

A Data Driven Approach to Derive Traffic Intersection Geography using High Resolution Controller Logs

Dhruv Mahajan, Tania Banerjee, Yashaswi Karnati, An. Rangarajan and Sanjay Ranka

Department of Computer and Information Science and Engineering, University of Florida, Gainesville, FL, U.S.A.

Keywords: Loop Detectors Systems, ATSPM, Controller Logs, Detector Mappings, Detector Configuration, Data Mining.

Abstract: Current traffic signal controllers are capable of recording events (signal events; vehicle arrival and departure) at very high resolutions (usually, 10Hz). The high resolution data rates enable the computation and study of various (granular) measures of effectiveness. However, without knowing the location of specific detectors on an intersection and the phases they are mapped to, a number of measures of effectiveness (of signal performance) cannot be evaluated. These mappings may not be available or up to date for many practical reasons (e.g., old infrastructure, mappings not machine readable, maintenance or addition of new lanes, etc.). In this paper, we develop an inference engine to map detectors to phases and distinguish between the stop bar and advance detectors, or in other words, infer the location of the loop detectors with reference to the intersection.

1 INTRODUCTION

Traffic signals are crucial in managing vehicular and pedestrian traffic at an intersection where two or more road segments meet. The new generation of signal controllers, based on the latest Advanced Transportation Controller (ATC) (Intelligent Transport Systems, 2009) standards, are capable of recording signal events as well as vehicle arrival and departure events at a very high resolution (10Hz). As a result of the high resolution data rates, it is now possible to compute signal performance metrics such as arrivals on red, arrivals on green, and platooning ratios on a cycle by cycle or sub cycle basis (U.S. Department of Transportation, 2013). A standard 4-way intersection with actuated or semi-actuated control, as shown in Figure 2, has eight *phases* (or directions of vehicular movement) and 4 ways to *approach* the intersection given by Figure 1. Each approach usually has multiple lanes and can have one or two permitted phases. There may be more than one vehicle *detector* on each lane. There are usually many detectors (e.g. stop bar detectors and advanced detectors) at an intersection, with more than one detector per lane. These can be of different types, however most detectors (at the very least) report vehicle arrivals and departures. Given a detector identifier in the log file, it is essential to know where the detector is located in the intersection to make meaningful observations about traffic behavior and the performance of the intersection. Thus, for

effective computation of performance measures, we need to have detector to phase mappings. The phase represents the direction of traffic movement on an intersection. Additionally, we would like the mappings indicate the location of a detector, such as advanced or stop-bar.

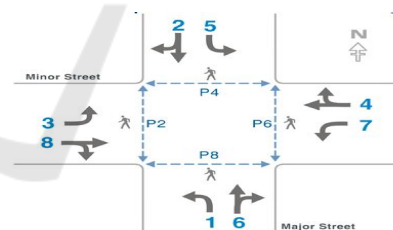


Figure 1: Phase Diagram Showing Vehicular & Pedestrian Movement at a Four Way Intersections. The Solid Gray Arrows Show Vehicle Movements (or *phases*). (U.S. Department of Transportation, 2008).

In many practical situations, these mappings are missing (e.g., the infrastructure was built decades ago and the mappings are not available in a machine-readable form) or incorrect (e.g., during maintenance or addition of new lanes, the contractor forgot to update the mappings). The absence of a detector to phase mapping limits the value of the high-resolution controller logs. This problem is further detailed in Section 2.

Our goal in this paper is to find the best mapping of detectors to phases and to classify detectors

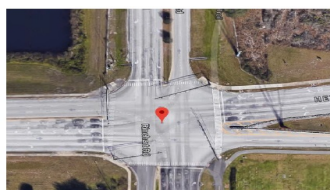


Figure 2: Example of a Standard 4 Way Intersection (*I*).

as stop-bar detectors or advance detectors based *only* on events in the high-resolution controller logs. These events include a change in the signaling state (for example, green, yellow, or red for vehicles, and walk, flashing do not walk, and do not walk for pedestrians) and a change in the detector state (based on whether the detection area is occupied or not).

Our algorithms are based on the following overarching intuition:

1. During normal traffic conditions, the traffic passing a detector when the corresponding phase is green will be higher than the other detectors.
2. During very low traffic conditions, the sequence of timestamps of vehicle arrivals and departures can be used to separate advance detectors from stop bar detectors.

