

Comparative Economic between Bat Algorithm (Ba) and Particle Swarm Optimization (Pso) for Solving Economy Dispatch

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Abstract: Artificial intelligence is intelligence made using the program and added to a system to efficiently accomplish human work. In this research utilizing an artificial intelligence that is the bat algorithm method to solve economic dispatch problems in PT. PERTAMINA RU V BALIKPAPAN This study consists of determining the configuration of the generation of power in eight generators and steam requirements, the efficiency of the configuration produced. In the 10 MW load variation, the bat algorithm produces a generation cost of 195.88 tons / h while the algorithm The PSO generates 196.83 tons / h. This shows that the bat algorithm can obtain a generation cost that is smaller than the PSO, whereas the convergent speed of the bat algorithm is faster than the PSO algorithm, this is shown from the 865-iteration algorithm in the bat can converge whereas at PSO requires iteration to 956. At 20 MW load variation the bat algorithm is better than the PSO algorithm in terms of the generation cost value and the speed of this is shown from the bat algorithm generation value is 201.96 tons / h and the iteration speed is 669 while the large PSO algorithm generation is 203.23 tons / h and speed the iteration is 976

1 INTRODUCTION

Electricity is an important component in the household, industrial, and commercial activities. Electricity is obtained from the activity of converting primary energy, which is then converted through generators (Kautsar and Nugroho, 2017). A generator is an electrical device used to convert mechanical energy into electrical energy. Companies like PT. PERTAMINA RU V has its own generator to meet its own electricity needs. Many things affect the amount of electricity generation expenditure itself, one of which is the operating costs of a generator or generator. The operation of a generator or generator is very dependent on fuel, so this can be a special concern because some of the operating costs incurred are for fuel purposes (Ilyas, 2010). Analysis of optimal power is needed to be able to minimize the cost of generation, commonly known as economic dispatch. Economic dispatch is the distribution of the load on generating units in the system optimally economic at a certain system price (Ilyas, 2010). The optimization algorithm is one method that can be

applied to solve economic dispatch problems. In the previous research, a modified improve particle swarm optimization algorithm was applied to the Java Bali 500kV thermal system generator. This method can reduce generation costs by 4.64% (Ilyas, 2010). Contraction factor-based particle Swarm optimization is an algorithm used to solve problems in the Java Bali 500kV thermal generator system. This method can reduce the cost of the generation of Rp 995,318,000.00 per hour (Kanata, 2013). The Bat algorithm can provide accuracy using Naive Bayes as its evaluator, which is quite promising at 98.29% when compared to the Exhaustive Search and Genetic Search methods, which respectively yield 82.97% and 82.55% results (Pallavi, 2013). Economic dispatch problems are experienced by various companies that have their own generators. PT. PERTAMINA RU V Balikpapan has the same problem because of PT. PERTAMINA RU V Balikpapan has a generator to operate refineries to be able to process the products they process. These problems form the background of this study. The author implements the bat algorithm at PT.

PERTAMINA RU V Balikpapan. The bat algorithm was chosen because the bat algorithm is included in the new algorithm method and based on previous research the bat algorithm has a more optimal optimization result, so it can produce more economical costs (Kautsar, 2017) The bat algorithm provides better performance when compared to some other algorithms such as the algorithm Genetics, Particle Swarm Optimization and Geometric Particle Swarm Optimization (Ahmad, 2013) and based on research in economic dispatch optimization problem bat algorithm able to save 1,23% compare to actual cost and 0.12% to firefly algorithm (Wulandhari et al., 2018), that's the reason why bat a was chosen. The target to be achieved by the author is the bat algorithm can determine the configuration of the generator power distribution PT. PERTAMINA RU V Balikpapan, knowing the efficiency of the configuration produced in terms of expenditure. The results obtained will be compared using Particle Swarm Optimization (PSO).

2 THEORETICAL BASIS

Work on this research requires information - information that can help the process of doing research well. This information is written in this section. Information about the definition of economic dispatch, bat algorithm, and particle swarm optimization.

