

Weak Ties Are Surprising Everywhere

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Abstract: Weak ties between people have been known as surprisingly effective to successfully achieve practical goals, such as getting a job. However, weak ties were often assumed to correlate with topological distance in virtual social networks. The unexpected novelty of this paper is that weak ties are surprisingly everywhere, independently of topological distance. This is shown by modelling luck with reference to a target task, as a composition of a surprise function expressing weak ties and a target relevance function expressing strong ties between people. The model enables an automatic luck generation software tool, to support target tasks mainly by the surprise function. The main result is obtained by superposing the luck model upon network topological maps of customer relationships to its followers in any chosen social network. The result is validated by surprise Keyword Clouds of customer followers and Keyword Frequencies for diverse followers. Results are illustrated by a variety of graphs calculated for specific customers.

1 INTRODUCTION

Two important roles of Online Social Networks are often treated as distinct and separate: 1- as a huge source of virtually any *discipline knowledge*; 2- as an information source on the *network members*.

We claim that these two network roles are dual and mutually benefit from each other. Indeed, in a recent paper (Exman, Ganon, Yosef, 2020), *network members* were modelled by functions estimating the potential luck for successful completion of chosen tasks, e.g. product marketing or finding people that help one to get a job. The functions' input was the *discipline knowledge* specific to the chosen task.

A central modelling assumption was Granovetter's hypotheses (Granovetter, 1973). First, the tie strength between two individuals is directly proportional to their friendship networks overlap. Second, *weak ties* to other people may be more significant than strong ties for certain tasks.

This paper further investigates the online social network dual roles. Network members are characterized both by their chosen task relevant knowledge and by their network topology. It turns out that weak ties are a dominant factor for potential successful completion of chosen tasks.

1.1 Weak Ties in Online Social Networks

Our previous work (Exman, Ganon, Yosef, 2020) defined *weak ties* between any pair of persons as the amount of semantic content *mismatch* between the pair of persons, relative to a given task. We called this semantic content mismatch the *Surprise*.

Analogously we also defined *strong ties* between any pair of persons as the amount of semantic content *match* between the pair of persons, relative to a given task. We called this semantic content match the *Relevance*.

Semantic content in both previous definitions is characterized by keyword sets for each person, relative to a keyword set of the chosen task context. We emphasize that the above definitions, do not involve any notions of geographical or topological distances between pairs of persons. In the more formal section 3 of this paper we refer to an idea of semantic content distance.

1.2 Automatic Generation of Luck

Informally, our definition of the potential *Luck* for successful completion of a chosen task is a composition of the *Relevance* with the respective *Surprise* for a given pair of persons.

The intuitive idea behind this definition is that potential Luck should certainly be *relevant* to the chosen task. But *Relevance* alone would be totally deterministic, and probably it would not be enough, to realistically cover the semantic content variety of people involved in the online social network interactions. One also needs an element of unexpectedness, as given by a calculated *Surprise*. We were inspired by a previous definition of Interestingness (Exman, 2009).

This positive pragmatic approach to Luck – as a systematic effort to attain successful completion of tasks, by possibly automatic software tools – is very different from the derogatory notion of Luck as obtaining undeserved results, by mere chance.

1.3 Online Social Networks Topology

In this paper, overall views of online social networks are displayed by network topological maps – i.e. graphs with indirect, unweighted edges – standing for any possible kind of interaction among members of the social network, where vertices represent network members. Network topological maps are presented in the results Section 4.

1.4 Paper Organization

The remaining of this paper is organized as follows. We concisely review Related Work in section 2. Luck modelling by Surprise and Relevance, is more formally defined in section 3. The central novelty of the paper, viz. that weak ties are ubiquitous and the most significant factor to generate Luck, is presented in section 4. The design and implementation of the Luck’o’-mation software tool appears in section 5. The Luck model is validated in section 6. We conclude the paper with a discussion in section 7.

2 RELATED WORK

This section concisely reviews the scientific literature on Luck, ties strength and social networks’ topology.

2.1 Systematic Luck

As already stated, our positive pragmatic view of Luck is very different from the negative stereotype of undeserved resources acquisition by mere chance.