Our goal is to develop automated machine-learning methods that derive these mappings using several months of loop detector data. This required us to develop the following novel approaches:

1. Automatically decomposing data streams into cycles and cluster these cycles based on similar phase timing patterns. This is necessary because combining data across multiple, distinct types of patterns can lead to lower discrimination between green versus red behavior. For this purpose, we developed frequent pattern mining based on n-grams and then applied clustering algorithms to derive clusters of similar cycles.
2. For really low volume cycles (e.g., during nighttime), when only one vehicle is potentially present, the time of arrival and departure along with signal timing data can be used to derive ordering of detectors. We develop algorithms that can leverage this information across multiple such cycles.
3. For low to medium volume cycles, we developed algorithms that can use green versus red departure information to derive a small subset of feasible phases for each detector. We then use frequent set mining within a given cycle cluster to derive a consistent mapping for that cluster.
4. We have developed algorithms to combine detector mappings derived for each cluster of similar

cycles to arrive at the overall mapping and the detector type.

Since some non-conflicting phases are synchronized, it may be infeasible to narrow down the mapping of a detector to one particular phase. Hence, to quantify the quality of mapping, we compute the prediction factor, which is the ratio of the number of detector-to-phase assignments obtained using our algorithms to the number of the actual detector-to-phase assignments. Ideally, the prediction factor should be 1. We applied our algorithms to 10 intersections on an arterial and found that the prediction factor was 1.3. For this set of 10 intersections, our prediction coincided with the available mappings, and we were able to map some more detectors unambiguously to one phase.

Figure 3 shows the overall flow diagram for our inference engine. The problems of developing an inference engine for detector locations (i.e., the approach or phase they belong to) and types from high-resolution controller logs may be divided into three parts. The first part is to map the detectors to phases. The second part is to classify the detectors as stop bar or advance detectors, using the controller logs. The last part is to use the inference engine to validate and update any known detector mappings. These three steps are described in Section 3, Section 4, and Section 5 respectively. Section 5 also presents the results obtained from several intersections, and the conclusions are presented in Section 6.

2 RELATED WORK

Traffic data that accurately reflect real-time traffic network conditions plays a very important role in improving traffic efficiency in Intelligent Transportation Systems (ITS) (Martin, 2013). The implementation and uses of an inductive loop detector system have been described in detail by Pursula et al. in (Pursula and Kosonen, 1989). Several measures of effectiveness used in recent times are heavily dependent on phase-specific traffic analysis. Purdue Coordination Diagrams (PCDs), arrivals on green (AOG) versus those on red (AOR), and other such measures (U.S. Department of Transportation, 2008; Day et al., 2014) need to precisely record the phase and location corresponding to vehicle arrivals. Yogesh et al. (Yogesh et al., 2018) also aim to improve the performance and efficiency of signalized intersections by proposing an improved design and signal processing algorithm to facilitate lane-by-lane detection in serially connected loop detectors. Lu et al. (Lu et al., 2008) propose ways to detect fault(s) in loop detection

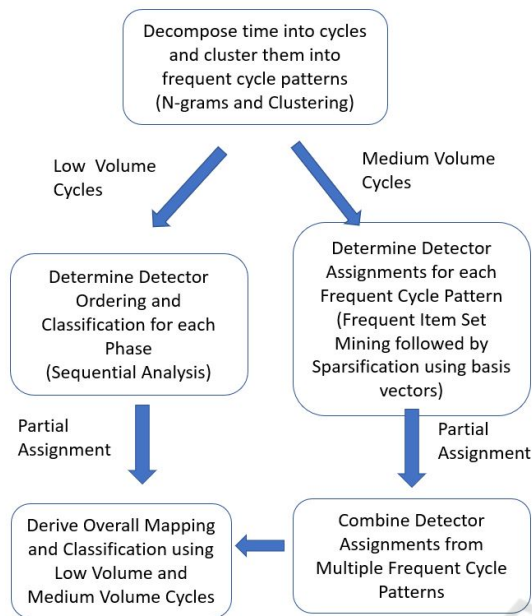


Figure 3: Flow Diagram for Our Methodology. We Separate out the Low Volume and Medium Volume Data from the Logs. The Medium Volume Data Is Used for Partial Assignments, and Low Volume Data Is Used to Distinguish between Stop Bar and Advance Detectors, Enable Ordering of Detectors.

systems and algorithms to temporarily correct/cleanse (impute) faulty detector data with similar motivations.

