

Hybrid Approach based on SARIMA and Artificial Neural Networks for Knowledge Discovery Applied to Crime Rates Prediction

Felipe A. L. Soares^a, Tiago B. Silveira^b and Henrique C. Freitas^c

Graduate Program in Informatics, Pontifícia Universidade Católica de Minas Gerais (PUC Minas),
Belo Horizonte, MG, Brazil

Keywords: Crime Rate Prediction, Mathematical Models, Artificial Neural Networks, SARIMA, Time Series, Knowledge Discovery.

Abstract: The fight against crime in Brazilian cities is an extremely important issue and has become a priority agenda in public, statutory or municipal discussions. Even so, reducing cases of violence is a complex task in large Brazilian cities, such as Rio de Janeiro and São Paulo, as these large cities have vast criminal points. Therefore, this paper presents the steps followed in the process of knowledge discovery applied to prediction of crime rate numbers in different regions of São Paulo city in order to better understand it and distribute the security forces more efficiently. Then, a hybrid model composed of an Artificial Neural Network and the SARIMA mathematical model was applied to databases related to different areas of the city. The average results showed assertiveness rates of 83.12% and 76.78% and root mean square deviation of 1.75 and 2.16 for two different tests.

1 INTRODUCTION

According to Lourenço et al. (2016), the fight against crime in Brazilian cities is an extremely important issue and the increase in cases of violence in certain regions worries the government authorities. The fight against crime must take place effectively, applying the available resources correctly.

With a direct impact on trade and industry in general, high crime rates coupled with low effectiveness of security forces are responsible for recurring expenses and expenditures in these sectors. Among these expenditures, private security investment accounts for most of the costs, followed by theft loss.

According to Tobar (2015), there is an increase in cases of violence in large cities and the theme has become a priority agenda in public discussions, whether statutory or municipal. However, reducing the number of cases of violence is a complex task in the large Brazilian metropolises, such as Rio de Janeiro and São Paulo, as they have vast criminal spots, which makes the analysis of past occurrences complex.

The analysis and extraction of knowledge from

these data allows the best distribution of security forces in order to effectively serve the population, allowing a more assertive allocation of them. According to He and Zheng (2009), the use of computational resources is fundamental in the process of knowledge discovery, helping decision making. However, these decisions are often made from feeling, which ultimately reduces efficiency.

Given this context, it is necessary to determine ways to make the allocation process of police resources more efficient, replacing or combining human feeling with computational techniques, in order to combat the high crime rates (Júnior et al., 2016).

Thus, the main contribution of this work is the proposal of a hybrid approach for the most efficient allocation of security resources, based on the use of the knowledge discovery process suggested by Fayyad et al. (1996). We used techniques for predicting time series values, in order to predict the amount of crime in different regions in the city of São Paulo (Brazil).

The results were obtained from a hybrid approach, combining the predictive results of the Seasonal Autoregressive Integrated Moving Average Model (SARIMA) and an Artificial Neural Network (ANN) applied to databases composed of crimes grouped by their geolocation. From this approach, it was possi-

^a <https://orcid.org/0000-0002-4141-060X>

^b <https://orcid.org/0000-0001-5378-2251>

^c <https://orcid.org/0000-0001-9722-1093>

ble to obtain satisfactory results, reaching an average of 76.68% assertiveness in the prediction of occurrence bulletins, thus presenting the efficiency in the use of computational models applied to knowledge discovery.

The remainder of this paper is organized as follows: Section 2 presents related work about knowledge discovery in crime-related areas. Section 3 presents the methodology, tests and the results obtained. Finally, Section 4 presents the conclusions and suggestions for future work.

2 RELATED WORK

Several papers seek to find ways to improve crime-related decision-making performance. Among these, Gerber (2014) and Wang et al. (2012) investigated how the use of tweets on the social network Twitter can help in prediction actions of crimes.

