A NEW FACE RECOGNITION SYSTEM
Using HMMs Along with SVD Coefficients

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Abstract: In this paper, a new Hidden Markov Model (HMM)-based face recognition system is proposed. As a novel point despite of 5-state HMM used in pervious researches, we used 7-state HMM to cover more details. As another novel point, we used a small number of quantized Singular Value Decomposition (SVD) coefficients as features describing blocks of face images. This makes the system very fast. In order to additional reduction in computational complexity and memory consumption the images are resized to $64 \times 64$ jpeg format. The system has been examined on the Olivetti Research Laboratory (ORL) face database. The experiments showed a recognition rate of 99%, using half of the images for training. Our system has been evaluated on YALE database too. Using five and six training images, we obtained 97.78% and 100% recognition rates respectively, a record in the literature. The proposed method is compared with the best researches in the literature. The results show that the proposed method is the fastest one, having approximately 100% recognition rate.

1 INTRODUCTION

Face recognition has been undoubtedly one of the major topics in the image processing and pattern recognition in the last decade due to the new interests in, security, smart environments, video indexing and access control. Existing and future applications of face recognition are many. A human face is a complex object with features varying over time. So a robust face recognition system must operate under a variety of conditions.

There have been a several face recognition methods, common face recognition methods are Geometrical Feature Matching (Kanade, 1973), Eigenfaces method (Turk and Pentland, 1991), Bunch Graph Matching (Wiskott et al., 1997), Neural Networks (Lin et al., 1997), Markov Random Fields (Huang et al., 2004) and Hidden Markov Models (Bicego et al., 2003; Kohir and Desai, 1998).

This paper presents a new approach using one dimensional Discrete Hidden Markov Model (HMM) as classifier and Singular Values Decomposition (SVD) coefficients as features for face recognition. We used a 7-state HMM to model face configuration. Here despite of previous papers, we added two new states to HMM to take into account the hair and eyebrows regions. The proposed approach has been examined on Olivetti Research Laboratory (ORL) database. To speed up the algorithm and reduce the computational complexity and memory consumption along with using small number of SVD coefficients we resized the $112 \times 92$ pgm formatted images of this database to $64 \times 64$ jpeg images. Image resizing results in information losing and therefore seems to reduce the recognition rate. But we have gained 99% classification accuracy while speeding up the system considerably. We also have examined the proposed system on YALE face database. We resized YALE database from $231 \times 195$ pgm format into $64 \times 64$ jpeg face images as well. Using five and six training images, we obtained 97.78% and 100% recognition rates respectively, a record in the literature.

The rest of the paper is organized as follows. In Section 2, Hidden Markov Models and SVD are briefly discussed. Section 3.1 describes an order-statistic filter and its role in the proposed system. Observation vectors calculations along with feature extraction process are discussed in Sections 3.2 and 3.3. Section 3.4 describes feature selection method. In Section 3.5 we introduce features quantization and labeling process. Sections 3.6 and 3.7 represent training and recognition procedures and discuss on results gained on face databases. Thus Section 3 completely describes the proposed system. Finally in Section 4 conclusions are drawn.
2 BACKGROUND

2.1 Hidden Markov Models

A HMM is associated with non-observable (hidden) states and an observable sequence generated by the hidden states individually. The elements of a HMM are as below:

- \( N = |S| \) is the number of states in the model, where \( S = \{s_1, s_2, \ldots, s_N\} \) is the set of all possible states. The state of the model at time \( t \) is given by \( q_t \in S \).

- \( M = |V| \) is the number of the different observation symbols, where \( V = \{v_1, v_2, \ldots, v_M\} \) is the set of all possible observation symbols \( v_i \) (also called the code book of the model). The observation symbol at time \( t \) is given by \( o_t \in V \).

Each observation vector is a vector of observation symbols of length \( T \). \( T \) is defined by user based on the in hand problem.

- \( A = \{a_{ij}\} \) is the state transition probability matrix, where:
  \[
  a_{ij} = P[q_{t+1} = s_j | q_t = s_i], \ 1 \leq i, j \leq N
  \]
  \[
  0 \leq a_{ij} \leq 1
  \]
  \[
  \sum_{j=1}^{N} a_{ij} = 1, \ 1 \leq i \leq N
  \]

- \( B = \{b_{ij}(k)\} \) is the observation symbol probability matrix, where:
  \[
  b_{ij}(k) = P[o_t = v_k | q_t = s_j], \ 1 \leq j \leq N, 1 \leq k \leq M
  \]

- \( \pi = \{\pi_1, \pi_2, \ldots, \pi_N\} \) is the initial state distribution, where:
  \[
  \pi_i = P[q_1 = s_i], \ 1 \leq i \leq N
  \]

Using shorthand notation HMM is defined as following triple:

\[
\lambda = (A, B, \pi)
\]

HMMs generally work on sequences of symbols called observation vectors, while an image usually is represented by a simple 2D matrix.

