On Reducing the Number of Visual Words in the Bag-of-Features Representation

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Abstract: A new class of applications based on visual search engines are emerging, especially on smart-phones that have evolved into powerful tools for processing images and videos. The state-of-the-art algorithms for large visual content recognition and content based similarity search today use the “Bag of Features” (BoF) or “Bag of Words” (BoW) approach. The idea, borrowed from text retrieval, enables the use of inverted files. A very well known issue with this approach is that the query images, as well as the stored data, are described with thousands of words. This poses obvious efficiency problems when using inverted files to perform efficient image matching. In this paper, we propose and compare various techniques to reduce the number of words describing an image to improve efficiency and we study the effects of this reduction on effectiveness in landmark recognition and retrieval scenarios. We show that very relevant improvement in performance are achievable still preserving the advantages of the BoF base approach.

1 INTRODUCTION

The use of local features, as for instance SIFT (Lowe, 2004), has obtained an increasing appreciation during the last decade, for its good performance in tasks like image matching, object recognition, landmark recognition, and image classification. Briefly, with these techniques an image visual content is described by identifying a set of (interest) points and by describing the region around them with histograms (the local feature), as for instance histograms of brightness gradients. The image match task is executed by first matching the local features, and then by checking if there is some (geometric) consistency between matched pairs of interest point, to decide if images, or objects in images, match as well.

The total number of local features extracted from an image depends on various setting of the feature extraction tools. However, typically it is of the order of some thousands. As a consequence, matching an image against a database of images becomes a very challenging task from the efficiency point of view. For instance, if the database contains one million images and on average every image has one thousand local features, matching a query image against this database requires matching 1,000 different local features, extracted from the query, against one billion local features, extracted from the database.

In order to mitigate this problem, some years ago the Bag of Feature approach (BoF) was proposed in (Sivic and Zisserman, 2003). The BoF approach quantizes local features extracted from images representing them with the closest local feature chosen from a fixed visual vocabulary of local features (visual words). In this way, images are no longer represented by a set of identifiers of visual words from the visual vocabulary that is used to replace the original local features. Matching of images represented with the BoF approach is performed with traditional text retrieval techniques and by verifying their (geometric) consistency. This process can be executed more efficiently, than linearly scanning the entire database, by using inverted files (Salton and McGill, 1986) and search algorithms on inverted files.

However, even if inverted files offer a significant improvement of efficiency, with respect to a trivial sequential scan search algorithm, in many cases, efficiency is not yet satisfactory. A query image is associated with thousands of visual words. Therefore, the search algorithm on inverted file has to access thousands of different posting lists of the inverted file. As mentioned in (Zhang et al., 2009), “a fundamental difference between an image query (e.g. 1500 visual terms) and a text query (e.g. 3 terms) is largely ignored in existing index design. This difference makes the inverted list inappropriate to index images”. From
the very beginning (Sivic and Zisserman, 2003) some words reduction techniques were used (e.g. removing 10% of the more frequent images). However, as far as we know, no experiments have been reported on the impact of the reduction on both efficiency and efficacy.

To improve efficiency, many different approaches have been considered including GIST descriptors (Douze et al., 2009), Fisher Kernel (Zhang et al., 2009) and Vector of Locally Aggregated Descriptors (VLAD) (Jégou et al., 2010). However, their usage does not allow the use of traditional text search engine which has actually been another benefit of the BoF approach.

In order to mitigate the above problems, this paper proposes, discusses, and evaluates some methods to reduce the number of visual words assigned to images. We will see that it is possible to significantly reduce their number with a very minor degradation of the accuracy, and with a significant efficiency improvement. Specifically, we propose and discuss methods based on the use of the scale of the local features that can be applied before the visual words have been assigned and also methods based on statistics of the usage of visual words in images (using the term frequency $tf$), across the database (relying on the inverse document frequency $idf$), and on the $tf*idf$ combination (Salton and McGill, 1986)). We also perform experiments using random reduction as a baseline. The $tf*idf$ approach was also presented in (Thomee et al., 2010) using the SURF descriptor. However, in their work the authors did not present any comparison with other approaches. The effectiveness of the approaches is measured on landmark retrieval and recognition tasks for which local features and in particular the BoF approach is today considered the state-of-the-art. Experiments were conducted on three dataset for testing both retrieval and recognition scenarios.