The book by the late Clayton Christensen and co-authors (Christensen et al., 2016) entitled “Competing against Luck” is an extended example of the negative meaning of Luck. It promotes causality

in contrast to random hit-and-miss development of new products.

Liechti (Liechti et al., 2012) defines luck with some similarity to our “surprise”. It is a sum of three terms standing for an unexpected performance:

- actual deviation from expected performance;
- an overconfidence bias;
- a look back bias (the expectation at a certain time t minus that at a previous time).

Dowding (Dowding, 2003, 2008) focuses on moral aspects of luck. His proposed luck measure expresses a relationship between expected value of outcome (EV) and an actual outcome (AV):

$$Luck = AV - EV \quad (1)$$

In a series of measurements, one expects AV to approach EV.

2.2 Social Networks’ Ties Strength

Granovetter (Granovetter, 1973, 1983) proposed Weak Ties as a significant notion in social networks. He also pioneered the application of his theory (Granovetter, 1995) in the context of “Getting a Job”.

Various studies of weak ties in social networks supported the theory – such as (Brown, Konrad, 2001), (DeMeo et al., 2014). The book by Ferguson (Ferguson, 2018) analyses networks in general from an historical point of view. Its Chapter 6 explicitly deals with weak ties. Other authors extended the theory to different applications, – such as (Baer, 2010), (Centola, 2007) – or provided general appraisals e.g. (Sinan, 2016).

On the other hand, there were researchers that emphasized the importance of strong ties – such as (Gee et al., 2017) and (Krackhardt, 2003). Measurement of tie strength is dealt with in the paper by (Marsden, Campbell, 1984).

Within the “Getting a Job” context, besides Granovetter, we can mention (Gee et al., 2017) and the paper by Tassier on “Labor Market implications of Weak Ties” (Tassier, 2006).

2.3 Related Social Networks’ Topology

There are three kinds of information available about online social networks:

- a) *Specific Grouping of Edges* – e.g. triples of vertices as opposed to transitive triangles.
- b) *Topological Distance Characterization* –in terms of discrete edge numbers between vertices;

- c) **Functional Distance Characterization** – as a continuous function, e.g. exponential;

(Mattie et al., 2018) discusses a particular grouping of edges, which they call “bow tie”, and infer their tie strength.

(Tassier, 2006) as an example of the functional distance characterization, states that weak ties in social networks grow with distance exponentially faster than strong ties.

3 LUCK GENERATION FROM WEAK TIES

In this section – whose definitions are partly based upon our previous paper (Exman, Ganon, Yosef, 2020) – we formalize the concepts of Luck, and its two components Relevance and Surprise. Then the respective formulas of match and mismatch are inserted into the Relevance and Surprise, to enable actual calculation of numerical values.

3.1 The Luck Model: Strong Ties Relevance & Weak Ties Surprise

We start by making an assumption, based on (Tassier 2006) “functional distance characterization”. Our liberal interpretation – justified by the results obtained in the next section 4 and validated in the Luck Model Validation in section 6 – is that the functional distance is applicable to semantic distance:

- **Complementary Exponential Decay of Ties** – strong ties decay exponentially with semantic distance, while weak ties increase exponentially.

Given this “Complementary Exponential decay” assumption, *Relevance* and *Surprise* are exponential functions, with complementary signs.

Moreover, by the considerations in sub-section 1.1, the semantic content of *Relevance* is given by a match function, while the semantic content of *Surprise* is given by a mismatch function. Thus:

$$Relevance = \exp(Match) \quad (2)$$

$$Surprise = \exp(Mismatch - Match) \quad (3)$$

Since Luck is a composition of Relevance and Surprise, we finally get:

$$Luck = \exp(Match) + \exp(Mismatch - Match) \quad (4)$$

The “plus” operator is the suitable composition of Relevance and Surprise. A “multiplier” operator is unsuitable, as it would cause undesirable exponents addition, and Match cancellation.

In practice, one still needs to normalize the expressions of Match and Mismatch (see the next sub-section), to eliminate dependence on set sizes.

3.2 Keyword Sets: Match & Mismatch

We begin by defining some necessary concepts.

Context is a keyword set defining a task, e.g. “*find a job as a knowledge engineer*”.