Importance of Detector Mappings. To measure performance of a signalized intersection in a meaningful manner or effect substantial performance improvements, it is critical to have vehicle detection sensors deployed. Another prerequisite for computing most performance measures in a semi-automated manner or fully automated manner is to have high fidelity (or resolution) data logging solutions deployed for all signal controllers. For correctly interpreting this high resolution data gathered at traffic intersections and computing performance measures at intersections, certain secondary set of data/information is needed. The most critical requirement for interpreting the high-resolution detector event data logged in a controller is the detector mapping information. This is outlined in (Day et al., 2016)

“Since any detector event must be understood as a vehicle arriving at some right-of-way and distance at the intersection, and any phase event must be understood as an interval of time elapsed for some movement, the detector mapping process is the critical step in guiding how signal output states and vehicle arrivals are to be interpreted relative to each other.”

Hence, the focus of this research is on deriving or updating these mapping using *only the high resolution event logs that have already been collected.*

3 DETECTOR TO PHASE MAPPING

Figure 2 shows the details of the intersection we use for demonstrating our methodology throughout the rest of the paper. This intersection is referred to as intersection *I*.

We represent the mapping of detector to phases in the form of a matrix, where the rows are the phases and the columns are the detectors. A matrix element is either zero, if the corresponding detector does not belong to the corresponding phase, or 1 if that detector may belong to that phase. Without any information, all the entries in the matrix are 1, i.e., this corresponds to a situation where a detector may belong to any phase. Applying our algorithms, we sparsify this matrix. Table 6 shows the final state of the matrix. Each phase may have multiple detectors, hence there would be many 1s in each row. However, usually, there should be only a few 1s or a single 1 per column because a detector often belongs to only one phase. If non-conflicting phases always start and end together, then it may not be possible to assign a detector to only one of these non-conflicting phases.

A signal cycle is defined as *“the total time to complete one sequence of signalization for all movements at an intersection. In an actuated controller unit, the cycle is a complete sequence of all signal indications.”* (U.S. Department of Transportation, 2008). As a first step, we automatically decompose data streams into cycles and cluster these cycles based on similar phase timing patterns. This is necessary because combining data across multiple different types of patterns can lead to lower discrimination between green versus red behavior. For this purpose, we develop frequent pattern mining on n-grams and use the results for clustering. In the following, we first describe how a single cycle is processed and then how we extend it to multiple cycles.

3.1 Cycle Identification and Clustering

The first step in our methodology is to identify the cycles and cluster the signal cycles. We create a representation of the SPaT data by writing out the phase or groups of phases that are green at any given time. For example, if the phases 2 and 5 receive green time simultaneously, followed by the phases 2 and 6; 4 & 8; 3 & 7; and 1 & 5, we represent these changes as

Table 1: Most Frequent 6-Grams Found in the SPAT Messages from a Controller. These Correspond to the Predominant Signal Timing Plans Deployed at This Controller.

6-Gram	Frequency	Timing Pattern
('2,5', '2,6', '1,6', '4,7', '4,8', '3,8')	117	Pattern 1
('2,6', '2,5', '3,7', '4,7', '4,8', '1,6')	84	Pattern 2
('2,6', '1,6', '3,8', '4,8', '4,7', '2,5')	67	Pattern 3
('2,5', '2,6', '1,6', '4,7', '4,8', '2,5')	17	Pattern 4

a sequence such as: '2,5', '2,6', '4,8', '3,7', '1,5', and so on. After creating a representation of the SPaT data in this manner, we identify cycles by computing n-grams.

Originally used in the field of computational linguistics and probability, n-grams are a continuous sequence of n elements in a text. We find n-grams in our SPaT representation to automatically detect signal timing patterns. For example, a repeated sequence of a 6-gram: ('2,5', '2,6', '4,8', '3,7', '1,5', '1,6') indicates this as the most dominant signal timing pattern. Figure 6 shows examples of n-grams in SPaT data. Table 1 presents the most frequent 6-grams, or timing patterns, for the intersection in Figure 2.

3.2 Deriving Detector Assignments

We consider cycles from time periods with moderate traffic activity. This is done by filtering out periods of very low (e.g., night time) and very high (e.g., rush hour) traffic. The rationale for doing this is that if there is little traffic, the detectors would not be activated, and on the other hand, if there are many vehicles at the intersection, then most detectors will be activated too frequently, which may make the differences in activation counts less perceptible.

