# 3D RECONSTRUCTION FROM LINE DRAWINGS 

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#### Abstract

In this work we introduce an approach for reconstructing digital 3D models from multiple perspective line drawings. One major goal is to keep the required user interaction simple and at a minimum, while making no constraints to the objects shape. Such a system provides a useful extension for digitalization of paper-based styling concepts, which today is still a time consuming process. In the presented method the line drawings are first decomposed in curves assembling a network of curves. In a second step, the positions for the endpoints of the curves are determined in 3D, using multiple sketches and a virtual camera model given by the user. Then the shapes of the 3D curves between the reconstructed 3D endpoints are inferred. This leads to a network of 3D curves, which can be used for first visual evaluations in 3D. During the whole process only little user interaction is needed, which only takes place in the pre- and post-processing phases. The approach has been applied on multiple sketches and it is shown that the approach creates plausible results within reasonable timing.


## 1 INTRODUCTION

Nowadays, digital 3D models are an important element in design and engineering processes. They are used for first visual evaluations and later on they serve as basis for Digital Mock-Ups or refined CAD models. Nonetheless, in the first phase of the product development, style concepts still start with sketches on paper. The problem of transferring those concepts from paper to the digital world is not fully addressed yet. During the styling phase a lot of sketches are created from different objects and views. Though only few of them are chosen for creating digital 3D models. Creating these 3D models is complex and time consuming and therefore usually not done by the creator of the sketch himself. Especially in companies where styling is essential (e.g. in the automotive industry), specially trained CAS (Computer Aided Styling) operators create such first 3D models. Beside the effort, which is put in this step, the stylists intentions may get lost.

We present a system, which a stylist can use with little effort to create first digital 3D models based on multiple but few perspective 2D line drawings. The system tolerates imprecision in the sketchy drawings including perspective variances. To our knowledge such a system does not yet exists.


Figure 1: Our proposed approach uses line drawings like these of a couch for the reconstruction of 3D models.

That it is reasonable to constrain the sketch complexity to line drawings is showed by (Tovey et al., 2003). They decomposed sketches in their different elements (form lines, components, form-shading, non-form shading) and identified the form lines as most important for transporting an idea of a shape. Line drawings like in Figure 1 consist primarily of those lines and therefore should be adequate for inferring 3D shapes.

Even with reduced sketch complexity many challenges have to be faced:

- Working with non-predetermined views, for using sketches as they are;
- Handling perspective imprecision, because sketches from the styling phase generally lack
perspective correctness;
- Line drawings of arbitrary freeform objects give little geometric cues about shape;
- Little and simple user interaction, so the system is useable by non experts with little effort;
- Handling ambiguity, which arise when inferring 3D information from 2D.


## 2 RELATED WORK

Extensive research is done in imitating sketching processes to interactively create 3D models. A comprehensive overview and taxonomy of interactive sketchbased modeling is given in (Olsen et al., 2008) and (Olsen et al., 2009). These methods are excellent for creating 3D models in an easy an intuitively way, but they seldom address the use of prior created hand drawn sketches.

Dealing with this (Kara et al., 2006) presented an interactive method for transferring the shape information from a sketch to a template model. For this purpose a scanned image of a sketch from a nonpredetermined viewpoint is used. The Template is then aligned with this image in an easy way by interactively drawing the virtual bounding box of the object. While redrawing the form lines of the sketch, the shape is transferred onto the 3D template. In a newer work Kara and Shimada (Kara and Shimada, 2008) use fiducial points for aligning the template with the sketch and for template deformation. Those fiducial points are given by the user for the sketch and correspond to fiducial nodes of the template. The above mentioned approaches have the benefit, that the user does most of the interpretation and filtering of the strokes in the sketches. So the approach itself does not need to cope with the heterogeneity of the input sketches. While this is a promising and applicable approach, in the end the user redraws his sketch.

