A LOSSLESS IMAGE COMPRESSION METHOD WITH THE REVERSIBLE DATA EMBEDDING CAPACITY

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Keywords: Reversible data embedding, Lossless image compression, Image processing.

Abstract: The current reversible data embedding techniques can be divided into 2 categories: those developed by the untreated original images and those developed by the images treated via the lossy compression as the reversible target. So far, there has not been any literature discussing the issue of the reversible data embedding action finished during the lossless still image compression. Our method employs Chuang and Lin’s simplified lossless image compression method to develop a reversible data embedding technique. Our method successfully embeds the secret data in the lossless image compression codes and have the secret data reversed to the original image as the secret data are retrieved from. According to the experimental results, the proposed method performs well on the embedding capacity and compression effects.

1 INTRODUCTION

An effective way to safely transmit secret data to the receiver by Internet is to embed the secret data into the digital media such as image and then transmit the embedded media. This technique is called the information hiding technique. If the embedded media reverse to the original media after the secret data are retrieved, it is called the reversible data embedding technique, otherwise, it is called the irreversible data embedding technique. The proposed technique is the reversible data embedding technique using still grayscale images as the media.

In the recent decade, there are many studies relating to the reversible data embedding techniques. There are 2 major categories under the properties of the media. One is the untreated original images (Alattar, 2004; Celik et al, 2005; Chang & Lu, 2006A; Ni et al, 2006; Thodi & Rodriguez, 2007; Tain, 2003) and another is the encoded images treated by the lossy compression (Chang & Lu, 2006B; Chang & Lin, 2006; Chang & Lin, 2007; Chang, Hsieh & Lin, 2007; Chang, Wu & Hu, 2007). Nevertheless, some application domains such as the medical images, military mapping images and digital artistic works employ the lossless compression techniques to guarantee the exact precision of the image quality for the image storage and transmission. Therefore, it is a key issue to discover the reversible data embedding technique able to add extra data to the images treated by the lossless compression techniques. This paper employs the images treated by Chuang and Lin’s (Chuang & Lin, 1998) simplified lossless image compression technique as the subject to develop a reversible data embedding technique able to successfully embed the secret data in the lossless image compression codes and have the embedded image reversed to the original image as the secret data are retrieved from. According to the experimental results, the proposed technique performs well on the embedding capacity and compression effects.

The rest of this paper is organized as follows. Section 2 introduces Chuang and Lin’s (Chuang & Lin, 1998) lossless compression method. In Section 3, our method is described. The experimental results are presented and discussed in Section 4. Finally, the conclusions are provided in Section 5.

2 CHUANG AND LIN’S (1998) METHOD

2.1 Compression

In this section, the lossless compression technique
proposed by Chuang and Lin for grayscale images is simply illustrated. First, the original grayscale image is divided into \( n \times n \) blocks of which each is treated by the lossless compression from left to right and up to down individually. Since Chuang and Lin have proved that the \( 3 \times 3 \) block leads to the optimal compression effect, the illustration of \( 3 \times 3 \) block is as below. The individual \( 3 \times 3 \) block is treated by the following steps.

Given a \( 3 \times 3 \) block as the subimage \( A \) of which 9 pixel values are \( g_0, g_1, \ldots, g_8 \), see Figure 1.

![Figure 1: Block A.](image)

Find the minimum \( m = \min \limits_{\text{pixel}} g_i \) and the base \( b = (\max \limits_{\text{pixel}} g_i - \min \limits_{\text{pixel}} g_i) + 1 \) in the block.

Then compute \( g'_i = g_i - m, i = 0, 1, 2, \ldots, 8 \). Let \( A' \) denote \( \langle g'_0, g'_1, \ldots, g'_8 \rangle \). We obtain \( \min g'_i = 0 \), \( \max g'_i = b - 1 \), so nine-dimensional vector \( \langle g'_0, g'_1, \ldots, g'_8 \rangle \) can be treated as a nine-digit number \( \langle g'_0 g'_1 \ldots g'_8 \rangle_b \) in base-\( b \) number system.