Next the two online social *network member roles*, for the same social network, are defined, with their respective notations:

- **Customer = C** – is a person demanding the performance of the Context task; (also its keyword set);
- **Follower = F** – a Customer follower in the social network sense; (also its keyword set); **F** can be a Follower of a Follower, etc. to any network topological distance from the Customer.

The Context keyword set is fixed before any computation. The keyword sets of the Customer and of each Follower are sub-sets of the Context. These are extracted from Social Network member pages, and subsequent calculation of their intersections with the Context keyword set.

Match and **Mismatch** are keyword set operations obtaining respectively the Relevance and Surprise functions, by comparing Customer **C** keyword sets with a Follower **F** keyword set.

Match calculates a similarity measure of the input sets, i.e. the *number of keywords* appearing in the intersection \cap of these sets:

$$Match = C \cap F \quad (5)$$

Mismatch calculates the sets’ dissimilarity, viz. the numerical symmetric difference Δ between **C** and **F**. It is the union \cup of the relative complements of these sets:

$$Mismatch = C \Delta F = (C - F) \cup (F - C) \quad (6)$$

Fig.1 shows a schematic Match and Mismatch diagram.

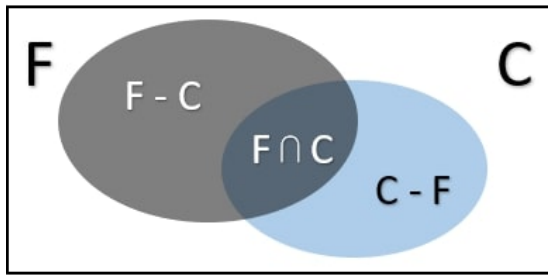


Figure 1: Schematic Match and Mismatch diagram – C stands for the Customer keyword set (light blue). F is the Follower keyword set (gray). Match is the intersection $F \cap C$. Mismatch is the union between the relative complements $C - F$ and $F - C$. (All figures are in color online).

4 WEAK TIES SURPRISE EVERYWHERE

This central section of this paper shows the novel significant results of this work.

As a preview, here are the results:

- **Weak Ties** – represented by the **Surprise** function – have a much more significant contribution than Relevance, to the numerical values of the calculated potential Luck;
- **Surprise** – is ubiquitous, i.e. it appears *everywhere throughout the network*, independently of the topological distance.

So, this is a double surprise: the overwhelming importance of weak ties and its ubiquity.

4.1 Luck vs Surprise

In this sub-section one can see the first computation result of this paper. The social network was chosen according to an available API. The computation refers to the *Context* task “find a job as Software Engineer”.

The **Context Keyword Set** used in the computations is seen in the next text-box.

Software, engineering, developer, DevOps, computers, algorithm, TechOps, python, programmer, java, ‘computer science’, ‘data science’, ‘data analyse’, C++, web, framework, embedded, ‘alpha version’, API, api, app, application, beta, version, bios, QA, automation, agile, scrum, demo, development, device, emulator, freeware, ‘open source’, interface, ‘operating systems’, workflow ‘machine learning’, ‘deep learning’, startup, innovation, internet, IoT, VR, code, coding.

Match and Mismatch functions normalization in equation (4) was done as follows: dividing the non-normalized outcome by a sum of the Context and Customer keyword sets intersection, with the Context and each Follower keyword sets intersection.

Fig. 2 shows a plot of Luck against Surprise for the data-set of a certain Customer JS.

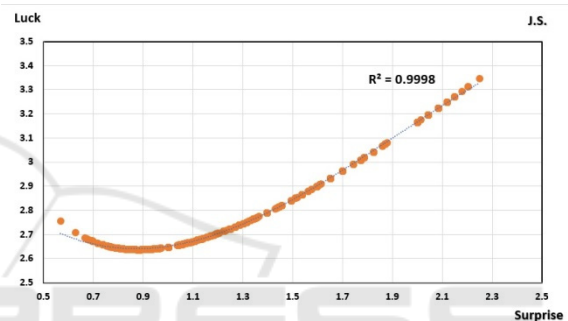


Figure 2: Plot of Luck vs. Surprise for Customer JS – The dots (in orange colour) are computation results for this data set. The trend-line is a very good polynomial fitting.

The plot in Fig. 2 displays the following features:

- **Surprise**, for Weak Ties, definitely increases when Luck increases (right-hand side of plot);
- **Relevance**, for Strong Ties, moderately increases, causing a smaller Luck increase (left-hand-side of the plot).