2 SELECTION CRITERIA

The goal of the BoF approach is to substitute each description of the region around an interest points (i.e., each local feature) of the images with visual words obtained from a predefined vocabulary in order to apply traditional text retrieval techniques to content-based image retrieval.

The first step to describe images using visual words is to select some visual words creating a vocabulary. The visual vocabulary is typically built grouping local descriptors of the dataset using a clustering algorithm such as $k$-means. The second step is to assign each local feature of the image to the identifier of the first nearest word in the vocabulary. At the end of the process, each image is described as a set of visual words. The retrieval phase is then performed using text retrieval techniques considering a query image as disjunctive text-query. Typically, the cosine similarity measure in conjunction with a term weighting scheme is adopted for evaluating the similarity between any two images.

In this section we present five criteria for local features and visual words reduction. Each proposed criterion is based on the definition of a score that allows us to assign each local feature or word, describing an image, an estimate of its importance. Thus, local features or words can be ordered and only the most important ones can be retained. The percentage of information to discard is configurable through the definition of a score threshold, allowing trade-off between efficiency and effectiveness.

The criteria we tested are:

- **random** – A very naive method to reduce the number of words assigned to an image is to randomly remove a specific percentage of local features in the image description. This method is used as a baseline in our experiments.

- **scale** – Most of the local features defined in the last years (e.g., SIFT and SURF) report the scale at which the feature was extracted for each key-point. The fact that extraction is not performed at the original resolution is actually the main reason for the scale invariant. Descriptions and interest points detected at higher scale should be also present at lower resolution versions of the same images or of the same object. The intuition is that the bigger the scale the higher the importance. This approach can be performed before the words assignment phase increasing performance also during the words assignment, since the cost of assigning words to images is linear with the number of local features. Please note that the scale threshold is not defined a priori but it depends on the number of local features actually extracted from the image.

- **$tf$** – During the BoF words assignment phase, each local feature is substituted with the identifier of the nearest word in the visual vocabulary. Thus, after this step every image is described with a set of visual words. Typically a word appears more than once in an image description because distinct but similar local features in the original description were substituted by the very same visual word. A possible approach for words reduction is to remove the words having the lowest number of occurrences. In this case we are ordering the
words with respect to their term frequency (tf) in the image. (Salton and McGill, 1986).

- **idf**: When words have been assigned to all the images in the dataset, it is possible to evaluate the inverse document frequency (idf) (Salton and McGill, 1986) of all the features in the vocabulary. In Information Retrieval words with highest idf are considered more important than the others (Salton and McGill, 1986). Note that depending on the relative idf values of the words describing an image, the same word could be discarded for a given image and retained in another.

- **tf*idf**: In information retrieval a very popular strategy to assign relevance to words is the tf*idf approach (Salton and McGill, 1986). This strategy states that the relevance of a word in a document is obtained by multiplying its tf in the given document by its idf. We can use the same strategy to order the visual words in an image and discard first the words with smaller tf*idf.

3 EXPERIMENTS

The effectiveness of the approaches is measured on both a image retrieval and a landmark recognition tasks using two distinct datasets. Efficiency is also tested on a larger professional dataset intended for similarity search. In the following we describe the recognition system, the performance measures, the datasets and we discuss the experimental results obtained.

