DEFINING THE IMPLEMENTATION ORDER OF SOFTWARE PROJECTS IN UNCERTAIN ENVIRONMENTS

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Abstract: In the competitive world in which we live, where every business opportunity not taken is an opportunity handed to competitors, software developers have distanced themselves, in both language and values, from those who define the requirements that software has to satisfy and come up with the money that funds its development process. Such a distance helps to reduce or, in some cases, completely eliminate the competitive advantage that software development may provide to an organization; transforming this value creation activity into a business cost that is better kept low and under tight control. This article proposes a method for obtaining the optimal implementation order of software units in an information technology development project. This method, which uses a combination of heuristic procedures and Monte Carlo simulation, takes into consideration the fact that software development is generally carried out under cost and investment constraints in an uncertain environment, whose proper analysis indicate how to obtain the best possible return on investment. The article shows that decisions made under uncertainty may be substantially different from those made in a risk-free environment.

1 INTRODUCTION

In the last decades Information Technology (IT) has become an important component of business strategy. Therefore, it should come as no surprise that in the American service industry alone IT is responsible for more than half of capital investment. In this day and age, IT has become the informational infra-structure of many organizations, helping the generation of new services and products, the creation of innovative managerial structures, to access new markets and establish new forms of speeding up the delivery of services and goods (Scott, 2006).

However, in the course of time, the practice of software development has become increasingly disconnected from those who define the requirements that software have to satisfy and fund the software development process. While IT professionals are generally concerned with software development methodologies, its related supporting tools, classes of objects and use cases, business oriented personnel are preoccupied with product marketable features, project cash flows, competitive advantage and, ultimately, return on investment (Denne and Cleland-Huang, 2003). This should come as no surprise as business related subjects are seldom part of the regular computer science or computer engineering curriculum at both undergraduate and graduate level (Joint Task Force, 2005; Verhoef, 2005).

This disconnection, in both language and value, has two important consequences for software development. First, as IT professionals become more technical and less business oriented, software development tends to be perceived by high management as a business cost, that is better kept low and under tight control. Second, the acceptable payback time of IT projects is likely to become much shorter, making it very difficult to develop long term projects, even though they might be strategically relevant. All of this, obviously, affects the way IT is used in the strategic context, transforming, in many circumstances, a value creation activity such as software development in a mere outsourceable part of business (Denne and Cleland-Huang, 2003).
Although, it is generally accepted that software development should be managed interactively as a result of smaller functional ready-to-use parts, little attention has been given on how software development should be funded. While agile methods such as Scrum and Extreme Programming (XP), do favor the construction of such parts, the full value that the right combination of these parts brings to business are still not fully unleashed (Germain and Robillard, 2005).

This article proposes a method for identifying the optimum implementation order of software units in an IT project. Such an order helps to place software at the center of business strategic decisions, making it possible to develop complex information systems from a relatively small investment. The method, based upon a combination of heuristic procedures and Monte Carlo simulation, takes into account that software development takes place in an uncertain environment, being subjected to cost and risk constraints.

2 CONCEPTUAL FRAMEWORK

Typically, the buying process of any product by consumers has four main components: (1) there is a need that has to be satisfied, (2) there is at least one product that is perceived as satisfying that need, (3) there is money available to pay for the product, and (4) consumers are willing to pay what they have asked for (Kotler and Armstrong, 2007). While simple products have a reduced set of features for which people are willing to pay, software may have a large collection of such features (Little, 2004).

According to Denne and Cleland-Huang (Denne and Cleland-Huang, 2003; Denne and Cleland-Huang, 2004; Cleland-Huang and Denne, 2005) software minimum marketable features, or MMFs for short, are software units that have an intrinsic marketable value. These software units create market value to business in one or several of the following areas:

- **Competitive differentiation** - the software unit allows the creation of service or product features that are valued by customers and that are different from anything else being offered in the market;

- **Revenue generation** - although the software unit does not provide any unique valuable features to customers, it does provide extra revenue by offering the same quality as other products in the market for a better price;

- **Cost savings** - the MMF allows business to save money by making one or more business processes cheaper to run;

- **Brand projection** - by building the software unit the business projects itself as being technologically advanced; and

- **Enhanced customer loyalty** - the software unit influences customers to buy more, more frequently or both.

Moreover, the total value brought to a company by a software consisting of several interdependent MMFs, each one with its own cash flow stream and precedence restrictions is highly dependent on the order of implementation of the MMFs.

Although an MMF is a self-contained unit, it is often the case that an MMF can only be developed after other project parts have been completed. These project parts may be either other MMFs or the architectural infrastructure, i.e. the set of basic features that offers no direct value to customers, but that are required by the MMFs.

