An Analysis of the Impact of Diversity on Stacking Supervised Classifiers

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Abstract: Due to the growth of research in pattern recognition area, the limits of the techniques used for the classification task are increasingly tested. Thus, it is clear that specialized and properly configured classifiers are quite effective. However, it is not a trivial task to choose the most appropriate classifier for deal with a particular problem and set it up properly. In addition, there is no optimal algorithm to solve all prediction problems. Thus, in order to improve the result of the classification process, some techniques combine the knowledge acquired by individual learning algorithms aiming to discover new patterns not yet identified. Among these techniques, there is the stacking strategy. This strategy consists in the combination of outputs of base classifiers, induced by several learning algorithms using the same dataset, by means of another classifier called meta-classifier. This paper aims to verify the relation between the classifiers diversity and the quality of stacking. We have performed a lot of experiments which results show the impact of multiple diversity measures on the gain of stacking.

1 INTRODUCTION

The scientific community has made much effort on pattern recognition area in order to develop ever better techniques used for data analysis. In this context, machine learning has been highlighted, mainly because it can perform pattern recognition by supervised learning. These learning methods can build from patterns available in a training dataset models or functions capable of classify new patterns.

However, the quality of the classification results will substantially depend on the quality and volume of data samples used into the training phase as well as the selection of features and the set up of parameters (Kuncheva and Whitaker, 2003).

Although some classifiers individually provide solutions which are considered effective, the experimental evaluation performed by (Dietterich, 2000) shows a drop in the quality when there are large sets of patterns and/or a significant number of incomplete data samples or irrelevant features. That is, such classifiers may not effectively and/or efficiently recognize patterns in complex problems.

In order to improve the classification results, techniques for combining classifiers have been used, aiming to take advantage of several classification schemes, where the outputs of each classifier can be combined in a final decision that improves the ability to generalization. Among these techniques, we highlight stacking as a way to combine classifiers that consists of using a second-level learning algorithm to optimally combine a collection of predictions made by different models (Wolpert, 1992).

In the stacking method the choice of base algorithms is very important. According to (Opitz and Maclin, 1999), the performance of the stacking strongly depends on the accuracy and diversity of classifiers results. To verify this diversity, there are several measures based on the (dis)agreement of the classifiers (Kuncheva and Whitaker, 2003).

Therefore, the use of base algorithms with different particulars is ideal, since the patterns learned tend not to be the same. Thus, even low accuracy classifiers combined can generate a strong classifier, providing gain for stacking. Otherwise, when several classifiers agree on the vast majority of responses (no diversity), the combination will possibly have the same result, with no improvement in the stacking quality.

The purpose of this paper is to evaluate the impact of classifier diversity on the quality of stacking. The experiments we have performed show the relationship between multiple diversity measures and the gain of stacking, considering 54 datasets extracted from UCI

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machine learning repository. The proposed idea is based on the hypothesis that the greater the diversity of patterns learned by base classifiers, the higher the quality of stacking.

2 BACKGROUND

Classification is the most usual task among data mining tasks. According to (Tan et al., 2005), classification can be defined as the process of finding, through supervised learning, a model or function that describes different classes of data. The purpose of classification is to automatically label new instances of the database with a given class by applying the model or function previously learned. This model is based on the fields of the training instances.

Classification algorithms can be organized into different types according to the technical features they use in learning. Each type is best suited for a particular dataset.

2.1 Combining Classifiers with Stacking

Classifiers that implement different algorithms potentially provide additional information on the patterns to be classified. The combination of the outputs of a set of different classifiers aims to get a more precise classification, i.e. to reach a greater accuracy. In this context, stacking (Ting and Witten, 1999) is a widely used method for combining multiple classifiers generated from different learning algorithms applied on the same dataset. It is also known in the literature as stacked generalization (Dzeroski and Zenko, 2004; Wolpert, 1992).

