A FULLY GPU-IMPLEMENTED RIGID BODY SIMULATOR

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Abstract: In this paper we study how to implement a fully GPU-based rigid body simulator by programming shaders for every phase of the simulation. We analyze the pros and cons of different approaches, and point out the bottlenecks we have detected. We also apply the developed techniques to two case studies, comparing them with the analogous versions running on CPU.

1 INTRODUCTION

The study of animation techniques has played a decisive role in the evolution of computer graphics. Traditionally in this topic, the issue of the physically based motion of rigid bodies has been one of the most attractive areas, mainly due to the high level of realism achieved when rendering the involved scenes. Since precision usually competes against the run-time cost, most rigid body simulators have specialized in configurations that get a trade-off between accuracy and efficiency. However, it is common to most of them to implement two phases to solve two tasks: collision detection and collision response. The first one looks for contacts between pairs of objects, and it is usually split in other two phases: the broad phase and the narrow phase. The broad phase applies bounding volumes to objects in order to check whether bounding volumes collide or not (Teschner et al., 2005). If a pair collides, the narrow phase determines if the included objects are in collision. Only after determining that there will be a real collision, the collision points are calculated. The reason to decompose collision detection in these two phases is that broad phase algorithms have a much lower cost than those involved in the narrow phase. Apart from these software solutions, there are also other collision detection approaches which use specific hardware (Raabe et al., 2006).

Different techniques have been proposed to deal with the collision response. Although some implementations allow interpenetration of objects, such as the penalty method (McKenna and Zeltzer, 1990), most of them try to avoid it by accurately computing the instant the impact comes up. This can be achieved with the classic bisection method (Baraff, 1997): the interval in which the collision takes place is gradually reduced by comings and goings in time. Once the collision instant is computed, the response can be obtained by applying the forces which solve certain constraints –Baraff’s constraint method (Baraff, 1989)– or by instantaneously modifying the velocity of the objects after computing the related impulse (Mirtich, 1996).

The efficiency of a rigid body simulator does not only depend on the components integrating the system, but also on the way they are integrated into the simulation loop, especially when a large number of objects are involved. Note that the collision time of a pair of objects can affect to –even avoid– many other collisions that come up later in the same loop iteration. For this reason, the computation of the instant for these other collisions is a useless task that could collapse the simulation as a whole. In order to prevent this eventuality, in a uniprocessor context, (Mirtich, 2000) proposed the timewarp algorithm which uses heaps as data structures.

On other hand, the evolution of GPUs, as regards performance and programmability, has brought about their intensive use in many applications. Today they are a key element in the design stage of any simulator. This is the case for the interactive visualization of particle systems (Krüger et al., 2005), where GPUs have been used to parallely manage the independent movement of each particle.

In the context of rigid body simulations, shaders have been used to relieve CPU of specific tasks, but never to solve the whole algorithm. For instance (Yuksel, 2007) introduces fragment shaders in the rendering phase to quickly support special effects,
while all the computations involved in the simulation part are implemented on the CPU. Concerning the simulation methodology, moving the detection of collisions to GPU has been the most studied topic. Collision detection algorithms on GPUs can be classified into two categories. On one hand, screen-space approaches use the depth or stencil buffers to perform the collision tests by rendering the geometry primitives (Govindaraju et al., 2005) (Teschner et al., 2005). Their main problems are that effectiveness is often limited by the image space resolution, and that only potentially colliding pairs are reported, so another test must be applied on the CPU later.

On the other hand, object-space approaches use the floating point bandwidth and programmability of modern GPUs to implement the collision test. (Zhang and Kim, 2007) performs massively-parallel pairwise, overlapping tests onto AABB streams, although exact primitive-level intersection tests are performed on CPU. (Greß and Zachmann, 2004) (Horn, 2005) (Greß et al., 2006) generate bounding volume hierarchies on the GPU from a geometry imaged (Gu et al., 2002) representation of the solids. In order to expose the parallel processing capabilities of the GPU, they breadth-first traverse these hierarchies by using the non-uniform stream reduction presented in (Horn, 2005). Nevertheless, these approaches cannot autonomously operate on the GPU, since the selection of the objects of the pair to be tested is usually chosen on the CPU. Furthermore, they do not apply any response when the objects actually collide, so they should require extra CPU collaboration to address interactions.