Gerber (2014) showed that, for 19 of the 25 types of crimes studied, Twitter data improves crime prediction performance compared to standard approaches. The author used linguistic analysis specific to Twitter and the statistical modeling of topics. The work has implications specifically aimed at criminal justice decision makers and those responsible for allocating resources for crime prevention.

Wang et al. (2012) studied how Twitter data can help predict crimes. The model was used to predict future hit and run crimes. The results indicated that the approach surpasses a reference model that also predicts this type of crime.

Silva et al. (2017) present an interactive system for analyzing criminal data in the state of Rio de Janeiro (Brazil), which provides graphical visualizations such as time series graph, projections, dispersion graph and parallel coordinates graph, based on data provided by the Institution Public Security. The system allows extracting important information on government policies related to the area of public security. In addition, the work also presents a case study to evaluate the developed system.

Almanie et al. (2015) analyzed databases from Denver and Los Angeles, both located in the United States (USA), using the Decision Tree and Naive Bayes classifiers to predict possible types of crimes. Applied to the cross-validation strategy, Naive Bayes achieved an accuracy of 51% and 54%, while the Decision Tree was accurate to 42% and 43% for both Denver and Los Angeles respectively. Iqbal et al. (2013) applied the same algorithms to crime databases from different US states to predict the category of crimes. The results showed that, in this con-

text, the Decision Tree surpasses Naive Bayes having an accuracy of 83.95%.

Wawrzyniak et al. (2018) developed techniques for predictive modeling using ANN deep learning. For this, the authors adopted databases from two regions of Poland, separated by different regions, and used the weekly seasonality of the database.

Cherian and Dawson (2015) used machine learning and statistical techniques for San Francisco crime classification and prediction problems. Among the machine learning algorithms, Random Forest was used, with a maximum precision of 31.84% for the proposed prediction.

Within the context of crime prediction in Brazilian cities, Júnior et al. (2016) performed the prediction using time series approach analyzing the amount of police occurrences in the city of Natal (Brazil), taking into account strategic regions adopted by the police. For this, a Autoregressive Integrated Moving Averages Model (ARIMA) was used, with the mean absolute percentage error (MAPE) of 0.3420 in the diagnoses.

Loureço et al. (2016) developed a system called Predictive Policing Support System (SiAPP) for analyzing and predicting crime-related patterns using machine learning. From automatic collections, creation of logical rules and geographical visualization of the discovered patterns, the results showed that the predictions for the region of Niterói (Brazil) had an accuracy greater than 83%.

Table 1 illustrates the differences between related papers from the literature and our proposed work, comparing the algorithms used in each study (Used Algorithms). In addition, for the tests and executions of the algorithms proposed in the works, databases referring to different locations were used, and these locations are also compared in this table (Locality). The literature does not present hybrid approaches for knowledge discovery, using mathematical models and ANN, applied to the prediction of the occurrence of crimes in a Brazilian city, which differs the proposed work from other works in the literature.

3 METHODOLOGY AND RESULTS

The database related to crimes in the city of São Paulo (Brazil) from 2006 to 2016 can be found at *Kaggle*¹. This base was used in the development of

¹<https://www.kaggle.com/inquisitivecrow/crime-data-in-brazil>. Accessed on July 4, 2019.

Table 1: Overview of related work.

Related Work	Used Algorithms	Locality
Júnior et al. (2016)	Mathematical model ARIMA	Natal (Brazil)
Almanie et al. (2015)	Naive Bayes and Decision Tree	Denver and Los Angeles (USA)
Iqbal et al. (2013)	Decision Tree and Naive Bayes	Different US States
Cherian and Dawson (2015)	Random Forest	San Francisco (USA)
Loureço et al. (2016)	Logical-relational learning through inductive logic programming	Niterói (Brazil)
Wawrzyniak et al. (2018)	ANN	Poland Regions
Our Proposed Work	Mathematical model SARIMA and ANN	São Paulo (Brazil)