For convenience, let \( V_{3 \times 3} \) be the collection of all \( 3 \times 3 \) subimage \( A' \), and the base-set \( B = \{ 1, 2, 3, \ldots, 256 \} \). Afterwards, define a function \( f = V_{3 \times 3} \times B \to \{ \text{non-negative integers} \} \)

\[
f(A', b) = b^{-1} \sum_{i=0}^{8} g'_i b^i \]

\( Z_b = \lfloor \log_b b^8 \rfloor \) represents the number of bits required by the binary transformation of \( f(A', b) \).

As to achieve the optimal compression effect, according to the \( b \)-value, there are 3 encoding cases:

**Case (1):** \( 1 \leq b \leq 11 \), the encoding as:

\[
\begin{align*}
&\text{if } c = 0 (1 \text{ bit}), b (7 \text{ bits}), m (8 \text{ bits}), f(Z_b) \text{ bits]), \\
&\text{if } c = 1 (0 \text{ bit}), b (7 \text{ bits}), m (8 \text{ bits}), P(\text{min}, \text{max}) (7 \text{ bits}), f(Z_b) \text{ bits})
\end{align*}
\]

**Case (2):** \( 12 \leq b \leq 127 \), the encoding as:

\[
\begin{align*}
&\text{if } c = 0 (1 \text{ bit}), b (7 \text{ bits}), m (8 \text{ bits}), P(\text{min}, \text{max}) (7 \text{ bits}), f(Z_b) \text{ bits))}
\end{align*}
\]

\( P(\text{min}, \text{max}) \) is used to record the locations of minimum (min) and maximum (max) values of \( A' \). Therefore, there are \( 9 \times 8 = 72 \) combinations. We need 7 bits to record all situations. The computation of \( P(\text{min}, \text{max}) \) is as follows:

**Case 1:** if \( \max - \min \) then

\[
P(\text{min}, \text{max}) = \min \times 8 + \max + 1 \quad (1)
\]

**Case 2:** if \( \max > \min \) then

\[
P(\text{min}, \text{max}) = \min \times 8 + \max \quad (2)
\]

Since the minimum and the maximum of \( A' \) is 0 and \( b - 1 \), recording \( P(\text{min}, \text{max}) \) equals to record 2 pixel values of \( A' \). Therefore, when computing \( f(A', b) \), we only need record the residual 7 pixel values. Consequently, in this case, it is \( Z_b = \lfloor \log_b b^7 \rfloor \) bits rather than \( Z_b = \lfloor \log_b b^8 \rfloor \).

**Case 3:** \( 128 \leq b \leq 256 \), the encoding as:

\[
[ c = 1 (1 \text{ bit}), \text{the 9 pixel values of the original block } (9 \times 8 \text{ bits}) ]
\]

Following the preceding techniques, the first bit value \( c \) of the compression codes of each block indicates that the following bits are either the original 9 pixel values or the compression codes.

The lossless compression technique proposed by Chuang and Lin employs the relation between \( c \) and \( b \) values to neglect \( c \) and further compress the remaining information. However, this paper employs merely the individual block compression technique of Chuang and Lin and introduces the reversible data embedding technique; therefore, the further compression part of Chuang and Lin's method is excluded here. Please see (Chuang & Lin, 1998) for the further detail inforamation.

### 2.2 Decompression

In the decoding procedures, first check the first bit \( c \).

Suppose \( c = 1 \), then take the next 72 bits to derive the original 9 pixel values in the block; suppose \( c = 0 \), then take the next 7 bits to obtain the \( b \) value. There are 2 cases under the \( b \) values.

**Case 1:** \( 1 \leq b \leq 11 \)

We obtain the values of \( m \) and \( f \) by taking the next 8 and \( Z_b = \lfloor \log_b b^9 \rfloor \) bits, respectively. Then represent the decimal integer \( f \) as a non-digit base-\( b \) number \( \langle g'_0 g'_1 \ldots g'_8 \rangle_b \). According to \( \{ g'_i \}_{i=0}^{8} \) and \( m \) values, we can derive the original 9 pixel values in the block.