In the context of deformable objects, recent papers have used the GPU capabilities to quickly update their geometry: (Pascale et al., 2005) proposes the use of vertex shaders to locally deform the object, (Zhang and Kim, 2007) employs a fragment shader to update the AABB streams, and (Kim et al., 2006) uses a fragment shader to compute the mass properties of rigid bodies in a buoyancy simulation. Nevertheless, none of these papers cover interactions between objects.

In this paper we study how to implement a fully GPU-based rigid body simulator, by programming shaders for every phase of the simulation. We analyze the pros and cons of different approaches, and point out the bottlenecks we have detected. We also apply the developed techniques to two case studies, comparing them with the analogous versions running on CPU.

2 THE SIMULATION LOOP

The animation in a rigid body simulation is achieved through a main loop, which updates the information related to every object, after a cycle or step has been completed. The size of the step must be accurately chosen because of stability reasons. So the realism level of the simulation directly depends on it.

In order to complete a step, the dynamics of every object (position of its center of mass \(x(t)\), orientation \(r(t)\), linear velocity \(v(t)\), and angular velocity \(w(t)\)) must be updated by using numerical methods to solve ordinary differential equations. Figure 1 shows both the configuration \(Y(t)\) of the state of an object and its time derivative in a 2D scenario. In this case, the vector \(r(t)\) and \(w(t)\) can be simplified to single scalars. Velocities change according to the action of forces, since there exist simple relations between their time derivatives and the applied forces. The torque generated by a force \(F(t)\) is defined as \(\tau(t) = (p-x(t)) \times F(t)\), where \(p\) is the location at which \(F(t)\) acts. Again the vector \(\tau(t)\) can be simplified to a single scalar in a 2D scenario. The mass \(M\) and the moment of inertia \(I\) are two scalars expressing the resistance of a body to a linear or an angular motion, respectively.

The collision computation is the main task involved in each step, since collisions make forces generate motion. It is made up the three sequential stages that will be presented in the following subsections. Roughly speaking, rigid body simulation can be considered as a large catalogue of subroutines, some of those are carefully chosen to fill each of these stages to build systems that efficiently solve the specific scenes they drive. Here we show how some of these subroutines can be implemented on GPU, analyzing pros and cons with respect to other approaches. Since the subroutines can be independently incorporated into the whole simulator, they are interchangeable parts; therefore systems alternating CPU- and GPU-computations are available. Nevertheless such hybrid simulators would require additional tasks to change the processor (e.g. transmitting data between CPU and GPU, binding textures to shaders, and assigning values to uniform variables) that could slow down the simulation. Thus we will only consider fully GPU-implementations in the sequel.
The programming of GPUs includes stream processing which is based on the definition of kernels and streams. Kernels process data in parallel, while streams organize the information in the memory card. In our GPU-implementations we use the following three textures of size $2^n \times 1$—where $2^n$ is the chosen number of objects; we use power-of-two sizes since they are required for the algorithm of Section 2.2—to store the state of any object:

- **Linear:** a RGBA-texture to store $x(t)$ and $v(t)$
- **Rotational:** a RGBA-texture to store $r(t)$ and $\omega(t)$
- **Geometry:** a RGBA-texture to store the geometry of any object as follows: component $R$ holds the index of the first vertex of the object, component $G$ is the number of its vertices, component $B$ keeps its mass, and component $A$ stores its moment of inertia.