The architecture itself can usually be decomposed into self-contained deliverable elements. These elements, called architectural elements, or AEs for short, enables the architecture to be delivered according to demand, further reducing the initial investment needed to run a project. For instance, in a web-based software system, the graphic interface library that allows software units to share a common graphic identity is an architectural element, as it has no value to customers, but common sense indicate that no software unit should be developed before it is built.

Figure 1 presents the precedence graph of a set of MMFs from an example taken from Denne and Cleland-Huang (Denne and Cleland-Huang, 2003). Note that A, B, ..., D are software-building activities and that an arrow going from A to B, i.e. A → B, indicates that the work on MMF A has to be completed before the work on B can start.

![Figure 1: The precedence graph of a set of MMFs.](image)

Table 1 shows the net Cash-Flow Stream (CFS) in US dollars of each MMF in Figure 1. For instance consider MMF A. It requires an initial investment of $50 thousand to be built. Once it is completed it generates a net revenue of $45 thousand per time period for a total of eight periods. MMF E, on the other hand, requires a higher investment of $60 thousand and generates a net revenue of $30 thousand per time period.
DEFINING THE IMPLEMENTATION ORDER OF SOFTWARE PROJECTS IN UNCERTAIN ENVIRONMENTS

Because it is improper to perform mathematical operations on monetary values without taking into account an interest rate, in order to compare the business value of different MMFs one has to resort to their discounted cash-flow. Table 2 shows the sum of the discounted cash-flow of each MMF in Figure 1, considering a discount rate of 2.4% per time period. Such a sum is the net present value (NPV) of all cash flow elements of an MMF considering that its development starts at period $n \in [1 .. 7]$. For instance, according to the information presented in Table 2, if MMF A is developed in the first period, it yields a net present value (NPV) of $231$ thousand, i.e.

\[
NPV_{A,1} = \frac{-50}{(1 + 0.024)^1} + \frac{45}{(1 + 0.024)^2} + \cdots + \frac{45}{(1 + 0.024)^8} = $231 \text{ thousand}
\]

If A is developed in the second period, it yields a $NPV_{A,2}$ of $189$, in the third $149$ and so on.

Obviously, not all MMFs can be developed in the first period. The precedence graph presented in Figure 1 indicates that only MMF A and D can be developed at that time. Because in this example each MMF requires exactly a period to be developed, MMF C cannot be developed until the third period. Furthermore, each particular sequence of MMF yields its own return on investment. For instance, sequence DABCE yields an NPV of $799$ thousand, i.e.

\[
NPV(DABCE) = NPV_{D,1} + NPV_{A,2} + \cdots + NPV_{E,5}
\]

Table 1: CFS of a set of MMFs in thousands of US dollars.

<table>
<thead>
<tr>
<th>Period</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>-50</td>
<td>-40</td>
<td>-20</td>
<td>-30</td>
<td>-60</td>
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<td>45</td>
<td>60</td>
<td>35</td>
<td>50</td>
<td>30</td>
</tr>
</tbody>
</table>

Table 2: NPV of cash-flow streams starting at different periods.

<table>
<thead>
<tr>
<th>Period</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>231</td>
<td>334</td>
<td>198</td>
<td>262</td>
<td>128</td>
</tr>
<tr>
<td>2</td>
<td>189</td>
<td>278</td>
<td>165</td>
<td>216</td>
<td>101</td>
</tr>
<tr>
<td>3</td>
<td>149</td>
<td>225</td>
<td>133</td>
<td>170</td>
<td>74</td>
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<td>4</td>
<td>109</td>
<td>169</td>
<td>102</td>
<td>126</td>
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<td>5</td>
<td>70</td>
<td>117</td>
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<td>6</td>
<td>30</td>
<td>66</td>
<td>41</td>
<td>40</td>
<td>-2</td>
</tr>
<tr>
<td>7</td>
<td>-5</td>
<td>16</td>
<td>12</td>
<td>-1</td>
<td>-26</td>
</tr>
</tbody>
</table>
• Only one MMF can be in the implementation process at any given time period,
• The process of developing an MMF can only start after its precedent MMFs are completed,
• The first MMF must start at time zero and
• Apart from the last, there is no time delay between the end of one MMF and the start of the next one.

In our example, there are ten valid sequences: ABCDE, ABDE, ABDE, ABDE, ADDE, DEABC, DAEB, DABE, DABE and DABE.

Given an MMF precedence graph, one is interested in finding a valid sequence \( v_1 \cdots v_n \), for \( v_1 \leq \cdots \leq v_n \in V \), such that

\[
\text{NPV}_{v_1,1} + \sum_{i=2}^{n} \text{NPV}_{v_i, \sum_{j=1}^{i-1} D_{v_j}}
\]

is maximized.

