Implementation of a Memetic Algorithm to Optimize the Loading of Kilns for the Sanitary Ware Production

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Abstract: One of the most important aspects to be considered in the production lines of sanitaries is the optimization in the use of critical resources such as kilns (industrial furnaces) due to the complexity of their management (they are turned on twice a year) and the costs incurred. The manufacturing processes of products within these kilns require that the capacity be maximized by trying to reduce downtime. In this sense, Artificial Intelligence provides bioinspired and evolutionary optimization algorithms which can handle these complex variable scenarios, the memetic algorithms being one of the main means for task scheduling. In present investigation, and based on previous works of the authors, a memetic algorithm is presented for optimization in the loading of kilns starting from a real production line.

1 INTRODUCTION

The never-ending competition among the companies from the ceramic and sanitary ware manufacturing industry has prompted these companies to seek to improve their quality and efficiency in the production process, so as to increase their revenues and minimize losses (Porras, 2018). The use of computer solutions is a fine example of this quest. However, although these focus on several aspects such as staff management, storage, sales records and so on, there is still a gap in the optimization of the manufacturing process stages.

This is the case of the firing stage that takes the longest and lacks a strategy for an optimum selection of pieces to be loaded into the kiln. As a result a bottleneck occurs in the process. The variety of models to be manufactured, number of pieces, colors as well as demand, weight and volume constraints (of kiln cars and kilns) makes pieces selection a challenge (Leon, Cueva, Tupia & Paiva Dias, 2019).

This problem does not only emerge in the sanitary ware manufacturing industry but also in others fields where products composed of several parts are manufactured and assembled. That is why several researches have been conducted to develop algorithm-based solutions that generate good results within reasonable times.

The most commonly used type of algorithms in these cases are metaheuristic ones. Within this category the genetic algorithm is the preferred one because of its simplicity. However, recent researches have shown that memetic algorithms produce positive solutions in a lower number of evaluations but with better quality.

This paper has taken into account the aforementioned and puts forward the design and the implementation of a memetic algorithm that generates a selection of pieces prioritizing those that take advantage of the capacity of the kilns and kiln cars weight and volume, considering the demand of product sets. This algorithm was then calibrated to improve it and, finally, was compared to a genetic algorithm to determinate which was the best suited to tackle this type of problem.

The memetic algorithm (MA) was chosen because of its advantages like exploitation of problemknowledge (Moscato & Cotta, 2003) and improved

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procedures for local search, which lead to a faster convergence and a statistically better solution (Wrona & Pawełczyk, 2013). In addition, it's easy to implement and more efficent and efective than traditional evolutionary algorithms (Zhang, Sun, & Wang, 2009). And the genetic algorithm its used to compared it to the MA because it's one of the most used algorithms to solve combinatorial optimization problems due to its robust nature and how easy it is to implement (Zhang, Sun, & Wang, 2009).

This paper is organized in the following manner: Section 2 addresses the issues and their impact on the industry; Section 3 displays the problem state-of-theart; Section 4 introduces the proposed algorithm and finally Section 5 deals with the numeric experimentation this algorithm went through. In the end, the project conclusions will be introduced.

2 PROBLEM DESCRIPTION

2.1 Current Situation

The sanitary ware manufacturing sector is characterized by a wide variety of products offered in different models, colors and sizes (Regalado, Maroto, Ruiz, & García del Río, 2011). Items may be composed of one or more pieces. Products of the same model and color pooled into sets are sold.

That is why – and because of the increase of data volume required to manage the value change – the sanitary ware manufacturing industry has increasingly used computer solutions aligned to the industry's characteristics (Ceramic Industry, 2015). Nevertheless, many of them are not focused on the optimization of the production process itself.

This process has several stages, including firing, which lasts the longest (Diaz, 2004). Within this stage, the selection of pieces is the most important step, which is quite complex since there are several factors to be considered such as demand, variety of models to be manufactured, number of pieces comprised, colors, products sets as well as weight and volume constraints in kiln cars and kilns.

Kilns used in sanitary ware manufacturing are rectilinear channels oriented to continuous production (Gómez Gutiérrez, C., 2010) where kiln cars are introduced. These cars have plates or shelves where pieces are put so that they don't stick together (Rhodes, 2004). In this paper, these specific places where pieces are put are called compartments.

