

Using Linear Regression, Ridge Regression, Lasso Regression, and Elastic Net Regression for Predicting Real Estate Price

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Abstract: In the contemporary economic landscape, the real estate market wields significant influence, with housing prices being a crucial factor affecting individuals, industries, and the overall economy. Fluctuations in housing prices can impact people's living standards, investment decisions, and the stability of related industries. Thus, accurately predicting housing sales prices is of utmost importance. This paper focuses on predicting housing sales prices using linear regression, ridge regression, Lasso regression, and elastic net regression. The principles and applications of the four regression models in price prediction are explored in detail. By calculating evaluation metrics such as Mean Absolute Error (MAE), Mean Squared Error (MSE), and Root Mean Squared Error (RMSE), the performance of each model is compared. The results show that linear regression has an MAE of 0.092129, indicating normal performance. Ridge regression can address multicollinearity issues with an MAE of 0.091513, but may overfit. Lasso regression and elastic net regression, with MAEs of 0.087802 and 0.087756 respectively, can simplify models through feature selection, reducing overfitting risks and improving the ability of generalization. Future research could expand data sources, incorporate external variables, adopt advanced models, and utilize big data and deep learning technologies. This research provides valuable references for real estate-related decision-making and promotes the development of real estate price prediction research.


1 INTRODUCTION

In today's modernized world and economic system, the real estate market occupies a crucial position. On the one hand, purchasing a house is one of the most important issues for most people. As Çilgın, C. & Gökçen, H. (2023) mentioned, owning a house is an essential issue for both low and middle income people. On the other hand, the real estate market plays a role in any related industries, which indicates its function in the world economy (Pai and Wang, 2020). However, the unexpected fluctuation of the real estate market can bring several influences both economically and socially. As Capellán, Sánchez Ollero, & Pozo (2021) have mentioned, after the period of the 2008 housing bubble burst, a decline of employment, unit sold, unit built, and number of companies appeared. Thus, forecasting real estate accurately is of great importance for not only publicity but also for real estate industries.

So far, the majority of scholars have been engaged

in exploring the current situation of machine learning in real estate prediction. Singh, Sharma, and Dubey (2020) utilized big data concepts and three models –linear regression, random forest, and gradient boosting –to forecast housing sale prices in Iowa. Their findings indicated that the gradient-boosting model outperformed the others in terms of forecasting accuracy. Pai and Wang (2020) employed four machine learning models, such as least squares support vector regression (LSSVR) and classification and regression tree (CART), along with actual transaction data from Taiwan. Among these, LSSVR demonstrated excellent performance in predicting real estate prices. AL - Gburey and Kurnaz (2020) combined an artificial neural network and a grey wolf optimizer to predict housing market prices, achieving a high accuracy rate. These studies explored diverse methods and models, offering valuable references for real estate price prediction.

The paper aims to construct an efficient housing sales price prediction model by applying three classic

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algorithms: linear regression, ridge regression, and Lasso regression. Initially, it conducts a thorough analysis of the housing price dataset, dealing with outliers and missing values. Then, it explores the algorithms' principles, model-building processes, and their applications in price prediction. Finally, it assesses the models' performance using multiple indicators, compares different algorithms, summarizes the research, and looks ahead to future research directions.

2 METHODS AND MATERIALS

2.1 Data Collection

This study utilizes the Ames Housing dataset, which was compiled by Dean De Cock for data science education purposes (<https://www.kaggle.com/competitions/house-prices-advanced-regression-techniques/overview>).

The dataset is characterized by its comprehensiveness, consisting of 79 explanatory variables that describe almost every aspect of residential homes in Ames, Iowa. These variables cover a wide range of features, including the physical characteristics of the houses (such as the height of the basement ceiling, and number of bedrooms), location-related factors (proximity to railroads), and various other details about the property. In terms of the sample size, the dataset contains a substantial amount of data, providing a rich source for in-depth analysis.