The dynamics of an object is updated after every simulation step, so the two first textures act as input and output at the same time, thus we use the ping-pong technique described in (Gödekke, 2005). Note that although only two components of the Rotational texture are required, the format RGBA has been chosen to allow the renderization to it. The Geometry texture can be seen as globally-shared read-only memory that always acts as input. It is used to determine the current coordinates of the vertices of the objects, which will be used in the following stages. We use the first two components of its texels to access the real coordinates of the vertices, which will be in a fourth texture called **Vertices**. This one can also be seen as globally-shared read-only memory to keep the –locally expressed– coordinates. In a 2D scenario, the format RGBA stores the coordinates of two vertices in each texel, so the size can be reduced to $\sum \lfloor \text{vertex}_i/2 \rfloor / 0 \leq i \leq 2^n-1$. The following is a fragment of the GLSL-code to access the vertices of an object. This is graphically shown in Figure 2.

```glsl
vec2 v1=textureRect(Vertices,vec2(index,0.5)).xy;
vec2 v2=textureRect(Vertices,vec2(index,0.5)).zw;
```

In order to focus on the GPU-implementation issues, we have chosen a 2D rather than a 3D scenario. Extending the algorithms we propose to the 3D case is a technical exercise, not covered by this paper. In this case, most of the data we manage would become larger, so additional textures would be required. For example, $x(t)$ and $v(t)$ should be stored in separated textures, since they are 3D vectors. Angular data as $\omega(t)$ and $\tau(t)$ also become 3D vectors, while $r(t)$ and $I$ should be implemented through quaternions and $3\times3$ matrices, respectively.

### 2.1 Detecting Collisions

In the collision detection stage, the simulator looks for contacts between pairs of objects. The realism of the simulation strongly relies on the accuracy in the detection and computation of these collisions. In order to minimize the computational effort to detect collisions, each object is wrapped with an axis aligned bounding box (AABB). The premise that motivates its use is the fact that intersections among AABBs are much easier to detect than the collisions between the actual objects.

In the simulation loop, prior to compute AABBs intersections, each volume must be updated depending on the current position of the contained object. There are two ways to envelop the object within a new AABB: either by using the vertices of the updated object or by using the vertices of the updated AABB. We have chosen the first method, which has an updating cost obviously greater than the second one, but more no-collision situations are discarded since the volume is tighter to its object.

In order to update bounding volumes, we require one pass of the kernel `UpdateAABB` which renders
to a RGBA-texture of size 2nx1 to encode the updated AABB related to any object. More precisely, RG and BA are used for its left-bottom and right-top corner, respectively. Each fragment processing includes reading both the current position and rotation of the object as well as mapping these transformations to all of its vertices to build the AABB. Thus, its inputs are the Linear, Rotational, Geometry and Vertices textures. The cost of fragment processing depends on the number of vertices of the related object; hence the whole pass is a linear operation w.r.t. the total number of vertices.

Once the AABBs have been updated, we check for overlapping by using one pass of the kernel \texttt{OverlapAABB}. Its input is the output of the previous kernel. It renders to a Luminance texture of size 2nX2n, where the texel \((i,j)\) indicates whether the AABBs of objects \(i\) and \(j\) get to be overlapped. Now, the cost of a fragment processing is constant, since only one comparison of the involved corners is required. Moreover the symmetry of the texture can be used to restrict the computation to the lower triangular (LT) region below its main diagonal.

The next phase consists in determining if the objects contained in the overlapping AABBs actually collide. We detect such collisions, and the related collision times, on GPU. In the case of convex polygons, specific algorithms have been designed to check whether two objects collide. We think the classic approach based on separating planes is not convenient for a GPU implementation, since they seem rather difficult to be reused in the simulation. Instead we use a simple algorithm which behaves well in almost every situation; we do not consider the remaining ones to be a problem since the paper does not focus on the simulation realism, but on comparing GPU- to CPU-implementations. We actually test if every vertex of a given polygon is inside the other one. This naive algorithm could be improved by using the O’Rourke’s approach (O’Rourke, 1993).