The lack of a strategy for an optimum selection of pieces causes a bottleneck. And this bottleneck is the

problem to be solved (Monzon, Cueva, Tupia & Bruzza, 2019).

2.2 Impact on the Sanitary Ware Manufacturing Industry

The lack of a selection strategy results in choosing pieces of only one model or color as well as the production delay of other models.

Under other circumstances, pieces of different models and colors are chosen but do not form any set, thus delaying subsequent stages of assembly and packaging. This also causes delayed production, affecting selling and as a result only a few complete models are in storage but with a huge amount of incomplete sets and loose pieces as well. As a consequence, clients are not timely serviced and supply takes too long, sells are lost, and in addition fines for delays, higher storage cost and underutilization of the production capacity occur (Savsar & Abdulmalek, 2008).

3 BRIEF SUMMARY OF STATE-OF-THE-ART

The current issue regarding the selection of pieces stage is of a combinatorial optimization type, known as the knapsack problem, which is highly complex and is considered as NP-difficult (Fuentes, Vélez, Moreno, Martínez & Sánchez, 2015). The knapsack problem consists of selecting a set of items that meet the constraints and generate the greatest benefit (Dorta, León, Rodríguez & Rojas, 2003).

Other industries, such as foundries and factories that produce a vast array of products composed of several parts to be later assembled, also pose similar difficulties (Tupia, Cueva & Guanira, 2017). This is the cause for researches have been conducted that although they do not exactly cover the same problem, they intend to solve similar problems (Koblasa, Vavrousek, & Manlig, 2017) (Baiqing, Haixing, Shaobu, Yifei, & Fei, 2016). The solutions proposal they put forward is the use of metaheuristics that have the advantage to be not specific to a problem but provide good solutions within a reasonable time (Blum & Roli, 2003).

Among the proposed metaheuristics, the most commonly used method with the best results is the genetic algorithm (Liu, Pan & Chai, 2015) (Duda & Stawowy, 2013). This algorithm was developed by Holland and is inspired in Charles Darwin's theory of evolution (Holland, 1992); among its advantages are simplicity, global perspective and intrinsic processing (Deb, 2004).

This method has been used to solve similar problems. For example, Liu, Pan & Chai put forward a specialized genetic algorithm (SGA) for the grouping of work orders, taking into account factors such as deadline, priority and demand (Liu, Pan & Chai, 2015). Wang, Ma, Luo & Qin introduced a new HGA-OVNS metaheuristics, which is the hybridization of the genetic algorithm, the Variable Neighborhood Search (VNS) and the Optimization Based Learning (OBL) to deal with the production planning problem in an assembly plant (Wang, Ma, Luo & Qin, 2016). Duda & Stawowy developed a genetic algorithm to optimize the selection of alloys and products to be manufactured in a foundry (Duda & Stawowy, 2013). In all the researches mentioned, the genetic algorithm was compared to other algorithms and even with commercial software. The outcome was that the genetic algorithm showed a better performance and generated better quality solutions.

Another algorithm successfully used in similar issues is the memetic one, which combines Local Search with genetic operators (Alba & Dorronsoro, 2005), balancing the exploration skills of evolutionary algorithms with the exploitation skills of the local search (Krasnogor & Smith). That is why, a lower number of evaluations is required to find top quality optima and solutions (Baesler & Palma, 2014).

4 PROPOSED ALGORITHMS

4.1 Data Structure

A structure is required that specifies which pieces will be loaded into the kiln. Each of the pieces will be placed in a different compartment, and there may be several pieces of the same type in the selected group.

Therefore, the solution's structure has been defined as a 2-dimensional matrix (compartment x kiln car). See Figure 1.

Kiln	Car	1	Kiln	Car	2	Kiln	Car	3

Compartment 1	1	10	10
Compartment 2	5	9	6
Compartment 3	у	9	0

Figure 1: Solution data structure.

Each row is identified with a specific compartment: the first row contains all the pieces that

will be placed in compartment 1; the second row, the compartment 2 and so on. In the case of the columns, each column represents a kiln car: column 1 represents the kiln car 1; column 2, kiln car 2 and so on.

The value within each of the cells is the code of the piece that will go in a specific compartment and in a specific kiln car. For example: in Figure 1, value *y* represents a piece with code *y* that has been placed in the compartment 3 in the first kiln car. The value 0 has been placed in empty compartments.