The graph asymmetry is very clear.

This plot is important since the same functional behaviour has been repeatedly found for all plots of this kind for a variety of different customers – see e.g. fig. 4 in our previous paper (Exman, Ganon, Yosef, 2020).

4.2 Online Social Networks Topology Maps

In this paper, online social networks topology is represented by “maps” – which mathematically are graphs with indirect, unweighted edges, between vertices. The vertices stand for members of the social

network, and the edges represent any possible kind of interaction among members of the social network.

Features that may be perceived in the network topological maps, are small clusters of the immediate followers, or more distant, followers of followers for any given members in the same network. Thus, one can naturally have an idea of the proximity levels of network members in the map.

In order to display and understand the results obtained in this paper, we do not consider necessary to focus on more specific structures within the network topology map, such as vertex triples or bow-ties as mentioned in the Related Work sub-section 2.3.

4.3 Surprise Is Everywhere in Network Topology Maps

A partial overall view of an online social network topology map centred on another customer LM is seen in Fig. 3. The view is partial, in the sense that it was limited by the number of follower levels (up to 8 levels) of the given customer.

Vertices were shown coded by three colours:

- *Green* – the Customer;
- *Purple* – Customer followers, whose Surprise value is above a certain threshold;
- *Blue* – any other social network members.

One perceives 1st level followers' clusters in several areas of the social network topology map.

The central result shown here is:

- Customer followers with a **high Surprise value** are **everywhere** in this network topological map: Surprise is independent of topological distance from the customer.

This result was consistently obtained for many different Customers, not necessarily semantically or topologically related, and whose followers do not significantly overlap network followers of the other Customers. We purposefully selected independent Customers to demonstrate the obtained result.

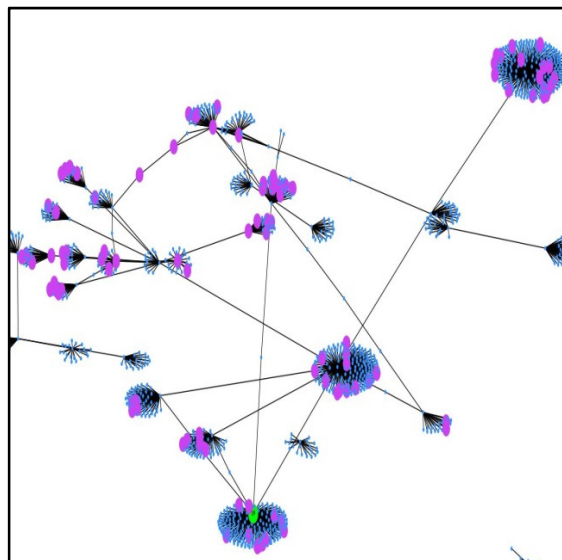


Figure 3: Surprise Social Network Topology Sample Map for Customer LM – The customer (in green) is seen in the lowest cluster. Customer Followers with high-value **Surprise** (in purple) are **seen everywhere**, i.e. in an overwhelming number of clusters in the network topology map.

5 LUCK'O'MATION DESIGN AND IMPLEMENTATION

Luck'o'mation is a software tool designed and implemented to run calculations of potential Luck, Surprise and Relevance, in order to test and validate the model proposed in this work.

It is an improved functionality and more efficient version of the software tool described and used for our previous work (Exman, Ganon, Yosef, 2020).

5.1 Software Design

The Luck'o'mation Software tool has well-designed modules with independent roles:

1. *Front-End* – for text and graph input/output;
2. *Command* – for efficient running of common options;
3. *APIs* – for interaction with any chosen social networks;
4. *Local Storage* – avoiding repeated network access, and an Inquirer to retrieve stored data;
5. *Calculators* – of Tie Strength and Luck.

The Luck'o'mation software architecture is seen in Fig. 4.