Before being used in this research, the dataset underwent preprocessing. The preprocessing steps included handling missing data and dealing with outliers. For missing data, different strategies were employed based on the proportion of missing values in each column. As for outliers, they were identified and removed by examining the correlation between variables such as 'SalePrice' and others like 'OverallQual' and 'GrLivArea'. This preprocessing was carried out to enhance the quality of the dataset, aiming to facilitate more accurate analysis and model building.

2.2 Methods

In the research of predicting housing sales prices, linear regression, ridge regression, Lasso regression, and elastic net regression were applied. Each algorithm has its unique concepts, principles, and characteristics.

2.2.1 Linear Regression

Linear regression is a basic yet important algorithm. Its concept is to establish a linear relationship between the dependent variable (housing sales price) and independent variables (such as house area, and number of rooms). The principle is to use the least squares method to find the optimal coefficients that minimize the sum of the squared differences between predicted and actual values. It is easy to interpret, as the coefficients directly show the impact of each factor on the price. However, it assumes a linear relationship and may not perform well when the relationship is complex or there are correlated variables.

2.2.2 Ridge Regression

Ridge regression is an improvement over linear regression. It addresses issues like multicollinearity by adding a penalty term (L2 regularization) to the loss function. The concept is to shrink the coefficients towards zero while fitting the model. This helps in stabilizing the model and improving its generalization ability. In housing price prediction, it can handle correlated features better than linear regression.

2.2.3 Lasso Regression

Lasso regression, using L1 regularization, has a distinct feature - it can perform feature selection. The concept is to minimize the sum of squared errors plus a penalty on the absolute values of the coefficients. This is very useful when dealing with a large number of features in housing price prediction, as it simplifies the model and improves interpretability. However, it is more sensitive to the choice of the value compared to ridge regression.

3 RESULTS

Table 1: The correlation between the explanatory variables and Saleprice

YearRemodAdd	0.507101
YearBuilt	0.522897
TotRmsAbvGrd	0.533723
FullBath	0.560664
1stFlrSF	0.605852
TotalBsmtSF	0.613581
GarageArea	0.623431
GarageCars	0.640409

GrLivArea	0.708624
OverallQual	0.790982
SalePrice	1

The paper aims to find the correlation between the 74 explanatory variables and the house price and find out that 10 of the variables-Fireplaces, YearRemodAdd, YearBuilt, TotRmsAbvGrd, FullBath, 1stFlrSF, TotalBsmtSF, GarageArea, GarageCars, GrLivArea, and OverallQual- process large coefficient association bigger than 0.5, which indicates the correlations between this variable and the house price is high (Table 1).

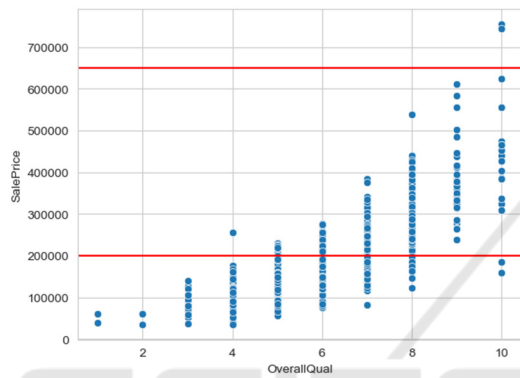


Figure 1: The correlation between House Sale Price and Overall Quality Score (Picture credit : Original)

Figure 1 shows that the variable SalePrice has a relatively low growth when OverallQual ranges from 2-4, however, it rises rapidly when OverallQual climbs to 8-10. Most data points cluster between 200,000 and 650,000, highlighting the relationship's significance for price prediction.

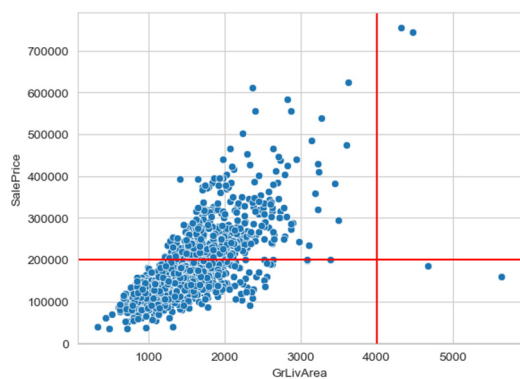


Figure 2: The Relationship between GrLivArea and SalePrice (Picture credit : Original).

