# VIOL: Viewpoint Invariant Object Localizator Viewpoint Invariant Planar Features in Man-Made Environments

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Abstract: Object detection is one of the fundamental issues in computer vision. The established methods, rely on different feature descriptors to determine correspondences between significant image points. However, they do not provide reliable results, especially for extreme viewpoint changes. This is because feature descriptors do not adhere to the projective distortion introduced with an extreme viewpoint change. Different approaches have been proposed to lower this hurdle, e.g., by randomly sampling multiple virtual viewpoints. However, these methods are either computationally intensive or impose strong assumptions of the environment. In this paper, we propose an algorithm to detect corresponding quasi-planar objects in man-made environments. We make use of the observation that these environments typically contain rectangular structures. We exploit the information gathered from a depth sensor to detect planar regions. With these, we unwrap the projective distortion, by transforming the planar patch into a fronto-parallel view. We demonstrate the feasibility and capabilities of our approach in a real-world scenario: a supermarket.

# **1 INTRODUCTION**

Object detection is one of the fundamental issues in computer vision. The problem can be summarized as finding objects in an image using a known image of the same object, e.g., localizing an item within a supermarket. The general idea relies on correspondences: matches that link significant points from one image to another. These feature correspondences are also required for a variety of other applications including Visual Odometry (Nister et al., 2006), Image Stitching (Brown and Lowe, 2007), or Object Tracking (Donoser et al., 2010). All of these applications typically require a significant number of correspondences.

A variety of different feature detection and description frameworks has been developed, e. g., Maximally Stable Extremal Regions (Matas et al., 2002), Scale Invariant Feature Transform (SIFT) (Lowe, 2004), Speeded Up Robust Features (SURF) (Bay et al., 2008), or Oriented FAST and Rotated BRIEF (ORB) (Rublee et al., 2011). They all share a common idea: features shall be distinctive against their spatial surroundings. Typically, feature matching algorithms are divided into three steps: i) significant points or regions within an image are detected, ii) these detected features are described with respect to their spatial sur-



(a) Fronto-parallel view of (b) Slanted view of the same different items within a shelf. items within the same shelf. Figure 1: While it is possible to detect different items in Figure 1(a) it is quite challenging to detect these objects in Figure 1(b). This is because SIFT does not adheres to the projective distortion introduced with the viewpoint change.

roundings, iii) and finally, these descriptions are matched to find correspondences between two different images.

If the viewpoint change from one image to another is reasonably small, state-of-the-art feature detection algorithms typically produce reliable and repeatable results. If the viewpoint change is large enough, the problem of matching features becomes challenging. Morel and Yu demonstrated that the established methods, e.g., SIFT as one of the de-facto-standards in this area, do not give suitable results if the viewpoint change is strong (Morel and Yu, 2009). This is because feature descriptors typically aim at providing a scale, rotation, and illumination invariant description. However, state-of-the-art descriptors do not ad-

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here to the projective distortion introduced by viewpoint changes of the camera, as illustrated in Figure 1.

Figure 1(a) illustrates an example from the supermarket: a shelf containing different items. Here, a viewpoint has been chosen, close to a fronto-parallel view - the camera is positioned close to the opposite normal direction of the plane defined by the shelf. Determining corresponding feature points in this image and an image from a database typically produces good results and demonstrates the applicability of state-ofthe-art algorithms.

If the viewpoint of the camera is moved as shown in Figure 1(b), the number of correspondences dramatically decreases due to the projective distortion introduced through the viewpoint change. This observation can be justified by evaluating state-of-theart feature descriptors: they typically consider a feature point as a local distinctive element on the image plane. If the image plane is nearly co-planar with the object plane in one image, whereas it is not in another image, the descriptions of the same physical point on the object plane differ and thus do correspond.

