

Performance Guarantee in a New Hybrid Push-Pull Scheduling Algorithm

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Abstract. The rapid growth of web services has already given birth to a set of data dissemination applications. Efficient scheduling techniques are necessary to endow such applications with advanced data processing capability. In this paper we have effectively combined broadcasting of very popular (push) data and dissemination of less popular (pull) data to develop a new hybrid scheduling scheme. The separation between the push and the pull data is called *cut-off point*. The clients send their request to the server, which ignores the request for the push items but queues the requests for the pull items. At every instance of time, the item to be broadcast is designated by applying a pure-push scheduling. On the other hand, the item to be pulled is the one stored in the pull-queue having the highest number of pending requests. Fixed a value for the cut-off point, an analytic model, validated by simulation, evaluates the average system performance. On the top of that, the major novelty of our system lies in its capability of offering a performance guarantee to the clients. For each request, the client specifies, along with the data item requested, the maximum interval of time it can afford to wait before its request will be served. Based on this particular access-time and on the analytic model, our hybrid system computes the cut-off point to fulfill the specific need of the client. The system offers a great flexibility for clients. It improves significantly upon a pure push system and some existing hybrid systems in terms of average waiting time spent by a client.

1 Introduction

Over the past few years, the overwhelming growth of web services has resulted in the emergence of applications capable of storing and processing a huge set of information. The prime objective of such *data dissemination* applications lies in delivering the data to a very large population of clients with minimum delay. Broadly, all data dissemination applications have two flavors: in a *push-based system* the clients continuously monitor a broadcast process from the server and obtain the data items they require, *without making any requests*; on the contrary, in a *pull-based system*, the clients initiate the data transfer by sending requests *on demand*, and the server then makes a schedule to satisfy these requests. Both push- and pull-based scheduling have their own advantages and disadvantages. However, neither push nor pull based scheduling alone can achieve

the optimal performance [3], [9]. A better performance could only be achieved when the two scheduling approaches are combined in an efficient manner.

In this paper, a new, hybrid scheduling is proposed that effectively combines broadcasting of more popular (push) data and dissemination upon-request for less popular (pull) data. The clients send their requests to the server, which queues them up for the pull items. The server continuously broadcasts one push item and disseminates one pull item. At any instance of time, the item to be broadcast is selected by applying a pure-push scheduling, while the item to be pulled is the one in the pull-queue having the maximum number of requests. The cut-off point, that is the separation between the push and the pull items, is determined in such a way that the clients are served before the deadline specified at the time of the request. In other words, the major novelty of our system lies in its capability of offering a performance guarantee to the clients.

Organization of the paper: The rest of the paper is organized as follows: Section 2 reviews related works and subsequently highlights the motivations behind using our new hybrid algorithm. Section 3 presents our basic algorithm and shows by a suitable queueing model how to evaluate the system performance, that is the average waiting time expected in the system, when the value K of the cut-off point is known. Subsequently, simulation results of the system behavior are discussed briefly. Then, in Section 4, the complete version of our new algorithm with performance guaranteed is discussed. Finally, Section 5 concludes the paper by summarizing our work and offers future directions of research.

2 Related Work and Motivations

As discussed earlier, scheduling algorithms can be broadly classified into push and pull based techniques. Given the wide variety of such push and pull based techniques we only highlight the major schemes here. The optimal expected access time is achieved when items are equally spaced [12]. The concept of fair channel utilization [6] and efficiency of Packet Fair Scheduling [10], [11] is also investigated. In order to get rid of fixed access frequencies and number of broadcast channels [14], different heuristics are also proposed in [15] to solve the NP-complete problem of dynamic broadcast channels. On the other hand, many preemptive and non-preemptive pull-based algorithms like First Come First Served (FCFS), Most Requests First (MRF) [13] and $R \times W$ algorithm [4] exist in literature. While MRF provides optimal waiting time for popular set of items, it suffers from un-fairness. FCFS on the other hand is fair, but suffers from sub-optimality and *convoy effect*. A combination of these two [4] often provides an acceptable solution.