Figure 2 reveals the positively correlated relationship between GrLivArea and SalePrice. When

GrLivArea is in the range of 0 - 1000, SalePrice shows a slow growth. But when GrLivArea reaches 4000, SalePrice rises more significantly. Data points mainly cluster in the lower-left area, where GrLivArea is small (around 0 - 3000) and SalePrice is relatively low (around 0 - 400,000), indicating a large number of such houses in the market.

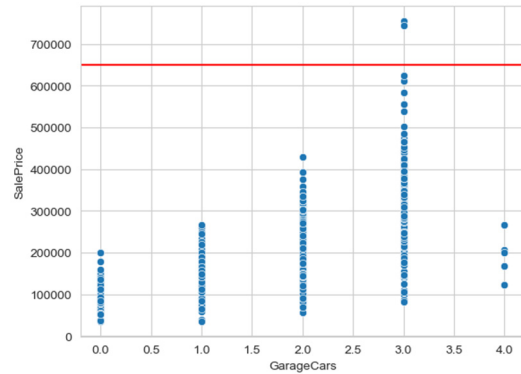


Figure 3: The Relationship between House Sale Price and the Number of Garage Cars (Picture credit : Original)

Figure 3 reveals a positive - correlation trend, though not strictly linear. As GarageCars increase, SalePrice generally rises. For different GarageCars values like 0, 1, 2, and 3, there are multiple SalePrice data points. A red horizontal line at $y = 650,000$ shows that high-price (above 650,000) houses are less in number.

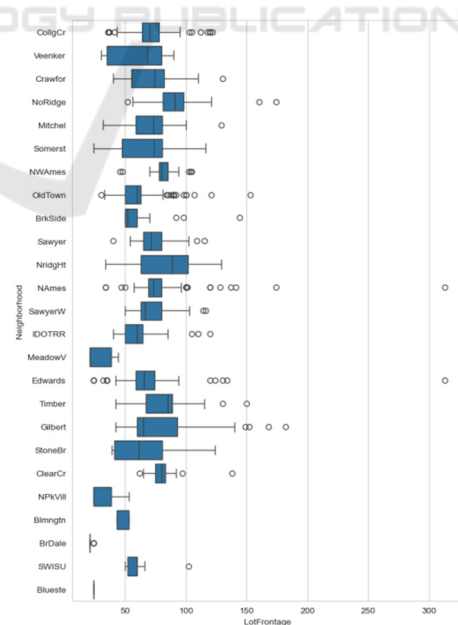


Figure 4: The Distribution of Lot Frontage among different Neighbourhoods (Picture credit : Original)

Figure 4 illustrates that as the values of LotFrontage change, the spread and central - tendency within each Neighbourhood differ. For different Neighbourhoods, there are multiple LotFrontage data points. The overall graph shows that extreme-value (either very high or very low) LotFrontage in some Neighbourhoods is less in number.

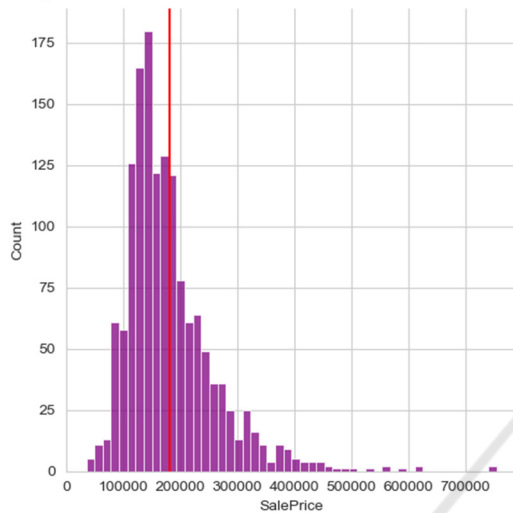


Figure 5: Distribution of House Sale Prices(Picture credit : Original)

Figure 5 reveals a left-skewed distribution. The data predominantly clusters on the left side, with most values below the mean of around 200,000. While there exist some higher - value outliers extending to the right, the majority of the data points contribute to the concentration on the lower-price end, highlighting the distinct left-leaning nature of the distribution.