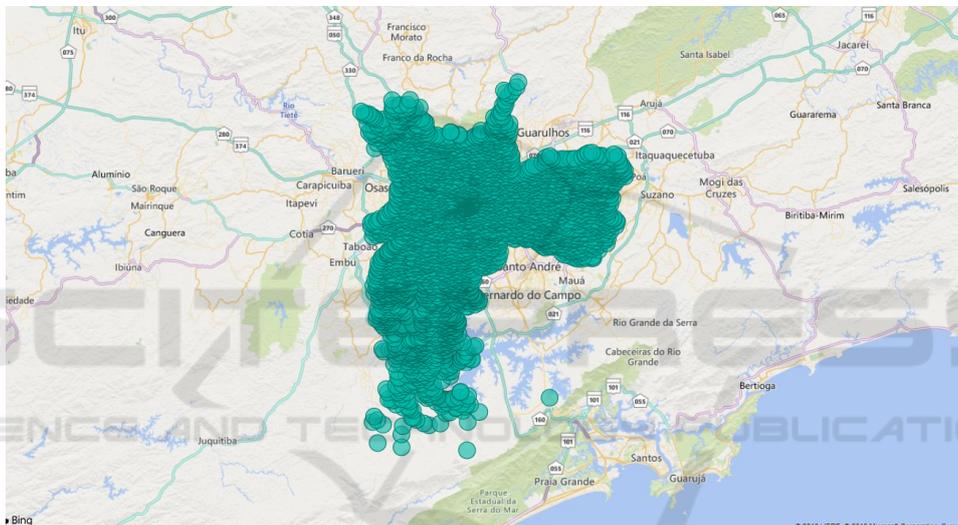


Figure 1: Crime locations in São Paulo.

the knowledge discovery process, and for that, it was necessary to prepare and verify its consistency.

According to Fayyad et al. (1996), knowledge discovery has five phases: the first is the selection where the data is organized, the second, called pre-processing, the data is analyzed and goes through an adequacy. In the third, the data is stored in order to facilitate the use of data mining techniques, which are applied in the fourth phase, and, finally, the interpretation and evaluation of the results is performed, verifying if the generated information has validity for the proposed problem.

Step 1 - Data Selection

First the data are analyzed in order to raise important points to predict the amount of crimes in different locations in the city of São Paulo. This step is to verify

their structure, from which it is determined which information is useful for the process of knowledge discovery.

After these definitions, data on the location of the crimes (latitude and longitude), as well as the date and time of the occurrence were selected and stored on a separate basis for the preprocessing step. Figures 1 and 2 show the locations with crime occurrences.

Step 2 - Preprocessing

The preprocessing step is responsible for analyzing the data from the Selection step. In this part, repeated, missing and discrepant data are identified. These data are processed in order to make them useful or to determine their disposal. This process is fundamental to make a homogeneous database, making possible a better processing by the algo-