In this paper we divided image faces into 7 regions which each is assigned to a state in a left to right one dimensional HMM. Figure 1 shows the mentioned seven face regions.

2.2 Singular Value Decomposition

The Singular Value Decomposition (SVD) has been an important tool in signal processing and statistical data analysis. As singular vectors of a matrix are the span bases of the matrix, and orthonormal, they can exhibit some features of the patterns embedded in the signal. SVD provides a new way for extracting algebraic features from an image.

A singular value decomposition of a \( m \times n \) matrix \( X \) is any function of the form:

\[
X = U \Sigma V^T,
\]

where \( U(m \times m) \) and \( V(n \times n) \) are orthogonal matrices, and \( \Sigma \) is and \( m \times n \) matrix of singular values with components \( \sigma_{ij} = 0, i \neq j \) and \( \sigma_{ii} > 0 \). Furthermore, it can be shown that there exist non-unique matrices \( U \) and \( V \) such that \( \sigma_{1} \geq \sigma_{2} \geq \ldots \geq 0 \). The columns of the orthogonal matrices \( U \) and \( V \) are called the left and right singular vectors respectively; an important property of \( U \) and \( V \) is that they are mutually orthogonal. Singular values represent algebraic properties of an image (Klema and Laub, 1980).
3 THE PROPOSED SYSTEM

3.1 Filtering

Most of the face recognition systems commonly use preprocessing to improve their performance. In the proposed system as the first step, we use a specific filter which directly affects the speed and recognition rate of the algorithm. Order-statistic filters are nonlinear spatial filters. A two-dimensional order statistic filter, which replaces the centered element of a $3 \times 3$ window with the minimum element in the window, was used in the proposed system. It can simply be represented by the following equation.

$$ f(x,y) = \min_{(s,t) \in S_{XY}} \{ g(s,t) \} $$  \hspace{1cm} (7)

In this equation, $g(s,t)$ is the grey level of pixel $(s,t)$ and $S_{XY}$ is the mentioned window. Most of the face databases were captured with camera flash. Using the flash frequently caused highlights in the subjects eyes which affected the classification accuracy (Haralick and Shapiro, 1992). According to sentences above, this filter is expected compensate the flash effect (see Figure 3). It also reduces salt noise as a result of the $\min$ operation.

3.2 The Observation Vectors

Since HMMs require a one-dimensional observation sequence and face images are innately two-dimensional, the images should be interpreted as a one dimensional sequence. The observation sequence is generated by dividing each face image of width $W$ and height $H$ into overlapping blocks of height $L$ and width $W$. The technique is shown in Figure 4. These successive blocks are the mentioned interpretation. The number of blocks extracted from each face image is given by:

$$ T = \frac{H - L}{L - P} + 1, $$  \hspace{1cm} (8)

where $P$ is overlap size of two consecutive blocks.

A high percent of overlap between consecutive blocks significantly increases the performance of the system consequently increases the computational complexity. Our experiments showed that as long as $P$ is large ($P \leq L - 1$) and $L = H/10$, the recognition rate is not very sensitive to the variations of $L$.

3.3 Feature Extraction

In order to reduce the computational complexity and memory consumption, we resize both face databases into $64 \times 64$ which results in data losing of images, so to achieve high recognition rate we have to use robust feature extraction method.

A successful face recognition system depends heavily on the feature extraction method. One major improvement of our system is the use of SVD coefficients as features instead of gray values of the pixels in the sampling windows. We use a sampling window of 5 pixels height and 64 pixels width, and an overlap of 80% in vertical direction. Using pixels value as features describing blocks, increases the processing time and leads to high computational complexity. In this paper, we compute SVD coefficients of each block and use them as our features.

3.4 Feature Selection

The problem of feature selection is defined as follows: given a set of $d$ features, select a subset of size $m$ that leads to the smallest classification error and smallest computational cost. We select our features from singular values which are the diagonal elements of $\Sigma$. It has been shown that the energy and information of a signal is mainly conveyed by a few big singular values and their related vectors. Figure 5 shows the singular values of a $64 \times 64$ face image. Obviously the first two singular values are very bigger than the other ones and consequently, based on the SVD theory, have more significance.

Figure 6 shows a face image along with its five approximations, using different combinations of the first three singular values and their related vectors.

![Figure 3: An example of operation of the order static filter. Image before filtering in (a) and after filtering (b).](image)

![Figure 4: The sequence of overlapping blocks.](image)

![Figure 5: The sequence of overlapping blocks.](image)
Figure 5: SVD coefficients of a 64 x 64 face image.