4.2 Proposed Memetic Algorithm

The pseudocode of the memetic algorithm is the following:

Input: initial population (pop) Output: best solution found (currentBest)
Initialize timer (t)
Set generation $= 0$
Set $gNoImprovement = 0$
Get the best solution (currentBest) in population pop
Repeat
Generate a new population (<i>newPop</i>) based on <i>pop</i> Update population
Get the best solution (<i>bestSol</i>) in population pop
If fitness(currentBest) >= fitness(bestSol)
Set $gNoImprovement = gNoImprovement + 1$
Else
currentBest = bestSol
Set gNoImprovement = 0
End
If gNoImprovement = limitNoImprovement
Restore population (pop)
End
Until generation > MaxGeneration or t > timeLimit
Return best solution found (currentBest)

Figure 2: Memetic Algorithm.

This algorithm takes as the initial parameter the population generated by a GRASP algorithm and it extracts the best solution (*currentBest*) from this population.

Then, it generates a new population (*newPop*) through the application of crossover operators, mutation and local search in the current population (pop).

Afterwards, it unifies the previous population with the new one to obtain another population with the best solution from both, and seeks the best solution of this population for any improvement with respect to the previous generation; if no improvement is seen, the *gNoImprovement* counter will be increased.

Finally, the algorithm checks if the no improvement generation limit is reached. If so, the conclusion is that the population degenerated (i.e., it comes to a standstill in a local optimun) so that it will be restored.

This process will be repeated until complying with any of the stop conditions: reaching the maximum number of generations or exceeding the deadline.

4.3 Brief Discussion of the Algorithm

The operators used in the memetic algorithm are below:

Selection operator: it chooses individuals to be affected by the recombination operator and chooses the solutions the local search will be applied to. For the selection the roulette method is used, allocating each solution a circular sector of the roulette proportional to its fitness value in such a manner that when spinning it the best solutions will have a higher likelihood. The roulette implemented has a binary search and in the worst case scenario it will require O(log n) comparisons to find the selected value (Lipowski & Lipowska, 2012).

Recombination operator: used to make up a new population. It uses individuals chosen by the selection operator and takes the crossover rate as its parameter, which determines the number of times to be applied. To carry out the operation the uniform recombination will be applied, thus generating a random number between 0 and 1 for each element that is part of the solution. If this number is lower than p_c , the element of the first father is then allocated to the first son and that of the second father to the second son, otherwise the allocation will be reversed (Magalhaes-Mendes, 2013).

Mutation operator: it slightly modifies a solution; using a mutation rate and a randomly generated value from 0 to 1; if the generated value is lower than the rate (mutationRate), the operator will be applied. The mutation will replace an item assigned by another one that fits in the same compartment.

Local search operator: it uses the k-opt heuristics that replaces k elements present in the current solution with others that are not part thereof. Based on the Ishibuchi, Tanigaki, et al. research, this search will be conducted each *gLs* iteration, and will be applied to a reduced number of individuals from the population (determined by *probLs* variable) and will only visit *nLs* neighbors (Ishibuchi, et. al, 2013).

4.3.1 Generation of a New Population

Figure 3 shows the pseudocode of the function that generates a new population.



Figure 3: Generate new population.

4.3.2 Updating of Population

Once the new population (*newPop*) is generated, this will be unified by the current (*pop*) one, selecting the best elements of both populations to form a group composed of the same number of individuals as the current population.

The addition strategy is chosen because it is fast, does not require a population of a high number of offspring and ensures that values of the target function do not get worse (Datoussaid, Verlinden & Conti, 2002).

4.3.3 Restoration of Population

A small percentage is preserved with the best solutions of the current population and the remainder is disposed. To complete the population, new solutions are generated through the GRASP algorithm, these will be mutated before they are added up to the population.