For every pair of objects that will collide after a complete step, we use the method of bisection to calculate the exact collision time by testing whether the objects collide each other in the middle of the current interval of time. Since the first iteration of this loop requires the texture produced by \texttt{OverlapAABB}, the bisection method has been divided into two kernels: \texttt{Bisection1} and \texttt{Bisection2}. Nevertheless, the two kernels are essentially the same. They share the Linear, Rotational, Geometry and Vertices textures as inputs, and they render to a RGBA-texture \texttt{HitTimes} of size 2nX2n, where each texel stores four data corresponding to the involved pair of objects: the bounds of the interval enclosing the collision, a flag to continue (0) or to reject (1) the search of collision, and the hit time. In order to integrate the loop related to \texttt{Bisection2} we have implemented two while-sentences. The first one occurs inside the shader and it is used to calculate the hit time. In order to prevent from the execution of too many iterations, we use an extra parameter -a uniform variable \texttt{iter}- to control the number of iterations, since the number of instructions available on the card is limited. The second one is outside the shader and it is used to execute the kernel several times. Due to this multi-pass approach, we successively use outputs as next inputs. Programming this way allows us to compare different combinations. The following is a fragment of the GLSL-pseudo-code of the \texttt{Bisection} kernels. The uniform variable \texttt{epsilon} is the accuracy when determining the hit time.

```glsl
uniform samplerRect Linear, Rotational, Geometry, Vertices, HitTimes;
uniform float epsilon;
uniform int iter;
vec4 Bisection(float coordObject1, float coordObject2, float maxTime, float minTime){
//\([\text{minTime, maxTime}]\) is the current interval
float maxT=maxTime; float minT=minTime;
vec4 result;
int i=0;
while((maxT-minT>epsilon) && (i<iter)){
float midT=(maxT+minT)/2.0;
if (collision in midT) maxT=midT;
else minT=midT;
i++;
}
if (maxT-minT<=epsilon)
result=vec4(minT,maxT,1,minT);//bisection ends
else result=vec4(minT,maxT,0,minT);//\([\text{minT, maxT}]\)
//is the interval for the next bisection pass
return result;
}
```

Table 1 shows timing data for two cases. In the column \texttt{Inside} (\texttt{iter=ceil(-log2(epsilon))}), every iteration takes place inside the shader, while in the column \texttt{Outside} (\texttt{iter=1}) only one takes place inside the kernel. As we see, executing the loop inside the shader is much better than a pure multi-pass approach. Along this paper, we have tested the GPU implementations on a NVIDIA GeForce 7900 GS card. All timing data will be always expressed in seconds along the paper.
2.2 Searching the First Collision

There are different ways to process the contacts computed in the previous phase. On one hand, we can arrange the contacts with respect to the collision time. The problem is that solving one collision may affect many other collisions produced later within the same step. To be precise, some of them could not be produced or even new collisions could arise. On the other hand, there is a simpler approach consisting in truncating the step at the just moment of the first contact, and discarding the rest. We have chosen this latter approach; so we have used the classic reduction kernel (Buck and Purcell, 2004) to compute the minimum of the collision times. Nevertheless, we have proposed and analyzed different methods to improve the classic reduction kernel by exploiting the symmetry of the input textures. For all of them, the input is a texture of size $2^n \times 2^n$, with the alpha component containing the hit time $t \in [0,1]$ for every pair of objects, or a constant greater than 1 to indicate that the related objects do not collide. Due to symmetry, the kernel only requires to process the LT region of the texture.