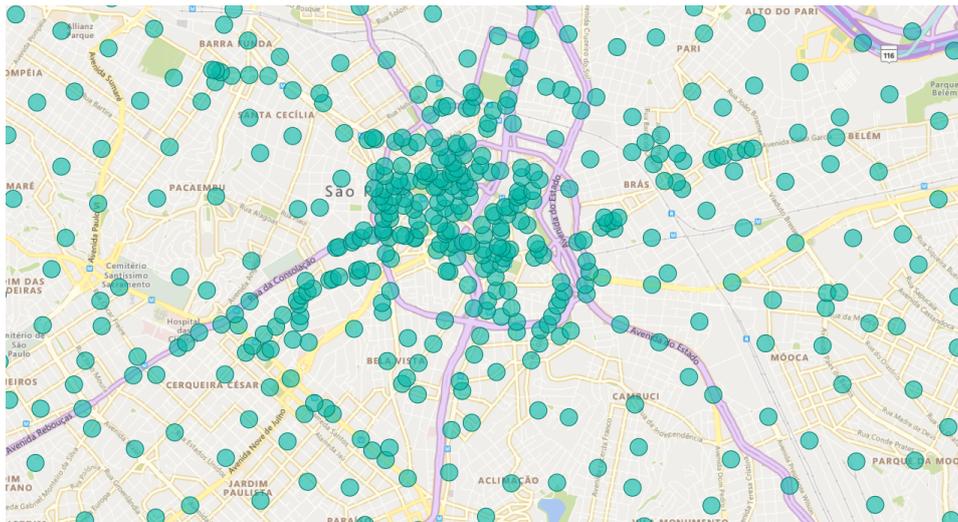


Figure 2: Crime locations in São Paulo neighborhoods.

rhythms, avoiding discrepancies and increasing the assertiveness percentage.

In the case study, we analyzed all occurrences with identification of the police station, year of the occurrence report and number of the same occurrence report (following the data documentation). Subsequently, all incomplete or repeated occurrences were removed from the data.

For detecting outliers, fields containing latitude and longitude were taken into account. From the analysis of these columns it was possible to determine occurrences whose coordinates represented discrepant locations of the group, these data were treated as outliers, being removed from the database.

In order to determine the occurrence of crimes in different areas of the city of São Paulo, it was necessary to subdivide the database by geolocation. Thus, the occurrences were subdivided into clusters or quadrants, aiming to reduce the problem in smaller groups. Thus, predictions can be made in isolated regions such as neighborhoods, communities, and surrounding specific regions such as parks, subway stations, event areas, and football stadiums, according to the needs or definitions of the authorities responsible for security matters.

The division was carried out in 15 different ranges according to the length of the crime occurrences, and each range has the same longitude spacing. Latitude was not considered for the creation of these tracks. Table 2 illustrates the minimum and maximum longitude of each range used to show the technique.

It is worth mentioning that both the number of ranges created and the technique used to perform these divisions can and should be changed according to the needs of those responsible for security matters.

Table 2: Longitude subdivision performed.

Data	Min. Longitude	Max. Longitude
C1	-46.82275°	-46.79229°
C2	-46.79229°	-46.76183°
C3	-46.76183°	-46.73137°
C4	-46.73137°	-46.70091°
C5	-46.70091°	-46.67045°
C6	-46.67045°	-46.63999°
C7	-46.63999°	-46.60953°
C8	-46.60953°	-46.57907°
C9	-46.57907°	-46.54861°
C10	-46.54861°	-46.51815°
C11	-46.51815°	-46.48769°
C12	-46.48769°	-46.45723°
C13	-46.45723°	-46.42677°
C14	-46.42677°	-46.39631°
C15	-46.39631°	-46.36584°

Figure 3 illustrates the subdivisions defined in Table 2, where different colors represent different clusters. The participation of a domain expert is indicated during the second step of the knowledge discovery process to improve cluster division. The expert has the role of determining the type of data grouping from knowledge and feeling about the problem, thus directing the analysis to specific regions, improving the local allocation of security forces from a more accurate estimate. the amount of resources to be allocated in the predetermined groups.

Finally, as the last preprocessing step, the occurrences of each cluster are grouped according to date, turning the base into a time series in the format shown



Figure 3: Data division into clusters.

in Table 3.

Table 3: Time series example.

Date	Total occurrences
2016-12-01	99
2016-12-02	87
2016-12-03	92
2016-12-04	75

Therefore, the total occurrences represents the number of occurrences that happened on that specific day, and for each day in the database there will be this corresponding quantity. It is worth mentioning that the grouping can be performed in different time intervals (such as day or multiple intervals per day) that should preferably be defined by the domain specialist. The result must always be a time series for the technique presented in this work.

For better knowledge of the data belonging to the clusters generated, statistical calculations were performed on them. Table 4 illustrates these calculations applied to the amount of crime in each database.

