

A Comparative Analysis of Solving Sudoku Using Genetic Algorithm and DLX

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Abstract: The Sudoku solving algorithms are very much essential for solving combinatorial optimization problems, especially in areas of artificial intelligence, operations research, and recreational mathematics. This research evaluates and compares the effectiveness of Genetic Algorithms (GA) and the Dancing Links (DLX) algorithm in solving Sudoku puzzles, focusing on performance, computational efficiency, and accuracy. The GA approach uses heuristics including population initialization, fitness evaluation, crossover, and mutation for iterative approximation of solutions, whereas the DLX algorithm, also known as Algorithm X, translates the Sudoku problem into an exact cover problem and employs a matrix-based linked list structure for deterministic solution finding. The results of comparative analysis over a variety of puzzle complexities indicate that the GA is considerably good at heuristic exploration. GA can solve relatively simpler puzzles with ease but consumes much more computational resources for complex cases. Meanwhile, DLX always obtains an exact solution with optimal efficiency but fails to explore suboptimal solutions flexibly. The results show the strengths and weaknesses of both techniques, and offer substantial insight for algorithm selection with criteria for problem conditions and complexity, relevant to a general class of larger combinatorial optimization problems.

1 INTRODUCTION

Solving Sudoku has emerged as an important topic within computational problem solving and optimization, as Sudoku-solving is characterized by its inherent complexity and practical relevance in fields such as artificial intelligence, operations research, and algorithmic research. The solving algorithms for Sudoku not only evaluate the efficiency of the algorithms but also cast insight into the solution of other combinatorial optimization problems. This work explores a comparative analysis of two distinct approaches: Genetic Algorithms (GA) and the Dancing Links (DLX) algorithm, each representing a unique paradigm in the tussle to solve Sudoku puzzles. The mechanism of GA is inspired by the principles of natural selection and genetics. It uses techniques such as population initialization, fitness evaluation, crossover, and mutation iteratively to refine solutions and navigate this vast solution space. Therefore, its adaptability is high, but for problems that are highly constrained, randomness can lead to

computational inefficiencies; that's why it is not suited for moderately complex problems.

However, the DLX algorithm transforms the Sudoku problem to be an exact cover problem and solves it with perfect determinism. This is achieved by using an efficient matrix-based linked list structure that systematically ensures that all Sudoku constraints are fulfilled with acceptable computational efficiency. But the determinism limits the ability to explore approximate or suboptimal solutions.

These methods are challenging in respect to balance accuracy, computational efficiency, and adaptability in solving Sudoku puzzles of various complexities. While GA needs to deal with issues like maintaining diversity in the solution pool and avoiding premature convergence, DLX requires careful handling of memory and computational resources, especially when dealing with large or dynamically changing problem instances.

This will be a project aiming to analyze and compare the two methods in terms of performance, efficiency, and accuracy for solving Sudoku puzzles.

Incorporating a number of benchmark puzzles at different complexity levels, the analysis will weigh the strengths and weaknesses of both approaches. Additionally, a closer and more detailed analysis of the trade-offs between heuristic exploration and deterministic precision will be conducted to highlight their applicability across different scenarios. These findings will be all the better to enrich general knowledge in combinatorial optimization algorithms and their ability to solve similar complex problems.

There is a list of related works in Section 2. In Section 3, the recommended methods are presented. The findings are presented in Section 4. The conclusion is presented in section 5. The future work is presented in section 6.

2 RELATED WORKS

Pratama et al. dealt with heuristic-based methods of solving Sudoku problem of varying degree of difficulty. The abstract mentioned that the paper addresses the efficiency and accuracy problems of heuristic search algorithms. The authors used a mixture of depth-first search and constraint propagation methods to minimize the space of the search. It relies on prioritizing cells with the fewest possible candidates, which enhances speed and accuracy. A major limitation is its vulnerability to multisolution puzzles, which might deteriorate its performance.