Hybrid approaches, that use the flavors of both push-based and the pull-based scheduling algorithms in one system, appears to be more attractive. In [3], the server pushes all the data items according to some push-based scheduling, but simultaneously the clients are provided with a limited back channel capacity to make requests for the items. A model for assigning the bandwidth to the push- and pull-scheduling in an adaptive way is proposed in [16]. A hybrid approach is also discussed in [9], which divides the data items in disjoint push and pull sets, according to their degree of access probability. The server broadcasts the push items, pre-computed by the Packet Fair Queuing scheduling,

and sends the pull item based on FCFS scheduling discipline, in a reciprocal way. Indeed, let the *push-set* consist of the data items numbered from 1 up to K (*cut-off point*), and let the remaining items from $K + 1$ up to D form the *pull set*. Hence, the average expected waiting time for the hybrid scheduling is defined as:

$$T_{exp-hyb} = T_{exp-acc} + T_{exp-res} = \sum_{i=1}^K P_i \cdot \overline{T_{acc,i}} + \sum_{i=K+1}^D P_i \cdot \overline{T_{res,i}}.$$

where: $T_{exp-acc}$ is the expected access time for the push-set, $T_{exp-res}$ is the expected response time for the pull-set, P_i is the access probability of item i . As the push-set becomes smaller, the $T_{exp-acc}$ becomes shorter, but the pull-set becomes larger, leading to a longer $T_{exp-res}$. The size of the pull-set might also increase the average access time $\overline{T_{acc,i}}$, for every push item. After having found the minimum number B , called *build-up point*, of items to be pushed so that the length of the pull queue in the system is in average bounded by a constant, [9] chooses, as the cut-off point, the value K such that $K \geq B$ and K minimizes the *average* expected waiting time for the hybrid system. However, when either the system has a high load, i.e. a high number of requests for unit of time, and/or all items have almost the same degree of probability, the distinction between the high and low demand items becomes vague, artificial, hence the value of build-up point B increases, finally leading to the maximum number D of items in the system. Thus, in those cases, the solution proposed in [9] almost always boils down to a pure push-based system. This motivates us to develop a more efficient algorithm capable of improving the access time even in high load with items having same degree of probability.

Our proposed solution partitions the data items in the push-set and the pull-set, but it chooses the value of the cut-off point K between those two sets independent of the build-up point. After each single broadcast, we do not flush out the pull-queue as in [9]. In contrast, we just pull one single item: the item, which has the largest number of pending requests. Note that simultaneously with every push and pull, N more access / requests arrive to the server, thus the pull-queue grows up drastically at the beginning. In particular, if the pull-set consists of the items from $K + 1$ up to D , at most $N \times \sum_{j=K+1}^D P_j$ requests can be inserted in the pull-queue at every instance of time, out of which, only one, the pull item that has accumulated the largest number of requests, is extracted from the queue to be pulled. However the number of distinct items in pull-queue cannot grow uncontrolled as it will be shown by the analytic model in the next section. Once that the analytic model has been devised, we take advantage from it to make our system more flexible. Indeed, since by the analytic model the system performance is already known with a good precision, it is possible to decide in advance if the value of K currently in use at the server will satisfy the client request on time. If not, K is updated in a suitable way again looking at the system performance analysis.