**Case 2:** \( 12 \leq b \leq 127 \)

We obtain the values of \( m, P(\text{min}, \text{max}) \) and \( f \) by taking the next 8, 7 and \( Z_b = \lfloor \log_b b^7 \rfloor \) bits respectively. Through the value of \( P(\text{min}, \text{max}) \) and Eq.s (1) and (2) we know the positions of the minimum and maximum in the block with the values 0 and \( b - 1 \). Then represent the decimal integer \( f \) as a
seven-digit base-\(b\) number to obtain the residual 7 values. According to \(\{g', h_{-}\}\) and \(m\) values, we can derive the original 9 pixel values in the block.

### 3 THE PROPOSED METHOD

In the following section, we describe how to develop a reversible data embedding technique applicable to the simplified Chuang and Lin’s lossless compression method. Our method embeds secret data in non-overlap blocks one by one. Our sequence is from right to left and from bottom to top. It is the backward sequence of Chuang and Lin’s method.

#### 3.1 One Bit Embedding Method

The image is segmented into \(3\times3\) blocks and each block thereof is encoded by the simplified Chuang and Lin’s method. For each block’s compressed code, we execute the following 1 data bit embedding steps.

**Step 1.** If the value \(c\) of the block’s compressed code to be treated is 1, there is no data embedding; if \(c\) is 0, then the residual codes \((b + m + f)\) or \(b + m + \text{P}(\text{min}, \text{max}) + f\) are processed by Step 2.

**Step 2.** If the data bit to be embedded is 0 (1), the designed \(X_0\) (\(X_1\)) is selected to XOR the residual code. The result of the XOR operation is the data embedded block’s final compression code.

**Step 3.** Verify whether the embedded data can be retrieved accurately in the process of retrieving. If it succeeds, we accomplish the data embedding process; if it fails, we cannot embed data this block and Case (3) \((c = 1)\) of Chuang and Lin’s technique is used to encode this block.

The preceding algorithm mentions that it is necessary to verify whether the correct retrieval of the embedded data in the process of retrieving them occurs. The main reason is that we fail to know whether the code is 1 or 0 embedded in the retrieving stage; therefore, we must XOR the data embedded compression code with \(X_0\) and \(X_1\) to obtain the 2 reversed codes and judge which one is the true embedded bit and the original compression codes. If the judgment conditions employed can exclude accurately the non-original compression codes and reverse the contents of the original block and obtain the embedded data, we embed data; otherwise, we do not embed data therein. The following is the conditions employed to exclude the inaccurate compression codes of the block:

1. The first judgment condition is that using the values of \(b, m, \text{P}(\text{min}, \text{max})\) and \(Z_0\) to decode all pixel values of the block must be within 0-255, so those rather than the preceding values are definitely not the original compression codes.

2. If the result fails to be obtained by the first condition, the coincidence of the contents of the adjacent known blocks and the pixel values of the tested block are used to judge which one is the original block. Except for few blocks which the edges pass through, the true original blocks share the high similarity with the adjacent blocks. Therefore, we select the tested block with the highest coincidence with the adjacent known blocks as our final result. We employ the side-matching idea to judge the coincidence of the tested and adjacent known blocks. See Figure 2. \(X\) is the block to be tested and \(X_{11}, X_{22}, X_{13}, X_{21}\), and \(X_{11}\) are the pixel values of \(X, U\) and \(L\) are respectively the upper and left known adjacent blocks of \(X, U_{11}, U_{22}, U_{33}\) and \(L_{13}, L_{23}, L_{33}\) are respectively the pixel values of \(U\) and \(L\). Eq. (3) is used to measure the coincidence of \(X\) and \(U&L\). The smaller value of \(\text{DIS}(X, U/L)\) indicates the higher coincidence of \(X\) and \(U&L\).

\[
\text{DIS}(X, U, L) = (X_{11} - (U_{11} + L_{11})/2)^2 + (X_{12} - U_{12})^2 + (X_{13} - U_{13})^2 + (X_{21} - L_{21})^2 + (X_{23} - L_{23})^2 + (X_{31} - L_{31})^2
\]

**3.2 One Bit Extraction Method**

As we retrieve the embedded data and obtain the original image by decoding, the block processing sequence is from left to right and up to down which is opposite to that of data embedding.