2.1 Economic Dispatch

The operation of a power plant is very dependent on fuel because most of the operating costs incurred are for fuel purposes. Therefore, saving fuel costs in a small percentage can have a very large effect on saving operating costs. To produce electricity in a power system requires a way how to make the cost of generator fuel consumption or operating costs of the whole system as minimum as possible by determining the combination of the output power of each generating unit under the constraints of the demands of the system load and the generation capability limit of each generating unit. This method is known as the Economic Dispatch (ED). A power system consisting of various thermal generating units used to meet the electricity needs to be carried out optimally and economically among the generating units in order to obtain a minimum overall generation cost (Dewa, 2016). The economic dispatch problem commonly found in a thermal generation is determining the power output of each power plant that can meet the

demand for power at a minimum cost while still considering the limits of generator generation (Rajah and Faharuddin, 2014). The following is modeling used for economic dispatch problems.

$$Ct = \sum_{i=1}^N C_i(P_i) \quad (1)$$

$$C_i(P_i) = a_i + b_i P_i + c_i P_i^2 \quad (2)$$

Where:

Ct: = Large costs required in the form of rupiah or steam consumption

N = Total generator available

CiPi = Generation cost from generator i (RP / hour) or (Ton / hour)

ai, bi, ci = Coefficient of generator i

Pi = Large power generator (MW)

i: = Index of dispatchable units

2.2 Bat Algorithm

The bat algorithm is an algorithm that was introduced by Xin-She Yang in 2010. The bat algorithm is found based on modeling of the behavior of bats in nature. Bats use echolocation or the ability to use waves to determine distances and differences between food or prey and obstacles; bats fly irregularly, taking into account the speed, position, and frequency, wavelength, and loudness to search for food. Bats can adjust wavelengths automatically (Yang, 2010). The bat algorithm can adjust the frequency (f) and loudness (A) values when hunting for prey, and if the bat encounters a close prey then the bat will increase the pulse rate (r) so that the echolocation frequency will increase while the loudness level will decrease to prevent the prey from escaping self. The bat algorithm has several parameters that are determined based on the characteristics of the bat. These parameters are written in equation 3 to equation 10.

$$f_i = f_{\min} + (f_{\max} - f_{\min})\beta \quad (3)$$

$$v_i^t = v_i^{t-1} + (x_i^t - x) f_i \quad (4)$$

$$x_i^t = x_i^{t-1} + v_i^t \quad (5)$$

$$A_i^{t+1} = \alpha_i^t \quad (6)$$

$$r_i^{t+1} = r_i^0 (1 - \exp(-\gamma t)) \quad (7)$$

$$f_i = f_{\min} - (f_{\max} - f_{\min})\beta \quad (8)$$

$$x_i^{ref} = lb + (ub - lb) * rand(1, population) \quad (9)$$

$$v_i^{ref} = random(1, population) \quad (10)$$

Where:

f_i = Bat frequency i.

β = Random numbers from 0 to 1.

- v_i^t = Bat velocity i on t-iteration.
- x_i^t = Bat position i in the t-iteration.
- A_i^{t+1} = Bat loudness in the t-iteration.
- r_i^{t+1} = Bat pulse rate i on the t-iteration.
- i = Index of bat members.
- t = Index of iteration.

Table 1: Pseudocode bat algorithm

<u>Pseudocode algorithm kelelawar</u>
Initializing objective functions (x)
Initialization of bat population, speed, frequency, pulse rate, and loudness
Determination of reference position values using equation (9)
Determination of the value of the reference speed using equation (10)
Obtained reference value (x)
While (t < iteration)
While (i < population)
Determination of speed using equation (4)
Positioning using equation (5)
Entering position values into objective functions
Obtained position, speed and value f(x) new
If (rand < max limit A)
Determination of frequency using equation (3)
Else
Determination of frequency using equation (8)
End
If (new f(x) value < f(x) min && rand < A (i))
Update value of f(x)
Set the pulse rate using equation (7)
Adjust loudness by using equation (6)
End
Take note of the value f(X)
End while

The equations found in Tables 3 to 10 are formed in a program arrangement so that they can solve the problem. The use of these equations will be discussed in pseudocode. The bat algorithm pseudocode is in Table 1.