Stacking method combines multiple base classifiers trained by using different learning algorithms *L* on a single dataset *S*, by means of a meta-classifier (Merz, 1999; Kotsiantis and Pintelas, 2004). Each training sample $s_j = (X_j, y_j)$ is a pair composed by an array of features X_j and the class label y_j .

The process can be described in two distinct levels as shown in Figure 1. The first level-0 defines a set of *N* base classifiers, where $C_i = L_i(S)|1 \le i \le N$. Level-0 classifiers are trained and tested using the cross-validation or leave-one-out procedure. The output dataset *D* used for training the meta-classier is composed by examples $((y_j^1, \ldots, y_j^i), y_j)$, i.e. a vector of predictions for each base classifier $y_j^i = C_i(X_j)$ and the same original class label y_j (Dzeroski and Zenko, 2004). In the second level-1, the meta-classifier combines base classifiers outputs from *D* into a final prediction y_j^f . The stacking pseudocode can be seen in Algorithm 1.

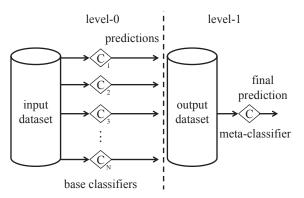


Figure 1: Representation of the stacking algorithm, based on (Opitz and Maclin, 1999).

According (Breiman, 1996), stacking can be used successfully to form linear combinations of different predictors for better accuracy. The authors have used regression trees of different sizes as base classifiers and a linear regression model in level-1. (Ting and Witten, 1999) use a linear regression adaptation called Multi-response Linear Regression (MLR) (Johnson and Wichern, 2002) as meta-classifier. (Dzeroski and Zenko, 2004) propose an extension of MLR stacking method that uses a Multi-response Model Tree in the meta-classifier. The training set used at level-1 has the following fields: (i) the probability distribution for each class, (ii) the probability distribution of each class multiplied by the maximum probability considering all classes, and (iii) the entropy of the probability distribution for each classifier. According to the authors, experimental results show that this approach is a good choice for learning in the meta-classifier, regardless of the classifiers chosen at level-0.

Several approaches have proposed the use of stacking to increase the classification quality in recent years. (Ebrahimpour et al., 2010) present a suitable

Algor	ithm 1: Combining classifiers with stacking.				
I	Input : training samples $s_j \in S$				
C	Dutput : final predictions y_j^f				
	egin				
2	Select N learning algorithms (L_1, L_2, \ldots, L_N) ;				
3	for $i = 1, 2,, N$ do				
4	Train $C_i = L_i(S)$ using cross-validation;				
5	Train $C_i = L_i(S)$ using cross-validation; $y_j^i = C_i(X_j);$				
6	end				
7	Make up a new dataset D combining all				
	predictions y_i^i ;				
8	Train $M = L(D)$ using cross-validation;				
9	$y_j^f = M(D);$				
10 e	nd				
11 r	11 return y_j^f				

solution using stacking to recognize low resolution face images. (Ness et al., 2009) describe how stacking can be used to improve the performance of an automatic system for tagging audio tracks. (Larios et al., 2011) propose a method for automatic identification of insects in species for biomonitoring purposes using space histograms and RF classifiers. (García-Gutiérrez et al., 2012) propose a method called EVOR-STACK to improve the accuracy of thematic maps. (Ali and Majid, 2015) propose a new system to predict amino acid sequences associated with breast cancer.

2.2 Diversity Measures

The diversity of predictions is a key issue in the combination of classifiers. (Kuncheva and Whitaker, 2003) define several measures of diversity and relate them to the quality of classification system. These measures are based on the agreement or disagreement of the classifiers used in the ensemble.

Let *n* be the number of instances evaluated by a pair of classifiers C_a and C_b and *R* be a relationship matrix between them, containing the number of instances in which each classifier hits (1) and/or misses (0) the prediction of the class label (Table 1). For example, n^{01} is the number of instances misclassified by C_a and correctly identified by C_b . The main diagonal shows the number of instances equally labeled by both classifiers. The secondary diagonal shows the number of records in which the classifiers disagree. The sum of all cells is the total number of instances evaluated by the analyzed classifiers.