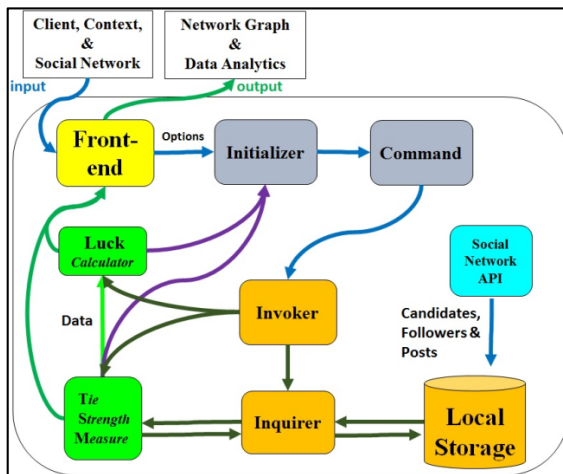


Figure 4: Luck'o'mation Software Architecture – The five independent modules are marked by different colors: 1- Front-End (yellow); 2- Command (purple); 3- APIs (blue); 4- Local Storage (orange); 5- Calculators (green).

5.2 Software Implementation

Luck'o'mation is programmed in the **Python** language. A user interacts with the software tool by means of a CLI (Command Line Interface) to run different simulations and scripts to analyse data.

Upon execution, the software builds a network map (unweighted, undirected graph) based on the data available from the input and store it in the RAM for data manipulation and visualization.

Libraries used in the software include:

- Network API – used to collect data from the social network;
- Networkx – used to create graphs and analyse them;
- Matplotlib – used to visualize graphs;
- Click, PyInquirer – used to create the CLI for any user to be able to run simulations and data analytics easily.

The database used is Sqlite to store the data collected from the social network, such as posts, network members and their connections among other information.

6 LUCK MODEL VALIDATION

Many facets of this work can serve to validate it. In this section we present three approaches:

- a) agreement with previously published research;

- b) self-consistency of semantic content viewed through keyword clouds;
- c) randomized dilution of followers' numbers per customer.

6.1 Independence of Topological Distance

The Luck model is based upon certain assumptions, most important among them the *Complementary Exponential decay* of weak and strong ties. These assumptions of the model can be validated by comparison of model consequences with previous research.

An unexpected and important result of this work is the ubiquitous and prominent availability of **Surprise**, *independently of network topological distance*.

The independence of network topological distance is confirmed by results obtained by different methods, e.g. in a paper by (Bhattacharyya, Garg, Wu 2011).

6.2 Self-Consistent Semantic Content in Word Clouds

Self-Consistency of Results means to obtain similar outcomes for very different Customers, Followers and Semantic Content in online social networks.

Semantic content is here calculated as follows. For each chosen customer in the social network, and for all its followers in our dataset, calculate surprise values, extracting the most frequent keywords contributing to the customer's surprise.

The most frequent keywords are visualized in a Keyword Cloud, with letter sizes proportional to keyword frequencies in the customer followers.

The conclusion of interest is that most of the high-frequency words are common to all followers of these customers. These are clearly observed to be: *api, version, demo, application, innovation, internet*.

Therefore, the calculated surprise for all these customers is not just the result of random disjoint (not-intersecting) sets of keywords. It shows self-consistent semantic content, which explains the utility of the calculated surprise to generate *luck* (success) for the chosen task.

Keyword Clouds are shown in Fig. 5, for four different customers and totally independent followers. The similar keyword clouds of the customers (CD, MM, SC), can be explained by network topology paths, linked at a given topological distance, enabling surprising keywords exchange. Especially interesting is the isolated LM customer,

with common prominent keywords, despite different followers and less linked paths.



Figure 5: Keyword Clouds of followers of four Customers – Keywords’ letter sizes are proportional to the occurrence frequency of each word in the calculated “surprise” for all followers of each customer. The customer name initials are seen in the upper-right corner of each cloud.

6.3 Randomized Dilution of Followers’ Number

The hypothesis for this validation approach is as follows. If surprise is really everywhere in the topological network, it should be independent of the specific choice of followers of any given customer.