2.3 Particle Swarm Optimization

PSO is a population-based optimization technique developed by James Kennedy and Russ Eberhart in 1995, inspired by the behavior of flocks of birds or fish. This method uses a set of particles that work together, where each particle represents a candidate solution to explore possible solutions to optimization problems. Each particle is initialized randomly, and then the particles are allowed to "fly." At each optimization step, each particle will evaluate its ability and the ability of the surrounding particles. Each particle can store the solution that produces the best capability as one of the best solution candidates for all the particles around it.

$$v_{id}^{(k+1)} = v_{id}^k + c_1 r_1^k (Pbest_{id}^k - x_{id}^k) + c_2 r_2^k (Gbest_d^k - x_{id}^k) \quad (11)$$

$$x_{id}^{k+1} = x_{id}^k + v_{id}^{k+1} \quad (12)$$

Where:

- x_{id}^k = particle position i, dimension d on iteration k
- r_1^k, r_2^k = random values between 0 and 1
- c_1, c_2 = coefficient of repetition
- $Pbest_{id}^k$ = the best local position of particle i, on iteration
- $Gbest_d^k$ = the best global position on particle i, on Iteration
- v_{id}^k = particle velocity i, dimension d in iteration k

Explanation of equations 11 and 12 is discussed with the Pseudocode PSO method in table 2 (Yang, 2010).

Table 2: Pseudocode PSO

<u>Pseudometode PSO</u>
FOR each particle i
FOR each dimension d
Initialize position X_{id} randomly within the permissible range
Initialize velocity V_{id} randomly within the permissible range
END FOR
END FOR
Iteration k=1
DO
FOR each particle i
Calculate fitness value
IF the fitness value is better than P_{bestid} in history
Set current fitness value as the P_{bestid}
END IF
END FOR
Choose the particle which is having the best fitness value as the g_{bestid}
FOR each particle i
FOR each dimension d
Calculate velocity according to the equation
$V_{id}(k+1)$
$= w * v_{id}(k) + c_1 * rand1(pid-xid)$
$+ c_2 * rand2(pgd-xid)$
Update particle position according to the equation
$x_{id}(k+1) = x_{id}(k) + v_{id}(k+1)$
END FOR
END FOR
$w = w_{max} - ((w_{max} - w_{min}) / iteras_{maksimum}) * iter$
$k = k + 1$
WHILE maximum iterations or minimum error criteria are not attained
End while

3 APPLICATION OF THE METHOD

The method used to conduct research in this journal is to determine the cost function and determine the maximum and minimum generator limits.

3.1 Minimum and Maximum Generator Limits

PT PERTAMINA RU V BALIKPAPAN has eight steam turbine generator (STG) generation systems, with four generators in power plant 1 and 4 generators in power plant 2.

Table 3: Minimum and maximum limit generator

Generator	Limit	
	Minimum (MW)	Maximum (MW)
Power Plant 2		
Steam Turbine Generator 2.1	0	8
Steam Turbine Generator 2.2	0	8
Steam Turbine Generator 2.3	0	8
Steam Turbine Generator 2.4	0	8
Generator	Limit	
	Minimum (MW)	Maximum (MW)
Power Plant 1		
Steam Turbine Generator 1.5	0	8
Steam Turbine Generator 1.6	0	8
Steam Turbine Generator 1.4	0	8
Steam Turbine Generator 1.3	0	8

Table 3 shows the maximum and minimum generation limits for each generator. The following is an example explanation of table 3.1 Steam turbine generator 2.1 has a minimum generation limit of 0 MW or is considered not to be used, and the maximum limit of generation is 8 MW, so a steam turbine generator 2.1 may not be generated more than 8 MW.

3.2 Cost Function STG 2.1

Figure 1 shows a graph of the ratio of power to steam consumption in a steam turbine generator 2.1. From the picture, we can take the following example for STG 2.1, generating 3 MW of power. It takes 48.1-tons of steam in one hour, whereas to generate 6 MW of electricity requires 82.2-tons in one hour. The formation of the cost function can be done using the data in Figure 1, in equation 13 it is a form of the cost function of Steam Turbine Generator 2.1.