The retrieval engine used in the experiments is built as following:

1. For each image in the dataset the SIFT local features are extracted for the identified regions around interest points.
2. A vocabulary of words is selected among all the local features using the k-means algorithm.
3. The Random or Scale reduction technique is performed (if requested).
4. Each image is described following the BoF approach, i.e., with the ID of the nearest word in the vocabulary to each local feature.
5. The tf, idf, or tf*idf reduction technique are performed (if requested).
6. Each image of the test set is used as a query for searching in the training set. The similarity measure adopted for comparing two images is the Cosine between the query vector and the image vectors corresponding to the set of words assigned to the images. The weight assigned to each word of the vectors are calculated using tf*idf measure.
7. In case the system is requested to identify the content of the image, the landmark of the most similar image in the dataset (which is labeled) is assigned to the query image.

Typically, the result obtained with the tf*idf weighting and cosine similarity measure using inverted index is reordered considering geometric checks based on RANSAC (Random Sample Consensus). However, in this paper we focus on optimizing the number of words to improve efficiency of the search performed through the inverted files and thus we do not leverage on geometric consistency checks, which are typically performed on a preliminary set of candidate results or by customized search indexes.

The quality of the retrieved images is typically evaluated by means of precision and recall measures. As in many other papers (Philbin et al., 2007; Jegou et al., 2009; Perronnin et al., 2010; Jegou et al., 2012), we combined this information by means of the mean Average Precision (mAP), which represents the area below the precision and recall curve.

For evaluating the effectiveness of the recognition, which is basically a classification task, we use the micro-averaged accuracy and macro-averaged F1 (i.e., the harmonic mean of precision and recall). Macro-averaged scores are calculated by first evaluating each measure for each category and then taking the average of these values. Note that for a recognition task (i.e., single label classification), micro-averaged accuracy is defined as the number of documents correctly classified divided by the total number of documents of the same label in the test set and it is equivalent to the micro-averaged precision, recall and F1 scores.

For evaluating the performance of the various reduction techniques approaches, we make use of three datasets. The first is the largely used Oxford Building datasets that was presented in (Philbin et al., 2007) and in many other papers. The dataset consists of 5,062 images of 55 buildings in Oxford. The ground truth consists of 55 queries and related sets of results divided in best, correct, ambiguous and not relevant. The dataset is intended for evaluating the effectiveness of a content based image retrieval systems that is expected to put the images related to the very same building at the top of the results list. In fact, the measure of performance used for the evaluation is the mean Average Precision (mAP). The authors of the datasets also made available the words assigned to the images using the BoF approach. The vocabulary used has one million words.

We decided to use a second dataset to better eval-
valuate the performance of a system intended for recognizing the landmark in photos. In this scenario it is not important to retrieve most of the related images in the dataset but to correctly classify the image. The Pisa dataset consists of 1,227 photos of 12 landmarks located in Pisa (also used in (Amato and Falchi, 2011) and (Amato et al., 2011)). The photos were crawled from Flickr. The dataset is divided in a training set (Tr) consisting of 226 photos (20% of the dataset) and a test set (Te) consisting of 921 photos (80% of the dataset). The size of the vocabulary used for the experiments with the BoF approach is 10k. In this context the performance measures used are typically accuracy, precision, recall and micro and macro-averaged $F_1$.

Finally, a larger dataset of about 400k images from the professional Alinari\footnote{http://www.alinari.it} archive was used for efficiency evaluation. All the images were resized to have a maximum between width and height equal to 500 pixels before the feature extraction process.

### 3.1 Evaluation

We first report the results obtained in a content based image retrieval scenario using the Oxford Building dataset using the ground truth given by the authors (Philbin et al., 2007). In Figure 1 we report the mAP obtained. On the x-axis we reported the average words per image obtained after after the reduction. Note that the x-axis is logarithmic. We first note that all the reduction techniques significantly outperform naive random approach and that both the $idf$ and scale approaches are able to achieve very good mAP results (about 0.5) while reducing the average number of words per image from 3,200 to 800. Thus, just taking the 25% of the most relevant words, we achieve the 80% of the effectiveness. The comparison between the $idf$ and scale approaches reveals that scale is preferable for reduction up to 500 words per image. Please note that it is almost impossible to only slightly reduce the number of words with the $tf$ approach because there is a large number of words (about 75%) per image that have just one occurrence. Using the $tf$ approach they have the same quality score and can be only filtered as a whole.