In the classic method, the fragment processing computes the minimum of a $2 \times 2$ square. Since the texture is symmetric, our approach only requires processing the LT region. If we applied the classic $2 \times 2$ reduction to the LT region, some texels would not be considered (Figure 3a). In order to include them, we must visit six texels when processing fragment $(i,j)$, those with coordinates $(2i,2j)$, $(2i+1,2j)$, $(2i,2j+1)$, $(2i+1,2j+1)$, $(2i-1,2j)$ and $(2i+1,2j+2)$. This solution, which we call 6-reduction, improves the classic algorithm, but it generates too many redundant readings (Figure 3b). In order to avoid them, we exploit the fact that only the adjacent components to the diagonal need to check the six elements, while the others only require the four elements of the classic method. Therefore this $(4+6)$-reduction is a combination of two shaders: one to check the six elements that correspond to fragments adjacent to the diagonal, and the other one to check the four elements that correspond to the remaining fragments of the LT region (Figure 3c).

The complexity of a pass reducing a texture of size $2m \times 2m$ to a texture of size $m \times m$ is $4m^2$ for the classic algorithm, $3(m^2-m)$ for the 6-reduction and $2(m^2-1)$ for the $(4+6)$-reduction, with respect to the number of required readings. Since the complete reduction process is based on a multi-pass approach, the quadratic coefficient involved in a single pass becomes critical. Table 2 compares the three options, running 1000 complete minimizations. As it was expected, results report that the $(4+6)$-reduction significantly reduces time as the texture size increases.

### Table 2: Comparing the three reduction methods for 1000 complete minimizations.

<table>
<thead>
<tr>
<th>$\text{Texture Size}$</th>
<th>Classic</th>
<th>6-reduction</th>
<th>$(4+6)$-reduction</th>
</tr>
</thead>
<tbody>
<tr>
<td>$2^2$</td>
<td>1.422</td>
<td>1.625</td>
<td>1.532</td>
</tr>
<tr>
<td>$2^3$</td>
<td>1.750</td>
<td>1.906</td>
<td>1.438</td>
</tr>
<tr>
<td>$2^4$</td>
<td>2.031</td>
<td>2.047</td>
<td>1.656</td>
</tr>
<tr>
<td>$2^5$</td>
<td>3.187</td>
<td>2.437</td>
<td>1.831</td>
</tr>
<tr>
<td>$2^6$</td>
<td>14.265</td>
<td>10.939</td>
<td>6.484</td>
</tr>
</tbody>
</table>

2.3 Solving the First Collision

After computing the minimum hit time, we must apply the related response on the GPU. Firstly, we...
check whether the contacts at the same time are real collisions. The relative velocity \( V_{rel} \) of the pair of objects A and B is useful to solve this question:

\[
V_{rel} = \left( \frac{dp_A}{dt}(t_{hit}) - \frac{dp_B}{dt}(t_{hit}) \right) \cdot n(t_{hit})
\]  

(1)

where \( \frac{dp}{dt} \) denotes the velocity of the contact point within the corresponding object, and \( n \) is the contact normal. If \( V_{rel}<0 \) (see Figure 4), the objects are colliding and an impulse must be computed to avoid that they get overlapped. The impulse \( J \) is an instantaneous force, thus it produces a variation of the velocities according to the following equations:

\[
\Delta v = \frac{J}{M} \\
\Delta \omega = \frac{\text{Torque}}{I}
\]

The impulse \( J \) is a vector whose direction is the contact normal \( n \) and whose magnitude \( j \) must be computed by using the following equation (2):

\[
j = \frac{-1 + \varepsilon}{M_A + M_B + n(t_{hit}) \left( \frac{r_A \times n(t_{hit})}{I_A} \right) \times r_A + n(t_{hit}) \left( \frac{r_B \times n(t_{hit})}{I_B} \right) \times r_B}
\]

where \( \varepsilon \) is the restitution coefficient between the two objects, \( V_{rel}^{-} \) is the relative velocity before the impulse, and \( r_A, r_B \) are the vectors from the center of mass of each object to the contact point \( p \). The action of \( J \) is positive \((+jn(t))\) on the object A and negative \((-jn(t))\) on B.

