Predicting the U.S. Stock Market Index Using LSTM with Different Financial Factors

Tingxi Zhang^{Da}

Shenzhen Audencia Financial Technology Institute, Shenzhen University, Guangdong, China

Keywords: Index Prediction, Long Short-Term Memory, Financial Factors.

Abstract: The complexity and dynamic nature of financial markets demand advanced tools for accurate forecasting. This is vital for investors, portfolio managers, and policymakers to make informed decisions regarding asset allocation and risk management. This study explores the potential of Long Short-Term Memory (LSTM) networks in predicting the S&P 500 index, augmented by a diverse set of financial factors including the Cboe Volatility Index (VIX), Effective Federal Funds Rate (EFFR), U.S. Dollar Index (USDX), and various U.S. Treasury rates. The research employs an approach involving data collection spanning from June 2010 to June 2023, preprocessing to ensure data suitability, and LSTM model development tailored to capture long-term dependencies. This article starts from two tasks, classification and regression, and focuses on predicting the S&P 500 index across varying time horizons. The study reveals that LSTM models augmented with relevant financial factors effectively predict short-term movements in the S&P 500 index, with low Root Mean Square Error (RMSE) and Mean Absolute Error (MAE) values for 1-day predictions. However, prediction errors increase significantly for longer horizons, particularly for variables highly sensitive to market volatility and interest rate changes. The findings contribute to developing more accurate forecasting tools for the financial industry, enhancing decision-making capabilities for various stakeholders.

1 INTRODUCTION

Expanding the potential of Long Short-Term Memory (LSTM) networks in predicting the S&P 500, research delves into the intricacies of applying this model & rationale for selecting financial factors (Lee & Kang, 2020). As a subclass of Recurrent Neural Networks (RNNs), LSTMs overcome vanishing exploding gradient issues, enabling them to retain past information effectively, ideal for capturing complex, nonlinear relationships and long-term dependencies in financial data (Wang et al., 2022).

Integrating factors like the Cboe Volatility Index (VIX), Effective Federal Funds Rate (EFFR), U.S. Dollar Index (USDX), and U.S. Treasury rates enhances predictive power. VIX insights into investor sentiment & market volatility aid in capturing sentiment impacts during uncertainty. EFFR, a monetary policy tool, influences borrowing costs and stock market movements. USDX reflects currency fluctuations, impacting international competitiveness and stock prices (Bhandari et al., 2022). Treasury rates offer insights into interest rates, economic growth, and inflation expectations, which are crucial for investment and financing decisions.

This research aims to improve S&P 500 forecasting accuracy for investors, managers, and, policymakers. Accurate forecasts inform asset allocation, risk management, & policy formulation. LSTM's pattern recognition & long-term dependency capture enable insights into U.S. equity market trends (Michańków et al., 2022).

Experimental approaches include data collection, preprocessing (cleaning, normalization, feature engineering), model development, and evaluation are used. Focusing on 1-day, 5-day, and 20-day forecasts, models undergo rigorous testing with regression (Root Mean Square Error (RMSE), Mean Absolute Error (MAE)) and classification (confusion matrix) metrics. This aims to develop models accurately forecasting S&P 500 changes and classifying market movements, guiding investments, risk management, and policy.

^a https://orcid.org/0009-0004-7252-6834

2 LITERATURE REVIEW

The literature concerning utilizing machine learning and deep learning methodologies for forecasting stock market trends is continually expanding and advancing. Early studies employed traditional statistical methods like Autoregressive Integrated Moving Average (ARIMA) models and exponential smoothing techniques (Vo & Ślepaczuk, 2022). However, these approaches struggled to capture the nonlinearities and complexities inherent in financial time series.

With the advent of artificial neural networks, researchers began exploring their potential for stock market forecasting. While standard feedforward neural networks showed some promise, they were limited by their inability to handle sequential data effectively. In 2009, an extensive review encompassing over 100 scholarly articles by the authors revealed that neural networks (NNs) demonstrate a superior capacity for enhancing market forecasting when juxtaposed against conventional methodologies (Atsalakis & Valavanis, 2009). This finding underscores the potential advantages of adopting NNs in predictive analytics within the market context. Exploring the Influence of Financial Ratios and Technical Analysis on Stock Price Forecasting Leveraging Random Forests, with an Emerging Trend in AI-assisted and Human Insight-Integrated Prediction Frameworks (Pramod & Pm, 2020).