Our approach is based on the fundamental observation that the number of vehicle departures reported on a lane will be more when the corresponding phase is green or yellow as compared to the number of departures when that phase is red. Thus, for example, by assigning a positive vote to each vehicle departure when phase 2 is green and by assigning a negative vote to each vehicle departure when phase 2 is red, it is expected that by the end of the signal cycle, all detectors which actually belong to phase 2 will be left with an overall positive voting score.

This scheme may be unable to disambiguate two phases that are non-conflicting and are served simultaneously. For example, if phases 2 and 6 are served simultaneously at all times, it will be virtually impossible to assign detectors specifically to 2 or 6. Instead, we will have a set of detectors that may belong to either 2 or 6. If the timing plan is such that during some

part of the day the non-conflicting phases are served separately, then it is possible to disambiguate these detector mappings by considering the number of departure votes over these special signal timing patterns. A visualization of the number of departures for multiple cycles is presented in Figure 4 where certain detectors report departures only when phase 2 is green. This can be seen as an indication that those detectors may be assigned to phase 2.

For each cluster of cycles, we compute the union of the results obtained from the cycles belonging to the same cluster. This effectively gives all the phases a detector can be mapped to based on cycles with similar behavior. Next, we take an intersection of the results from different clusters, to arrive at the final assignment of detectors to phases. This is because each cluster corresponds to a potentially different combination of phases.

The details of each of these steps are presented below.

Inference using a Single Cycle: A basis vector for each phase is created during a cycle. The basis vector is an array of numbers that are either +1 or -1, depending respectively on whether the phase was active or not during a time interval. Algorithm 1 presents a method to infer partial detector-to-phase mappings (or partial sparsification) using a single cycle. If we aggregate the events to a resolution of 5 seconds and we are analyzing a signal cycle of length 35 seconds, then, a basis vector, b_1 for phase 2 would have 7 entries, given by, for example, [-1,-1,-1,+1,+1,-1,-1]. This representation shows that phase 2 was active between seconds 20 through 30 and inactive for the rest of the time. Figure 5 is a visual representation of how the scores for each detector are computed. Algorithm 1 is a description of the same and is the first step in the sparsification process. The inference from one cycle may have problems if two phases were served simultaneously. For example, if phases 2 and 6 are served simultaneously and detectors d_2 and d_6 belong to phases 2 and 6 respectively, they are both identified as potentially belonging to phase 2 or 6.

Inference from a Single Cluster: Any inference from a single cycle is subject to errors. This is because traffic in a single cycle may be abnormally high in a given phase or direction. Combining these results across multiple cycles has the benefit of reducing this error, especially if the results are consistent across multiple cycles.

For combining across multiple cycles, it is useful to cluster cycles with similar ordering of phases and then combining the results within each cluster sepa-