4.4 Mathematical Model

The target function chooses the selection of pieces that maximize demand satisfaction, kiln volume and kiln car weigh capacity use. The target function is:

$$Max \sum_{w=1}^{W} \left[\left(\frac{W * \sum_{i=1}^{N} V_{iw}}{MaxKilnVol} \right) \times CV + \left(\frac{\sum_{i=1}^{N} P_{iw}}{MaxCarW} \right) \times CW \right] + \left(\frac{SP \times CD}{MaxCPrior} \right)$$
(1)

where:

$$SP = \sum_{y=1}^{SP} C_{y}$$

$$\times \left\{ AP_{y} \times \sum_{m=0}^{np_{y}-1} level\left(\frac{miss_{y}-m}{maxMiss}\right) \right\}$$

$$AP_{y} = SAP_{s},$$

$$(3)$$

$$\forall X_{yd} \times X_{ds} = 1, \forall y \in Y, \forall s \in S$$

$$SAP_{s} = \frac{\sum_{p=0}^{r} X_{ps} \times RC_{p} \times DD_{p} \times CP_{p}}{\sum_{p=0}^{P} X_{ps} \times RC_{p}}$$
(4)

$$np_{y} = min\left(\sum_{w=1}^{W}\sum_{i=1}^{N}X_{iwy}, miss_{y}\right)$$
(5)

 $maxMiss = max\{miss_y: y = 1..N\}$ (6)

$$level(x) = \begin{cases} a+1, b > 0\\ a, b = 0 \end{cases}, (7)$$

$$a \times 10 + b = x \times 100$$

Equation 2, defines sum of selected pieces considering penalties (m). Equation 3, establishes the average priority of piece y is equal to the average priority of the set it belongs to, which is the average priority of requests and considers the amount requested, the proximity of delivery and the customer priority level (as defined in Equation 4). Equation 5, constraints the number of pieces y considered in the sum in *SP* to the necessary amount to satisfy the demand. Equation 7 defines a function that returns an

integer value between 0 to 10 according to demand pending to be satisfied.

Table 1: Variables definition.

	Coefficients that add up 1 and represent				
CV, CW,	the importance of volume factor, weigh				
CD	and demand.				
16 7711 77 1	and demand.				
MaxKılnVol	Maximum kiln volume.				
MaxCarW	Maximum weight supported by kiln car.				
MaxCPrior	Maximum value of the addition of				
	priorities of pieces that can be loaded				
	into a kiln car.				
W_i, H_i, D_i	Compartment <i>i</i> 's dimensions (width,				
	height and depth)				
W	Number of kiln cars				
N	Number of compartments in kiln car.				
Y	Number of different types of pieces.				
S	Number of different types of sets				
	Amount of orders				
Vi	Volume of piece placed in the				
• <i>tw</i>	compartment <i>i</i> of kiln car w				
D.	Weight of piece placed in the				
1 iw	comportment in kiln eer w				
W II	compartment <i>i</i> in kiln car <i>w</i> .				
Wiw, Hiw,	in the comportment i in hill corve				
	in the compartment <i>i</i> in kin car <i>w</i> .				
C_y	It is 0 if no piece of type y has been				
	loaded. Otherwise, it is 1.				
AP_y	Average priority of piece y.				
SAP_s	Average priority of requested set <i>s</i> .				
X_{yd}	It is 1 if piece y belongs to product d .				
Xyd	Otherwise, it is 0				
X_{yd} X_{ds}	It is 1 if piece y belongs to product d . Otherwise, it is 0 It is 1 if product d belongs to set s .				
X _{yd} X _{ds}	It is 1 if piece y belongs to product d . Otherwise, it is 0 It is 1 if product d belongs to set s . Otherwise, it is 0				
Xyd Xds Xps	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order.				
Xyd Xds Xps	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0				
Xyd Xds Xps Xiwy	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment				
Xyd Xds Xps Xiwy	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i in kiln car w. Otherwise, it is 0				
Xyd Xds Xps Xiwy RCp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i in kiln car w. Otherwise, it is 0 Amount requested in order p.				
Xyd Xds Xps Xiwy RCp DDp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i n kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p.				
Xyd Xds Xps Xiwy RCp DDp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i n kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5				
Xyd Xds Xps Xiwy RCp DDp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i in kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one.				
Xyd Xds Xps Xiwy RCp DDp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i n kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p.				
Xyd Xds Xps Xiwy RCp DDp CPp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3 with 3				
Xyd Xds Xps Xiwy RCp DDp CPp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i in kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important				
Xyd Xds Xps Xiwy RCp DDp CPp	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i in kiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important.				
Xyd Xds Xps Xiwy RCp DDp DDp CPp npy	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important. Amount of pieces of y-type taken into account in the sum of priorities				
Xyd Xds Xps Xiwy RCp DDp DDp CPp npy mics	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important. Amount of pieces of y-type taken into account in the sum of priorities.				
Xyd Xds Xps Xiwy RCp DDp DDp CPp npy missy	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important. Amount of pieces of y-type taken into account in the sum of priorities. Amount of pieces y pending to be kilned in order to fulfil the orders.				
Xyd Xds Xlas Xiwy RCp DDp DDp CPp npy missy	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important. Amount of pieces of y-type taken into account in the sum of priorities. Amount of pieces y pending to be kilned in order to fulfil the orders.				
Xyd Xds Xlas Xiwy RCp DDp DDp CPp npy missy maxMiss	It is 1 if piece y belongs to product d. Otherwise, it is 0 It is 1 if product d belongs to set s. Otherwise, it is 0 It is 1 if order p is a set s's order. Otherwise, it is 0 It is 1 if piece y is placed in compartment i nkiln car w. Otherwise, it is 0 Amount requested in order p. Level of proximity of delivery date p. Integer value between 1 to 5, with 5 being the closest one. Customer priority level of order p. Integer value between 1 to 3, with 3 being the most important. Amount of pieces of y-type taken into account in the sum of priorities. Amount of pieces y pending to be kilned in order to fulfil the orders. Maximum missing amount per piece				