3 Basic Hybrid Algorithm: Performance Modelling, Simulation Framework

The basic hybrid algorithm assumes that the value K of the cut-off point is given and that the client makes a data request without any deadline. Then, the items from 1 to

K are pushed according to Packet Fair Scheduling algorithm and the remaining items from $K + 1$ to D are pulled according to Most Request First (MRF) algorithm. The server listens to all the requests of the clients and manages the pull-queue. The pull-queue, implemented by a max-heap, keeps in its root, at any instant of time, the item with the highest number of pending requests. For any request i , if i is larger than the current cut-off point K , i.e. $i > K$, it is inserted in the pull-queue, the number of the pending requests for i increased by one, and the heap information updates accordingly. Vice versa, if i is smaller than or equal to K , i.e., $i \leq K$, the server simply drops the request because that item will be broadcast by the push-scheduling. The scheduling is derived as explained in Figure 1, where the details for obtaining the push scheduling are omitted. The interested reader can find them, for example, in [7]. To retrieve a data item, a client performs the actions as illustrated in Figure 2. Note that the behavior of client is independent of the fact that the requested item belongs to the push-set or to the pull-set.

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Procedure HYBRID SCHEDULING;
while (true) do
begin
  obtain an item from the push scheduling;
  broadcast this item;
  if the pull-queue (is not empty) then
    extract the most requested item;
    clear the requests pending for it;
    pull this item;
  end-if
end;

```

Fig. 1. Hybrid Scheduling at the Server

In the remaining of this section, we investigate into the performance evaluation of our basic hybrid scheduling system by developing suitable analytical models. Subsequently, we also validate this performance analysis by developing a simulation framework and performing simulation experiments. Before going into the details of analytical underpinnings, we explicitly state the underlying assumptions in our framework.

1. The arrival rate in the entire system is assumed to obey Poisson distribution with mean λ_1 .
2. The service times of both the push and pull systems are exponentially distributed with mean μ_1 and μ_2 , respectively.
3. The server pushes K items and clients pull the rest $(D - K)$ items. Thus, the total probability of items in push-set and pull-set are respectively given by $\sum_{i=1}^K P_i$ and $\sum_{i=K+1}^D P_i = (1 - \sum_{i=1}^K P_i)$, where P_i denotes the access probability of item

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Procedure CLIENT-REQUEST ( $i$ ):
/*  $i$  : client's required item */
begin
  send to the server the request
  for item  $i$ ;
  repeat
    wait;
  until (listen  $i$  on channel)
end

```

Fig. 2. Algorithm at the Client Side

i . We have assumed that the access probabilities P_i follow the *Zipf's distribution* with *access skew-coefficient* θ , such that, $P_i = \frac{(1/i)^\theta}{\sum_{j=1}^n (1/j)^\theta}$.

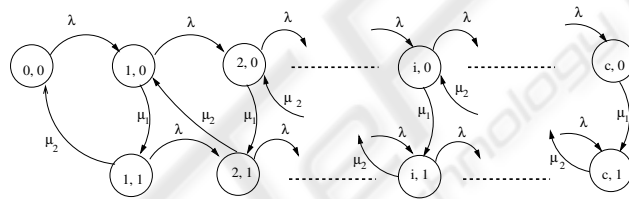


Fig. 3. Performance Modelling of Hybrid System

Figure 3 illustrates the underlying birth and death process of our system, where the arrival rate in the pull-system is given by $\lambda = (1 - \sum_{i=1}^K P_i) \lambda_1$. Any state of the overall system is represented by the tuple (i, j) , where i represents the number of items in the pull-system. On the other hand, j is a binary variable, with $j = 0$ (or 1) respectively representing whether the push-system (or pull-system) is currently being served by the server. Naturally, both the arrival of the data items and their service are responsible for the dynamics associated with the state transitions in the system. One major goal of this performance analysis is to capture this system dynamics. This will lead to get an expected, overall estimate of the system performance. We now enumerate these system dynamics resulting from arrival and service of data items.