Table 1: The relationship matrix R between a pair of classifiers C_a and C_b .

	C_b hits	C_b misses
C_a hits	n^{11}	n^{10}
C_a misses	n^{01}	n^{00}
$n = n^{11} + n^{11}$	$n^{10} + n^{01} + n^{01}$	$-n^{00}$

The following subsections present several measures of diversity in classifier ensembles (Kuncheva and Whitaker, 2003) used in the experimental evaluation of this paper.

2.2.1 Double-fault *df*

The double-fault measure df is defined by Equation 1 as the proportion of instances simultaneously misclassified by a pair of classifiers (Giacinto and Roli, 2001). df returns values in the closed range [0, 1] and it is inversely proportional to the diversity between classifiers.

$$df = \frac{n^{00}}{n^{00} + n^{01} + n^{10} + n^{11}} \tag{1}$$

2.2.2 Disagreement Dis

The disagreement measure Dis is defined by Equation 2 as the ratio between the amount of instances in which the classifiers disagree and the total number of instances (Ho, 1998). Dis varies in the closed range [0, 1] and it is directly proportional to the diversity between classifiers.

$$Dis = \frac{n^{01} + n^{10}}{n^{00} + n^{01} + n^{10} + n^{11}}$$
(2)

2.2.3 Q Statistic

The Q statistic is pairwise measure of diversity defined by Equation 3 (Afifi and Azen, 2014). This measure return values in the closed range [-1,1], being inversely proportional to the diversity between classifiers.

$$Q = \frac{n^{11}n^{00} - n^{01}n^{10}}{n^{11}n^{00} + n^{01}n^{10}}$$
(3)

2.2.4 Correlation Coefficient p

The correlation coefficient between two classifiers is defined by the Equation 4 (Sneath and Sokal, 1973). As the *Q* statistic, it returns values in the range [-1, 1]. ρ it is also inversely proportional to the diversity.

$$\rho = \frac{n^{11}n^{00} - n^{01}n^{10}}{\sqrt{(n^{11} + n^{10})(n^{01} + n^{00})(n^{11} + n^{01})(n^{10} + n^{00})}}$$
(4)

2.2.5 Kohavi-Wolpert Variance KW

The Kohavi-Wolpert variance measures the diversity among a set of N classifiers (Kohavi et al., 1996). It returns values in the range [0, 1/2] and it is directly proportional to the diversity. KW diverges from the average of several pairwise disagreement measures Dis_{avg} by a coefficient, according to the Equation 5.

$$KW = \frac{N-1}{2N} Dis_{avg}$$
(5)

2.2.6 Interrater Agreement k

The interrater agreement k is defined by Equation 6, where \bar{p} denotes the average individual classification accuracy (Dietterich, 2000). This measures performs on the predictions of a set of N classifiers and returns a value in the the closed range [-1, 1]. It is inversely proportional to the diversity among the classifiers.

$$k = 1 - \frac{N}{(N-1)\bar{p}(1-\bar{p})}KW$$
 (6)

2.2.7 Entropy *E*

Entropy performs on the output of a set of N classifiers and is defined by Equation 7, where n is the number of instances and $l(s_j)$ is the number of classifiers that properly label the instance s_j (Cunningham and Carney, 2000). E varies in the range [0, 1] and it is directly proportional to the diversity among classifiers.

$$E = \frac{1}{n} \sum_{j=1}^{n} \frac{\min[l(s_j), N - l(s_j)]}{N - [N/2]}$$
(7)

3 PROPOSED METHOD

This section describes the proposed method for analyzing the impact of diversity on stacking supervised classifiers, which are graphically represented in Figure 2.

For each analyzed dataset, different learning algorithms are used to train multiple base classifiers. The predictions returned by these classifiers are evaluated and used to perform several measures of diversity. These measures check whether and how the classifiers agree or disagree on the predicted class label. At level-1, classifiers predictions for each original instance are used to compose a new dataset that is submitted to another algorithm for training the metaclassifier. Final prediction is determined from the combination of knowledge learned by the base classifiers.