Solutions generated must comply with the following restrictions:

$$\sum_{i=1}^{N} P_{iw} \leq MaxCarW, \forall w \in W$$
(8)

$$\sum_{w=1}^{W} \sum_{i=1}^{N} V_{iw} \leq MaxKilnVol$$
(9)

$$\max\{D_{iw}, W_{iw}, H_{iw}\} \le \max\{D_i, W_i, H_i\}, \quad (10)$$
$$\forall i \in N \ \forall w \in W$$

$$\min\{D_{iw}, W_{iw}, H_{iw}\} \le \min\{D_i, W_i, H_i\}, \qquad (11)$$
$$\forall i \in N \forall w \in W$$

$$D_{iw} + W_{iw} + H_{iw} - max\{D_{iw}, W_{iw}, H_{iw}\} - min\{D_{iw}, W_{iw}, H_{iw}\} \leq D_i + W_i + H_i - max\{D_i, W_i, H_i\} - min\{D_i, W_i, H_i\}, \forall i \in N \forall w \in W$$

$$(12)$$

$$\sum_{y=1}^{Y} X_{iwy} \le 1, \forall i \in N, \forall w \in W$$
(13)

$$\sum_{w=1}^{W} \sum_{i=1}^{N} X_{iwy} \le PH_y, \forall y \in Y$$
(14)

Equations 8 and 9 constrain the weight to be borne by a car and the total volume to be loaded into the kiln. Equations 10, 11 and 12 indicate that the piece must fit in the compartment it is placed. Equation 13 ensures that up to one piece is placed in each compartment. Equation 14 checks that the amount of pieces y allocated to the compartments do not exceed the initial number of pieces y pending to be kilned.

The only constrains not considered in this paper are baking time required per piece and color combinations per selected group, which consist of not allowing in a selection certain combination of colours because the resulting pieces might not end up with the expected colours. These constraints could be added in future works.

5 NUMERIC EXPERIMENTATION

The developed algorithm was compared to a genetic algorithm, which takes as its starting point the same initial population as the memetic one and uses the same roulette method with binary search as selection operator, as well as: crossover method, crossover rate and stop conditions. With a slightly different application of the mutation process where the number of solutions to be mutated is a fixed proportion of the population and the solutions selected are chosen with the roulette method. Before comparing them, the memetic (MA) and genetic algorithms (GA) were calibrated in order to get better results. In this process, real data about kiln, kiln cars and products was used as well as 40 orders lists that were generated randomly. Using each combination of the parameter values, the algorithms were applied to each of the order lists 40 times and the average fitness for each combination was calculated. As a result, the parameters were set on the following values:

Table 2: Parameters values.

Stage	Parameter	MA	GA
Crossover	Crossover Rate	65%	65%
	Crossover probability	70%	70%
Mutation	Mutation rate	6%	7%
Local search	Generation interval (gLs)	1	
	Application rate (probLS)	5%	
	Neighbors visited (nLs)	100	
Restoration /	Percentage preserved	7%	10%
Depuration	Alpha	0.4	

The purpose of the comparison was to determine which of them was the best suited for this type of problems.

The data used in the comparison was extracted from the results of 40 tests conducted with different datasets. Each test was repeated 10 times for each algorithm and based on this data the average value of the algorithms' performance was calculated.