Step 3 - Data Storage

After the previous steps, filtered and preprocessed information is stored in databases prepared for applying data mining techniques. The database was then subdivided into 15 smaller ones, representing different locations in the city of São Paulo. However, it is suggested the analysis of a domain expert to organize the data in order to meet the needs.

Table 4: Statistical calculations performed on databases.

Data	Min.	Max	Mean	Std.
C1	8	71	39.25	9.6
C2	18	120	67.06	14.19
C3	19	91	54.02	11.69
C4	10	55	33.69	8.45
C5	9	84	52.16	12.34
C6	19	108	72.63	15.91
C7	10	56	33.85	8.26
C8	12	70	39.52	9.69
C9	16	107	67.83	15.25
C10	10	97	51.8	11.91
C11	9	68	42.03	9.76
C12	6	48	22.86	6.78
C13	13	76	42.67	9.98
C14	9	57	31.69	7.96
C15	26	199	89.12	17.58

The stored data has information about the locality, containing the latitude and longitude of the occurrence, as well as its date and time.

Step 4 - Data Mining Techniques

After the data preparation and storage steps, Step 4 consists of applying data mining techniques. The techniques chosen to predict the amount of crime in different regions of the city of São Paulo were: mathematical model SARIMA and ANN.

According to Martinez et al. (2011), the SARIMA

model is useful in situations where the database is a set of time series that have seasonal periods that occur with the same time intensity (either time, day, month or year). Already ANN use methods that simulate the problem solving ability of human brains in information systems (Kraft et al., 2003). Both algorithms have good applicability and assertiveness in future prediction systems, and the union of the two methods can assist in the prediction of both seasonal (using SARIMA) and atypical (using ANN) situations.

For setting the SARIMA parameters, the Autocorrelation (*ACF*) and Partial Autocorrelation (*PACF*) Functions were used, thus defining the best order and seasonal order parameters for each grouping within the time base characteristics. The ANN was implemented using a sequential model of the Tensor Flow package with 1000 neurons in the first layer and 100 in the second, using the total of 2000 epochs, inputting dates that change the seasonal component of the series, such as holidays, recesses and events in the city, generating a quantitative output. Both algorithms were implemented in Python and the ANN settings were defined from empirical tests.

The databases were subjected to a seasonal decomposition step. From the calculations performed at this stage, a seasonal period of 7 days was determined for the bases. This period was used in the SARIMA model. From observations in the databases, it was also possible to determine changes in the incidence of occurrences on holidays, optional points and dates that occurred special events (such as football games, concerts and events), being called *special events*. This information, along with the day, month, year, and day of the week, was used as input to ANN.

Step 5 - Results Interpretation and Evaluation

From the results obtained by the SARIMA method and the ANN method, a model for the union of these results was proposed. We used values found by ANN on dates that differed from the linear component of the series, (*special events*), and the results of the SARIMA method for occurrences on normal days. The use of this approach provided a gain in the assertiveness of the proposed method, where it takes into account dates whose seasonality is not effective.

To perform the tests and validate the results, predictions were made for the events of November 2016 and December 2016 in all predetermined sub-groups. The results were compared with the actual values of the data.

The results interpretation and analysis is funda-

mental for the knowledge extraction process. For this, two evaluation parameters were used: the assertiveness of the algorithm and the Root Mean Square Deviation (RMSD). Assertiveness is the percentage that represents the proximity of the prediction to the real value, and its formula is presented in Equation 1:

$$\delta = (1 - |1 - P_i/O_i|) * 100 \quad (1)$$

where δ represents assertiveness, P_i represents predicted value and O_i represents actual value. This formula is derived from Equation 2 and it normalizes the values within the range of 0% to 100%.

$$\delta = (P_i/O_i) * 100 \quad (2)$$

According to Willmott (1982), RMSD is one of the best general measures of model performance and its error value is presented in the same dimensions as the analyzed variable. The RMSD measure is given by Equation 3:

$$RMSD = \sqrt{\frac{1}{n} \sum_{i=1}^n (P_i - O_i)^2} \quad (3)$$

where P_i is the predicted value, O_i is the actual observed value, and n is the amount of values analyzed. The closer the RMSD result is to 0, the greater the assertiveness of the algorithm.