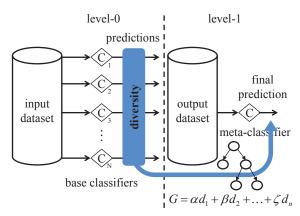


Figure 2: The proposed method for analyzing the impact of diversity on stacking supervised classifiers.

The gain of stacking *G* is computed as shown by Equation 8, where E_{MC} is the evaluation metric achieved by the meta-classifier and $E_{C_{best}}$ by the best base classifier.

$$G = \left(\frac{E_{MC}}{E_{C_{best}}}\right) - 1 \tag{8}$$

Finally, the relationship between the diversity measures and the gain of stacking computed previously for multiple datasets is induced by means of a regression model.

3.1 Classifiers

The feature vectors for each training set are made up of all data fields and the class label. The following algorithms are used at level-0 of the stacking method. This choice was motivated mainly because the algorithms are quite heterogeneous, since they are based on distinct particulars:

- MLP (Haykin, 2007) artificial neural network, based on function;
- SMO (Platt, 1999) variation of SVM (Boser et al., 1992), based on function;
- NB (John and Langley, 1995) based on Bayes's theorem;
- RIPPER (Cohen, 1995) based on rules;
- C4.5 (Quinlan, 1993) based on decision trees;
- RF (Breiman, 2001) based on a set of decision trees.

The test method to generate the predictions is cross-validation.

The meta-classifier is trained using any classification algorithm combining the knowledge learned by the base classifiers, and it is finally used to get a final prediction. Training set fields for learning the metaclassifier vary according to the base classifier algorithms. For NB, the prediction is the posterior probability of a record belonging to the same class. For RIPPER, C4.5 and RF algorithms, the prediction is the precision of the rule or node that classified each sample. In function-based algorithms, it is directly mapped to the class label. Regardless of the base classifiers, the last field is the same original class label.

3.2 Analyzing the Impact of Diversity

The impact of diversity on stacking can be analyzed by observing the relationship between diversity measures values and the gain of stacking for multiple datasets. It is expected that the most diverse sets of classifiers will contribute to the quality of stacking. This relationship is deduced using linear regression or regression model trees with the gain of stacking *G* as the target field. The vector of features is composed by the diversity measures d_1, d_2, \ldots, d_n previously computed. The regression models show how much each measure pitches in with the gain of stacking.

4 EXPERIMENTAL EVALUATION

This section describes the experiments conducted to evaluate the proposed method for analyzing the impact of diversity on stacking supervised classifiers. Each algorithm cited in Section 3 was also used to train the meta-classifier. Base classifiers and the stacking were evaluated based on the accuracy (Tan et al., 2005), which estimates the quality of classification, i.e. the prediction capacity of the model.

The experiments were performed on a personal computer using the data mining tool Weka¹ (Witten and Frank, 2011). The algorithms were parameterized with the default values of this tool, using 10 partitions in the cross validation.

4.1 Datasets

We have used 54 classification datasets extracted from UCI machine learning repository ²: Abalone, Annealing, Audiology (Std.), Balance Scale, Banknote Authent., Blood Transf. Serv. Center, Breast Cancer Wisconsin, Car Evaluation, Chess (K-R vs. K-P), Chronic Kidney Disease, Congressional Voting Rec., Connect. Bench (S,M vs. R), Connect. Bench (VR-DD), Contrac. Method Choice, Credit Approval, Dermatology, Diabetic Retinopat. Debrec., Dresses Attribute Sales, Ecoli, Forest type mapping, Glass Identification, Hill-Valley, ILPD -Indian Liver Patient, Ionosphere, Leaf, Low Resolution Spectrometer, Mammographic Mass, Molec-(S-junction), Multiple Features, Nursular Bio. ery, Opt. Recog. Handwrit. Dig., Page Blocks Classification, Pen-based Recog. Handwrit., Phishing Websites, Primary Tumor, QSAR biodegradation, Qualitative Bankruptcy, Seismic-Bumps, Solar Flare, Soybean (Large), Spambase, SPECT Heart, Statlog (Vehicle Silh.), Thoracic Surgery, Thyroid Disease (Hypothyr.), Thyroid Disease (Sick), Tic-Tac-Toe Endgame, Turkiye Student Eval., Vertebral Column, Waveform Database Gen. (V2), Wholesale customers, Wilt, Wine Quality, and Yeast.