In this paper, we extend the capabilities of stateof-the-art feature matching frameworks. Therefore, we focus on objects in man-made environments. We make use of the observation that man-made environments are rich of planar, rectangular structures. This is because they typically contain some sort of structured objects, e.g., walls, windows, shelves, or paintings. We exploit this observation with Microsofts HoloLens to detect planar rectangles within the image. We use these to recover a fronto-parallel view to reduce the projective distortion. We call these fronto-parallel views viewpoint invariant planes. Based on these, we compute SIFT features to achieve viewpoint invariance of the SIFT descriptors. We generate viewpoint invariant planes relying only on the vertices of the planar rectangles. We demonstrate the feasibility of our approach in a real-world scenario: a supermarket. Further, we show similarities and differences to other state-of-the-art viewpoint invariant feature matching frameworks. We address in particular extreme viewpoint changes to evaluate the viewpointvariance of our approach.

Our contribution is two-folded. On the one hand, we propose a straight forward system to achieve viewpoint invariance for man-made planar objects. Thereby, we describe how the proposed approach can be integrated into a modern mixed reality device. On the other hand, we do not impose constraints on our environment, except for that it contains planar elements. In contrast to other approaches, we do not restrict our environment by imposing a Manhattan-world assumption. The paper is structured as follows: We present related work of other authors in Section 2. Afterwards, in Section 3, we describe the proposed method to detect viewpoint invariant features with the help of viewpoint invariant planes. In Section 4 we evaluate the proposed method in our real world scenario. We conclude our work in Section 5.

## 2 RELATED WORK

In this section, we summarize existing approaches specifically designed for projectively distorted scenes. We distinguish two types of methods: those that rely on the pure image data and those that additionally use depth data.

An approach of the first category was proposed by Morel and Yu. They proposed an affine invariant feature matching approach (Morel and Yu, 2009; Yu and Morel, 2009) - an extension of the well-known SIFT framework (Lowe, 1999). Different viewpoints are simulated by sampling different longitudes and latitudes of a view-hemisphere over the image. The authors propose to calculate an affine transformation to unwrap the projective distortion. SIFT features of simulated views are matched and the highest amount of matches represents the result. Cai et al. proposed a similar approach (Cai et al., 2013). Here, the authors calculate a homography to unwrap the projective distortion. Both approaches cannot determine correct correspondences if multiple planes are visible on a single image. Further, they are computationally intensive due to the subsequent matching of simulated views.

To relax the computationally complexity, an iterative approach has been proposed (Yu et al., 2012). The approach has a significant drawback: its success is based on the initial matching of the two images. If, e. g., because of a strong viewpoint change, matching fails, the algorithm is not able to produce reliable results. Chen et. al. proposed to extract MSER (Matas et al., 2004) and fit them into ellipses (Chen et al., 2013). These ellipses are assumed to be circular in a fronto-parallel view. Thus, they transform them into circular areas and describe and match SIFT features.

After all, especially for man-made environments, rectangular areas are more likely, e. g., for doors, windows, shelves, and building facades. This observation can be intensified by incorporating the Manhattan world assumption, whereby it is assumed that a scene contains sufficient structure to align planes to three orthogonal directions (Yuille and Coughlan, 2000). (Srajer et al., 2015) exploit this assumption. The authors propose to estimate the room geometry by fitting a textured 3D cuboid into the scene. Finally, they rectify the individual cuboid surfaces and determine SIFT correspondences. However, this permits usage in a Non-Manhattan World. Filax et al. proposed QuadSIFT (Filax et al., 2017). Here, the authors proposed to detect quadrilaterals, unwrap them to rectangles and determine SIFT correspondences. The approach does not incorporate a Manhattan-world assumption, but this raises additional difficulties in detecting quadrilaterals.

An approach of the second category was published by Köser and Koch. They proposed a perspectively invariant feature descriptor for local regions that can be approximated by a plane relying on depth data (Köser and Koch, 2007). Based on MSER (Matas et al., 2004), a fronto-parallel view is generated for every detected feature. Therefor, the 3D points are meshed and textured from the original view. Afterwards a virtual camera is moved to a position in normal direction from the surface. Finally, every feature in the synthetic view is described via SIFT. Wu et al. proposed a quite similar approach, the idea is to calculate a tangent plane for every feature point (Wu et al., 2008). In contrast to (Köser and Koch, 2007), they propose to detect features via SIFT directly in the query image. By projecting the texture of the 3D model onto a tangent plane at every feature point, they gain the ability to unwrap the projective distortion. Finally, they calculate the descriptors based on the synthetic projections and and determine correspondences. However, SIFT also detects features at edges where an approximation of the tangent plane within the 3D model might be unreliable.