Lina et al. compared two algorithms in solving Sudoku: Breadth-First Search (BFS) and Depth-Limited Search (DLS). In the abstract, it briefly states that each method will be understood for its computational complexity and feasibility. BFS is complete since it explores all possible possibilities while having high memory usage. DLS, though has reduced memory demands because it limits recursion depth, may fail to find any solution. The core limitation of this paper is that it simply cannot solve the advanced Sudoku puzzles, due to scalability issues with BFS and suboptimal depth limits with DLS.

Jana et al. their paper presents a hybrid approach combining Genetic Algorithm (GA) with the Firefly Mating Algorithm (FMA) to solve Sudoku. The abstract mentions that this synergy between GA's exploration capability and FMA's local search efficiency describes the capability of the hybrid algorithm. The hybrid approach combines crossover, mutation, and firefly-inspired movement to iteratively improve solutions. Although the method is generally good for many different scenarios, it has a

disadvantage of leading to higher overheads due to the hybridization process, which makes it unsuitable for real time.

Indriyono et al. presents a paper of traditional backtracking and brute force methods of solving Sudoku is conducted. The abstract is about the ease and dependability of these methods for providing accurate solutions. Backtracking uses a form of recursive traversal, while brute force attempts to exhaustively try all combinations. Although simple, both approaches suffer from high time complexity and are inefficient for more difficult puzzles.

Wang et al. their paper introduces an evolutionary algorithm enhanced with local search strategies targeting columns and sub-blocks in Sudoku puzzles. The abstract on the algorithm indeed shows a balance between exploration and exploitation. Implementation details show integration of crossover, mutation, as well as adaptive local search. Though it is found effective, its limitation lies in the sensitivity to poor initial populations, which leads to slow convergence.

Bukhori et al. reviews an application of GAs toward puzzle games, including Sudoku. The abstract mostly emphasizes the versatility and adaptability of the GA method. Standard genetic operations such as selection, crossover, and mutation are observed to be implemented with variations geared toward the different types of puzzles being solved. This reviewer found the review too generic, in which there was not enough insight into domain-specific challenges or optimizations uniquely particular to Sudoku.

Jana et al. presents Inspired by neighborhood search, a new mutation mechanism to improve the GA for Sudoku solving is discussed in this paper. The abstract shows that there would be better convergence rates due to targeted mutations based on cell neighborhoods. The implementation adjusts the mutation rates dynamically based on the quality of the solutions obtained. However, this might not generalize for all different puzzles due to its parameter-dependent nature.

Bhasin et al. in their paper, the use of GAs to solve the N-Puzzle problem, similar in complexity to that of Sudoku. The abstract demonstrates the algorithm's adaptability to combinatorial puzzles. Key genetic operations with heuristic evaluations guide the search process. A major limitation is its heavy dependency on initial populations, whereby it degrades badly in poorly initialized scenarios.

Silva et al. applies GAs to Beehive Hidato puzzles, emphasizing adaptability to unique grid configurations. The abstract highlights genetic operations tailored to hexagonal grids. While the

implementation successfully generalizes GA to different puzzles, its limitation lies in scalability, as computational costs increase with puzzle size.

Sevaljevic et al. discusses the application of Dancing Links implementations of the Exact Cover Problem which directly applies to Sudoku. Abstract Discusses DLX's efficiency in dealing with constraint satisfaction problems. Implementation The DLX Algorithm with use of dynamically variable constraints based on linked lists. Its limitation relies strictly on very precise formulations and offers little margin of error in setup.

3 METHODOLOGY

3.1 Theoretical Structure

The focus of the Sudoku Solver project is on designing an efficient system that would work to solve Sudoku puzzles using two different algorithms—Genetic Algorithm (GA) and Dancing Links (DLX)—for a comparative study of their efficiency. The solver aims to address the computational challenge that occurs when solving

Sudoku puzzles of different levels of difficulty while analyzing performance along key metrics of execution time, accuracy, and adaptability.