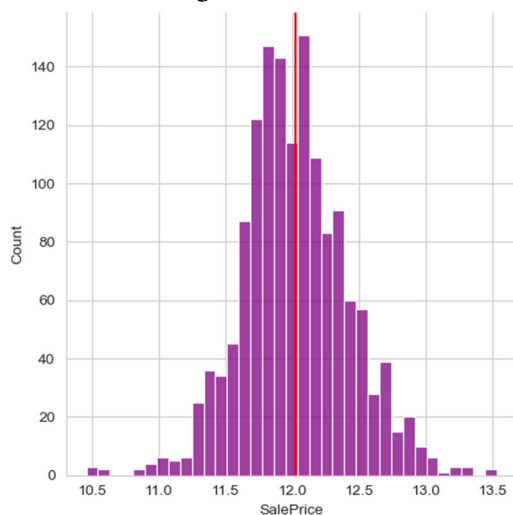


Figure 6: Near-Normal Distribution of Log-Transformed SalePrice Data(Picture credit : Original)

This barplot of SalePrice, after the np.log1p transformation on the horizontal axis, reveals a near-normal distribution (Figure 6). The data is symmetrically clustered around the mean. The mean of the data, indicated by the red vertical line, is approximately at the value of around 12.0 on the log-transformed scale.

Table 2: The Impact of Housing Features on Sale Price Based on the Linear Regression Model

Id	-0.000008
LotArea	0.000004
LotFrontage	0.000455
OverallCond	0.037583
OverallQual	0.037434
SaleCondition_AdjLand	0.181921
SaleCondition_Alloca	0.050358
SaleCondition_Family	0.000965
SaleCondition_Normal	0.075244
SaleCondition_Partial	0.068994

The coefficients in Table 2 result from defining feature matrix X (excluding the SalePrice column) and target variable y (the SalePrice column), splitting the dataset into 70% training and 30% test sets, and training a linear regression model.

These coefficients show each feature's influence on SalePrice. A large absolute-value coefficient like SaleCondition_AdjLand's (0.181921) implies a stronger impact, while smaller coefficients suggest weak correlations. This might be due to feature irrelevance, multicollinearity, or data issues. Incorrect train-test splits can cause underfitting or overfitting, affecting model performance.

3.1 Linear Regression

Table 3: Performance Metrics of the Linear Model: MAE, MSE, and RMSE

	Quantity
MAE_linear	0.092129
MSE_linear	0.032784
RMSE_linear	0.181063

The evaluation metrics MAE (0.092129), MSE (0.032784), and RMSE (0.181063) in Table 3 suggest that the linear regression model has a relatively good predictive performance. The presence of a certain deviation between the predicted and actual values is evident, as indicated by these metrics. This implies that the model has room for improvement in accurately predicting the target variable.

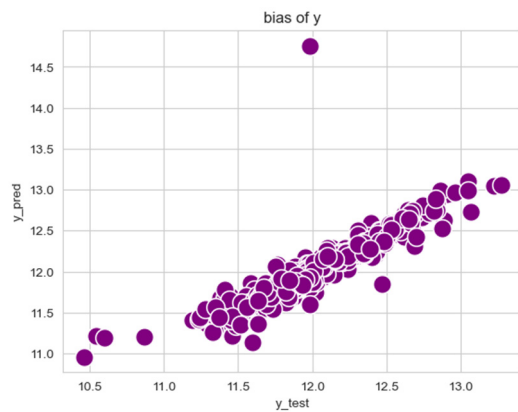


Figure 7: Correlation between Predicted and Actual House Sale Prices(Picture credit : Original)

From Figure 7, it can be observed that the data points are roughly distributed around a straight line with x indicating the real value of the house sale price and y revealing its predicted value, yet there are discrete points. This indicates that there is a certain correlation between the model's predicted values and the actual values, but also a certain degree of deviation.