In contrast more direct reconstruction need to cope with the heterogeneity of input sketches and 3D models. This often results in making restrictions to sketches and 3D models. One of the first work, which engages the direct reconstruction from a line sketch was by Lipson and Shpitalni (Lipson and Shpitalni, 1996). In their paper they present a method for reconstructing a polyhedron from one orthographic line drawing. The approach used geometric information like parallelism and orthogonality of lines in the sketches. This method is restricted to polyhedra and does not support curved elements. (Varley et al., 2004) propose a two stage approach where, the user is asked to create a drawing of a curved object
and a corresponding polyhedron. In the first stage the polyhedron is reconstructed and serves as template. In the second stage the edges and surface are deformed to match the drawing of the curved object, so that a curved object is reconstructed. A method for elements with planar curves is presented in (Masry and Lipson, 2005). In this paper first the depths of the vertices from the line drawing are determined by checking the consistency with an underlying orthogonal axis system. Planar curves are then reconstructed by determining their plane equation by using an optimization function. According to the authors this algorithm performs best on sketches that exhibit strong orthogonal trends. Opposite to our approach, where we not rely on orthogonality and aim for the reconstruction of non-planar curves.

While the previous works used single views there also exist approaches working with multiple sketches. (Wang and Latif, 2003) proposed a method for inferring a solid 3D model from engineering drawings, therefore extruding 3D objects from the 2D sketches and combining them using constructive solid geometry methods. Their approach is restricted to the orthographic front, side and top views. Zhang et al. cover in (Zhang et al., 2004) the reconstruction of a wireframe model consisting of conic curves. In their work the views are restricted to the same three main views. In contrast, we use perspective sketches from arbitrary viewpoints.

Even though many different approaches for interpreting drawn sketches exist, to our knowledge, no approach for reconstructing a 3D model, consisting of curves, using perspective sketches with little user interaction, has been presented so far.

## 3 OUR PROPOSED METHOD

We divide the reconstruction process into three main stages (see also Figure 2). These stages will be covered more detailed in the following section.

The first stage is vectorization. In this stage we convert the raster image to a suitable 2D representation of the sketch, which then will be used for the reconstruction. In this vectorization stage we convert off-line scanned images into a network of 2D curves, which are linear approximated. We use a rather simple vectorization algorithm, because we support only line drawings. The vectorization stage is covered in Section 4.

The second one is the actual 3D reconstruction process where the 2 D information from multiple sketches is combined to infer a 3D wireframe model. To receive a transformation from 2D sketch space to


Figure 2: Our proposed algorithm is divided in three main stages.

3D object space we utilize a virtual camera model. Then we determine the 3D positions to the endpoints of the curves resulting from the vectorization. For the transfer to 3D we are using the estimated projection matrix from the camera model and the connectivity information of the 2D network. In the following step we deform the edges in 3D to the shape inferred from their correspondent 2D curves. For this purpose we divide the edge in 3D in a set of linear segments. The forming is done by extruding the 2D curves into 3D space, thus creating a surface on which the edge is fitted. Details are covered in Section 5.

The last stage is the post-process where the model is visualized. The user has the possibility to modify the model. Because we only reconstruct the visible side of an object, the user can define a mirror plane to extend symmetric objects. This is outlined in Section 6.

## 4 VECTORIZATION

To get a suitable representation, the sketch is vectorized to a network of linear line segments (Figure 3). This will be converted into a network of curves, where the crossings of the drawn lines are the nodes and the drawn lines the curves.


Figure 3: On the left: The vectorization result of the left sketch from Figure 1. The drawn curves are approximated polygonally. On the right: The 2D nodes from the network of curves.

The vectorization algorithm we use is intended for grayscale line drawings with roughly uniform line thickness and without shading, like the two examples shown in Figure 1. This is done with the following image processing methods:

- First the image is converted to in a binary image using an adaptive threshold algorithm, dividing the raster image in foreground and background.
- With the morphological erosion operation we remove small artifacts created through the scanning and binarization process. With the dilation operation we close gaps between strokes.
- In a last step of morphological operations the drawing is skeletonized. This means the lines are thinned to a minimum while keeping the end points.
- The skeleton, which results is now segmented in polylines approximating the drawn curve.
- In the final step we simplify the mesh by removing small dangling edges.
The vertices of the vectorization with a valency higher or equal than three are considered as endpoints of the curves. The path between two of these endpoints consist of linear edges and approximates the drawn line polygonally. An example is shown in Figure 3. After this step the user can insert new nodes and so additionally divide the curve. This is a useful function, because in the following reconstruction
stage we receive better results when the topologies of the networks of curves are similar.