Table 5 illustrates the assertiveness and RMSD of the mathematical model SARIMA, ANN and the union of the two models in each database (representing each region of the city of São Paulo) from the tests performed for the month of November. The results were satisfactory, with the highest assertiveness 86.83% (C15) and the best RMSD 0.81 (C12), and the average assertiveness of the 15 clusters 83.12% and the average of RMSD 1.75.

To prove the results found in the tests carried out for the month of November, the same tests were carried out for the month of December. Table 6 illustrates the assertiveness and RMSD of the mathematical model SARIMA, ANN and the union of the two models in each database of São Paulo from the tests performed for the month of December. The results were satisfactory, with the highest assertiveness 85.41% (C13) and the best RMSD 1.25 (C12), and the average assertiveness of the 15 clusters 76.68% and the average of RMSD 2.16.

The results using the union of the SARIMA mathematical model with ANN (SARIMA+ANN) showed (for almost all cases with exceptions in only two of them) better results, both in the assertiveness and in the *RMSD* compared to the results using only the mathematical model SARIMA or only ANN.

Table 5: Assertiveness and RMSD results for Test 1 - November 2016.

Data	δ		RMSD		δ		RMSD	
	<i>SARIMA</i>	<i>SARIMA</i>	<i>ANN</i>	<i>ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>
C1	82.46%	1.41	80.23%	1.78	83.80%	1.31		
C2	83.63%	2.86	83.86%	3.07	85.53%	2.66		
C3	83.12%	2.07	76.17%	2.63	82.50%	2.13		
C4	77.97%	1.41	74.88%	1.58	79.13%	1.32		
C5	84.65%	1.79	83.02%	1.97	86.00%	1.64		
C6	84.92%	2.43	84.36%	2.54	85.79%	2.39		
C7	78.30%	1.56	73.70%	1.91	79.02%	1.54		
C8	81.45%	1.63	74.76%	2.08	82.29%	1.60		
C9	82.05%	2.51	77.70%	3.04	82.87%	2.52		
C10	79.86%	2.03	81.06%	2.05	83.28%	1.71		
C11	81.19%	1.63	82.50%	1.69	83.32%	1.47		
C12	79.33%	0.88	64.51%	1.79	81.66%	0.81		
C13	81.70%	1.54	71.54%	2.29	82.66%	1.44		
C14	81.01%	1.29	70.10%	2.00	82.11%	1.25		
C15	85.10%	2.80	69.31%	5.46	86.83%	2.50		
Mean	81.78%	1.86	76.51%	2.39	83.12%	1.75		

Table 6: Assertiveness and RMSD results for Test 2 - December 2016.

Data	δ		RMSD		δ		RMSD	
	<i>SARIMA</i>	<i>SARIMA</i>	<i>ANN</i>	<i>ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>
C1	70.18%	1.96	75.71%	1.58	75.31%	1.67		
C2	76.34%	2.79	76.67%	2.43	81.75%	2.47		
C3	76.16%	2.06	67.74%	2.92	80.10%	1.98		
C4	68.81%	1.69	65.07%	1.94	73.27%	1.61		
C5	69.43%	2.78	61.54%	3.36	70.75%	2.65		
C6	74.27%	3.45	70.80%	3.70	77.78%	3.33		
C7	77.04%	1.35	70.25%	1.73	79.50%	1.37		
C8	71.87%	1.75	66.32%	2.17	73.67%	1.81		
C9	68.88%	3.46	67.66%	3.62	74.02%	3.18		
C10	71.08%	2.36	63.83%	3.10	74.13%	2.30		
C11	65.10%	2.25	64.15%	2.37	69.49%	2.13		
C12	70.53%	1.26	62.78%	1.49	73.90%	1.25		
C13	80.96%	1.59	79.24%	1.73	85.41%	1.49		
C14	76.53%	1.29	74.64%	1.46	79.45%	1.30		
C15	77.39%	4.02	74.70%	4.24	81.62%	3.83		
Mean	72.97%	2.27	69.41%	2.52	76.68%	2.16		