Another approach of the second category was proposed by Baatz et al.. Their system was designed for place-of-interest recognition in an urban environment (Baatz et al., 2010). Their system requires an offline data acquisition phase to determine the urban 3D geometry and build a database of fronto-parallel synthetic views of buildings. In the recognition phase they propose to detect line segments and to unwrap the projective distortion by using Manhattan-world assumption similar to (McDonald, 2009). The authors rectified an image according to pairs of vanishing points. Finally, they compute SIFT features to determine correspondences with the database. However, this approach requires a query image which is rich of line segments. Further, it is desirable that most of the line segments correspond to orthogonal vanishing points. Again, this approach permits usage in a Non-Manhattan-world scene.



Figure 2: VIOL: We use the 3D model gathered with a *HoloLens* to achieve viewpoint invariance of features. Therefore, we unwrap locally planar rectangles within an image to fronto-parallel views - so called viewpoint invariant planes. Finally, we detect and describe SIFT features on them.

# **3** VIEWPOINT INVARIANT OBJECT LOCALIZATOR

In this section, we describe our system VIOL, which was designed to detect objects in an unknown manmade environment using Microsofts *HoloLens*. To the current day, the *HoloLens* is one of the most famous, publicly available, head-mounted devices which acquires a model of the environment. Different cameras and an inertial measurement unit track the users head movements, aided by a time-of-flight depth sensor. The sensor data is used to triangulate the environment. The generated map is refined and extend as the user moves.

The generated map in combination with 2D images are the enabling techniques for our system. The goal of VIOL is to determine the position of different objects. The goal adheres an everyday use-case: searching for items in a supermarket.

However, especially in an unknown supermarket, this is only helpful, if VIOL is able to detect objects reliably. This is especially true for objects distorted due to a slanted view as shown in Fig. 1(b). We extend SIFT to cope with projective distortion: first, we detect planar rectangular structures using 3D sensor data. Then, we determine the rectangles that are visible to the camera and project them onto the camera image. Finally, we compute a viewpoint invariant plane for every projected rectangle and finally extract viewpoint invariant SIFT features. An outline of the proposed approach is depicted in Fig. 2. In the following, we explain every step in detail.

#### **3.1 Acquire Local Geometry**

VIOL relies on a 3D model of the environment. The first step of the approach consists of acquiring the local geometry with the built-sensors. We designed our VIOL explicitly for the use with Microsofts *HoloLens*. The head-tracking cameras, inertial measurement units, and time-of-flight depth sensor are used to acquire a 3D mesh of the environment. As the user continues to move, the triangular mesh is continuously grows.

#### 3.2 Detect Planar Structures

In the second step, we detect planar, physical structures. Planar regions within the scene are of interest as they are most resistant to occlusion. If a region within the scene is planar, it is not likely to change its visual appearance under strong projective distortion.

We detect planar regions in the previously generated 3D triangular mesh of the environment. We use the publicly available source from Microsoft<sup>1</sup>. First, the curvature for every vertex of the mesh is calculated. Second, the curvatures for every vertex are smoothed to adhere to noise. Next, potential planes are found by flood-filling over the vertex curvatures. Neighboring vertices are considered as potentially planar if the curvature at every vertex and the difference of two neighboring normals are reasonable small. Then, the plane equations of found potential planes are determined via Principal Component Analysis. Using the plane equations, the area of the potential planes is extended using vertices, that are close to the plane. Finally, rectilinearity is enforced by determining an oriented bound box for every plane candidate.

#### 3.3 Select Visible Planes

The 3D model of the environment continuously grows, due to the nature of the *HoloLens*. Therefore, not every previously detected plane might be visible for the user. As we aim at comparing visual features within the planes, we do not have to process invisible planes.

In this step, we determine the subset of visible planes with respect to the current viewpoint of the camera. To achieve this, we select visible planes by projecting multiple rays from the camera center through the image plane. We divide the image into different cells and project a ray through the center of every cell. Finally, we build the set of visible planes, by selecting the closest 3D planar rectangles which intersect with at least one ray.