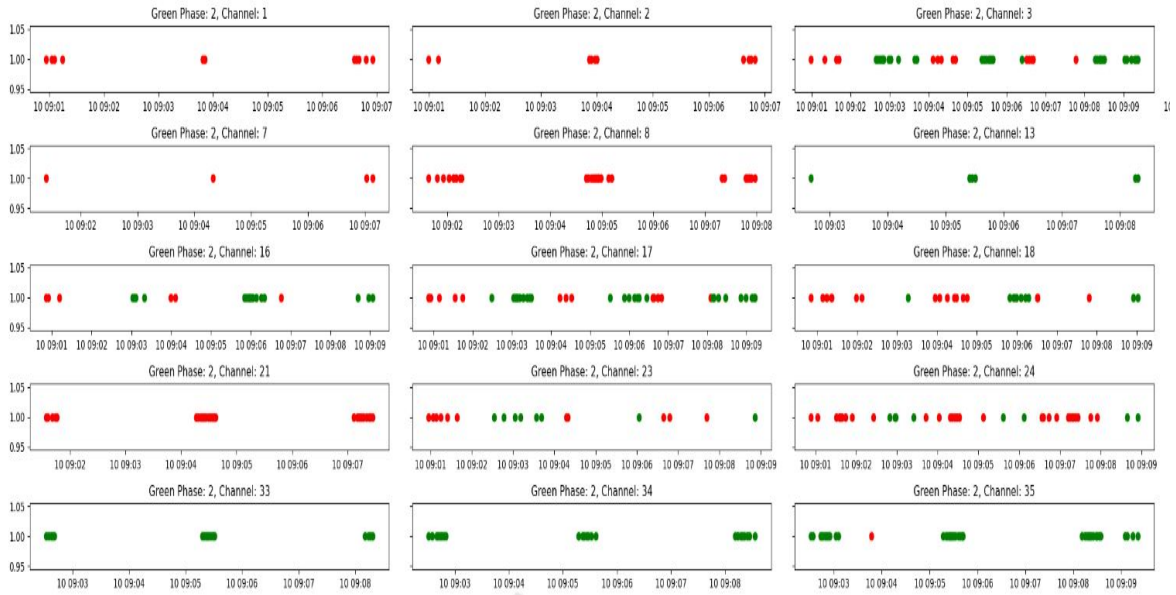


Figure 4: A Visualization of Departures Reported by Some Detectors of Intersection *I* for Multiple Cycles. Certain Detectors Report Departures Only When Phase 2 Is Green. This Is a Strong Signal That These Detectors Belong to Phase 2.

Table 2: Partial Assignment Matrix Based on Pattern 1. This Assignment Matrix Is Derived from Pattern 1 in Table 1. Detectors (Columns) Are Assigned Tentative Phases Based on the Number of Departures on Green vs. Red. But, It Is Difficult to Distinguish between Phases That Were Green Together, E.G., Phases 1 and 6.

Channels	1	2	7	8	13	14	15	16	17	18	21	26	33	34	40	41	45	46
Phase 1	464	578	-86	-790	-114	-218	312	307	189	88	-638	-589	-378	-466	-963	-849	254	189
Phase 2	-464	-578	-86	-790	114	218	-312	-307	-189	-88	-638	-589	378	466	-963	-849	-254	-189
Phase 3	-464	-578	86	-790	-114	-218	-312	-307	-189	-88	492	439	-378	-466	-963	-849	-254	-189
Phase 4	-464	-578	-86	790	-114	-218	-312	-307	-189	-88	-492	-439	-378	-466	963	849	-254	-189
Phase 5	-464	-578	-86	-790	114	218	-312	-307	-189	-88	-638	-589	378	466	-963	-849	-254	-189
Phase 6	464	578	-86	-790	-114	-218	312	307	189	88	-638	-589	-378	-466	-963	-849	254	189
Phase 7	-464	-578	-86	544	-114	-218	-312	-307	-189	-88	-638	-589	-378	-466	697	729	-254	-189
Phase 8	-464	-578	86	-544	-114	-218	-312	-307	-189	-88	638	589	-378	-466	-697	-729	-254	-189

$$\begin{aligned}
 b1 &= [-1,-1,-1,+1,+1,-1,-1] \text{ (basis vector)} \\
 d1 &= [0,0,1,10,10,2,0] \text{ (departures on detector 1)} \\
 d2 &= [7,9,11,2,0,0,0] \text{ (departures on detector 2)} \\
 \\
 b1 * d1 &= +17 \\
 b1 * d2 &= -25
 \end{aligned}$$

Figure 5: An Example of Computing Scores for Each Detector. Based on the Dot Product, That *d2* Does Not Belong to Phase 2 Whereas *d1* May Belong to Phase 2.

rately. This process is explained using the most popular patterns *Pattern 1* and *Pattern 2* from Table 1. For two cycles that have same pattern, we take a set union of the results for these two cycles. The rationale for taking a union is that the assignments may be slightly different for the two cycles based on specific traffic conditions during the occurrence of these cycles. For example, in one case the volume of traffic may be low, resulting in the mapping of fewer detectors. Tables 2 and 3 show the detector to phase mappings obtained from *Pattern1* and *Pattern2*, respectively, by applying the union operation on all cycles with the same

```

'2,5', '2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,5',
'2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6',
'3,8', '4,8', '4,7', '2,5', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6', '3,8'

Examples of 2-grams: '2,5', '2,6' | '1,6', '4,7' | '2,6', '2,5' |

'2,5', '2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,5',
'2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6',
'3,8', '4,8', '4,7', '2,5', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6', '3,8'

Examples of 3-grams: '2,5', '2,6', '1,6' | '1,6', '4,7', '4,8' | '2,6', '2,5', '3,7' |

'2,5', '2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,5',
'2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6',
'3,8', '4,8', '4,7', '2,5', '2,6', '2,5', '3,7', '4,7', '4,8', '1,6', '2,6', '1,6', '3,8'

Examples of 6-grams: '2,5', '2,6', '1,6', '4,7', '4,8', '3,8', '2,6', '2,5', '3,7',
'4,7', '4,8', '1,6',
    
```

Figure 6: 2,3 and 6-Grams in the SPAT Data. We Use This Approach to Infer Signal Timing Plans from SPAT Messages.

pattern. Tables 4 and 5 show these mappings for the *Pattern1* and *Pattern2*, respectively.