The introduction of RNNs, and subsequently LSTM networks, revolutionized the field by enabling the models to retain information from previous time steps, making them particularly suited for time-series analysis. Several studies have utilized LSTM networks for stock market prediction, demonstrating their effectiveness in capturing the dynamic behavior of stock prices and indices. These models have been found to outperform traditional statistical and even other machine learning methods in predicting stock market trends. Besides using some financial news, economic indicators, or sentiment data from social media (Vargas et al., 2017), the inclusion of financial factors as input features has further enhanced the predictive accuracy of LSTM models, as they provide a more comprehensive view of the market's underlying dynamics. In particular, the VIX index, as a measure of market uncertainty and expected volatility, has been widely used in stock market forecasting models (Roszyk & Ślepaczuk, 2024). Its predictive power stems from its ability to capture investor sentiment and risk appetite, which are crucial factors influencing stock prices. The EFFR, a key interest rate that influences the cost of borrowing and lending, also holds considerable sway in shaping the overall economic well-being and, consequently, the performance of the stock market (Bhandari et al., 2022).

Similarly, the USDX and U.S. Treasury rates are essential indicators of the dollar's strength and the country's debt market conditions, respectively. Their inclusion in stock market prediction models provides valuable insights into global macroeconomic trends and their potential impact on the U.S. equity market.

By synthesizing the insights from previous research and incorporating a diverse set of financial factors, this study aims to advance the field of stock market prediction using LSTM networks and contribute to a more nuanced understanding of the relationships between these factors and the S&P 500 index.

3 DATA AND METHOD

3.1 Dataset Introduction

This study employs a comprehensive methodology to forecast the future value of the S&P 500 index using daily market data and various financial factors. The dataset, sourced from Kaggle, spans from June 29, 2010, to June 27, 2023, encompassing 3271 days of information. It includes closing prices for the S&P 500 index, alongside selected financial indicators such as the VIX, EFFR, USDX, and a range of U.S. Treasury rates.

Data processing begins with acquiring the daily S&P 500 market data and relevant financial factors, followed by data cleaning to rectify errors, standardize date formats, and filter for the desired date range. The cleaned datasets are then integrated into a single CSV file. Before analysis, preprocessing steps include feature scaling using MinMaxScaler to normalize values between 0 and 1, merging processed feature columns with the target column into a DataFrame, defining key parameters such as timesteps and forecast horizon, and converting the DataFrame into a NumPy array for integration into the model. Then preprocessed data is partitioned into training and testing sets at an 80:20 ratio for model evaluation.

3.2 Method

3.2.1 Algorithm

LSTM is a specialized RNN, that utilizes gates and a cell state to alleviate gradient issues in long sequences, enabling it to capture long-term dependencies. It has the advantage of long-term memory capacity in requiring sequence prediction.

The core of the model is an LSTM layer that processes the input sequence. In this case, the hidden size is set to 128 and there are 3 layers. The batch first parameter is set to True to indicate that the input tensor's first dimension corresponds to the batch size. This layer is used to capture the temporal dependencies within the input sequence. Following the LSTM layer, a linear layer is used as the Fully Connected Layer (FC) to map the output of the LSTM to the desired output size, which corresponds to the forecast horizon in this case. The output of the LSTM layer's last time step is passed through this layer to produce the final predictions. During the forward pass, the LSTM layer initializes its hidden state (h0) and cell state (c0) to zero tensors of appropriate sizes, ensuring that the model's initial state is clean for each new input sequence (Mehtab et al., 2021).

3.2.2 Parameter Introduction

In this work, the input size is different for two types of groups. For the blank group (only Close price), it is set to be 2; for the experimental group, it is set to be 3. Then the hidden size is fixed at 128, balancing model complexity and computational efficiency. Three layers are stacked to capture intricate temporal patterns in the input sequence. The output size corresponds to the forecast horizon, tailored to the specific prediction task.

Adam optimizer is used and the learning rate is chosen to be 0.001 for the complexity of the data. Then Mean Squared Error (MSE) is used to be the Loss Function. There are 300 epochs to ensure thorough training and performance monitoring. The model with the lowest test loss is chosen to prevent overfitting and ensure good generalization as the best model.