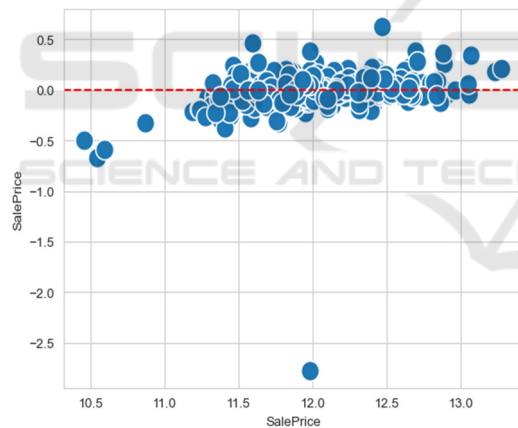


Figure 8: Correlation between Predicted and the Difference between Actual and Predicted Prices(Picture credit : Original)

Figure 8 shows the relation between the real house sell price and the difference value of the real and predicted sale price, indicating that there still exist discrete points.

Overall, the linear model is inappropriate for this model with some of the discrete data.

3.2 Polynomial Regression model

Table 4: Variations between Actual and Forecasted Sale Prices

Y_Test	Y_Pred	Y_Pred_2	Residuals
666	11.76758	13.16222	-1.39464
104	12.04061	11.96373	0.076878
528	11.36211	11.16076	0.201354
18	11.97667	12.19577	-0.2191
1151	11.91773	11.99526	-0.07753

Table 4 illustrates that there is a fluctuation between the real house sale price and the predicted price.

Table 5: Performance Metrics of the Polynomial Regression model: MAE, MSE, and RMSE

	Metrics
MAE_Poly	0.309979
MASE_Poly	1.018768
RMSE_Poly	1.009240

Table 5 shows the MAE, MSE, and RMSE of this model. With the value 0.309979 of MAE, it shows a possibility of applying this model, however, the value of MSE and RMSE are all above 1, which shows the inaccuracy of the model in contrast.

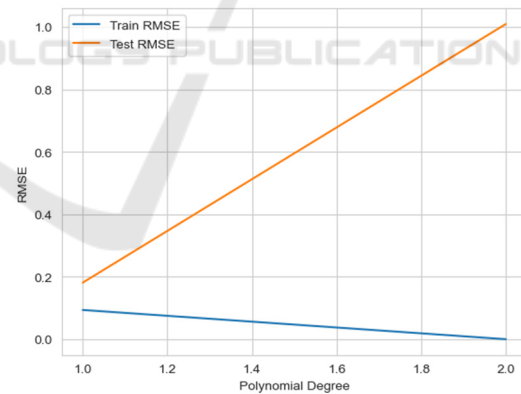


Figure 9: Comparison of Training and Test Set RMSE with Varying Polynomial Degrees from 1 to 2(Picture credit : Original)

From Figure 9, although the training-set RMSE experiences a slight decrease as the polynomial degree increases from 1 to 2, the test-set RMSE rises significantly. This indicates that increasing the polynomial degree fails to improve the model's predictive ability for new (test) data overall. Instead, it may lead to overfitting, preventing the effective reduction of errors.

3.3 Ridge Regression model

Table 6: Performance Metrics of the Ridge Regression model: MAE, MSE, and RMSE

	Metrics
MAE_Ridge	0.091513
MSE_Ridge	0.031576
RMSE_Ridge	0.177697

In Table 6, the evaluation metrics of the ridge regression model are MAE (0.091513), MSE (0.031576), and RMSE (0.177697), indicating a relatively good predictive performance. These metrics show that there is still some deviation between the predicted and actual values. However, compared to the linear regression model, the ridge regression model has smaller values for MAE, MSE, and RMSE, suggesting an improvement in accurately predicting the target variable..