Inference from Multiple Clusters: For two or more clusters consisting of cycles with different patterns, we take a set intersection of the assignment matrix

Table 3: Partial Assignment Matrix Based on Pattern 2. This Assignment Matrix Is Derived from Pattern 2 in Table 1. We Combine the Results from Pattern 1 (Table 2) and Pattern 2 in Figure 7 to Get Better Mappings.

Channels	1	2	7	8	13	14	15	16	17	18	21	26	33	34	40	41	45	46
Phase 1	446	551	-152	-923	-187	-250	449	385	187	82	-819	-718	-432	-467	-1062	-1040	614	518
Phase 2	-446	-551	-152	-923	187	250	-449	-385	-187	-82	-819	-718	432	467	-1062	-1040	-614	-518
Phase 3	-446	-551	152	-923	-187	-250	-449	-385	-187	-82	-819	-718	-432	-467	-1048	-1040	-614	-518
Phase 4	-446	-551	-152	923	-187	-250	-449	-385	-187	-82	819	718	-432	-467	1048	1040	-614	-518
Phase 5	-446	-551	-152	-923	187	250	-449	-385	-187	-82	-819	-718	432	467	-1062	-1040	-614	-518
Phase 6	446	551	-152	-923	-187	-250	449	385	187	82	-819	-718	-432	-467	-1062	-1040	614	518
Phase 7	-446	-551	152	-291	-187	-250	-449	-385	-187	-82	-819	-718	-432	-467	-116	-168	-614	-518
Phase 8	-446	-551	-152	291	-187	-250	-449	-385	-187	-82	819	718	-432	-467	116	168	-614	-518

Algorithm 1: Map Detectors Using One Signal Cycle.

```

function MAPDETECTORS(LogsData , x, y)
Require: LogsData - High resolution controller logs of
the intersection being studied.
x - Intersection ID y - Time window of one observation
for every time window z do
    Select cycles with moderate volumes.
    Create basis vectors for each phase (bx).
    Create departure vectors for each detector (dy).
    Compute the vector dot product of each basis vec-
tor, bx with each departure vector dy.
    Select the ones with the highest results for the par-
tial assignment matrix.
end for
end function
    
```

derived for each cluster in the previous step. For example, using the results from Tables 4 and 5, we are able to further disambiguate the overlapping assignments. Here, detectors 21 and 26, are assigned to phase 8 in Table 2 because the score for Phase 8 is higher than the score for Phase 3. And the same detectors are assigned to phases 4 and 8 in Table 3. Taking an intersection, we assign these detectors to phase 8. Next, detectors 1 and 2 can be assigned to both Phase 1 and Phase 6. This is because they have the exact same scores in Tables 2 and 3. Thus, applying a combination of the set union (within a cluster) and intersection operations (across multiple clusters), we arrive at the final assignment results shown in Figure 7. Algorithm 2 presents the overall algorithm.

Table 4: Partial Mapping Deduced Using Only Pattern 1. This Is a Transactional Representation of the Results Presented in Table 2.

Detector Number	Possible Phases
13,14	Phase 2 or Phase 5
1,2	Phase 6 or Phase 1
21,26	Phase 8
8,40,41	Phase 4 or Phase 7

Table 5: Partial Mapping Deduced Using Only Pattern 2. This Is a Transactional Representation of the Results Presented in Table 3.