The chosen datasets cover several areas of knowledge: business, computer, financial, game, life, physical and social. Many of them were widely cited in the scientific literature and they have sundry objectives. The field data types can be integer, real or categorical. The amount of instances ranges from 187 to 12,960. The number of fields and class labels varies from 5 to 217 and from 2 to 48 respectively. These datasets were deposited in the UCI repository from the year 1987 to 2015.

A set of preprocessing operations was applied in order to standardize the content make the datasets able to execute the algorithms in Weka. The main operations were removal of double spaces between instances, naming data fields, changing field delimiter and data types from numeric to nominal. After preprocessing they were used to train heterogeneous classification models, i.e. using different algorithms described in the previous section. Base classifiers predictions are stacked composing the level-1 training set on which the final classification model is learned.

4.2 Results

The experimental results are summarized in Table 2 that shows for each dataset the following information: the computed diversity measures double fault (df), disagreement (Dis), statistic (Q), correlation coefficient (ρ) , interrater agreement (k), Kohavi-Wolpert variance (KW) and entropy (E); the algorithm used to learn the best base classifier (L_0) and its accuracy in percentage (A_{L_0}) ; the algorithm used to learn the best meta-classifier (L_1) and its accuracy (A_{L_1}) ; and the gain of stacking (G), used to sort the results, also in percentage. Values of df, Dis, O and ρ are averages of the computed values for each pair of base classifiers. Moreover, this table presents Q', ρ' , k' and KW'that are the original diversity measures standardized in a distribution of values in the closed range [0, 1], as well as df, Dis and E.

We showed the results about datasets that reached the worst and best *G* values, i.e. we have omitted the results when the gain of stacking is not significant and ranges between -1 and 1%. Observing Table 2, we notice that stacking worked well only for 8 out of 54 datasets, where the gain ranged from 1.2 to 5.1% (lines 1-8). The best gain of stacking was reached by Balance Scale dataset, in an already very accurate result (90.7%) which is very difficult to improve. The most frequent algorithm that reaches the best accuracy for level-0 was MLP ranging $26.6 \le A_{L_0} \le 90.7$, followed by RF with $84.8 \le A_{L_0} \le 92.9$. In the level-1, the best meta-classifiers were trained with SMO ($26.9 \le A_{L_1} \le 94.9$) and RF ($83.7 \le A_{L_1} \le 95.4$).