## 5 3D RECONSTRUCTION

In the reconstruction stage we use multiple networks of curves from the multiple sketches, for inferring a network of 3D curves. This is done in three steps, explained in the following sections.

### 5.1 Calibrating a Virtual Camera

For the calibration of a virtual camera model we proceed like previously described by Kara et al. in (Kara et al., 2006). We first need a set of pairs (at least 6) of correlating 2D and 3D points. These points we get by letting the user draw the projection of a virtual bounding box into the sketch (see Figure 4). With the eight corner points of the bounding box and the approximate dimensions of the object (also given by the user). We calculate an estimated projection matrix from 3D to 2D, their inverse and the position of the virtual camera.


Figure 4: This figure shows a bounding box given by a user the corners of this box are used to calibrate a virtual camera.

### 5.2 Reconstruction of Nodes in 3D

In this step we aim to reconstruct points in 3D, which serve later as nodes of a network of 3D curves.

First we generate candidate nodes. A candidate node is a node in 3D, which has the chance to become the reconstruction of a 2D node. For the construction of those candidates, we divide the 3D space into a voxelgrid. For each voxel of that grid, we calclulate the 2 D projection in the several sketches and determine the nearest 2D node. These 2D nodes are saved on the voxel as witnesses, which means that this 2D node could support the creation of a 3D node in this voxel. After this we examine the voxels with two or more witnesses. This implies that our algorithm needs object nodes to be visible in more than one sketch.


Figure 5: This picture shows the 3D candidate nodes generated from the two sketches shown in Figure 1. The edges visualize the candidates connectivity inferred from the networks of 2D curves.

Observing the voxelspace, we now see that clouds of voxels have evolved. These voxel clouds contain voxels which share the same set of witnesses. They are compressed to their center creating a point in 3D. This point is candidate to be the 3D representative of its witnesses and so a candidate to be a 3D node of the reconstruction. In Figure 5 we see the resulting candidate nodes. An edge between two candidates indicates that those two nodes have witnesses, which are connected by a drawn curve in a sketch.

To filter the candidate nodes, we make use of the connectivity information in the network of 2D curves. The candidates are added to the resulting 3D network by a greedy algorithm, which adds the nodes by a rating. The rating we applied here, reflects how well a candidate is connected in the 3D network. Therefore, we calculate the sums of lengths of all paths, which starts at the 3D candidate node. These paths travel over the neighbor candidates, while only using candidates with at least two witnesses, which were not witnesses of candidates prior on the path. Is a candidate added to the 3D network, its witnesses are removed from the witness list of the remaining candidates. Therefore it is necessary to recalculate the rating after each addition of a candidate to the 3D network.

This approach guaranties that a 3D node has only one 2 D representative per sketch and a 2 D node has only one 3 D representative. So we resolved the ambiguity by using the heuristic of connectivity of the 2D nodes. Now, we have a 3D wireframe model with linear edges. The next step is to reconstruct the shape information for these edges.

### 5.3 Shape Reconstruction

The main idea behind the shape reconstruction step is to deform the edges in 3D in such a way that they conform to the 2D sketch.


Figure 6: The candidate nodes are now filtered and only the edges between the resulting 3D nodes remain. The candidates in the picture which are not connected to the network are those which are discarded.

First we generate a 3D curve for each reconstructed edge in 3D. Polylines serve as approximation for the 3D curves. They are created by dividing an edge in equally spaced linear segments.

We transfer the 2D shape information to 3D by extruding a surface from the corresponding 2 D curve. We know the corresponding 2D curves for each 3D curve from the reconstruction step of the 3D Nodes. For extruding the surface we use the inverse of the projection matrix from Section 5.1. With this matrix we determine the rays from the virtual camera center through the vertices of the 2D curve. These rays fan the surface, like in Figure 7.

Then we deform the 3D curve by projecting the vertices of the 3D curve onto this surface. For this purpose we calculate for each 3D vertex a corresponding interval on the 2D curve. Then the vertex is moved to its nearest point on the part of the surface created by the determined interval. This will allow us to adapt extreme curves.


Figure 7: The extrusion of a 2D curve leads to a surface, which is used for shaping the 3D curve.