The computation of the impulse is carried out by the kernel \text{Impulse}. Its inputs are the Linear, Rotational, Geometry, Vertices and HitTimes textures, and the minimum hit time. It renders to a RGBA-texture of size \( 2n \times 2n \), where the texel \((i,j)\) stores the accumulation of the impulses between the objects \( i \) and \( j \), since several collisions points can simultaneously arise. The impulse is computed whenever the collision time equals the minimum hit time. If this is the case, the accumulation of impulses is performed as the following pseudo-code shows.

```c
while (i<numVerticesA)
    while (j<numEdgesB) {  
        if (i-th vertex of A is on the j-th edge of B) {  
            1.- Compute \( V_{rel} \) of A and B in the i-th vertex of A  
            2.- If (\( V_{rel}<0 \)) {  
                2.1.- Compute the impulse  
                2.2.- Accumulate the impulse  
            }  
        }  
    }  

//Repeat with vertices of B and edges of A

Finally we execute one pass of any of the following kernels to update the scene after a step of the simulation: NoCollisionForward and CollisionForward. Their inputs and outputs are the Linear and Rotational textures. The kernel NoCollisionForward is used when the instant of the first collision is greater than a step of time. In this case, no collision is produced, the impulse is not computed, and the kernel updates the objects until the end of the step of time. Thus, processing a fragment requires constant time. The kernel CollisionForward is used otherwise and includes the output texture of the kernel Impulse as input. This kernel accumulates the impulses between an object and the remaining objects, and applies the total impulse. Hence processing a fragment requires linear time.

3 THE RENDERING PHASE

The image of the objects after a step is obtained by a vertex shader, which applies the transformations needed to suitably translate and rotate the object in the scene. This entails two jobs.

First of all, the translation and the rotation of the processed object must be loaded. Since the Linear and Rotational textures are located in memory card, they must be read back from GPU to CPU after any step. This option is called \text{toCPU} in Table 3. On the other hand, we can access these data within the shader itself by using a uniform variable to hold the texture coordinates that must be read. We use such a variable as an index, which must be properly assigned before rendering the object. This option is called \text{Index} in Table 3. The total cost of the latter approach includes two texture accesses per vertex, plus an extra uniform assignment per object.
Second, the shader needs the local coordinates of every vertex. Now we must decide how to send vertices to the pipeline. We propose these options:

1. Sending fictitious coordinates that will be replaced with the coordinates stored in the Vertices texture. In order to access the Geometry and Vertices textures, the shader needs the index of the object and the ordinal of the vertex within the object. To this aim, the simplest way is to use the fictitious coordinates to communicate these data to the shader. More precisely, the $x$-coordinate indicates the object and the $y$-coordinate refers to the vertex offset when accessing the Vertices texture. Hence any fragment processing requires two texture accesses: one to read the object data in the Geometry texture, and another to get the local coordinates of the vertex in the Vertices texture.

2. Sending fictitious coordinates and using one of them to indicate the ordinal of the vertex within the object, as in the previous option, and the other one to refer to the location of the first vertex of the object within the Vertices texture. Thus, we save one access per vertex.

3. Directly sending the local coordinates of each vertex to save the two accesses. The disadvantage of this option is that a copy of the Vertices texture must be located in CPU memory.