¹http://www.cs.waikato.ac.nz/ml/weka

²http://archive.ics.uci.edu/ml

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y_{4} y_{4} y_{4} x_{4} <								7		JBI						* MLP reaches equal results
y_{4} y_{4} y_{4} x_{4} <				0.19	0.13	0.06	0.69	0.39	0.71	0.41	0.88	0.76	0.15	_	0.74	ts)
y_{4} y_{4} x_{4} <	45.4		NB	0.25	0.16	0.08	0.80	0.60	0.80	0.61	0.95	0.89	0.19		0.33	
Σ_{4} Σ_{4} V_{4} Λ_{4} <	51.0		RF	0.46	0.30	0.15	0.61	0.23	0.62	0.25	0.73	0.47	0.36		0.18	Spectrometer
y_{4} y_{4} x_{4} <	79.2		MLF	0.16	0.10	0.05	0.81	0.63	0.82	0.64	0.97	0.94	0.13		0.72	
Σ_{4} Σ_{4} V_{4} Λ_{4} <	60.2 60.2		JRip	0.10 0.32	0.22	0.00	0.73	0.07	0.73	0.47	0.88	0.77	0.10 0.26		0.02 0.46	tribute Sales
y_{\pm} y_{\pm} x_{\pm} <	86.0 70.9		RF 148	0.14	0.09 0.13	0.05	0.78	0.64	0.79	0.57	0.96 0.96	0.92	0.11		0.79	Ecoli 0.79 Solar Flare 0.62
y_{4} y_{4} x_{4} y_{4} y_{6} y_{6} y_{4} <	85.7		RF	0.17	0.12	0.06	0.74	0.48	0.75	0.50	0.93	0.85	0.14		0.77	t Approval
y_{4} y_{4} x_{4} y_{4} y_{6} <	79.0		RF	0.40	0.27	0.13	0.65	0.30	0.66	0.33	0.80	0.61	0.32		0.49	s Identification
y_{1} y_{2} y_{2} x_{4} y_{4} x_{4} x_{4} x_{4} x_{4} x_{4} x_{4} x_{4} x_{4} y_{4} <	* 78.8		MLP	0.37	0.25	0.12	0.67	0.33	0.68	0.37	0.85	0.70	0.30		0.52	
Σ_{ψ} Σ_{ψ} V_{ψ} κ_{ψ} <	86.1 76.0		RF MI D	0.23	0.16	0.08	0.69	0.38	0.69	0.39	0.87	0.74	0.19		0.72	Vertebral Column 0.72
$\Sigma \downarrow$ $\Sigma \downarrow$ $\Gamma \downarrow$ $\Lambda \downarrow$ $\Lambda \mu$ $\Lambda \mu$ $\Lambda \mu$ L_1 Λ_{L_0} L_1 Λ_{L_1} L_1 Λ_{L_1} L_1 Λ_{L_1} L_1 Λ_{L_1} L_1 Λ_{L_1} L_1 Δ_{L_1} L_1 D_1 D_2 D_2 D_2 D_2 D_1 D_2 D_2 D_1 D_2 D_1	55.3		MLF	0.36	0.24	0.12	0.71	0.42	0.71	0.42	0.85	0.71	0.29		0.38	ethod Choice
Yet P + P + A + AW AW AW AW AU AU <th< td=""><td>94.9</td><td></td><td>RF</td><td>0.13</td><td>0.10</td><td>0.05</td><td>0.69</td><td>0.38</td><td>0.70</td><td>0.41</td><td>0.92</td><td>0.83</td><td>0.12</td><td></td><td></td><td>0.83</td></th<>	94.9		RF	0.13	0.10	0.05	0.69	0.38	0.70	0.41	0.92	0.83	0.12			0.83
$\Sigma \downarrow$ $\Sigma \downarrow$ $P \downarrow$ $\Lambda \downarrow$ ΛW ΔW <	73.8		MLF	0.41	0.27	0.13	0.64	0.29	0.65	0.29	0.78	0.56	0.32	Ĭ		Debrec. 0.49
Wey Wey Wey Wey Wey Melo	83.7		MLP	0.37	0.25	0.13	0.64	0.28	0.66	0.32	0.82	0.64	.30			0.55
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Table 2: Diversity measures and the stacking results.

However, stacking decreased the classification quality for some datasets (lines 9-17) reaching in the worst case G = -9.4%. The most frequent algorithms with best accuracy were RF (L_0) and SMO (L_1). For some datasets, more than one classifier used at level-1 returned the same result. For instance, SMO and MLP reaches equal values ($A_{L_1} = 78.8\%$) for Leaf dataset (line 9).

We have considered good values of diversity those that were sufficiently larger or smaller than the average for all 54 datasets. These values are highlighted. A general analysis of them indicates that there is more diversity in the experiments in which there was gain of stacking (lines 1-8) than in those in which there was loss of quality (lines 9-17).