First, the first bit \(c\) of compression code of each block is checked. If \(c = 1\), it denotes that there is no data embedding and the following \(8\times9 = 72\) bits represent the original 9 pixel values; therefore, it is applicable to reverse the block directly. If \(c = 0\), it denotes that there is data embedding. Therefore, we
take the following 72 bits to XOR with \(X_0\) and \(X_1\) to obtain 2 compression codes to be tested. Afterwards, we obtain the accurate length of the test codes and judge which is the true original codes in accordance with the verification conditions prescribed in Section 3.1. Since we have confirmed that the accuracy of the retrieved original codes in the process of retrieving data as embedding data, we can obtain the original compression code and get the embedded data without any problem. As we verify the embedded data as 0 or 1, we can obtain the original 9 pixel values by decoding the original codes with the decoding method proposed by Chuang and Lin.

### 3.3 XOR Patterns Design

In the proposed technique, XOR patterns \(X_0\) and \(X_1\) are used to be the media of data embedding. Apparently, the design of XOR patterns impacts the information quantity embedded in the image. A good designed XOR pattern decreases the opportunity of data cannot be embedded in blocks and advanced the whole information embedding capacity accordingly.

Through the experiments, we obtain the regularity of the XOR patterns design. The designed XOR patterns are able to reduce the opportunity of misjudgment during the retrieval of embedded data, which leads to the reduced inapplicability of data embedding. The longest length of codes is 72 bits, so the length of XOR patterns is all 72 bits.

If there is 1 data bit embedded in a block, it demands only 2 XOR patterns \(X_0\) and \(X_1\). The design manner is the different 8th bit and all other bits are 0 in \(X_0\) and \(X_1\). See Figure 3. Such a design results from that the 8th bit of \(X_0\) or \(X_1\) indicates the first bit of \(m\) part of the compressed codes; accordingly, in the reversing process of original pixel values of the block, the difference between the pixel values of the true original block and the other block at the relative position is 128. At this rate, the pixel values of the other block may not be within 0-255. Even though aforesaid values are within 0-255, there is a huge difference between the aforesaid block and its adjacent block, leading to the judgment of non-original block. Consequently, most blocks are verified to be applicable to data embedding in the data embedding stage as to increase the embedding capacity.

If there are 2 data bits to be embedded in each block, it demands 4 XOR patterns as \(X_0\), \(X_1\), \(X_2\) and \(X_3\). We let the 8th and 9th bits differ of 30 \(X_i\), \(X_j\), \(X_k\), \(X_l\), \(X_m\), \(X_n\), \(X_o\), \(X_p\). We let the 8th and 9th bits differ of 30 \(X_i\), \(X_j\), \(X_k\), \(X_l\), \(X_m\), \(X_n\), \(X_o\), \(X_p\). We let the 8th and 9th bits differ of 30 \(X_i\), \(X_j\), \(X_k\), \(X_l\), \(X_m\), \(X_n\), \(X_o\), \(X_p\). If there are 3 data bits to be embedded in each block, it demands 8 XOR patterns as \(X_0\), ..., \(X_7\). At this time, in addition to the different 8th and 9th bits, we employ the alteration of the first bit because it is the first bit responding to part \(b\) of the compressed codes. For this reason, there is a difference of 64 of the base values in the process of retrieving data and reversing the original values of the block, leading to the values out of 0-255. Even though the values are within 0-255, there is a huge difference between the aforesaid block and its adjacent block, leading to the judgment of non-original block.