Figure 6: a) Original image, b) $\sigma_1 u_1^T$, c) $\sigma_2 u_2^T$, e) b+c and f) b+c+d are approximations of the original image.

The last approximation (Figure 6f) contains all three singular values together and simply shows the large amount of the face information. To select some of these coefficients as feature, a large number of combinations of these were evaluated in the system. As expected, the two biggest singular values along with $u_1$ have the best classification rate.

Based on the above discussion we use two first coefficients of matrix $\Sigma$ and first coefficient of matrix $U$ as three features ($\sigma_{11}$, $\sigma_{22}$, $u_1$) associating each block. Thus each block of size 320 pixels, is represented by 3 values. This decreases computational complexity and sensitivity to image noise, changes in illumination, shift or rotation.

3.5 Quantization

The SVD coefficients have innately continuous values. These coefficients build the observation vectors. If they are considered in the same continuous type, we will encounter an infinite number of possible observation vectors that can’t be modeled by discrete HMM. So we quantize the features described above. To show the details of the quantization process, used in the proposed system, consider a vector $X = (x_1, x_2, ..., x_N)$ with continuous components. Suppose $x_i$ is to be quantized into $D_i$ distinct levels. So the difference between two successive quantized values will be as equation x.

$$\Delta_i = \frac{x_{i_{\text{max}}} - x_{i_{\text{min}}}}{D_i}$$

$x_{i_{\text{max}}}$ and $x_{i_{\text{min}}}$ are the maximum and minimum values that $x_i$ gets in all possible observation vectors respectively.

$$x_{i_{\text{quantized}}} = \left\lfloor \frac{x_i - x_{i_{\text{min}}}}{\Delta_i} \right\rfloor$$

At last each quantized vector is associated with a label that here is an integer number. Considering all blocks of an image, the image is mapped to a sequence of integer numbers that is considered as an observation vector. In this paper we quantized the first feature ($\sigma_{11}$) into 10, the second feature ($\sigma_{22}$) 7 and the third one ($u_1$) into 18 levels, leaving 1260 possible distinct vectors for each block.

3.6 The Training Process

After representing each face image by observation vectors, they are modeled by a 7-state HMM shown in Figure 2. Five images of the same face are used to train the related HMM and the remaining images are used for testing.

A HMM is trained for each person in the database using the Baum-Welch algorithm (Rabiner, 1989). At the first step $\lambda = (A, B, \pi)$ is initialized. The initial values for $A$ and $\pi$ are set due to the left to right structure of the face model corresponding to Figure 2.

The initial values for $A$ and $\pi$ are as follows:

$$a_{i,i+1} = 0.5 \quad 1 \leq i \leq 6$$

$$\pi_{i,0} = 1$$

Initial estimates of the observation probability matrix $B$ are obtained as following simple Matlab statement:

$$B = \frac{1}{M} \text{ones}(N, M)$$

Where $M$ is the number of all possible observation symbols obtained from quantization procedure and $N$ is the number of states.

After representing the images by observation vectors, the parameters of the HMM are estimated using the Baum-Welch algorithm which finds $\hat{\lambda} = \max_\lambda P(O | \lambda)$. In the computed model the probability of the observation $O$ associated to the
learning image is maximized. Figure 7 shows the estimation process related to one learning image. This process is iterated for all training images of a person. The iterations stop, when variation of the probability of the observation vector (related to current learning image) in two consecutive iterations is smaller than a specified threshold or the number of iterations reaches to an upper bound. This process is reiterated for the remaining training images. Here the estimated parameters of each training image are used as initial parameters of next training image. The estimated HMM of the last training image of a class is considered as its final HMM.

3.7 Face Recognition

After learning process, each class (face) is associated to a HMM. For a K-class classification problem, we find K distinct HMM models. Each test image experiences the block extraction, feature extraction and quantization process as well. Indeed each test image like training images is represented by its own observation vector. Here for an incoming face image, we simply calculate the probability of the observation vector (current test image) given each HMM face model. A face image \( m \) is recognized as face \( d \) if:

\[
P(o^{(m)} | \lambda_d) = \max_{\lambda_n} P(o^{(m)} | \lambda_n)
\]

The proposed recognition system was tested on the ORL face database. The database contains 10 different face images per person of 40 people with the resolution of 112×92 pixels. As we mentioned before in order to decrease computational complexity (which affects on training and testing time) and memory consumption, we resized the pgm format images of this database from 112×92 to 64×64 jpeg format images. Five images of each person were used for the training task. The recognition rate is 99%, which corresponds to two misclassified images in whole database. Table 1 represents a comparison among different face recognition techniques and the proposed system on the ORL face database. It is important to notice that all different face recognition techniques in Table 1 use 112×92 resolution of ORL face database where we use 64×64 image size. The significance of this result is that such a high recognition rate is achieved using only three features per block along with image resizing. Figure 8 shows the 10 images of one subject from ORL face database.