The Genetic Algorithm (GA) applies an evolutionary approach inspired by biological operators such as crossover, mutation, and selection. Starting from an initial population of random potential solutions, the GA computes a measure of how close each solution is to being a valid Sudoku solution. Through generations, it applies operators of selection, crossover, and mutation to evolve the population toward finding a good solution. The algorithm is particularly well-suited for puzzles where heuristic or approximate solutions are enough because it explores a diverse space and continuously enhances solutions iteratively.

On the other hand, the Dancing Links (DLX) algorithm takes advantage of the Knuth's Algorithm X's ability to find the exact cover problem. DLX uses a doubly linked list structure that facilitates an effective representation of the Sudoku constraints and adopts a backtracking mechanism for the systematic exploration of all potential solutions. The algorithm guarantees the fulfillment of each Sudoku rule by every solution found and, therefore, is a very effective algorithm to look for exhaustive solutions.

Algorithm 1. Genetic Algorithm for the NRP

Input: Instance P , size α of population, rate β of elitism, rate γ of mutation, number δ of iterations

Output: solution X

```

// Initialization
1 generate  $\alpha$  feasible solutions randomly;
2 save them in the population  $Pop$ ;
// Loop until the terminal condition
3 for  $i = 1$  to  $\delta$  do
// Elitism based selection
4 number of elitism  $ne = \alpha \cdot \beta$ ;
5 select the best  $ne$  solutions in  $Pop$  and save them in  $Pop_1$ ;
// Crossover
6 number of crossover  $nc = (\alpha - ne)/2$ ;
7 for  $j = 1$  to  $nc$  do
8 randomly select two solutions  $X_A$  and  $X_B$  from  $Pop$ ;
9 generate  $X_C$  and  $X_D$  by one-point crossover to  $X_A$  and  $X_B$ ;
10 save  $X_C$  and  $X_D$  to  $Pop_2$ ;
11 endfor
// Mutation
12 for  $j = 1$  to  $nc$  do
13 select a solution  $X_j$  from  $Pop_2$ ;
14 mutate each bit of  $X_j$  under the rate  $\gamma$  and generate a new solution  $X_j'$ ;
15 If  $X_j'$  is unfeasible
16 update  $X_j'$  with a feasible solution by repairing  $X_j'$ ;
17 endif
18 update  $X_j$  with  $X_j'$  in  $Pop_2$ ;
19 endfor
// Updating
20 update  $Pop = Pop_1 + Pop_2$ ;
21 endfor
// Returning the best solution
22 return the best solution  $X$  in  $Pop$ ;

```

Figure 1: Genetic algorithm.

To assess the performance of these algorithms, a comparative analysis is performed. The system measures aspects such as:

1. Execution Time: The time taken by each algorithm to solve the puzzles for various complexities.
2. Solution Accuracy: The solutions obtained are valid and complete.

- 3. Resource Usage: Memory and computational overhead for each approach
 - 4. Adaptability: Performed ability across puzzles with constraint density and sizes.
- As an implementation aspect, this approach integrates a test suite of Sudoku puzzles that validate the algorithms. Under controlled conditions of evaluation, the analysis highlights the strengths and weaknesses of heuristic methods, such as GA, versus deterministic approaches like DLX.

It not only documents detailed insight in two contrasting algorithmic paradigms, but also contributes towards the larger field of constraint satisfaction problems. The results can have implications on the establishment of hybrid or adaptive solvers for the consideration of more similar problem-solving strategies in actual applications. The Genetic Algorithm is as shown in Figure 1.

3.2 System Overview

Input Interface: A user-friendly graphical interface or command-line input for the users to present the initial Sudoku puzzles. It should validate that the input format follows the standard Sudoku rules for the grid.

Algorithm Selection: Users can choose between the two algorithms: GA or DLX. This module helps ensure that the user is able to make a comparison over the very same input for both algorithms.

Genetic Algorithm Module: This module implements the GA, containing components for the generation of a population, fitness evaluation, crossover, mutation, and selection. It solves the Sudoku puzzle heuristically and returns the solution along with some performance metrics such as execution time and fitness score.