In the Ridge regression model, different features are assigned varying weights. Features with positive coefficients have a positive impact on the target variable, while those with negative coefficients exert a negative effect. Features with a coefficient of zero indicate that they are not utilized in the model or contribute minimally to the prediction. The regularization mechanism in Ridge regression effectively reduces the coefficients of certain features, particularly those with redundancy or high correlation, thereby enhancing the model's stability and generalization ability. Overall, regularization helps reduce overfitting and improves both the interpretability and predictive accuracy of the model.

3.4 Lasso Regression model

Table 7: Performance Metrics of the Lasso Regression model: MAE, MSE, and RMSE

	Lasso Metrics
MAE_Lasso	0.087802
MSE_Lasso	0.031073
RMSE_Lasso	0.176275

The evaluation metrics for Lasso regression, including MAE (0.087802), MSE (0.031073), and RMSE (0.176275), indicate that the model demonstrates reasonably good predictive performance (Table 7). However, these metrics also reveal some discrepancy between the predicted and actual values, suggesting that there is still potential for the model to improve in terms of accurately forecasting the target variable.

Lasso regression results in a model with several zero coefficients. This sparsity makes the model

simpler and more interpretable, reducing the risk of overfitting and enhancing the model's generalization ability.

3.5 Lasso Regression model

Table 8: Performance Metrics of the Elastic net Regression model: MAE, MSE, and RMSE

	Elastic Metrics
MAE_Elastic	0.087756
MSE_Elastic	0.029672
RMSE_Elastic	0.172257

The evaluation metrics MAE (0.087756), MSE (0.029672), and RMSE (0.172257) for the Elastic regression model indicate a reasonably good predictive performance (Table 8). However, the presence of some deviation between predicted and actual values, as reflected by these metrics, suggests that the model still has potential for improvement in accurately forecasting the target variable.

Elastic net regression yields a model with several zero coefficients. This sparsity makes the model simpler and more interpretable, reducing the risk of overfitting and enhancing the model's generalization ability.

4 DISCUSSIONS

This study has yielded valuable results; however, several limitations need to be addressed. Firstly, the study uses a small and homogeneous sample, which may limit the generalizability and reliability of the findings, particularly across different regions or groups. Secondly, the regression model assumes fixed relationships, which fails to capture the complexity of real-world dynamics. For example, external factors such as policy changes or market non-linearity are not fully considered, which may lead to prediction errors. Thirdly, the study only considers a limited set of features (e.g., price, location) and overlooks potentially important factors such as surrounding amenities or socio-economic conditions. Finally, while the regression model is effective, it is sensitive to outliers and noise, limiting its ability to handle complex, nonlinear data patterns.

To improve the study, several suggestions can be made. First, using diverse data sources and larger samples would enhance the accuracy and applicability of the findings. Second, incorporating external factors such as policy changes and economic trends would improve prediction accuracy, especially in volatile markets like real estate. Third, more

advanced techniques (e.g., SVM, Random Forests) should be employed to better handle non-linearities. Finally, integrating Big Data and Deep Learning technologies could improve model accuracy and capture complex relationships within the data.

With improved data and computation, future research can expand the study's scope and incorporate interdisciplinary methods for better prediction capabilities.

5 CONCLUSION

This study focuses on predicting housing sale prices using linear regression, ridge regression, ridge regression, Lasso regression, and Elastic Net regression. First, the housing data set from the Kaggle platform was employed. After preprocessing the data to handle missing values and outliers, the principles and model-building processes of four regression algorithms were explored. Then, these algorithms were applied to construct prediction models and multiple evaluation metrics like MAE, MSE, and RMSE were used to assess the model's performance.

The research findings indicate that different regression models have varying different performances. The linear regression model shows mediocre predictive ability; ridge regression has the potential for application but may suffer from overfitting; Lasso regression and Elastic Net regression can simplify the model through feature selection, with relatively small error values, reducing the risk of overfitting and enhancing generalization ability.

Looking ahead, future studies can expand the data sample size and source to improve accuracy and applicability. Incorporating external variables such as policy and economic trends, and adopting advanced techniques like SVM and random forests can better capture complex relationships. This research is significant as it provides a reference for making decisions related to real estate, which helps market participants like home buyers, developers, and investors make more informed choices.

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