#### 3.4 Acquire 2D Projection

In this step, we project the vertices of the 3D planar rectangles onto the image plane. Speaking mathematically, projecting an arbitrary point into the image space can be expressed as

$$\tilde{x} = K(RX + T) \tag{1}$$

whereas X represents the point in 3D and  $\tilde{x}$  the projected point on the image plane. K encapsulates the internal parameters and R and T represent the external parameters: camera rotation, and translation (Hartley and Zisserman, 2004).

We project the 3D vertices of visual planes, defined in the 3D mesh of the environment, onto the image plane with Equation 1. We thereby obtain the pixel coordinates of the plane. Note, that projecting a 3D planar rectangle onto the image plane introduces projective distortion. Thereby, the 3D rectangles looses some properties in image space, e. g., rectilinearity. The 3D rectangle, projected into a 2D quadrilateral, is typically not rectangular in image space. In the following phases, we unwrap the projective distortion introduced through the projection.

#### 3.5 Viewpoint Invariant Planes

In the previous step, we projected physically planar rectangles into image space, whereby they lose significant properties, such as rectilinearity. We recover this property by unwrapping the projected plane into a viewpoint invariant plane. Therefore, we determine a homography that maps the projected rectangular, the quadrilateral, into a viewpoint invariant plane. We calculate the homography, mapping a given set of at least four points into another set of four points, with the well-known Direct Linear Transformation algorithm (Hartley and Zisserman, 2004). We use the vertices of the quadrilateral and the vertices of the viewpoint invariant plane to estimate the homography. We unwrap the projective distortion of the planar object by applying the homography to every rectangle that has been projected into a quadrilateral in image space.

Before we can apply the homography, we have to estimate it. Therefore, we need to estimate a valid set of vertices of the viewpoint invariant plane in image space. We require a viewpoint invariant plane to have

<sup>&</sup>lt;sup>1</sup>https://github.com/Microsoft/MixedRealityToolkit

rectangular vertices in image space. Therefore, we might simply choose the vertices as a squared patch of an arbitrary size. Although this recovers the rectilinearity, it does not preserve the physical aspect ratio. As we pointed out in (Filax et al., 2017), it is important to preserve the aspect ratio, as it enhances the matching results dramatically. Due to the sensor data of the *HoloLens*, we do have access to the physical aspect ratio of every 3D plane. Thus, we determine the set of rectangular vertices with respect to the physical aspect ratio of every 3D plane.

Due to its nature, a homography is typically defined up to scale. Thus, the scale of the rectangular set of vertices can freely be chosen. Although feature descriptors typically adhere changes to scale, we choose to fix the scale of every viewpoint invariant plane with respect to the physical size of the corresponding 3D plane. We fixed the scale for every viewpoint invariant plane to 20 dots per inch.

## 3.6 Detect, Describe and Match SIFT Features

We use SIFT (Lowe, 2004) to detect and describe features of two viewpoint invariant planes. We rely on OpenCV to detect and describe SIFT features using the default parameters in combination with a brute force matching strategy. To detect if a descriptor in one viewpoint invariant plane matches another descriptor in the other viewpoint invariant plane we follow Lowe's well-known ratio test: If the nearest distance of the best match for a descriptor is smaller than k times the second best match for that descriptor, the best match is considered to be valid with k = 0.6 (Lowe, 2004). Next, we remove invalid matches with a reprojection error of 4.0 pixels and larger. Finally, we consider two images as matching if the number of correspondences is larger than six.

## **4 EXPERIMENTS**

We evaluate our method with real world images taken in a local supermarket. Our database comprises two different arbitrarily selected shelves. Fig. 3 depicts examples. These images were taken with the camera of Microsofts *HoloLens* and have a resolution of 1280x720 pixels. Note that we used the grayscale images to preserve the comparability between the different approaches. The images were taken from various viewpoints in an unstructured manner to mimic natural behavior.

Our evaluation is two-folded: on the one hand, we detect correspondences between different images



shelf whereas  $\Phi \cong 0^\circ$ . shelf with  $\Phi \cong 50^\circ$ .