If there are 4 data bits to be embedded in each block, the XOR patterns are similar to those embedding 3 data bits. The alteration of the 1st, 2nd, 8th and 9th bits is used to construct \(X_{15}\). If there are 5 data bits to be embedded in each block, it demands the alteration of the 1st, 2nd, 8th, 9th and 16th bits to construct \(X_{31}\). If there are 6 data bits or more to be embedded in each block, it extends the case of 5 data bits embedding. That is, the alteration of the 1st, 2nd, 8th, 9th and 16th bits plus 17th and 18th bits to construct the required XOR patterns.

<table>
<thead>
<tr>
<th>(X_0)</th>
<th>(X_1)</th>
<th>(b) (7 bits)</th>
<th>(m) (8 bits)</th>
<th>(P) (57 bits)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10000000</td>
<td>00000000</td>
<td>00000000</td>
<td>0000…0000</td>
<td></td>
</tr>
</tbody>
</table>

**Figure 3:** XOR patterns design schematic.

### 3.4 Multi-bits Embedding and Extracting

In this Section, we describe how to extend the technique of embedding and extracting 1 data bit in a block prescribed in Subsections 3.1 and 3.2 to the multi-bits embedding and extracting.

If there are multi-bits to be embedded in a block, the modification of Step 2 of the embedding method mentioned in Subsection 3.1 is needed. The steps of embedding \(n\) data bits in a block are as follows.

**Step 1.** If the value \(c\) of the block’ compressed code to be treated is 1, there is no data embedding; if \(c\) is 0, then the residual codes \(b+m+f\) or \(b+m+P\) are processed by Step 2.

**Step 2.** If the decimal value of the \(n\)-digit to be embedded is \(i,0\leq i<2^n-1\), the designed \(X_i\) is selected to XOR the residual code.

The result of the XOR operation is the data embedded block’s final compression code.

**Step 3.** Verify whether the embedded data can be retrieved accurately in the process of extraction. If it succeeds, we accomplish the data embedding process; if it fails, we
Table 1: Various image sizes and embedding capacities.

<table>
<thead>
<tr>
<th>Attributes</th>
<th>Lena</th>
<th>Baboon</th>
<th>Pepper</th>
<th>Gold</th>
<th>Girl</th>
<th>F-16</th>
</tr>
</thead>
<tbody>
<tr>
<td>Original image sizes (bits)</td>
<td>2080800</td>
<td>2080800</td>
<td>2080800</td>
<td>2080800</td>
<td>2080800</td>
<td>2080800</td>
</tr>
<tr>
<td>Lossless compressed image sizes</td>
<td>1381455</td>
<td>1727667</td>
<td>1384059</td>
<td>1488330</td>
<td>1419340</td>
<td>1317704</td>
</tr>
<tr>
<td>Number of blocks</td>
<td>28900</td>
<td>28900</td>
<td>28900</td>
<td>28900</td>
<td>28900</td>
<td>28900</td>
</tr>
<tr>
<td>Number of Case 3 blocks</td>
<td>107</td>
<td>438</td>
<td>123</td>
<td>6</td>
<td>101</td>
<td>96</td>
</tr>
</tbody>
</table>

Embed 1 data bit / block

| Capacity (bits) | 28793 | 28449 | 28496 | 28894 | 28799 | 28804 |
| Number of increasing Case 3 blocks | 0 | 13 | 281 | 0 | 0 | 0 |

Embed 2 data bits / block

| Capacity (bits) | 57456 | 55158 | 56806 | 57694 | 57550 | 57294 |
| Number of increasing Case 3 blocks | 65 | 883 | 374 | 47 | 24 | 157 |

Embed 3 data bits / block

| Capacity (bits) | 85404 | 75813 | 84594 | 85872 | 85983 | 84975 |
| Number of increasing Case 3 blocks | 325 | 3191 | 579 | 270 | 138 | 479 |