Dancing Links Module: This module uses the DLX algorithm that converts the Sudoku problem to an exact cover one. Using a matrix-based approach, it finds the solution deterministically and reports the result along with the execution time.

Output Module: This component presents the solutions generated by the selected algorithm, along with performance metrics such as computational time, accuracy, and number of iterations. It also provides visualizations of the solved Sudoku grid for better clarity.

Workflow: The workflow (illustrated in the architecture diagram) begins by taking a Sudoku puzzle as input. The user selects one of the two algorithms to solve the puzzle. If GA is used, the system generates an initial population, determines the fitness and iterates through crossover and mutation to find a solution. If DLX is used, the system converts the puzzle into a binary matrix and applies the exact cover technique to find the solution. The system will then output the solution, its performance metrics and a visual presentation of the solved grid.

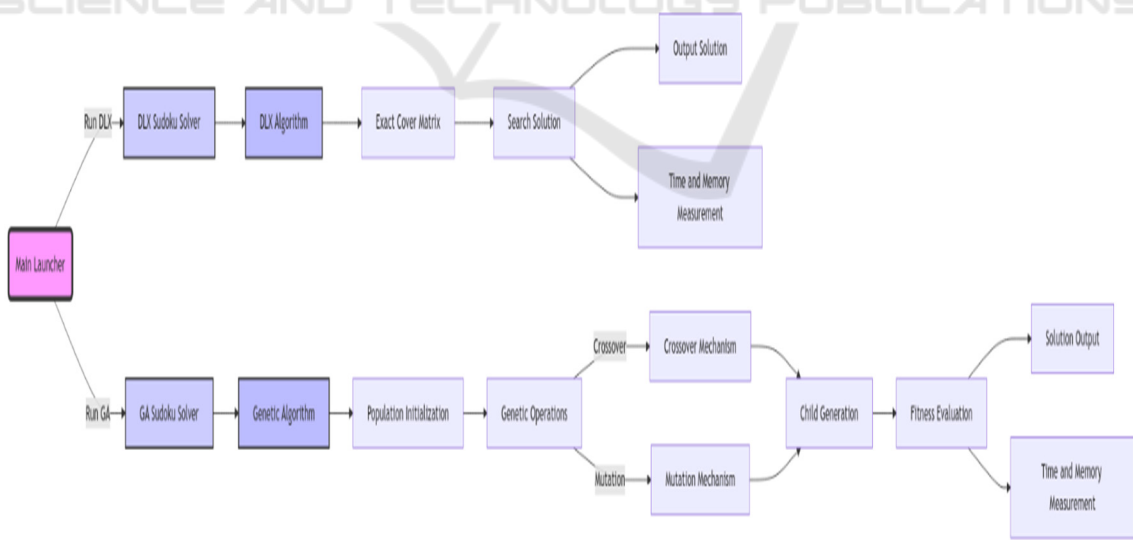


Figure 2: Architecture diagram.

The workflow in Figure 2 reads a Sudoku puzzle and normalizes it according to standard rules. Further, the chosen algorithm might use the puzzle to generate

GA or DLX. The system computes performance measurements such as execution time, accuracy, and computational efficiency. The result is the solved grid

along with the comparative results of algorithms used. This design thus offers a strong framework for comparing the capability and performance of Genetic Algorithms and Dancing Links in solving Sudoku puzzles.

4 RESULTS AND EVALUATION

4.1 Statistical Evaluation

The number of difficulty variations is available as well as options for new game generation as shown in Figure 3. The fully filled grid thereby indicates that the puzzle is completed effectively, as confirmed by the indication of the solution after several iterations of the interface. The overall performance metrics presented here-in comprise time taken and memory used, which are indicators of the resource consumption involved in running the Genetic Algorithm. The Genetic Algorithm has successfully filled the Sudoku grid. It solves the puzzle correctly with no conflicts or placement errors. It was also reached within a computable number of generations, signifying that the algorithm performs good convergence towards the solution. The program supplies information about the consumption of computational resources: the time spent solving and memory used, revealing the efforts made by a genetic algorithm when using it to solve this particular type of puzzle.