While the average number of words is useful to describe the length of the image description, it is actually the number of distinct words per image that have more impact on the efficiency of searching using inverted index. Thus, in Figure 2, we report mAP with respect to the average number of distinct words. In this case the results obtained by $tf*idf$ and $tf$ are very similar to the ones obtained by $idf$.

A second set of experiments was conducted on a landmark recognition task using the Pisa dataset (see Section 3). For this dataset we used a smaller vocabulary of 10k words and features were extracted from a lower size images (maximum 512 pixels per side). Figure 3 reports the accuracy obtained by the various approaches. On the x-axis we reported the average words per image obtained after the reduction. All the approaches, as expected, significantly outperform the random selection used as a baseline. The best results are obtained by the $idf$ approach. It is also interesting to notice that the scale approach performs very well for reduction up to 25%.

In Figure 4 we report the accuracy obtained with respect to the average number of distinct words per image by the various reduction approaches. The results significantly differ from the previous ones. In particular, the $tf*idf$ and $tf$ approaches exhibit better results. It is worth to say that while the $tf*idf$ approach relies on information about the training set for...
evaluating the $idf$ values, the $tf$ approach performs almost as better as $tf*idf$ can be applied not considering the dataset but only the image for which the words have to be reduced. The $scale$ approach exhibits good results for average number of distinct words down to 300 (i.e., a 25% reduction). Note that the $scale$ technique can be applied before the words assignment thus reducing not only the search cost but also the cost for the words assignment.

The $accuracy$ measure captures the overall effectiveness of the algorithm with respect to the expected distribution of query between the classes. In order to also evaluate the effectiveness across the various classes (e.g., landmarks) we use the macro-averaged $F_1$ measure. Macro-averaged values are calculated by first averaging the measures obtained for each category. In Figure 5 we report the $F_1$ obtained by the various approaches in terms of the average number of distinct words per image. The most important differences between these results and the one obtained considering $accuracy$ are related to the $idf$ and $scale$ approaches. While the $scale$ approach reveals better performances for small reduction even increasing the overall efficacy, the $idf$ results becomes worse than both the $tf$ and $idf$ ones. The intuition is that $idf$ relies on information related to the dataset and thus is influenced by the different number of training images per class. On the other hand, the $scale$ approach is independent from the dataset, given that it does not rely on the words; thus not even on the vocabulary.

In Figure 6 we report the average query execution time obtained on the 400k image dataset with respect to the average distinct words. Results are shown for reducing the visual words on query only and on query and dataset. While results are shown for the $tf*idf$ approach, similar performance are achieved with the other approaches. In fact, for efficiency, it is actually important only the average number of distinct words. The results reveal, as expected, that high efficiency gains can be obtained reducing the number of distinct visual words. Note that the x-axis is logarithmic.

4 CONCLUSIONS

In this work, we have investigated visual words reduction approaches in order to improve efficiency of the BoF approach minimizing the lost in effectiveness. The gain in efficiency was tested on a similarity search scenario of about 400k images, while effectiveness was tested on two smaller datasets intended for content based image retrieval and landmark recognition.

We proposed methods that can be applied before the visual words have been assigned and also methods
based on statistics of the usage of visual words in images (tf), across the database (idf), and on the tf*idf combination.

In the content based image retrieval scenario the scale approach performed best and even better than using all the words. However, for reduction over an order of magnitude effectiveness significantly decreases. In the landmark recognition task, the most interesting results were obtained considering the macro-averaged $F_1$ effectiveness measure with respect to the average number of distinct words per image. The tf*idf obtained the best results, but it is interesting to see that the tf approach, which does not rely on dataset information, obtained very similar results. It is worth to note that the recognition task is more robust than the retrieval to words reduction. Moreover, for small local features reductions scale was the overall best.

We plan to define new approaches and compare with the ones proposed in this work on larger dataset in the near future.

REFERENCES