Since we are working with multiple sketches more than one corresponding curve exists. It seems sug-


Figure 8: An example for reconstructed 3D shape information is shown. The marked curves will be deleted by the user when he mirrors the object in the post-processing step (see Section 6).
gestive to use the shape information of at least two curves. This resolves ambiguity, because the 3D curve is then well defined by the intersection of two extruded surfaces. We have implemented it by minimizing the distance of the 3D curve vertices to two extruded surfaces. However, when the surfaces are nearly parallel, the intersection prone to big deviations in view direction. This is intensified by the inaccuracy in the sketch and can lead to implausible curves. In these cases best results were achieved by using only one 2D curve. For this purpose, we want to select the 2D curve which might give the best result. So we use the longest 2D curve, under the assumption that it contains better shape information than a shorter one.

At this point we have a network of 3D curves like the one showed in Figure 8.

## 6 POST-PROCESSING

The received 3D model from the previous section can now be evaluated by the user. Many designed objects are symmetric. Therefore, it seems sensible to give the user at least the ability to extend the model by adding the mirrored result. This gives the user a more complete impression of the object. However, it can lead to double curves, where curves are visible two times in the sketch (e.g. on the near and the far side of the object), like those marked in Figure 8. Some doubled curves may be unwanted, stemming from imprecision or misinterpretation in the reconstruction. The user has the possibilty to remove such curves at will.


Figure 9: Result "Spiral" a) Two line drawings of a 3D spiral on the left. One from top view the other from side view. b) The reconstructed spiral in two views on the right. This shows that our method can reconstruct complex curves.


Figure 10: Result "Car" a) Two line drawings of a car on top. b) On the left: The resulting 3D model with all reconstructed and deformed edges. c) Second from left: the model without manually deleted edges as preparation for the mirroring. d) Second from right: The side view on the model. e) On the right: A mirror plane was defined to extend the model.


Figure 11: Two views of the final result from the two sketches shown in Figure 1 for the couch example.

## 7 RESULTS

We show the implementation results on sketches of three different objects in Figures 11-10.

The couch example (result in Figure 11) accompanied us throughout the paper. It is a good example for sketches that lack perspective precision. It also contains a drawn line which is not connected to the rest of the model but nonetheless has a plausible reconstruction. This example was mirrored in the postprocess and three curves (those marked in Figure 8) were removed. In the pre-processing step four 2D nodes where inserted in each sketch.

Another example - a sketch of a spiral (see Figure
9) - shows that our method is able to reconstruct nonplanar curves. This is true as long as the drawn curve is not self-intersecting. On self-intersecting curves our vectorization algorithm creates a 2D node which makes a reconstruction more difficult.

The reconstruction of a complex model is shown by an example of a car (see Figure 10). Here the user inserted 2D nodes on the contour leading to a more suitable segmentation of the curve. Furthermore in the post-processing step the user has removed the edges on the farther side of the symmetry plane and mirrored the object.

The reconstruction stage took for all models only few (2-5) seconds on a stand-alone PC, without the time needed for camera calibration. The time needed for interaction varied from 2 minutes (spiral, couch) to 5 minutes (car). These durations cover all the interaction (camera calibration, insertion of 2D nodes, mirroring, removing 3 D curves). We believe that these timings are fast enough to justify further exploration of the approach in a productive styling environment. An obvious next step is to add surface reconstruction out of the 3D curves e.g. through Coons patches.

## 8 CONCLUSIONS AND FUTURE WORK

We have shown an approach for reconstructing a 3D model existing of curves from multiple but few sketches. Only little user interaction is needed and takes place in a pre- and post-processing step. In the automated reconstruction process, we assume that parts of an object, which should be reconstructed, are present in at least two views with the same level of detail. The sketches used, are perspective and show the object from different not predetermined viewpoints. Here the chosen voxel-based approach allows us to handle perspective imprecision of the sketches to a certain degree. With such features this method could be part of a system to evaluate first styling concepts.

However we want to do more evaluations of the system with regard to user effort and robustness. A further object of special attention is handling silhouette lines. Silhouettes in sketches convey important shape information. However the handling is difficult, because they are varying from view to view. Another focus of our future work is to utilize robust vectorization approaches like (Hilaire and Tombre, 2006) so we can use sketches containing more complex-tohandle content such as shading.

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