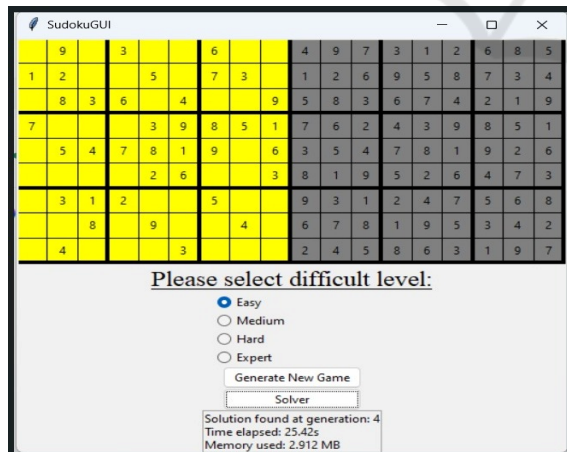


Figure 3: Genetic algorithm.

Options in the solver as shown in Figure 4 allow for the choice of difficulty level and playing a new game or solving an existing puzzle. The grid is fully filled in, which results from the DLX algorithm's ability to solve the puzzle effectively and with minimal time

with no errors. The puzzle is completely solved such that the DLX algorithm accurately fills every cell with a number based on Sudoku's strict rules. The solver solves it so fast, which is an indication of DLX's efficiency in running its algorithms to solve constraint satisfaction problems quickly and accurately. It only consumes a small amount of memory, indicating the low overhead of the DLX algorithm and its utility in applications where resource computation is critical. This interface does not only make it easy to solve Sudoku puzzles but also shows the relevance of the DLX algorithm for real-time applications and especially underscores such an aspect as rapid processing with the use of minimal resources.

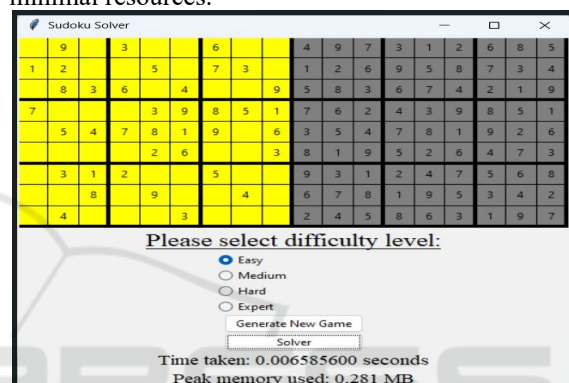


Figure 4: DLX algorithm.

4.2 Comparison

The graph "Comparison of Execution Time by Puzzle Size" as shown in figure 5c displays the performance of the Genetic Algorithm (GA) and Dancing Links X (DLX) across increasing Sudoku puzzle sizes (9x9, 16x16, 25x25). It illustrates how execution time increases sharply in GA with puzzle size, indicating a scalability problem, whereas the increase in DLX is relatively less steep, indicating that DLX is much more efficient and better scalable to larger puzzles. Whereas GA might be competitive for small-size puzzles due to potentially faster solutions, DLX's continued performance over the whole range of sizes makes it a choice for large-size challenges, where the reliability and predictability of operation matter.

This comparison highlights DLX as an algorithm of choice for hard tasks; indeed, GA needs additional optimization or hybrid strategy in order to handle sizeable puzzles properly.

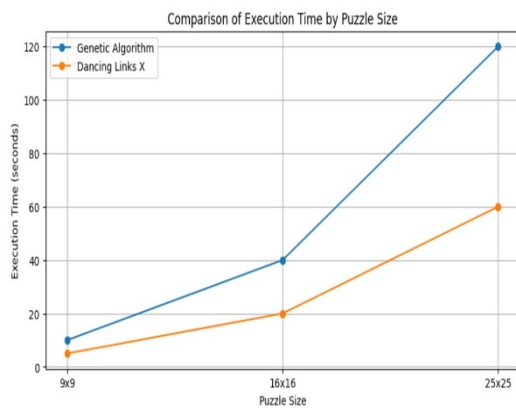


Figure 5: Comparison of execution time by puzzle size.