1. The arrival of a data item in the pull-system, results in the transition from state (i, j) to state $(i + 1, j)$, $\forall i$, such that $0 \leq i < \infty$ and $\forall j \in [0, 1]$.
2. The service results in two different actions. Since, the push system is governed by Packet Fair Queuein Scheduling, the service of an item in the push-queue results in transition of the system from state $(i, j = 0)$ to state $(i, j = 1)$, $\forall i$ such that $0 \leq$

- $i < \infty$. On the other hand, the service of an item in the pull results in transition of the system from state $(i, j = 1)$ to the state $(i - 1, j = 0)$, $\forall i$, such that $1 \leq i < \infty$.
3. The state of the system at $(i = 0, j = 0)$ represents that the pull-queue is empty and any subsequent service of the elements of push system leaves the system in the same $(0, 0)$ state.
 4. Obviously, the state $(i = 0, j = 1)$ is not valid because the service of an empty pull-queue is not possible.

As the system reaches the steady-state, the total flow needs to be conserved. The overall behavior of the system for both push (upper chain) and pull part (lower chain) can now be estimated from *Chapman-Kolmogorov's* general equation [8]. The steady-state equations representing the push and pull parts of the system is given below:

$$p(i, 0)(\lambda + \mu_1) = p(i - 1, 0)\lambda + p(i + 1, 1)\mu_2 \quad (1)$$

$$p(i, 1)(\lambda + \mu_2) = p(i, 0)\mu_1 + p(i - 1, 1)\lambda, \quad (2)$$

where $p(i, j)$ represents the probability of state (i, j) . However, since the state $(0, 1)$ is invalid and any service from state $(0, 0)$ leaves the system in same state, the initial condition of the system is represented by:

$$p(0, 0) \lambda = p(1, 1) \mu_2. \quad (3)$$

The most efficient way to solve Equations (1) and (2) is using *z-transforms* [8]. From the definition of *z-transforms*, the resulting solutions will be of the form: $P_1(z) = \sum_{i=0}^{\infty} p(i, 0) z^i$ and $P_2(z) = \sum_{i=0}^{\infty} p(i, 1) z^i$. Hence, dividing both sides of Equation (1) by μ_2 , letting $\rho = \frac{\lambda}{\mu_2}$, $f = \frac{\mu_1}{\mu_2}$, and performing subsequent *z-transforms*, we get,

$$\begin{aligned} P_2(z) &= p(1, 1) + z(\rho + f)[P_1(z) - p(0, 0)] - \rho z^2 P_1(z) \\ &= \rho p(0, 0) + z(\rho + f)[P_1(z) - p(0, 0)] - \rho z^2 P_1(z), \text{ [using Equation (3)]} \end{aligned} \quad (4)$$

Now, investigating the system behavior at the initial conditions, we can derive the following two normalization criteria:

1. The occupancy of pull states is the total traffic of pull queue. This occupancy is given by:
 $P_2(1) = \sum_{i=1}^{\infty} p(i, 1) = \rho$.
2. The occupancy of the push states (upper chain) is similarly estimated by:
 $P_1(1) = \sum_{i=1}^{\infty} p(i, 0) = (1 - \rho)$.

These above two relations can be used in Equation (4), to obtain the idle probability, $p(0, 0)$:

$$\begin{aligned} P_2(1) &= \rho p(0, 0) + (\rho + f)[P_1(1) - p(0, 0)] - \rho P_1(1) \\ \rho &= f(1 - \rho) - f p(0, 0), \text{ (using values of } P_1(1) \text{ and } P_2(1)) \\ p(0, 0) &= 1 - \rho - \frac{\rho}{f} \end{aligned} \quad (5)$$

Generalized solution of Equation (4) to obtain all values of probabilities $p(i, j)$ become very complicated. Thus, the most efficient way is to go for an expected measure

of system performance, such as the average number of elements in the system and average waiting time. This expected system performance can be conveniently obtained by differentiating the z -transformed variables, $P_1(z)$ and $P_2(z)$ and capture their values at $z = 1$. Proceeding in this way and differentiating both sides of Equation (4) with respect to z at $z = 1$, we get an estimate of the expected number of elements in the pull-system ($E[\mathcal{L}_{pull}]$) as follows:

$$\frac{dP_2(z)}{dZ}\Big|_{z=1} = (\rho + f) \frac{dP_1(z)}{dZ}\Big|_{z=1} + P_1(1) (f - \rho) - p(0,0) (\rho + f) - \rho \frac{dP_1(z)}{dZ}\Big|_{z=1} \quad (6)$$

$$\begin{aligned} E[\mathcal{L}_{pull}] &= (\rho + f) E[\mathcal{L}_{push}] + (1 - \rho) - (\rho + f)(1 - \rho - \frac{\rho}{f}) - \rho E[\mathcal{L}_{push}] \\ &= \frac{\mu_1}{\mu_2} \sum_{i=1}^K S_i \hat{P}_i + \left(1 - \frac{\lambda}{\mu_2}\right) - \left(\frac{\lambda + \mu_1}{\mu_2}\right) \left(1 - \frac{\lambda}{\mu_2} - \frac{\lambda}{\mu_2}\right), \text{ (as } E[\mathcal{L}_{push}] = \\ &\sum_{i=1}^K S_i \hat{P}_i) \end{aligned} \quad (7)$$

where $E[\mathcal{L}_{push}]$ denote the the expected system performance for the push part, and where, according to the Packet Fair Queueing Scheduling, S_i is the space between two instances of the same data item i defined as $S_i = \frac{\sum_{j=1}^K \sqrt{\hat{P}_j}}{\sqrt{\hat{P}_i}}$ and $\hat{P}_i = \frac{P_i}{\sum_{j=1}^K P_j}$. Once, we have the expected number of items in the pull system from Equation (6), using Little's formula [8], we can easily obtain the estimates of average waiting time of the system ($E[W_{pull}]$), average waiting time of the pull queue ($E[W_{pull}^q]$) and expected number of items ($E[\mathcal{L}_{pull}^q]$) in the pull queue as:

$$E[W_{pull}] = \frac{E[\mathcal{L}_{pull}]}{\lambda}; \quad E[W_{pull}^q] = E[W_{pull}] - \frac{1}{\mu_2}; \quad E[\mathcal{L}_{pull}^q] = E[\mathcal{L}_{pull}] - \frac{\lambda}{\mu_2} \quad (8)$$

In conclusion, the expected access-time ($E[T_{hyb-acc}]$) of our hybrid system is given by:

$$E[T_{hyb-acc}] = \sum_{i=1}^K S_i \hat{P}_i + E[W_{pull}^q] \times \sum_{i=k+1}^D P_i \quad (9)$$

The expressions provided in Equations (6), (8) and (9) provide an estimate of the average behavior of our hybrid system when the cut-off assume the value of K .

In order to validate the performance analysis, we have compared our analytical results, obtained from plotting the numerical values of Equation (9), with the simulation results assuming $D = 100$, $\lambda_1 = 10$ (analytic), $N = 10$ (experimental), $0.50 \leq \theta \leq 1.30$ in correspondance of the value of K which minimize the expected waiting time in our experiments. The value of μ_1 and μ_2 are estimated as $\mu_1 = \sum_{i=1}^K P_i$ and $\mu_2 = \sum_{i=K+1}^D P_i$. Figure 4 demonstrates analytical results closely follow the simulation results with a deviation of 15%-20%.

Moreover, Figure 5 illustrates, by experimental results, the dynamism of expected access-time with variation of θ for $N = 10$ and $D = 100$. The access-times for different values of θ have a similar trend and decreases for a cut-off point in the range $K \in [0, 35]$. The curves remains almost flat in the region $35 \leq K \leq 50$. This points out a