The problem of finding the valid sequence that delivers the maximum NPV was shown to be in the category of NP-hard problems by Denne and Cleland-Huang (Denne and Cleland-Huang, 2003), which also showed several heuristics to find polynomial-time approximations to the optimal solution.

### 3 CASH-FLOW STREAM PATTERNS

The estimated benefits generated by a software project composed of several MMFs is most usually expressed as a fixed net present value. See Table 2. Unfortunately, in most projects in the real-world one does not know for certain the value of each cash-flow element. Those have to be estimated by experts, who use past project information, their own opinion or a combination of both to express the uncertainty related to cash-flow elements in the form of Probability Density Functions (PDFs) (Vose, 2000). See (Hubbard, 2007) for a discussion on how these estimates may be obtained in real-world projects. See (Vose, 2000) for an introduction to the concept of uncertainty in project management.

Most frequently these estimates are presented in the form of ordered tuples of three points defining triangular PDFs, i.e. the minimum value it is believed that the real value may take (Min), its most likely value (ML) and the maximum value (Max) (Kotz and van Dorp, 2004). Table 3 presents three point estimates for the set of MMFs in Figure 1.

Note that in these circumstances \( CFS_{ij} \) is a random variable, and so it is \( \text{NPV}_{ij} \), the net present value of the sum of the discounted cash flow elements of MMF \( M_i \) starting at time \( t \), and also the total benefit generated by a sequence of related MMFs.

Finding the sum of random variables representing the set of discounted cash-flow elements can be a very difficult task. If these elements are statistically independent, then their sum can be approximated by Laplace’s Central Limit Theorem (CLT), which states that a sum of \( n \) independent random variables will approach a normal probability density function, as the value of \( n \) increases (Thomas and Duffy, 2004).

A more complex case occurs when the cash-flow elements are related to one another, i.e. when they are statistically correlated. This correlation can appear both among elements of the same CFS as among elements of different CFSs. In this case, since one cannot use the CLT approximation to determine the sum of cash-flow elements, this problem becomes too complex to be resolved by analytical means. Nevertheless, good computational approximations can be obtained using sampling procedures like the Monte Carlo method (Robert and Casella, 2005).

Figure 2, for instance, shows the Cumulative Density Function (CDF) of the NPV of all valid sequences of the MMFs presented in Figure 1. The graphic presented in the picture was built from a sample of 5,000 observations generated by a Monte Carlo simulation model. According to the information shown in the graphic, under the criteria of probabilistic dominance, the sequence ABDE provides the best investment alternative since its PDF dominates all the other sequences, i.e. for any given probability it will always yield a better net present value.

![Figure 2: CDF of valid sequences.](image-url)
Due to the exponential nature of the problem, the method of sampling all valid sequences is unfeasible. For a set of \( n \) MMFs one may have to examine \( n! \) sequences. Therefore, an approximative heuristic may have to be used. Denne and Cleland-Huang (Denne and Cleland-Huang, 2003) suggest the use of an heuristic algorithm which they have named “Incremental Funding Method” (IFM). Also, because it is not always the case that one comes across a dominating sequence when solving the problem of finding the sequence of MMFs that yields the best return on investment, one needs a procedure for decision making under uncertainty.

Both the heuristic algorithm and the generation of data for the process of decision making under uncertainty are addressed by the method described in the next section.

4 THE METHOD

The method for obtaining an approximate solution to the optimal order of execution of a software project consists of the following steps:

1. Partition the product to be developed into a set of \( n \) MMFs.
2. Define the precedence relations among the MMFs.
3. Estimate the PDF of each cash-flow element associated with each MMF.
4. Calculate the number of scenarios (NS) that must be generated in order to obtain an estimate of the probability of a given sequence being chosen by the heuristic procedure, such that the error of its the estimated CDF is kept below a certain value under a required confidence level (Knuth, 1998).
5. Repeat the procedure below NS times:
   (a) obtain one scenario consisting of sampled values for each cash flow element of each MMF.
   (b) apply an heuristic procedure for finding and recording the sequence which maximizes the NPV of the scenario.
6. Let SVS be the set of sequences generated in step 5. Obtain the PDF and CDF of the NPV of each selected sequence by running a second set of NS scenarios for each element of SVS. It is important to notice that, in some cases, it may be necessary to select a subset of SVS in order to reduce the number of candidate sequences.
7. Apply a decision criteria for selecting the preferred sequence given a set the NPV of the selected sequences. Two basic approaches can be utilized: the direct choice and certainty equivalent(Holloway, 1979). The direct choice utilizes the CDF and the PDF of the NPV of each sequence in order to understand the uncertainty and evaluate the risk. Outcome and probabilistic dominance can used in this case. The certainty equivalent approach establish an equivalence between uncertain events and a certain value. This process simplifies decision making by the removal of uncertainty.