Abalone dataset (line 8) had the best value of double fault df due to the low accuracy presented by the base classifiers $(A_{L_0} = 26.6\%)$. Many of them fail together because these is a multi-classification problem involving 28 distinct class labels. We notice that for this dataset, all the measures of diversity return good values, collaborating with the hypothesis that the greater the diversity, the greater the quality of stacking. However, the experiment involving Low Resolution Spectrom eter dataset (line 16) revealed the opposed behavior where the gain of stacking was negative (G = -5.6%), i.e. the quality of classification decreased considerably, even with high values for all measures of diversity. These high values are returned because there are 531 instances distributed in 48 classes, making even hard the agreement of many classifiers. Balance Scale dataset (line 1) is another counterexample in which there was no diversity among classifiers, however the stacking has reached the best G among all the performed experiments.

The impact of diversity on the gain of stacking was performed using a linear regression function and a regression model tree induced by the algorithm M5 (Quinlan, 1992). We have trained these models with only the 17 datasets present in Table 2 and considering all 54 datasets. Table 3 shows the best results comparing the evaluation of linear regression and model trees, using correlation coefficient and root relative squared error (RRSE).

Table 3: Evaluation of the regression models.

Datasets	Model	Correlation	RRSE
54	linear	0.4081	91.58%
17	M5	0.5243	79.67%

Equation 9 shows the linear model. We notice that only df and KW had impact on the gain of stacking. Other diversity measures were irrelevant in estimating the gain.

$$G = 0.0971 df + 0.3757 KW - 0.0957$$
(9)

The minimum number of instances to allow at a leaf node in M5 ranged from 2 to 4, however the result was the same tree with only one node containing the model described by Equation 10. For this model, df remains having a positive impact on the gain but the influence of ρ was negative. *KW* and other measures were not used.

$$G = 0.1278 \, df - 0.2189 \, \rho + 0.0168 \tag{10}$$

5 CONCLUSION

This paper presented an analysis of the impact of diversity on stacking multiple classifiers. The experiments we have performed show some link between the studied diversity measures and the gain of stacking considering 54 real datasets.

The regression models revealed connections between some measures and the quality of stacking. df, KW and ρ are related to the final classification accuracy, but low values of the correlation coefficients and high values of RRSE imply a weak relationship. So, as suggested by the literature for bagging and majority voting ensembles, predicting the improvement on the best individual accuracy using diversity measures is possible inappropriate.

As future work, we intend to conduct experiments with additional diversity measures and with synthetic datasets, aiming to better understand the relations between data distribution, classifiers diversity and the quality of stacking.

REFERENCES

- Afifi, A. A. and Azen, S. P. (2014). *Statistical analysis: a computer oriented approach*. Academic press, New York.
- Ali, S. and Majid, A. (2015). Can-evo-ens. Journal of Biomedical Informatics, 54(C):256–269.
- Boser, B. E., Guyon, I. M., and Vapnik, V. N. (1992). A training algorithm for optimal margin classifiers. In Proceedings of the Annual Workshop on Computational Learning Theory, pages 144–152. ACM.
- Breiman, L. (1996). Stacked regressions. Machine Learning, 24(1):49–64.
- Breiman, L. (2001). Random forests. *Machine learning*, 45(1):5–32.
- Cohen, W. W. (1995). Fast effective rule induction. In *Proceedings of the International Conference on Machine Learning*, pages 115–123.