Table 3 compares the six combinations related to the solutions of the two jobs, that is, the two options to read the transformations and the three options to send the coordinates to the pipeline. The time measures correspond to 1000 renderings of a random scene configuration. In the last row we show how many texture accesses ($a$) are required per vertex, how many uniforms ($u$) must be assigned per object, and how many textures ($t$) have to be read from GPU to CPU. Note that texture accesses from vertex shaders are only available from shader model 3.0.

### 4.1 Circles

Circles are the simplest shapes in rigid body simulation, mainly because rotations can be skipped. It is also possible to compute the hit time of two circles algebraically, thus the bisection loop can be changed into a constant time code. It is enough to solve the equation

$$\text{distance}(A+ta,B+tb)=r_A+r_B,$$

where $r_A$, $r_B$ are the radius, $A$, $B$ are the centres, and $a$, $b$ are the linear velocities of the two circles. It leads to a second order equation which must be solved to find the, at the most, two values of $t$. Nevertheless the difference between both approaches is irrelevant since the few but expensive computations of the algebraic approach can be compared to the low-cost but many iterations of the bisection loop. Table 4 compares both approaches. The walls are also easy to implement since perfect reflections are applied.

### 4.2 Convex Polygons

For the sake of convenience, we only generate scenes with regular polygons. In fact we only use triangles in Table 4. The bisection kernels are required to compute hit times. Walls are implemented as rectangular objects with infinite mass, so they are static objects. Table 4 shows that the GPU implementation significantly reduces time as the number of objects increases.
Table 4: Comparing the three circles implementations (GPU-algebraic, GPU-bisect, CPU-bisect) and the two polygons ones (GPU-bisect, CPU-bisect).

<table>
<thead>
<tr>
<th>2^n</th>
<th>Circles</th>
<th>Polygons</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>GPU-alg</td>
<td>GPU-bis</td>
</tr>
<tr>
<td>2^4</td>
<td>33.62</td>
<td>33.56</td>
</tr>
<tr>
<td>2^5</td>
<td>50.16</td>
<td>50.16</td>
</tr>
<tr>
<td>2^10</td>
<td>83.49</td>
<td>83.47</td>
</tr>
<tr>
<td>2^11</td>
<td>166.79</td>
<td>166.89</td>
</tr>
</tbody>
</table>

Table 5 shows the timing data of the main kernels of the simulation algorithm after running 1000 steps on the same initial random configuration. Hence we cannot use it to deduce which kernel is the most demanding one, since their execution depends on the initial configuration. For instance, the bisected kernel will not run whenever the overlapAABB kernel computed no pair of overlapping AABBs, and the Impulse and the collisionForward kernels do not run whenever no collision arises.

<table>
<thead>
<tr>
<th>2^n</th>
<th>Update</th>
<th>Overlap</th>
<th>Bisection</th>
<th>Impulse</th>
<th>Forward</th>
</tr>
</thead>
<tbody>
<tr>
<td>2^4</td>
<td>0.1599</td>
<td>0.2500</td>
<td>0.6100</td>
<td>0.3200</td>
<td>0.0390</td>
</tr>
<tr>
<td>2^5</td>
<td>0.1700</td>
<td>0.6869</td>
<td>0.7200</td>
<td>0.3200</td>
<td>0.0799</td>
</tr>
<tr>
<td>2^10</td>
<td>0.1899</td>
<td>2.4700</td>
<td>0.7600</td>
<td>0.3600</td>
<td>0.2100</td>
</tr>
<tr>
<td>2^11</td>
<td>0.2300</td>
<td>9.4600</td>
<td>1.1400</td>
<td>0.5200</td>
<td>0.2300</td>
</tr>
</tbody>
</table>

Finally, we show in Figure 5 a snapshot of the rigid body simulator applied to a scene made up of 1024 dynamic triangles, with a detail of the scene highlighted.

Figure 5: Snapshot of the rigid body simulator.

5 CONCLUSIONS

In this paper we have presented a fully GPU-implemented rigid body simulator, which is suitably composed of different fragment and vertex-shaders to execute both the simulation and the renderization tasks. Moreover we have proposed several solutions for many of the development phases, comparing their behavior. Finally, we have applied these techniques to two case studies, one based on circles and another on convex polygons.

The main contribution of the paper is to show that the GPU capabilities can be used to improve the overall timing of a CPU implementation. In the case studies, we compare our GPU solutions to analogous CPU versions, showing that GPU implementations win as the number of objects increases.

REFERENCES