Detector Number	Possible Phases
13,14	Phase 2 or Phase 5
1,2	Phase 6 or Phase 1
7	Phase 3 or Phase 7
21,26	Phase 4 or Phase 8

Pattern 1	\cap	Pattern 2	=	Result A
Phase 3 \rightarrow 7,21,26	\cap	Phase 3 \rightarrow 7	=	Phase 3 \rightarrow 7
Phase 4 \rightarrow 8,40,41	\cap	Phase 4 \rightarrow 8,21,26,40,41	=	Phase 4 \rightarrow 8,40,41
Phase 7 \rightarrow Null	\cap	Phase 7 \rightarrow 7	=	Phase 7 \rightarrow Null
Phase 8 \rightarrow 7,21,26	\cap	Phase 8 \rightarrow 21,26	=	Phase 8 \rightarrow 21,26

Figure 7: We Use the Set Intersection Operation to Combine the Partial Mappings Derived Using Data from Different Timing Patterns.

4 CLASSIFYING DETECTORS

We use low volume cycles to infer the relative locations of the detectors from the stop bar. For example, a single car arriving at an intersection would trigger the detectors in order. We filter out signal cycles with only n ($n=3$) reported departures within a short duration of time. We choose the number three because

Algorithm 2: Map Detectors Using Multiple Signal Cycles.

```

function MAPDETECTORS(Mx , Patterns)
Require: Mx - Collection of Partial Assignment matrices
obtained using only one pattern.
Patterns - The collection of signal timing pattern corre-
sponding to the mapping
for each phase p (varying 1 to 8) do
    Take an intersection of the results from each as-
signment matrix.
    Obtain the final assignment matrix.
    Use the low volume data to order the detec-
tors(stop bar vs advance).
end for
end function
    
```

Table 6: Final Mapping or Assignment Matrix Deduced Using a Combination of *Pattern 1* and *Pattern 2*. We Start with the Assumption That Every Detector May Be Assigned to Any Phase. Hence, We Assume That All the Cells in the Assignment Matrix Are Green. Techniques Presented in This Paper Can Be Used to Sparsify the Initial Matrix and Arrive at This Final Mapping Where Green Cells Represent Likely Assignment.

Channels	1	2	3	4	6	7	8	13	14	15	16	17	18	19	20	21	26	33	34	35	36	38	39	40	41	42	43	44	45	46	49	50	51	64		
Phase 1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	
Phase 2	0	0	1	1	0	0	0	1	1	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Phase 3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Phase 4	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	0	0	1
Phase 5	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Phase 6	1	1	0	0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	0	0	0	0	1	1	0	0	0	1	1	1	1	1	1	0	0	
Phase 7	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Phase 8	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	

Table 7: Frequent Item Sets Observed Using Very Low Volume Observation Periods. These Results Are in Agreement with the Results Presented in Table 6. They Also Help Us Distinguish between Stop Bar and Advance Detectors.

Item Set	Frequency	Green Phases
6,4,36	35	Phase 2 and 6
17,15,45	26	Phase 2 and 6
18,16,46	23	Phase 2 and 6

a single vehicle can cross a maximum of three detectors while crossing the intersection. Next, we compute the most frequently occurring ordered item sets of detectors that report departures during these periods. For example, if detector 6 reports a departure and that is followed by a departure event on detectors 4 and 35. If this particular order of events is observed with a high frequency, we can use these observations to order the three detectors. We could only derive potential orderings for Phases 2 and 6 using this technique. Table 7 presents the results for the order derived using time periods with low volumes for intersection ID 1995.

5 VERIFICATION

Assume that a (partial) mapping is available for an intersection. The approach described above can be used to determine a sparse assignment matrix of detector-to-phase mapping. If this mapping is conflicts with the mapping provided, then the derived mapping can be effectively used to provide suitable corrections. We applied our algorithm for a set of 10 intersections in Seminole County. This corridor was selected to test our algorithms because all the controllers on this corridor are ATC compliant and detector-to-phase assignment was available for all of them. It was found that the actual assignments are a subset of our predictions. However, due to the problem presented by synchronized phases, the model might make more than one assignment prediction. To quantify this, we define the following metric:

$$Prediction\ Factor = \frac{No\ of\ assignments\ suggested}{No\ of\ actual\ assignments} \tag{1}$$

On this corridor of 10 intersections, we made (on average) 1.3 predictions of assignment instead of 1, hence our Prediction Factor was 1.3.

Our techniques can also be used to update previously known mappings to generate a more complete picture or validate and update out-of-date mappings. For example, for one of the signals the previously known mappings are presented in Table 8. It can be observed that we started with partial information for Phases 2 and 6 and no information for the other phases. The derived detector mappings are presented in Table 9. Note that for Phases 2 and 6, the mappings are ordered, i.e., it was deduced that detectors 2,3 and 11,12 are advance detectors whereas the others are stop bar detectors.