We obtained 99% recognition rate by using 1260 symbols. To illustrate the relation between number of symbols and recognition rate we varied the number of symbols from 8 to 1800. The recognition rate is illustrated in Figure 9. Increasing the number of symbols to achieve greater recognition rate leads to more time consumption for training and testing procedure. To prevent this event we can use low number of symbols. For example as we can see in Figure 9 our system achieve 80%, 94.5% and 97% accuracy respectively with 24, 182 and 630 symbols.

![Figure 7: The training process of a training image.](image)

![Figure 8: A class of the ORL face database.](image)

<table>
<thead>
<tr>
<th>Method</th>
<th>Error</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Eigenface</td>
<td>9.5%</td>
<td>(Turk and Pentland, 1991)</td>
</tr>
<tr>
<td>Pseudo 2D HMM+gray tone features</td>
<td>5%</td>
<td>(Samaria and Young, 1994)</td>
</tr>
<tr>
<td>PDNN</td>
<td>4%</td>
<td>(Lin et al., 1997)</td>
</tr>
<tr>
<td>Continuous n-tuple classifier</td>
<td>2.7%</td>
<td>(Lucas, 1997)</td>
</tr>
<tr>
<td>Ergodic HMM + DCT coefficient</td>
<td>0.5%</td>
<td>(Kohir and Desai, 1998)</td>
</tr>
<tr>
<td>Pseudo 2D HMM + Wavelet</td>
<td>0%</td>
<td>(Bicego et al., 2003)</td>
</tr>
<tr>
<td>Markov Random Fields</td>
<td>13%</td>
<td>(Huang et al., 2004)</td>
</tr>
<tr>
<td>1D HMM+SVD</td>
<td>1%</td>
<td>(Proposed method)</td>
</tr>
</tbody>
</table>

![Figure 9: Showing the relation between number of symbols and recognition rate. Maximum value is 99% and encounter on 1260 symbols.](image)
Table 2 shows a comparison of the different face recognition techniques on the ORL face database which reported their computational cost. As we can see from Table 2 our system has a recognition rate of 99% and a low computational cost. Proposed system was implemented in Matlab 7.1 and tested on a machine with CPU Pentium IV 2.8 GHz with 512 Mb Ram and 1 Mb system cache.

Finally we tested our system on YALE face database. The Yale face database contains 165 images of 15 subjects. There are 11 images per subject with different facial expressions or lightings. Figure 10 shows the 11 images of one subject. We resized YALE database from $231 \times 195$ into $64 \times 64$ jpeg face images. No other changes like background cutting or cropping the images were preformed. We obtained our system results on 1 image to 10 images for training using 960 symbols. Table 3 shows Comparative results on this database.

Table 3: Experiments on YALE face database. Our accuracy obtained on $64 \times 64$ resolution face images.

<table>
<thead>
<tr>
<th># of train image(s)</th>
<th>MRF (Huang et al., 2004)</th>
<th>PCA (Huang et al., 2004)</th>
<th>Proposed method</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>81.6%</td>
<td>60.04%</td>
<td>78%</td>
</tr>
<tr>
<td>2</td>
<td>93.11%</td>
<td>75.2%</td>
<td>82.22%</td>
</tr>
<tr>
<td>3</td>
<td>95.17%</td>
<td>79.03%</td>
<td>90.83%</td>
</tr>
<tr>
<td>4</td>
<td>95.9%</td>
<td>79.75%</td>
<td>94.29%</td>
</tr>
<tr>
<td>5</td>
<td>96.11%</td>
<td>81.13%</td>
<td>97.78%</td>
</tr>
<tr>
<td>6</td>
<td>96.67%</td>
<td>81.15%</td>
<td>100%</td>
</tr>
<tr>
<td>7</td>
<td>98.67%</td>
<td>81.9%</td>
<td>100%</td>
</tr>
<tr>
<td>8</td>
<td>97.33%</td>
<td>81.24%</td>
<td>100%</td>
</tr>
<tr>
<td>9</td>
<td>97.33%</td>
<td>81.73%</td>
<td>100%</td>
</tr>
<tr>
<td>10</td>
<td>99.33%</td>
<td>81.73%</td>
<td>100%</td>
</tr>
</tbody>
</table>

4 CONCLUSIONS

A fast and efficient system was presented. Proposed system used SVD for feature extraction and 1-D HMM as classifier. The evaluations and comparisons were performed on the two well known face image databases; ORL and YALE. In both databases, approximately having a recognition rate of 100%, the system was very fast. This was achieved by resizing the images to smaller size and using a small number of features.

Future work will be directed towards evaluating the proposed system on larger face databases.

REFERENCES