3.2.3 Evaluation

In this work, the evaluation is RMSE and MAE for the regression part and accuracy for the classification part. The regression is evaluated by using the RMSE and MAE to the changing value but not the index value itself between the predicted value and real value. Then a threshold of 0 is applied to define binary labels (Decrease or Increase) based on changes in the target variable (Ding & Qin, 2020). After that, classification performance is evaluated using accuracy. Also, a classification report and a confusion matrix can help to further evaluate the model. (For example, if the recall of increase or decrease is lower than 0.5, the accuracy of this group will be marked in italic in Table 4). The assessment metrics give a further insight into the efficacy of the model, highlighting areas for improvement and ensuring its practical significance in investment prediction.

4 EXPERIMENTAL RESULTS

4.1 Model Performance

This model's performance exhibits notable variations across diverse time horizons and financial indicators. After predicting, the figure of the target (S&P500 index) value and the change of target value can be drawn. The input is the target and different features that vary from groups. After using the model mentioned above, a regression evaluation can be used and the output is shown in the pictures. All the pictures in Figure 1 show the best model in their horizon. The regression evaluation metrics are calculated by the change value of the predicted value and the true value of the target (Avoiding evaluating the index value itself). The RMSE and MAE metrics offer valuable insights into the predictive prowess of this model. Table 1 and Table 2 show the results of RMSE and MAE.

RMSE	blank	USDX	EFFR	VIX	US30Y	US20Y	US10Y	US7Y
1-day	47.7831	48.7075	47.9827	49.3035	47.8874	47.8192	47.9292	48.1814
5-day	92.2823	95.7983	91.9878	99.1853	157.5846	133.8851	152.5618	126.2125
20-day	183.9919	173.7341	302.0017	188.2947	396.0349	296.6774	758.4307	571.4574
RMSE	US5Y	US3Y	US2Y	US1Y	US6M	US3M	US1M	
1-day	48.3179	47.9508	47.7837	47.4222	47.5952	48.1978	47.7664	
5-day	168.6958	136.6147	151.8824	136.541	110.0165	117.7768	96.0132	
20-day	389.5934	426.5298	398.0085	261.923	301.5459	314.9735	299.2177	

Table 1: RMSE of the change value in different groups.



Figure 1: Figure of regression. (a) is True vs Predicted values of 1-day horizon (Close+US1Y), (b) is True vs Predicted changes of the 1-day horizon (Close+US1Y), (c) is True vs Predicted values of the 5-day horizon (Close), (d) is True vs Predicted changes of the 5-day horizon (Close), (e) is True vs Predicted values of the 20-day horizon (Close+USDX), (f) is True vs Predicted changes of the 20-day horizon (Close+USDX) (Photo/Picture credit : Original).

MAE	blank	USDX	EFFR	VIX	US30Y	US20Y	US10Y	US7Y
1-day	36.2807	36.2915	35.9285	37.6879	36.0179	35.9536	36.0336	36.3091
5-day	71.0963	72.8989	70.2543	77.3336	132.9187	111.5851	127.9587	103.846
20-day	148.1766	139.2767	256.1971	143.1215	346.526	250.634	718.5778	523.7565
MAE	US5Y	US3Y	US2Y	US1Y	US6M	US3M	US1M	
1-day	36.4255	36.3041	36.0454	35.6879	35.7133	36.3581	35.8566	
5-day	143.9013	112.3368	124.6026	110.7712	86.4111	93.9518	74.5086	
20-day	348.5007	384.4366	339.1228	223.5755	259.2718	268.1143	261.8683	

Table 2: MAE of the change value in different groups.

4.1.1 RMSE Analysis

1-Day Prediction RMSE: The RMSE values for 1-day predictions are generally low, ranging from 47.4222 for the 1-month U.S. Treasury yield (US1Y) to 49.3035 for the Volatility Index (VIX). The model demonstrates its proficiency in effectively capturing

short-term fluctuations in a wide array of financial indicators.

5-Day Prediction RMSE: As the prediction horizon increases to 5 days, the RMSE values increase significantly, particularly for longer-term interest rates (e.g., US30Y: 157.5846, US20Y: 133.8851) and the VIX (99.1853). This highlights the model's difficulty in accurately predicting longerterm trends, especially for volatile indicators.