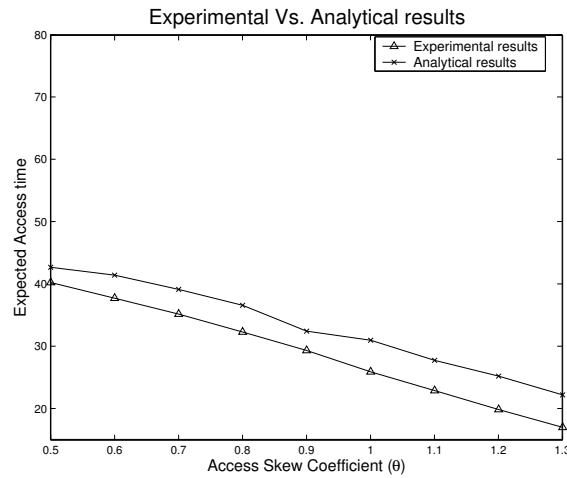


Fig. 4. Comparison of Experimental and Analytical Performances

fair and optimal mix of push and pull scheduling. Then the expected access-time start increasing again.

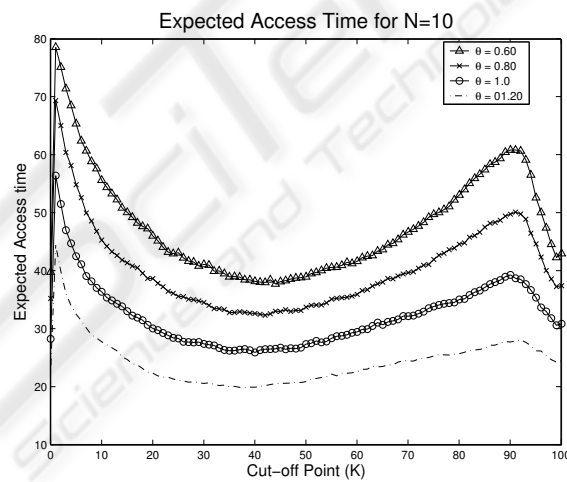


Fig. 5. Expected Access Time for $N = 10$ and $D = 100$

Simulation experiments are also performed to compare our hybrid scheduling scheme with previous existing scheduling algorithms. We have chosen our previous hybrid scheduling algorithm [9], and pure-push scheduling algorithm as performance benchmarks of our new scheduling algorithm. The simulation experiments are evaluated for

$D = 100$, for $N = 10$ and $N = 20$. and for θ varying from 0.50 to 1.30. The results are reported in Table 1 and 2, respectively for $N = 10$ and $N = 20$.

Figures 6 and 7 (B) show the results of performance comparison between our new algorithm with that of pure-push scheduling and the comparison of the cut-off point between the new algorithm and [9] when K is selected so that the average waiting time is minimized. Both of these figures reveal that our basic new algorithm achieves an improvement over our existing strategy and over the existing pure-push system. As earlier discussed, when the system is highly loaded, the scheduling algorithm in [9], whose cut-off point K must be larger than the build-up point B , almost reduces to the pure-push scheduling. Contradictory to [9], the new basic hybrid algorithm, even with very high loaded system, experiments better results than a pure-push based system as illustrated in Figure 6. Besides, in Figure 7, the values of the cut-off point K for which the access waiting time of the system is minimal for the basic hybrid algorithm, and for the hybrid scheduling proposed in [9] are depicted for $N = 10$ and $N = 20$.

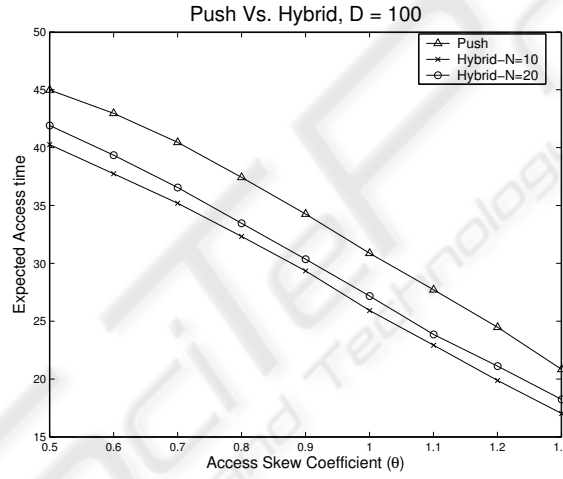


Fig. 6. Pure-Push Scheduling Vs New Algorithm

Table 1. $T_{exp-hyb}$ for different values of θ (in columns) and different algorithms when $N = 10$