The results found by the model for the tests performed in December were compared with the prediction results using an approach based on the Random Forest algorithm configured with 1000 trees, in which this configuration was defined from empirical tests. According to Breiman (2001), this

algorithm combines several decision trees to perform the prediction.

Therefore, the comparison allows us to visualize the gain of our proposed approach related to the algorithms used in other works. (Almanie et al., 2015), (Iqbal et al., 2013), (Cherian and Dawson, 2015).

Table 7: Comparison between Random Forest (RF) and our proposed approach (SARIMA+ANN).

Data	δ	RMSD	δ	RMSD
	<i>RF</i>	<i>RF</i>	<i>SARIMA + ANN</i>	<i>SARIMA + ANN</i>
C1	63.29%	12.16	75.31%	1.67
C2	65.04%	20.83	81.75%	2.47
C3	76.43%	11.99	80.10%	1.98
C4	64.24%	9.43	73.27%	1.61
C5	55.67%	17.24	70.75%	2.65
C6	68.98%	20.01	77.78%	3.33
C7	77.03%	8.61	79.50%	1.37
C8	71.33%	10.61	73.67%	1.81
C9	63.19%	19.75	74.02%	3.18
C10	60.94%	57.11	74.13%	2.30
C11	57.11%	13.61	69.49%	2.13
C12	62.84%	7.74	73.90%	1.25
C13	78.01%	9.99	85.41%	1.49
C14	72.65%	8.15	79.45%	1.30
C15	71.46%	22.99	81.62%	3.83
Mean	67.21%	13.88	76.68%	2.16

Table 7 illustrates the comparison of the assertiveness (δ) and RMSD results using Random Forest (RF) and the proposed approach (SARIMA+ANN), showing that the proposed approach has higher assertiveness and lower RMSD in the results of all clusters, showing that it is more efficient.

The algorithms results can assist in the police forces distribution within the defined regions. Thus, clusters in which the predictive outcome indicated a higher number of crimes should receive greater attention from security forces in relation to clusters whose predicted number of crimes was lower. Thus, prediction can define how many future crimes will be in each given region, advancing police actions, reducing idleness, and thereby helping to prevent crime.

4 CONCLUSIONS

Proposing strategies to reduce crime rates has become a priority in public discussions, as reducing violence is a complex task in the large Brazilian metropolises. Within this scenario, the knowledge discovery process is a powerful decision-making tool, providing techniques to solve the problem of correct resource allocation, which in this context reflects the distribution of security forces as appropriately as possible.

This way, our work used stages of the knowledge

discovery process, applying Mathematical Models and Artificial Neural Networks in order to obtain predictions to make the resource allocation process more assertive. The proposal consists of a hybrid approach, combining predictive results from the SARIMA Mathematical Model and results achieved by an Artificial Neural Network, to predict the number of future crime occurrences in different regions of the city of São Paulo.

Tests and results showed that the found patterns were satisfactory for the proposed predictions, obtaining average hit rates of 83.12% and 76.78% and RMSD of 1.75 and 2.16 for the two tests performed. The presented technique has the potential to reduce the percentage of crimes in the analyzed areas, enabling a method that seeks to improve the distribution of police forces to serve the population more effectively.

For further tests, it is suggested to divide the regions alongside a specialist in the field of public security, in order to predict the amount of crimes in strategic regions to combat them.

ACKNOWLEDGEMENTS

The present work was carried out with the support of the Coordenação de Aperfeiçoamento de Pessoal de Nível Superior - Brazil (CAPES) - Financing Code 001. The authors thank CNPq, FAPEMIG, PUC Mi-

nas and REVEX for the partial support in the execution of this work.