Every test included the same type of sets, products and pieces, changing only the orders' files. We can see fitness results on figure 4:



Figure 4: Fitness test results.

After conducting the ANOVA test, it was determined that the difference between the two algorithms was not significant, so that it was concluded that both provide solutions of the same quality level.

In addition, other tests were run changing the amount of generations and the time to analyze the

behavior of the algorithm in two aspects (showed on table 3 and 4 respectively):

 How long do algorithms take to reach the 99% of their optimum value?

	Memetic		Genetic	
	Min	Max	Min	Max
Generations	54.33	69.17	180.39	208.65
Time	29.40	32.37	105.29	121.26
(seconds)				

Table 3: Average comparison values.

 How long does the genetic algorithm require to reach the same performance than the memetic one?



Table 4: Average comparison values.

Figure 5: Behavior comparison by generations.



Figure 6: Behavior comparison by execution time.

6 CONCLUSIONS

A memetic algorithm was proposed as a method to solve the selection of pieces issue in the firing stage of the sanitary ware production. This algorithm was chosen because of its similarities to the genetic one – the most commonly used method for this type of problems – and because it shows the same exploration skills but a higher capacity of exploitation when incorporating the local search.

After calibrating these algorithms to improve the solutions generated, it was determined that the difference between the solutions obtained for the algorithm was not significant, so that we can conclude that both provide solutions of the same quality level.

Additionally, it was found that the memetic algorithm takes a smaller number of generations to reach 99% of the optimum value while it requires a shorter execution time than the genetic one. For this reason, this method should be recommended to sectors and industries where obtaining a good solution in a short amount of time is vital.

In conclusion, this research offers a valid solution for the pieces selection into the problem at sanitary ware manufacturing industry. This solution is fast and it's adapted to the industry necessities and can be applied in other fields where products composed of several parts are manufactured and assembled. In addition, this research takes into account multiple factors related to demand such as client's priority, delivery dates and required amounts of products while many others only consider a subset of this ones.

REFERENCES

- Alba, E., & Dorronsoro, B., 2005. The exploration/exploitation tradeoff in dynamic cellular genetic algorithms. *IEEE transactions on evolutionary computation*, 9(2), 126-142.
- Baesler, F., & Palma, C., 2014. Multiobjective parallel machine scheduling in the sawmill industry using memetic algorithms. *International Journal of Advanced Manufacturing Technology*, 74(5-8), 757-768.
- Baiqing, Z., Haixing, L., Shaobu, B., Yifei, T., & Fei, H., 2016. Study on the charging combination optimization for forging production based on discrete shuffled frog leaping algorithm. *Mechanics*, 22(5), 425-431.
- Blum, C., & Roli, A., 2003. Metaheuristics in combinatorial optimization: Overview and conceptual comparison. ACM computing surveys (CSUR), 35(3), 268-308.
- Ceramic Industry, 2015. Case Study: Collaborative Robots in Technical Ceramic Parts Production.
- Datoussaid, S., Verlinden, O., & Conti, C., 2002. Application of Evolutionary Strategies to Optimal Design of Multibody Systems. *Multibody System Dynamics*, 8(4), 393-408.
- Deb, K., 2004. Introduction to Genetic Algorithms for Engineering Optimization. In *New Optimization*

Techniques in Engineering (pp. 13-51). Springer, Berlín, Heidelberg.