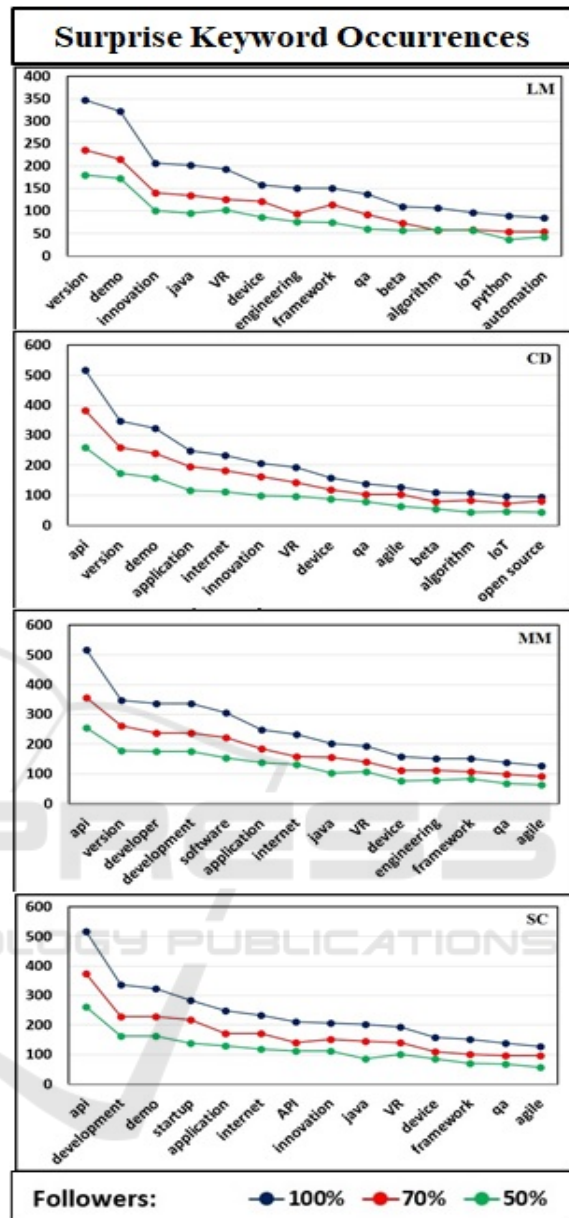


Figure 6: Randomized Dilution of the followers’ number for each of the four Customers – No dilution, 100% (blue data) fits the Keyword Clouds in Fig. 5. Diluted data are obtained by randomized followers’ shuffling, taking the upper 70% (red data) and upper 50% (green data) of the respective surprise keywords for each customer.

Thus, if one performs randomized dilution of the followers of a customer, the relative frequency functional behaviour of the followers’ surprise keywords should remain virtually unchanged.

The dilution experiment was performed for the same four customers shown in Fig. 5. The followers of each customer were randomly shuffled according

to a uniform distribution. Then, certain percentages of the upper followers in the list (70% and 50% in Fig. 6) were selected and their surprise keyword occurrences were calculated.

Results, seen in the graphs of Fig. 6, show that the relative surprise keyword frequencies, for each customer, preserve the same overall functional behaviour, independently of dilution, corroborating the hypothesis.

7 DISCUSSION

This discussion focuses on the appraisal of the main results obtained, viz. the significance and ubiquity of *Surprise* in the online social network. It is concluded by future work to be done, and main contribution.

7.1 The Weak Ties Topology Surprise

The *unexpectedness* of the prominence of Weak Ties is a consequence of widely held, but misleading perceptions. We mention three of these perceptions:

- The very name of “*Weak*” ties, suggests less influence than Strong ties, in contrast to Granovetter’s hypotheses;
- the apparent balance between Weak and Strong ties as pointed out by a non-negligible number of authors;
- an initial conjecture of symmetric exponential decay of Relevance and Surprise.

But computed results from empirical data extracted from actual online social networks, in sections 4 and 6, clearly show the greater importance and everywhere availability of weak ties.

7.2 Future Work

Future work to be done within this project, include the following issues:

- Extensive Data Analysis** – since the datasets accumulated in this work until now are very large, compared to datasets of previously published research by other authors, we still need to invest time in a dedicated analysis;
- Diverse Social Networks and Datasets** – in order to test the generality and robustness of the assumptions, one needs to use it with a few different social networks and additional datasets, to compare their behaviours and results;

- Model Variations** – we have used a bag-of-words modelling approach. We should test our hypotheses with word embedding approaches.

7.3 Main Contribution

The main contribution of this work is the ubiquity and importance of Surprise – standing for online social network weak ties – as a component of systematic generation of potential Luck towards successful completion of chosen tasks.

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