5 AN EXAMPLE

According to Benjamin Franklin (1706 - 1790), one of the Founding Fathers of the United States: “A good example is the best sermon”. As a result, this section starts with an example of the algorithm presented in Section 4.

5.1 Partition the Product

Consider a software \( S \) that can be divided into six MMFs. Also, allow for the existence of three software units that are essential for the implementation of one or more of those MMFs, but that returns no revenue.

5.2 Define the Precedence Relation

Figure 3, borrowed from (Denne and Cleland-Huang, 2003), shows the precedence graph of the MMFs and AEs . In that figure \( A, B, \ldots, F \) are MMFs and 1, 2 and 3 are AEs.

![Figure 3: The precedence graph of the MMFs and AEs of software S.](image)

5.3 Define the PDF of Cash Flow Elements

Table 4 presents the average present value of discounted cash flow of the MMFs of software \( S \), considering a discount rate of 2.4% per time period. In this example, each cash-flow element bears an uncertainty of 25%. Therefore, if MMF \( A \) is implemented
in the first period it requires an initial investment between

\[-250 \text{ thousand} \ (-200 - 50) \]

and

\[-150 \text{ thousand} \ (-200 + 50) \].

Table 4: The mean value of the cash flow elements.

<table>
<thead>
<tr>
<th>Period</th>
<th>MMF</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
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<tbody>
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<td>-138</td>
</tr>
</tbody>
</table>

The same procedure can be applied to define the discounted cash-flow of the AEs, using the same discount rate of 2.4% per period.

5.4 Sample Cash Flow Streams

With the support of a Monte Carlo simulation tool a sample of the discounted cash flow containing 5,000 observations is generated, using the look-ahead heuristic proposed by Denne and Cleland-Huang (Denne and Cleland-Huang, 2003).

It is important to note that because software S yields a total of nine software units, potentially there is a total of \(362,880 = 9!\) MMF sequences whose NPV has to be calculated. The heuristic reduces the number of sequences to four. The results are presented in Table 5.

Table 5: Results of the Monte Carlo Simulation with a 25% uncertainty.

<table>
<thead>
<tr>
<th>Sequences</th>
<th>Freq.</th>
<th>Min</th>
<th>Max</th>
<th>Mean</th>
<th>Std. Dev.</th>
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<tr>
<td>1ABC3F2DE</td>
<td>4,800</td>
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<td>3,009</td>
<td>2,649</td>
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<tr>
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<td>2,505</td>
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<td>82</td>
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<td>2DE1ABC3F</td>
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<td>2,983</td>
<td>2,983</td>
<td>2,652</td>
<td>93</td>
</tr>
</tbody>
</table>

5.5 Obtain the CDF of the Selected Sequences

Because the number of sequences is rather small (4 sequences), all are selected. A new 5,000 sample is collected to reach the required error margin, within a confidence interval, for the CDF of the NPV for the implementation sequence. Figure 4 shows these results.

![CDF of selected sequences](image)

5.6 Apply Decision Criteria

It should be noted that sequence 1ABC3F2DE, which presents the best results under the mean value (see (Denne and Cleland-Huang, 2003)), and 2DE3F1ABC are outperformed by sequences 1AEC3F2DE and 2DE1ABC3F, which yield equivalent value to business and are the optimal choices under the uncertainties facing the project. A Wald-Wolfowitz run test, with a 95% confidence interval, does support these claims (Hill and Lewicki, 2005).

6 CONCLUSIONS

This article presents a method for maximizing the financial return on investment in software projects. The method considers that investment is maximized if the software is divided into smaller software units, where some of them have marketable value and others do not. However, as the latter is essential for the development of the former, the investment necessary to develop such units influences the return on investment yielded by the software and must be taken into account.

The method, which is based upon Monte Carlo simulation, extends the ideas presented by (Denne and Cleland-Huang, 2003; Denne and Cleland-Huang, 2004; Cleland-Huang and Denne, 2005), allowing for uncertain cash-flow streams, which are
so common in software projects and can actually be found in many other kinds of projects.

The case study presented in the article shows that results obtained taking uncertainty into account can be very different from the ones assuming a known cash-flow stream. Therefore, the investment made on software must take uncertainty into account, specially in the turbulent and globalized world where software development takes place these days.

REFERENCES