Embed 4 data bits / block

| Capacity (bits) | 115172 | 87884 | 111204 | 111460 | 113000 | 111440 |
| Number of increasing Case 3 blocks | 942 | 6491 | 976 | 1029 | 549 | 1019 |

Embed 5 data bits / block

| Capacity (bits) | 137545 | 105995 | 143885 | 135535 | 139245 | 137525 |
| Number of increasing Case 3 blocks | 1284 | 7263 | 1382 | 1787 | 950 | 1299 |

Embed 6 data bits / block

| Capacity (bits) | 159228 | 108600 | 157530 | 148872 | 160698 | 159600 |
| Number of increasing Case 3 blocks | 2255 | 10362 | 2522 | 4082 | 2016 | 2204 |

Embed 7 data bits / block

| Capacity (bits) | 1443427 | 1885390 | 1467086 | 1620516 | 1487441 | 1386402 |
| Number of increasing Case 3 blocks | 3723 | 14167 | 4187 | 7354 | 3592 | 4660 |

cannot embed data in this block and Case (3) \( c = 1 \) of Chuang and Lin’s technique is used to encode this block.
The verification method of the accuracy of the data retrieval in the process of retrieving them is identical with that mentioned in 3.1, so there is no more repeated illustration.

4 EXPERIMENTAL RESULTS

As far as we know, this is the unprecedented paper that employs the reversible data embedding technique to the lossless compression. Hence, the experimental emphasis is the inquiry on the alteration of embedding quantity of the diverse images and the impact of the data embedding quantity on the compression ratio.

Six 512 × 512 sized grayscale images are used to conduct the experiments for verifying the effect of the proposed technique. The 6 images are Lena, Baboon, Pepper, Gold, Girl and F-16.

The compression ratio is used to assess the entire compression effect. See Eq. (4).

\[
CR = \frac{\text{File size after compression}}{\text{Original file size}} \times 100\% \quad (4)
\]

The experimental data of the embedding capacity are shown in Tables 1.

The experimental results in Table 1 indicate that there is a significant difference of the embedding capacity between Baboon and other images. The
main reason is Baboon is a complex image. Therefore, there are more blocks unable to be encoded by the lossless compression (blocks in Case 3). Thus, we can not embed data therein. Likewise, even the block can be compressed, there are more blocks where the data unable to be retrieved successfully so that we fail to embed data therein. As a result, the entire embedding quantity is relatively less.

As for the performance of the compression ratio, when there is only 1 data bit embedded in each block, except for the slight advancement of Baboon and Pepper, the compression ratio of other images are identical with that of the original compression ratios. That is, the codes remain the same after we embed data. As the embedding capacity increases, the codes expand slowly as well. However, the speed of the expansibility of the codes is much slower than that of the increased data embedding quantity. Except for the case that there are 7 data bits embedded in the blocks of Baboon. What is worthwhile mention is that the compression ratio of other images before and after data embedding differs within 1% except for that of Baboon when there are less than 5 data bits embedded in each block. Based on the result, it proves that the designed XOR patterns perform well on the advanced embedding capacity.

To sum up, we successfully propose a new technique adding the reversible data embedding to the lossless compression. The proposed technique performs well in the smooth images whereas it fails to function well on the complex images concerning the information embedding quantity and the expansibility of compression codes.

5 CONCLUSIONS

This paper employs the simplified Chuang and Lin’s method to develop a reversible data embedding technique applicable to the lossless compression technique. According to the experimental results, such a technique performs well on the information embedding quantity and expansibility of compression codes. As far as we know, this is the unprecedented paper that employs the reversible data embedding technique to the lossless compression. We will dedicate ourselves to the reduced compression ratio and the advanced embedded information quantity and the further research of other reversible data embedding techniques of lossless compression techniques.

ACKNOWLEDGEMENTS

This work was supported in part by National Science Council of Taiwan, R.O.C. under Grant no. NSC 97-2221-E-018-023.

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