(c) Fronto-parallel view of (d) Slanted view of Fianother shelf with  $\Phi \cong 0^{\circ}$ . gure 3(c) with  $\Phi \cong -50^{\circ}$ .

Figure 3: Examples from the database: Figure 3(a) depicts a fronto-parallel view of a shelf with cereals. In Figure 3(b) the viewpoint was changed. Figure 3(c) depicts another shelf. This shelf does not contain repetitive items as the shelf in 3(a). Figure 3(d) depicts a slanted view of 3(c). Note, that we blurred the images after the evaluation.

from arbitrary viewpoints of the shelf. On the other hand, we recognize objects within these shelves. We determine the quality of our approach by determining the total number of correspondences found. We compare the proposed method with SIFT (Lowe, 2004) and ASIFT (Yu and Morel, 2011). Note, that these methods do not rel y on 3D data, but seem to be the de-facto standard in this particular field of research.

# 4.1 Shelf Detection

We evaluate our method by matching different scene images in a man-made environment in this section. Table 1 comprises the results for the scene *Cereals*. Example images are depicted in Figure 3(a) and Fi-

Table 1: Quantitative evaluation of SIFT, ASIFT and VIOL for the shelf *Cereals*.  $\Phi$  denotes the estimated viewpoint change with respect to the shelf in Figure 3(a). *M* denotes the absolute number of correspondences and *R* comprise this value with respect to the cardinality of features in Figure 3(a).

Φ	SIFT		ASIFT		VIOL	
	M	R	М	R	М	R
$-50^{\circ}$	4	0,05%	40	0,09%	23	0,37%
-45°	2	0,02%	25	0,06%	32	0,52%
$-30^{\circ}$	16	0,18%	77	0,18%	101	1,65%
20°	64	0,74%	750	1,76%	269	4,38%
30°	20	0,23%	509	1,19%	164	2,67%
35°	10	0,11%	452	1,06%	134	2,18%
45°	5	0,06%	218	0,51%	92	1,50%
50°	7	0,08%	109	0,26%	64	1,04%
55°	4	0,05%	22	0,05%	33	0,54%



Figure 4: Typical examples from our scene detection test sets. The first column depicts the result of the state-of-the-art approach. The second column depicts results generated by ASIFT and the last column depicts our results. We denote the absolute number of correspondences M and the detection rate R in brackets for every approach.

gure 3(b). The first column depicts the estimated viewpoint change with respect to the shelf in Figure 3(a). M denotes the absolute number of correspondences whereas R comprises the absolute values with respect to the absolute number of features extracted from Figure 3(a).

As indicated with bold values: ASIFT outperforms the other approaches in terms of absolute feature correspondences. This becomes clear if we put it into the context of detected features. SIFT, for instance, detected 8700 features in Figure 3(a). VIOL computes 6138 because our approach does not incorporate features that do not belong to a plane. ASIFT detects 42.601 features in Figure 3(a) because it incorporates a two-resolution procedure and uses the implementation of Lowe and whereas we rely on OpenCV (for SIFT and VIOL). To overcome this, we choose to display the detection rate R.

*R* describes the percentage of correspondences with respect to the cardinality features in the frontoparallel image. VIOL outperforms the other approaches here as shown in Table 1. This because VIOL does not *estimate* the projection from one image to another, due to the fact that we use the 3D information to *measure* the projection, our viewpoint invariant plane is not subject to protective distortion.

The same observation is present in the second test set *Lego*. Table 2 depicts the results. ASIFT outperforms the other approaches generally in terms of the absolute number of correspondences. Again, this is due to the fact, that ASIFT detects more features in

Table 2: Quantitative evaluation of SIFT, ASIFT and VIOL for the shelf *Lego*. Here, the different images are matched with Figure 3(c). The notation is equivalent to Table 1. Bold numbers represent the best results for the given set of images.