- Cunningham, P. and Carney, J. (2000). Diversity versus quality in classification ensembles based on feature selection. In *European Conference on Machine Learning*, pages 109–116, Berlin, Heidelberg. Springer Berlin Heidelberg.
- Dietterich, T. G. (2000). An experimental comparison of three methods for constructing ensembles of decision trees: Bagging, boosting, and randomization. *Machine Learning*, 40(2):139–157.
- Dzeroski, S. and Zenko, B. (2004). Is combining classifiers with stacking better than selecting the best one? *Machine Learning*, 54(3):255–273.
- Ebrahimpour, R., Sadeghnejad, N., Amiri, A., and Moshtagh, A. (2010). Low resolution face recognition using combination of diverse classifiers. In *Proceedings of* the International Conference of Soft Computing and Pattern Recognition, pages 265–268. IEEE.
- García-Gutiérrez, J., Mateos-García, D., and Riquelme-Santos, J. (2012). Evor-stack: A label-dependent evolutive stacking on remote sensing data fusion. *Neurocomputing*, 75(1):115–122.
- Giacinto, G. and Roli, F. (2001). Design of effective neural network ensembles for image classification purposes. *Image and Vision Computing*, 19(910):699–707.
- Haykin, S. (2007). Neural Networks: A Comprehensive Foundation. Prentice-Hall, Inc., Upper Saddle River, USA.
- Ho, T. K. (1998). The random subspace method for constructing decision forests. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 20(8):832– 844.
- John, G. H. and Langley, P. (1995). Estimating continuous distributions in bayesian classifiers. In *Proceedings* of the Conference on Uncertainty in Artificial Intelligence, pages 338–345. Morgan Kaufmann Publishers Inc.
- Johnson, R. A. and Wichern, D. W. (2002). Applied multivariate statistical analysis. Prentice hall Englewood Cliffs.
- Kohavi, R., Wolpert, D. H., et al. (1996). Bias plus variance decomposition for zero-one loss functions. In *International Conference on Machine Learning*, pages 275– 83.
- Kotsiantis, S. B. and Pintelas, P. E. (2004). A hybrid decision support tool-using ensemble of classifiers. In *Proceedings of the International Conference On Enterprise Information Systems*, pages 448–453.
- Kuncheva, L. I. and Whitaker, C. J. (2003). Measures of diversity in classifier ensembles and their relationship with the ensemble accuracy. *Machine learning*, 51(2):181–207.
- Larios, N., Lin, J., Zhang, M., Lytle, D., Moldenke, A., Shapiro, L., and Dietterich, T. (2011). Stacked spatialpyramid kernel: An object-class recognition method to combine scores from random trees. In *Proceedings* of the IEEE Workshop on Applications of Computer Vision, pages 329–335. IEEE.
- Merz, C. J. (1999). Using correspondence analysis to combine classifiers. *Machine Learning*, 36(1-2):33–58.

- Ness, S. R., Theocharis, A., Tzanetakis, G., and Martins, L. G. (2009). Improving automatic music tag annotation using stacked generalization of probabilistic svm outputs. In *Proceedings of the ACM International Conference on Multimedia*, pages 705–708. ACM.
- Opitz, D. and Maclin, R. (1999). Popular ensemble methods: An empirical study. *Journal of Artificial Intelli*gence Research, 11:169–198.
- Platt, J. C. (1999). Probabilistic outputs for support vector machines and comparisons to regularized likelihood methods. In *Proceedings of the Advances in Large Margin Classifiers*. MIT Press.
- Quinlan, J. R. (1992). Learning with continuous classes. In Proceedings of the Australian Joint Conference on Artificial Intelligence, volume 92, pages 343–348, Singapore. World Scientific.
- Quinlan, J. R. (1993). C4.5: programs for machine learning. Morgan Kaufmann Publishers Inc., San Francisco, USA.
- Sneath, P. H. A. and Sokal, R. R. (1973). Numerical taxonomy. The principles and practice of numerical classification. W.H. Freeman and Company, San Francisco, USA.
- Tan, P.-N., Steinbach, M., and Kumar, V. (2005). Introduction to Data Mining. Addison-Wesley.
- Ting, K. M. and Witten, I. H. (1999). Issues in stacked generalization. *Journal of Artificial Intelligence Re*search, 10:271–289.
- Witten, I. H. and Frank, E. (2011). *Data Mining: Practical machine learning tools and techniques*. Morgan Kaufmann.
- Wolpert, D. H. (1992). Stacked generalization. Neural networks, 5(2):241–259.