	0.50	0.60	0.70	0.80	0.90	1.00	1.10	1.20	1.30
New	40.30	37.78	35.23	32.36	29.38	25.95	22.95	19.90	17.04
[9]	44.54	42.35	40.01	37.31	34.12	29.93	24.38	20.61	17.04
Push	45.03	43.01	40.50	37.47	34.30	30.90	27.75	24.50	20.86

Table 2. $T_{exp-hyb}$ for different values of θ (in columns) and different algorithms when $N = 20$

	0.50	0.60	0.70	0.80	0.90	1.00	1.10	1.20	1.30
New	41.96	39.39	36.59	33.49	30.39	27.20	23.88	21.14	18.26
[9]	44.44	42.45	40.10	37.39	33.78	30.69	27.54	23.23	19.49
Push	44.70	42.61	40.30	37.65	34.12	30.78	27.71	23.94	21.07

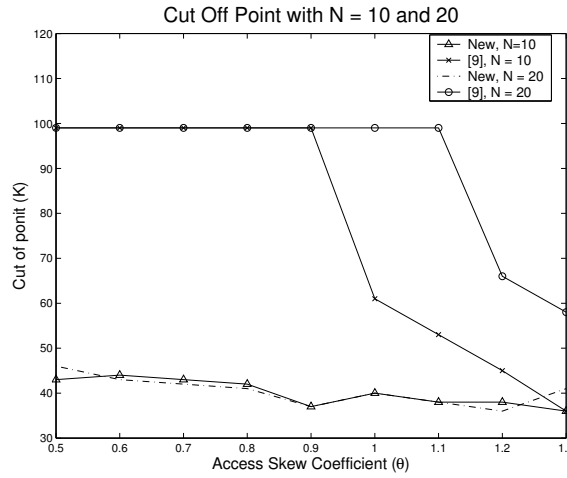


Fig. 7. Cut-Off Point when $N = 10, 20$.

4 New Hybrid Scheduling Algorithm

While the performance evaluation of our new basic hybrid scheduling algorithm has already pointed out its significant gains in both response time and minimizing the value of the cut-off point when compared to existing algorithms and pure push-based scheduling, we now proceed to mention the complete version of our new algorithm with performance guaranteed quality that our new scheduling scheme is capable to offer. Such performance guarantee is required to deliver, for example, the wireless voice and data packets within a precise time-frame of service, thereby ensuring a certain level of quality-of-service (QoS).

Essentially for all D possible values of the cut-off point, the server computes the expected hybrid waiting time $E[T_{hyb-access}]$ using the Equation (9) in Section 3. From now on, let $E[T_{hyb-access}(i)]$ denote such expected hybrid waiting time when i is the cut-off point value. These D expected waiting times are stored, one-at-a time along with the index of the cut-off point that generates it, sequentially in a vector V . That is, for all $1 \leq i \leq D$, $V[i, 1] = [E[T_{hyb-access}(i)]$ and $V[i, 2] = i]$. Moreover V is maintained sorted with respect to the first component, i.e. the expected hybrid waiting time. With this structure, the server can extract the first element $V[0]$ of this vector in a single access, which will indicate in correspondence of which value K_0 of the cut-off point the minimum expected hybrid waiting time $V[0, 1] = E[T_{hyb-access}(K_0)]$ is achieved. The server broadcasts $V[0]$ from time to time, thereby informing the clients of the best performance it can provide. Moreover, the server continuously broadcasts the basic hybrid scheduling that corresponds to the cut-off point K in use we discussed in previous section. On the other side, when a client sends a request for any item j , it also specifies an expectation $\Delta(j)$ of its possible waiting time for item j . Indeed, $\Delta(j)$

reflects the nature of the application, and the tolerance of the client. For example, a client requesting for any real-time video application, will expect a time much lower than any client requesting data service-specific applications. Moreover, an impatient client could ask that its request is served in a time much lower than its moderate counterparts.