REFERENCES

- Almanie, T., Mirza, R., and Lor, E. (2015). Crime prediction based on crime types and using spatial and temporal criminal hotspots. *CoRR*, abs/1508.02050.
- Breiman, L. (2001). Random forests. *Machine Learning*, 45(1):5–32.
- Cherian, J. and Dawson, M. (2015). Robocop: Crime classification and prediction in san francisco. *Forest*, 15:70–69.
- Fayyad, U., Piatetsky-Shapiro, G., and Smyth, P. (1996). From data mining to knowledge discovery in databases. *AI magazine*, 17(3):37.
- Gerber, M. S. (2014). Predicting crime using twitter and kernel density estimation. *Decision Support Systems*, 61:115 – 125.
- He, T. and Zheng, S. (2009). Time series analysis and forecast based on active learning artificial neural network. In *2009 Second International Symposium on Knowledge Acquisition and Modeling*, volume 1, pages 84–87.
- Iqbal, R., Murad, M. A. A., Mustapha, A., Panahy, P. H. S., and Khanahmadliravi, N. (2013). An experimental study of classification algorithms for crime prediction. *Indian Journal of Science and Technology*, 6(3).
- Júnior, A. D. d. A., Martins, A. d. M., Verdier, R., and Cacho, N. A. A. (2016). Predição de ocorrências policiais em natal: Uma abordagem em análise de séries temporais. *Workshop sobre cidades inteligentes – WCID 2016*.
- Kraft, M. R., Desouza, K. C., and Androwich, I. (2003). Data mining in healthcare information systems: case study of a veterans’ administration spinal cord injury population. In *36th Annual Hawaii International Conference on System Sciences, 2003. Proceedings of the*, pages 9 pp.–.
- Lourenço, V., Mann, P., Paes, A., and de Oliveira, D. (2016). Siapp: Um sistema para análise de ocorrências de crimes baseado em aprendizado lógico-relacional. In *Anais do XII Simpósio Brasileiro de Sistemas de Informação*, pages 168–175, Porto Alegre, RS, Brasil. SBC.
- Martinez, E. Z., Silva, E. A. S. S., and Fabbro, A. L. D. (2011). A SARIMA forecasting model to predict the number of cases of dengue in Campinas, State of São Paulo, Brazil. *Revista da Sociedade Brasileira de Medicina Tropical*, 44:436 – 440.
- Silva, L. J. S., González, S. F., Almeida, C. F. P., Barbosa, S. D. J., and Lopes, H. (2017). Crimevis: An interactive visualization system for analyzing crime data in the state of rio de janeiro. In *Proceedings of the 19th International Conference on Enterprise Information Systems - Volume 1: ICEIS*, pages 193–200. INSTICC, SciTePress.
- Tobar, F. S. (2015). Tendências criminais sul-americanas em perspectiva comparada. In *Revista Brasileira de Segurança Pública*, volume 9, pages 88–109, São Paulo, SP, Brasil.
- Wang, X., Gerber, M. S., and Brown, D. E. (2012). Automatic crime prediction using events extracted from twitter posts. In Yang, S. J., Greenberg, A. M., and Endsley, M., editors, *Social Computing, Behavioral - Cultural Modeling and Prediction*, pages 231–238, Berlin, Heidelberg. Springer Berlin Heidelberg.
- Wawrzyniak, Z. M., Jankowski, S., Szczechla, E., Szymański, Z., Pytlak, R., Michalak, P., and Borowik, G. (2018). Data-driven models in machine learning for crime prediction. In *2018 26th International Conference on Systems Engineering (ICSEng)*, pages 1–8.
- Willmott, C. J. (1982). Some comments on the evaluation of model performance. *Bulletin of the American Meteorological Society*, 63(11):1309–1313.