- Díaz, M., 2004. Estudio de información del proceso productivo de la corporación Cerámica S.A.
- Dorta, I., León, C., Rodríguez, C., Rodríguez, G., & Rojas, A., 2003. Complejidad Algorítmica: de la Teoría a la Práctica. In III Jornadas de Enseñanza Universitaria de Informática.
- Duda, J., & Stawowy, A., 2013. Optimization methods for lot-sizing problem in an automated foundry. Archives of Metallurgy and Materials, 58(3), 863-866.
- Fuentes, A., Vélez, D., Moreno, S., Martínez, M., & Sánchez, O., 2015. Problema de la mochila (Knapsack problem). XIKUA Boletín Científico de la Escuela Superior de Tlahuelilpan, 3(6).
- Gómez Gutiérrez, C. (2010). Modelamiento y simulación de un horno túnel industrial. Universidad Nacional de Colombia, Medellín. Recuperado a partir de http://www.bdigital.unal.edu.co/1882/1/71265369.201 0.pdf
- Holland, J., 1992. Adaptation in Natural and Artificial Systems: An Introductory Analysis with Aplications to Biology, Control, and Artificial Intelligence. MIT Press.
- Ishibuchi, H., Tanigaki, Y., Akedo, N., & Nojima, Y., 2013. How to strike a balance between local search and global search in multiobjective memetic algorithms for multiobjective 0/1 knapsack problems. In 2013 IEEE Congress on Evolutionary Computation (pp. 1643-1650).
- Koblasa, F., Vavroušek, M., & Manlig, F. (2017). Threedimensional Bin Packing Problem with heterogeneous batch constraints. In 35th International Conference Mathematical Methods in Economics (pp. 330-335). Hradec Králové: University of Hradec Králové.
- Krasnogor, N., & Smith, J., 2005. A tutorial for competent memetic algorithms: model, taxonomy and design issues. *IEEE Transactions on Evolutionary Computation*, 9(5), 474-488.
- Leon, P., Cueva, R., Tupia, M., & Paiva Dias, G. (2019). A Taboo-Search Algorithm for 3D-Binpacking Problem in Containers. Advances in Intelligent Systems and Computing, 930, 229-240. doi: DOI: 10.1007/978-3-030-16181-1 22.
- Lipowski, A., & Lipowska, D., 2012. Roulette-wheel selection via stochastic acceptance. *Physica A: Statistical Mechanics and its Applications*, 391(6), 2193-2196.
- Liu, Y., Pan, Q., & Chai, T., 2015. Magnetic Material Group Furnace Problem Modeling and the Specialization of the Genetic Algorithm. *IEEE Transactions on Engineering Management*, 62(1), 51-64.
- Magalhaes-Mendes, J., 2013. A comparative study of crossover operators for genetic algorithms to solve the job shop scheduling problem. WSEAS transactions on computers, 12(4), 164-173.
- Monzon, J., Cueva, R., Tupia, M., & Bruzza, M. (2019). A cuckoo search algorithm for 2d-cutting problem in decorative ceramic production lines with defects. In 11th International Conference on Agents and Artificial

Intelligence, ICAART 2019 (pp. 547-553). Prague: Institute for Systems and Technologies of Information, Control and Communication (INSTICC).

- Moscato, P., & Cotta, C. (2003). An introduction to memetic algorithms. *Inteligencia Artificial, Revista Iberoamericana de Inteligencia Artificial*, 19, 131–148.
- Porras, L. F. T (2018). Propuesta de mejora de una empresa de producción de sanitarios y accesorios de baño en Lima Metropolitana. Pontificia Universidad Católica del Perú.
- Regalado, E., Maroto, C., Ruiz, R, & García del Río B. (2011). Análisis de la programación de la producción en el sector cerámico español. *Boletín de La Sociedad Española de Cerámica y Vidrio, ISSN 0366-3175, Vol.* 44, Nº. 1, 2005, Pags. 39-44, 44.
- Rhodes, D. (2004). Hornos para ceramistas. CEAC.
- Savsar, M., & Abdulmalek, F. (2008). Modeling of a pullpush assembly control system to minimize inventory and demand delay costs. *International Journal of Industrial Engineering: Theory, Applications and Practice, 15*(1), 83–91.
- Tupia, M., Cueva, R., & Guanira, M. (2017). A bat algorithm for job scheduling in ceramics production lines. In International Conference on Infocom Technologies and Unmanned Systems: Trends and Future Directions (ICTUS 2017) (pp. 266-270). Dubai: IEEE.
- Wang, K., Ma, W., Luo, H., & Qin, H., 2016. Coordinated scheduling of production and transportation in a twostage assembly flowshop. *International Journal of Production Research*, 54(22), 6891-6911.
- Wrona, S., & Pawełczyk, M. (2013). Controllability-Oriented Placement of Actuators for Active Noise-Vibration Control of Rectangular Plates Using a Memetic Algorithm. Archives of Acoustics, 38(4), 529– 536. https://doi.org/10.2478/aoa-2013-0062
- Zhang, Q., Sun, X., & Wang, Z. (2009). An Efficient MA-Based Materialized Views Selection Algorithm. 2009 IITA International Conference on Control, Automation and Systems Engineering (Case 2009), 315–318. https://doi.org/10.1109/CASE.2009.111