20-Day Prediction RMSE: For 20-day predictions, the RMSE values surge even further, with the highest value recorded for the 10-year U.S. Treasury yield (US10Y) at 758.4307. This emphasizes the model's limited ability to anticipate trends over extended periods, particularly for highly sensitive indicators.

4.1.2 MAE Analysis

1-Day Prediction MAE: Similar to RMSE, 1-day MAE values are relatively low, ranging from 35.6879 for US1Y to 37.6879 for VIX. This underscores the model's effectiveness in short-term forecasting.

5-Day Prediction MAE: The MAE values increase for 5-day predictions, particularly for interest rates and VIX, indicating larger average prediction deviations over a longer horizon. However, the increases are less pronounced compared to RMSE, suggesting MAE may be a more stable metric for assessing prediction performance.

20-Day Prediction MAE: For 20-day predictions, MAE values continue to rise, with the highest being 718.5778 for US10Y. This trend aligns with the RMSE analysis, confirming the model's reduced accuracy in long-term forecasting.

4.2 Classification Results

After using a threshold of 0 to define binary labels (Decrease or Increase) based on changes in the target variable, the accuracy and classification report can be shown. Although the best model has the highest accuracy, the RMSE and MAE may not be the lowest but their value is fairly low compared with other groups (The classification report of the best model in different forecast horizons is shown in Table 3.

According to the result of each group, the accuracy is shown in Table 4 while some values are marked in italic because in this group the recall of increase type or decrease type is lower than 0.5 which does not have realistic investment meanings.

1-Day Accuracy: For 1-day predictions, the highest accuracy of 0.7730 is observed for US1Y, followed closely by the USDX and several other yield curves. This suggests that the model performs best in predicting short-term market movements, particularly for the 1-month Treasury yield.

5-Day Accuracy: In the 5-day forecasts, the accuracy decreases significantly across all indicators, with the lowest scores observed for the longer-term Treasury yields (US30Y, US20Y, and US10Y). This decline indicates that predicting market movements over a longer horizon (5 days) introduces more uncertainty and complexity, leading to reduced accuracy.

However, the 1-month Treasury yield again shows relatively higher accuracy (0.736), highlighting the model's potential for short-term predictions.

20-Day Accuracy: For the 20-day forecasts, the accuracy levels are further diluted, with most indicators falling below 0.7. The highest accuracy of 0.7774 is recorded for USDX, suggesting a somewhat stable performance for the currency index over a longer period. However, the significant drops in accuracy for the yield curves indicate that predicting longer-term market trends is challenging.

1 day (Close+US1Y)				5 days (Close)			20 days (Close+USDX)				
	precision	recall	f1		precision	recall	f1		precision	recall	f1
Decrease	0.79	0.74	0.76	Decrease	0.74	0.7	0.72	Decrease	0.82	0.56	0.67
Increase	0.76	0.8	0.78	Increase	0.78	0.81	0.8	Increase	0.76	0.92	0.83
accuracy		0 77		accuracy		0 76		accuracy	accuracy 0.78		

Table 3: Best model in different forecast horizon.

Table 4: Accuracy of each group.										
accuracy	blank	USDX	EFFR	VIX	US30Y	US20Y	US10Y	US7Y		
1-day	0.7623	0.7699	0.7638	0.7638	0.7699	0.7669	0.7623	0.7623		
5-day	0.764	0.7593	0.7236	0.7345	0.6848	0.6863	0.6863	0.6957		
20-day	0.7641	0.7774	0.7021	0.7643	0.6825	0.7038	0.6105	0.6301		
accuracy	US5Y	US3Y	US2Y	US1Y	US6M	US3M	US1M			
1-day	0.7638	0.7638	0.7638	0.773	0.7653	0.7623	0.7592			
5-day	0.6491	0.6941	0.6817	0.6879	0.7283	0.7236	0.736			
20-day	0.6432	0.6694	0.653	0.7021	0.7021	0.7087	0.6939			

5 LIMITATIONS AND FUTURE OUTLOOKS

The present study, while demonstrating the potential of LSTM networks in predicting the S&P 500 index with the augmentation of financial factors, is not without its limitations. One key limitation lies in the reliance on a simple LSTM architecture. As the financial forecasting landscape evolves rapidly, exploring alternative LSTM variants, such as stacked or bidirectional LSTMs, or hybrid architectures combining LSTMs with CNNs or attention mechanisms, could potentially enhance predictive capabilities. Additionally, the evaluation framework, utilizing RMSE, MAE, and classification accuracy, provides valuable insights but may be further refined by incorporating metrics like R-squared for regression or F1-score for imbalanced classification problems.