4.3 Memory Consumption

The bar graph as shown in figure 6d compares the memory consumption of the Genetic Algorithm (GA) and Dancing Links X (DLX) as they solve Sudoku puzzles of varying sizes (9x9, 16x16, and 25x25). The graph reveals that, with problem size, the memory usage of GA really shoots up. For 9x9 problems, it uses up to 10 MB and jumps to 45 MB for 25x25. This therefore represents a very sharp increase as the problem size increases. As compared to DLX, this is much steeper; it uses 5 MB for 9x9 and 20 MB for 25x25 problems. This shows how DLX has good memory performance, making it a better choice for more complex problems where the memory effectiveness is most valued. The comparison between the two algorithms shows that GA requires much more resources and how DLX is perfectly suited for scenarios when free memory usage might be very limited.

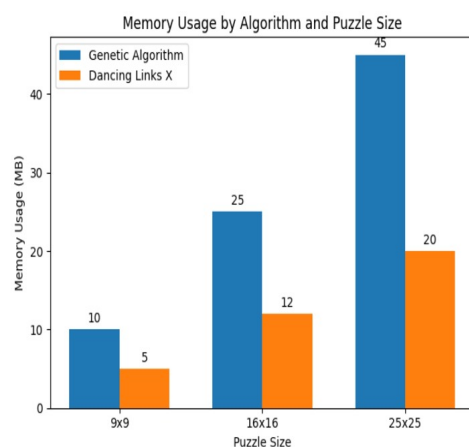


Figure 6: Memory consumption of GA and DLX.

5 CONCLUSIONS

Our work in this paper expands on these developments concerning the methodologies for solving Sudoku problems. We present a comparative study of Genetic Algorithm (GA) and Dancing Links (DLX) implementations. This is based on an analysis of prior research, indicating that whereas exact solutions are provided by techniques such as backtracking and brute force, they do not overcome the challenge of computations for bigger complex puzzles. On the contrary, heuristic and hybrid algorithms specifically those that use Genetic Algorithms are scalable and efficient but are sensitive to parameter tuning and incur some computational overhead.

Dancing Links appears to be promising where the problems can be constrained appropriately as evidenced by its successful application to the Exact Cover Problem. Its disadvantage would be that it relies heavily on exact input formulations. The juxtaposition of the two methodologies applied will enable the strengths of evolutionary techniques for adaptive applicability and the mathematical correctness of DLX for precision.

Our work is a contribution to understanding the performance of these different paradigms in finding solutions for Sudoku puzzles with different levels of difficulty. Through time complexity, convergence behavior, and precision analysis, it is hoped that light will be shed on their applicability. Therefore, our effort eventually aims at developing a computationally efficient yet adaptive robust framework that propels state-of-the-art combinatorial problem-solving techniques forward.

6 FUTURE ENHANCEMENT

The horizon for future improvements upon this effort includes hybrid approaches that integrate the fluidity of Genetic Algorithms (GA) with the strength of Dancing Links (DLX). These two methodologies could effectively be integrated to create a solid framework that capitalized on the best features of the two methods, using the efficiency GA can produce navigating difficult and vast search spaces and then deploy DLX for solving exact constraints with mathematical integrity.

In addition to this, machine learning techniques would be used to dynamically optimize the parameters of GA; this includes mutation rate, crossover strategy, and selection mechanisms. The

second case is the use of machine learning models to fine-tune configurations with DLX to achieve better performance for a variety of Sudoku puzzles with different degrees of difficulty.

The other areas for enhancement would be extending this work into real-time applications. Putting it into an interactive Sudoku solver or an embedded system would then enable the algorithms to be actually tested in the real world, measuring responsiveness and accuracy under time constraints.

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