Φ	SIFT		ASIFT		VIOL	
	M	R	М	R	M	R
$-70^{\circ}$	4	0,05%	178	0,38%	0	0,00%
$-60^{\circ}$	4	0,05%	0	0,00%	14	0,26%
$-50^{\circ}$	6	0,07%	195	0,42%	44	0,81%
$-45^{\circ}$	7	0,08%	504	1,09%	100	1,85%
$-40^{\circ}$	8	0,09%	697	1,51%	159	2,94%
$-30^{\circ}$	306	3,58%	2745	5,94%	663	12,28%
30°	348	4,07%	3927	8,49%	594	11,10%
$40^{\circ}$	31	0,36%	969	2,10%	112	2,07%
50°	5	0,06%	205	0,44%	21	0,39%

an image. If we put this into context with the cardinality of detected features, we observe that VIOL performs atleast comparable or even better. However, we need to consider a special case:  $\Phi \cong -70^{\circ}$ . Here, our system failed to determine the correct physical plane. Therefore, it was unable to recover correspondences.

Figure 4 depicts typical example images from our testset. VIOL was able to detect the correct shelf, except for  $\Phi \approx 50^{\circ}$ . This is due to the greedy plane selection approach.

#### 4.2 **Object Detection**

In this section, we localize a specific item within an arbitrary shelf. We examine the capabilities of VIOL



Figure 5: Typical examples from our object detection test set. This comparative overview illustrates that our system outperforms the existing approaches.

on the shelf *lego* and an arbitrarily chosen item. Figure 5 depicts some examples and Table 3 displays the results. As shown in that table, that our approach outperformed the existing approaches. For  $\Phi \approx -70^{\circ}$  VIOL could not detect the correct 3D planar rectangle and therefore did not produce any correspondences. SIFT was unable to locate the desired item as expected, due to the projective distortion introduced through the given viewpoints. Although there were a variety of false positives, we were unable to determine valid correspondences using SIFT.

Table 3: Quantitative evaluation of shelf *Lego*. Here, we want to detect a specific item within the shelf. VIOL outperforms ASIFT and SIFT in terms of absolute and relative feature correspondences. Again, VIOL was unable to detect a valid plane in  $\Phi \approx -70^{\circ}$ .

Φ	SIFT		ASIFT		VIOL	
	M	R	M	R	М	R
$-70^{\circ}$	5	0,07%	0	0,00%	0	0,0%
$-60^{\circ}$	1	0,01%	0	0,00%	6	1,28%
$-50^{\circ}$	2	0,00%	0	0,00%	19	4,06%
$-45^{\circ}$	1	0,01%	0	0,00%	26	5,56%
$-40^{\circ}$	3	0,04%	0	0,00%	26	5,56%
$-30^{\circ}$	5	0,07%	32	0,08%	82	17,52%
30°	6	0,09%	26	0,06%	77	16,45%
$40^{\circ}$	2	0,03%	0	0,00%	36	7,69%
50°	1	0,01%	0	0,00%	7	1,50%

ASIFT fails as well. This is because the available version downscales input images to 800x600 pixels. Then, it processes the images, samples different viewpoints, and return the combination yielding the highest correspondences. Finally, it upscales the correspondences to the size of the input images. This is feasible as long as both input images are of the same aspect ratio. However, if the approach is used to determine correspondences for two images with different aspect ratios, this becomes erroneous. The descriptors of two actually corresponding features differ due to the different scaling in x and y direction. Therefore, ASIFT was unable to determine correspondences for almost every sample in our test set, except for  $\Phi \cong -30^\circ$  and  $\Phi \cong 30^\circ$  whereas the downscaled aspect ratios of the object and the object within the shelf were similar.

## 5 CONCLUSION

In this paper, we proposed VIOL, a system to detect objects within a supermarket. Therefore, we extended a state-of-the-art feature matching framework. We designed our system such that it detects different shelves within a supermarket. Additionally, it tries to identify objects within these shelves as soon as they come in sight. We made use of the observation that man-made environments are rich of planar, rectangular structures. Therefore, we relied on the sensors of Microsofts *HoloLens* to detect 3D planes and determined viewpoint invariant planes. Finally, we computed SIFT features and determined correspondences using two viewpoint invariant planes.

In the future, we plan to overcome issues while detecting visible planes. As we have shown in our evaluation, it possible that we discard planes using our greedy selection approach. Additionally, we plan a more extensive evaluation of the system.

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