Table 8: Known Mapping for an Intersection. This Can Be Contrasted with the Final State in Table 9.

Detector Number	Possible Phases
2,3	Phase 2
11,12	Phase 6

Table 9: Final Mapping Deduced Using a Combination of All Techniques in This Paper. We Validate the Known Mappings in Table 8 and Update Them at the Same Time.

Detector Number	Possible Phases
1	Phase 1
2,3,26,27	Phase 2
29	Phase 3
7	Phase 5
11,12,13,14	Phase 6
15	Phase 7
16,17	Phase 8

6 CONCLUSIONS

We have proposed a framework to derive loop detector mappings if none or only partial mappings are

available. We also presented a way to identify top-bar and advance detectors on the same lane. Our main contributions are as follows:

1. We have developed novel algorithms for automatically decomposing data streams into cycles and to cluster these cycles based on similar phase-timing patterns. For this purpose, we developed frequent pattern-mining bases on n-grams and then applied clustering algorithms.
2. For really low volume cycles (e.g., during nighttime), when only one vehicle is potentially present, the time of arrival and departure along with signal timing data can be used to derive ordering of detectors. We develop algorithms that can leverage this information across multiple such cycles.
3. For low to medium volume cycles, we developed algorithms that can use green versus red departure information to derive a small subset of phases for each detector. We then use frequent set mining within a given cycle cluster to derive a consistent mapping for that cluster.

There are several avenues for improving the work presented in this paper. In the intersection defined in Section 3, we note that for the timing plans deployed, phases 1,6 and 2,5 are partially synchronized. In some cases, it may be possible to compute and deploy a customized timing plan for a short period of time (non-peak hour, to minimize impact on Quality of Service) where phases 1 and 5 are synchronized. These customized basis vectors (signal-timing plans) can help us reduce the Prediction Factor (Step 2, Figure 7). We also plan to treat permissive left and right turn lanes differently in the future.

ACKNOWLEDGEMENTS

This work was supported by NSF CNS 1922782, by the Florida Dept. of Transportation (FDOT) and FDOT District 5. The opinions, findings and conclusions expressed in this publication are those of the author(s) and not necessarily those of the FDOT or the National Science Foundation.

REFERENCES

Day, C., Bullock, D., Li, H., Remias, S., Hainen, A., Freije, R., Stevens, A., Sturdevant, J., and Brennan, T. (2014). *Performance Measures for Traffic Signal Systems: An Outcome-Oriented Approach*. Purdue University, West Lafayette, Indiana.

- Day, C. M., Bullock, D. M., Li, H., Lavrenz, S., Smith, W. B., and Sturdevant, J. R. (2016). Integrating traffic signal performance measures into agency business processes. *Joint Transportation Research Program*.
- Intelligent Transport Systems, U.S. Department of Transportation, F. H. A. (2009). Ite advanced transportation controller (atc) family of standards. <https://www.standards.its.dot.gov/Factsheets/Factsheet/14>. (Accessed on 7/20/2019).
- Lu, X.-Y., Varaiya, P., Horowitz, R., and Palen, J. (2008). Faulty loop data analysis/correction and loop fault detection. In *15th World Congress on Intelligent Transport Systems*, pages 12–24.
- Martin, Peter T; Feng, Y. W. X. (2013). Detector technology evaluation. <https://digitallibrary.utah.gov/awweb/awarchive?item=30285>. (Accessed on 7/20/2019).
- Pursula, M. and Kosonen, I. (1989). Microprocessor and pc-based vehicle classification equipments using induction loops. In *Second International Conference on Road Traffic Monitoring, 1989.*, pages 24–28.
- U.S. Department of Transportation, F. H. A. (2008). Traffic signal timing manual. <https://ops.fhwa.dot.gov/publications/fhwahop08024/index.htm>. (Accessed on 7/20/2019).
- U.S. Department of Transportation, F. H. A. (2013). Measures of effectiveness and validation guidance for adaptive signal control technologies. <https://ops.fhwa.dot.gov/publications/fhwahop13031/index.htm>. (Accessed on 7/20/2019).
- Yogesh, G. K. V., Sharma, A., and Vanajakshi, L. (2018). An improved inductive loop detector design for efficient traffic signal operations and leaner space requirements. *Transportation Research Record*, 2672(18):143–153.