrude1.”

This inherited dependency occurs naturally in single body parts as a by-product of the Boolean operations that are performed internally to manipulate geometric bodies. As new features are created and added to the model, they are automatically merged or combined with existing features to create one single block of geometry. As a result, all new features will depend, one way or another, on previous geometry. However, from a practical modeling standpoint, these dependencies do not add value to the visualization. The fact that all features are merged together in one single body implies that these types of dependencies exist and that the chain of dependencies always flows from the feature that is created first to the feature that is created last.

To illustrate the situations discussed earlier, we can analyze how the two models react to changes when the geometry is modified by adding a new feature (a third extrusion that passes through point P1) before the hole is cut. While version A will...
update correctly, version B will return a rebuild error because point P1 will no longer available after the third extrusion is created. The sequences of changes are shown in Figure 7.

This example demonstrates how current graph-based representation methods for parametric models, even those implemented by commercial systems, are imprecise when dealing with multi-level or inherited dependencies in single body parts. When such relations are displayed, the resulting graph becomes ambiguous, as it allows for multiple interpretations, each of which represents a different CAD model.

As a solution to this problem, we suggest labelling or marking the inherited dependencies, or using a different color, line type, or symbol for the connector. In certain cases, inherited dependencies can even be eliminated, especially in multi-level relations (such as great-grandparent, grandparent, parent, child) that involve single-body parts with features that already share a different type of dependency. These simplifications can significantly reduce the visual complexity of the graph and help users easily determine the most relevant parametric constraints. This statement reinforces the position of authors Marchenko et al. (2011), whose research pointed out the problem of visually overwhelming users with unnecessary dependencies.

3.2 The Role of Sketches

Although certain 3D features do not require the use of two-dimensional sketches (fillets and chamfers, for example, only consume existing 3D edges, and mirror creates a symmetrical copy of a set of features about a face or a plane), most 3D operations that are used to define the building blocks of a feature-based parametric 3D model require prior definition of one or more sketches as input to generate the desired volume. From a purely functional point of view, however, the vast majority of 2D sketches are used only once (and almost exclusively by one feature). Only occasionally are sketches shared among multiple features to define different geometric elements (a situation that translates into a graph with one parent sketch node and multiple child feature nodes) or used as connecting nodes of a sketch-to-sketch dependency (which is represented as a parent sketch node with a child sketch node).

In this regard, most sketches are shown as intermediate elements in the dependency graph linking two feature nodes, which results in an extra level of connectors that add unnecessary clutter to the graph but no added value in terms of visualization of the parametric relations. To simplify the overall graph, these sketch nodes can be represented with distinctive styles or even eliminated from the graph.
Figure 8: Modeling steps (top) and three visualizations of the model structure (bottom). The classic design tree representation (bottom left) does not provide information on interdependencies. Notice the reduction of nodes in the simplified graph (bottom right) when compared to the full graph (middle) when connecting sketches in single body parts are not shown.

An example of a CAD model (displayed as the sequence of sketching and modeling steps require to build the geometry) along with its corresponding full graph (including all sketch nodes) and the simplified version of the graph according to the criteria discussed in this section are shown in Figure 8.

4 IMPROVED GRAPH VISUALIZATION

Based on the discussion from previous sections, we propose a simplified representation of a dependency graph for parametric CAD models that is more readable, less cluttered, and reduces ambiguity. Our representation is built by reducing the number of nodes in the graph according to the following criteria:

- Connecting sketches used to create a feature that will be merged with previous geometry do not provide value to the user in terms of visualizing and understanding the graph complexity. Therefore, sketch nodes are not displayed, unless they are explicitly used as part of a constraint. Connecting sketch nodes can be identified easily as sketch elements with only one child node (the 3D feature they generate).
- Inherited dependencies are not displayed. Multi-level relations (grandparent-parent-child) are only displayed if there is a specific
constraint that relates the grandparent node to the child node. Otherwise, the dependencies can be implied and therefore, there is no need to make them visible.

The pseudo code for a simplification algorithm to reduce the node and dependency count in the model graph can be written as:

```plaintext
TraverseModel()
For each node n {
If n is a Sketch and has only one child node then {
  //Reconnect dependencies
  For each Parent(n)
    Reconnect to Child(n);
  Remove(n);
}
Else If n is a Feature then
  For each Child(n)
    Check constraints;
    If there is only one constraint and constraint is 'Merge geometry' then
      //multi-level
      delete dependency;
}
}
```

Using two CAD models, a side-by-side comparison of the full graph and our simplified version of the graph according to the criteria discussed in this paper is provided in Figure 9. Node names have been omitted for clarity.

5 CONCLUSIONS

The constant need for tools and methods to support design activities and reuse increasingly complex CAD models naturally demands the development of efficient visualization systems to manage parametric model geometry.

In this paper, we have reviewed some of the most common representation and visualization methods for parametric 3D CAD models, particularly focusing on dependency graphs. Our work describes a series of problems with current graph representation techniques and analyzes the consequences of certain dependencies and CAD elements, and the effects of representing relations that have not been rigorously examined. In both cases, a considerable level of ambiguity is introduced to the graph, resulting in an imprecise or cluttered representation of the model.

Figure 9: Comparison of the full graph and simplified version for two CAD models (A and B). Node names have been omitted for clarity.
We have proposed a simplified representation of the dependency graph by eliminating sketch nodes that do not add value to the overall visualization and only showing the multilevel dependencies (grandparent-child) that are explicitly defined by geometric and dimensional constraints. The result is a clearer and more intuitive representation of the internal structure of the parametric model. While the system need to be tested on a large, "real-world" example with a more extensive group of models, in many cases the number of nodes can be reduced by at least half, which contributes to a more effective visualization.

Although the algorithm presented in this paper was implemented as an add-in for the CAD package SolidWorks, further developments are planned for the near future. At the present time, the software prototype can extract model information and export it to a graph structure (which is visualized by an external application), but a complete interactive solution that is fully integrated within the CAD environment would be beneficial. In addition, the simplified model representation can be analyzed, restructured, and optimized by applying clustering and partitioning algorithms, which have the potential to make models more flexible and reusable. Furthermore, comparative studies of the graph structures can be performed and assessed using complexity metrics.

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