Looking ahead, the dynamic nature of financial markets necessitates mechanisms for model retraining and adaptation to maintain predictive accuracy over time. Continuous monitoring of market dynamics and regular updating of model parameters are crucial. Moreover, there may be other relevant variables, such as financial news, economic indicators, or sentiment data from social media, that could be incorporated to improve predictive power. Future research should aim to address these limitations by exploring alternative architectures, refining evaluation metrics, incorporating additional data sources, and implementing mechanisms for continuous model updating.

6 CONCLUSIONS

This study has shown the potential ability of LSTM networks to predict the S&P 500 index, particularly when augmented with financial factors. The findings underscore the effectiveness of LSTM models in capturing short-term market fluctuations, evidenced by their relatively low RMSE and MAE values for 1day predictions. However, as the study also highlights, predicting longer-term trends remains a challenge, with errors increasing for 5-day and 20day horizons, especially for variables sensitive to market volatility and interest rate changes. Looking toward the future, it is crucial to acknowledge that the dynamic nature of financial markets necessitates ongoing efforts to maintain predictive accuracy. This includes exploring alternative LSTM variants and hybrid architectures, refining evaluation metrics,

incorporating additional information sources encompassing financial updates, economic metrics, and public opinion reflected on social media platforms, and implementing mechanisms for continuous model updating and adaptation. By addressing these limitations and harnessing the full potential of LSTM networks, the model can further enhance the ability to forecast the S&P 500 index while providing valuable insights for investors, portfolio managers, policymakers, and so on.

REFERENCES

- Atsalakis, G. S., Valavanis, K. P., 2009. Surveying stock market forecasting techniques–Part II: Soft computing methods. Expert Systems with applications,36(3), 5932-5941.
- Bhandari, H. N., Rimal, B., Pokhrel, N.R., Rimal, R., Dahal, K. R., & Khatri, R. K., 2022. Predicting stock market index using LSTM. Machine Learning with Applications,9, 100320.
- Ding, G., Qin, L., 2020. Study on the prediction of stock price based on the associated network model of LSTM. International Journal of Machine Learning and Cybernetics, 11(6), 1307-1317.
- Lee, J., Kang, J., 2020. Effectively training neural networks for stock index prediction: Predicting the S&P 500 index without using its index data. PloS one, 15(4), e0230635.
- Michańków, J., Sakowski, P., Ślepaczuk, R., 2022. LSTM in algorithmic investment strategies on BTC and S&P500 index. Sensors, 22(3), 917.
- Mehtab, S., Sen, J., Dutta, A., 2021. Stock price prediction using machine learning and LSTM-based deep learning models. In Machine Learning and Metaheuristics Algorithms, and Applications: Second Symposium, SoMMA 2020, Chennai, India, October 14-17, 2020, Revised Selected Papers 2 (pp.88-106). Springer Singapore.
- Pramod, B. S., Pm, M. S., 2020. Stock price prediction using LSTM.Test Engineering and Management, 83, 5246-5251.
- Roszyk, N., Ślepaczuk, R., 2024. The Hybrid Forecast of S&P 500 Volatility ensembled from VIX, GARCH and LSTM models.arxiv preprint arxiv:2407.16780.
- Vargas, M. R., De Lima, B. S., Evsukoff, A. G., 2017. Deep learning for stock market prediction from financial news articles. In 2017 IEEE international conference on computational intelligence and virtual environments for measurement systems and applications (CIVEMSA) (pp. 60-65). IEEE.
- Vo, N., Ślepaczuk, R., 2022. Applying hybrid ARIMA-SGARCH in algorithmic investment strategies on S&P500 index. Entropy, 24(2), 158.
- Wang, C., Chen, Y., Zhang, S., Zhang, Q., 2022. Stock market index prediction using deep Transformer model. Expert Systems with Applications, 208, 118128.