In order to accept a client request for item j with expectation $\Delta(j)$, the server estimates the expected waiting time for j at this current time instant using the values stored in vector \mathbf{V} and the knowledge of the current cut-off point K in use for the hybrid scheduling algorithm broadcasted by the server. If the expected hybrid waiting time provided by the system is smaller or equal to the expectation time of the client's request, then the certain level of QoS expected by the client is guaranteed. Otherwise, the server checks whether the item j belongs to its current push set, that is if $j \leq K$. If this is true, it compares the client request deadline with the expected waiting time guaranteed by the Packed Fair Scheduling Queueing for the push part of the system, say $E[T_{PFS}(j)]$. Recall that such a value is known and it is proportional to the space S_j between two instances of j in the Packed Fair Queueing Scheduling [10], and it is different from the overall expected waiting time of the server although it depends on the cut-off point in use. Now, if the expectation of the client $2E[T_{PFS}(j)]$ is smaller than or equal to $\Delta(j)$, the request can still be accepted and the performance guarantee. Note that the $E[T_{PFS}(j)]$ is doubled to take in the figure the fact that the system pulls one item between two consecutive pushed items. Otherwise, the request can be accepted only if the cut-off point is updated. Indeed, the server will perform a binary search on the vector \mathbf{V} to look for a cut-off point value whose corresponding expected hybrid waiting time is the largest value smaller than or equal to $\Delta(j)$. Note that such a value always exists if $\mathbf{V}[0, 1] \leq \Delta(j)$. Then, the cut-off point is updated accordingly and the scheduling re-initialized. Note that the adjustment in push and pull sets results in some overheads, and in practice, the server may be forced to reject requests to avoid to pay such an overhead too frequently. Figure 8 provides a pseudo-code for this entire procedure of performance guarantee.

5 Conclusion

In this paper we have proposed and analyzed the performance guarantee of a new hybrid, scheduling algorithm. In Section 3, we have evaluate a basic hybrid algorithm which separates the items in two sets, one to be pushed and one to be pulled. The second contribution of our approach lies in offering to each client the possibility to specify a deadline, providing him/her the flexibility to choose his/her best suitable access-time. To react to a request with expectation time, the system may need to recompute the cut-off point. The overhead of this operation is kept as low as possible. Future work will be devoted to study the overhead incurred by the system and how to keep it as low as possible.

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1. for ( $i=1$  to  $D$ ) do
2.     compute the average waiting time  $E[T_{hyb-access}(i)]$ ;
3. sort all the values of  $E[T_{hyb-access}(1)], \dots, E[T_{hyb-access}(D)]$  and
   store them in increasing order in a vector  $\mathbf{V}$ 
4. broadcast to the clients the min{affordable waiting time}  $\mathbf{V}[0]$ ;
do
5. accept the client's request for any item  $j$  with expected
   waiting-time  $\Delta(j) \geq E[T_{hyb-access}(K)]$ , where  $K$  = current cut-off;
6. if (condition at line 5 is not verified and  $j \leq K$ )
   accept the client's request for any item  $j$  with expected
   waiting-time  $\Delta(j) \geq 2E[T_{PFS}(j)]$ , where  $E[T_{PFS}(j)]$  is the
   expected waiting time guaranteed by Packet Fair Scheduling;
7. if (both conditions at lines 5 and 6 are not verified) and
   ( $\Delta(j)$  is larger than expected waiting time stored in  $V[0,1]$ )
8.     get the largest value of  $E[T_{hyb-access}(j)] \leq \Delta(j)$  from  $\mathbf{V}$ 
9.     adjust the cut-off point and restart new hybrid scheduling;
10. otherwise reject the request.
while (true)

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Fig. 8. Performance Guarantee in Hybrid Scheduling

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