$$y = 0.24209x^2 + 9.3967x + 21.838 \quad (13)$$

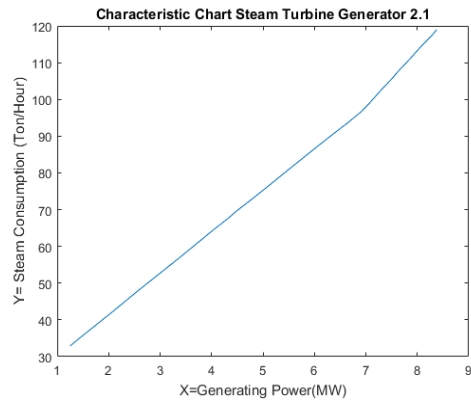


Figure 1: Characteristics STG 2.1

3.3 Cost Function STG 2.2

Figure 2 shows a graph of the ratio of power to steam consumption in a steam turbine generator 2.2. It can be seen that generating power starts from 3 MW and requires the consumption of 43 tons in one hour while generating 6 MW requires 63 tons in one hour. The formation of the cost function on Steam Turbine Generator 2.2 can be done using data 2. The results of the cost function are in equation 14.

$$y = 0.034x^2 + 3.25x + 43.6 \quad (14)$$

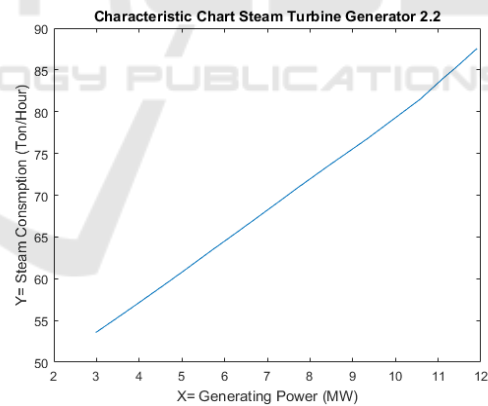


Figure 2: Characteristics STG 2.2

3.4 Cost Function STG 2.3

Figure 3 shows the graph of the comparison of power with steam consumption in a 2.3 steam turbine generator. It can be seen that the generation power starts from 3 MW and requires the consumption of 43 tons in one hour, whereas to generate 6 MW requires 63 tons in one hour, whereas to generate 6 MW requires 63-tons in one hour. The formation of

the cost function on Steam Turbine Generator 2.2 can be done using data 2. The results of the cost function are in equation 15.

$$y = 0.034x^2 + 3.25x + 43.6 \quad (15)$$

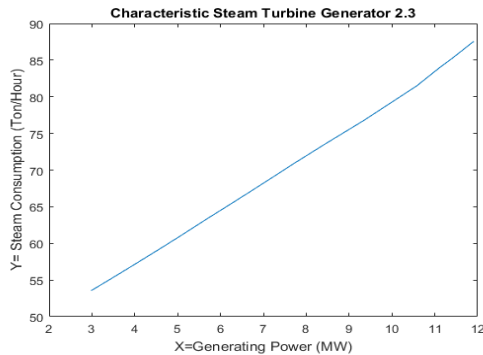


Figure 3: Characteristics STG 2.3

3.5 Cost Function STG 2.4

Figure 4 shows a graph comparing the power with steam consumption in a 2.4 steam turbine generator. From the picture, we can take the following example for STG 2.4 generating 3 MW of power required steam of 19-tons in one hour. The cost function can be done using the data in Figure 4, in equation 16, a form of the cost function of Steam Turbine Generator 2.4.

$$y = 0.047x^2 + 4.6x + 4.3 \quad (16)$$

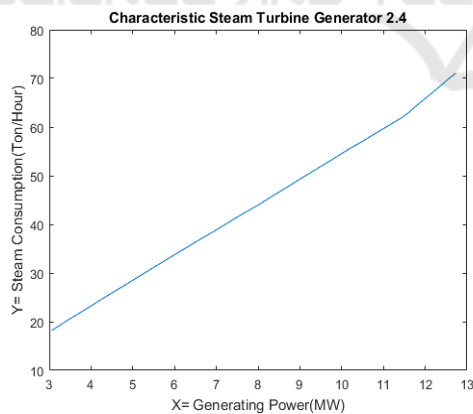


Figure 4: Characteristics STG 2.4

3.6 Cost Function STG 1.5

Based on Figure 5, the cost function of Steam Turbine Generator 1.5 can be established. In equation 17 is the result of forming a cost function from Steam Turbine Generator 1.5.

$$y = -0.17x^2 + 11x + 51 \quad (17)$$

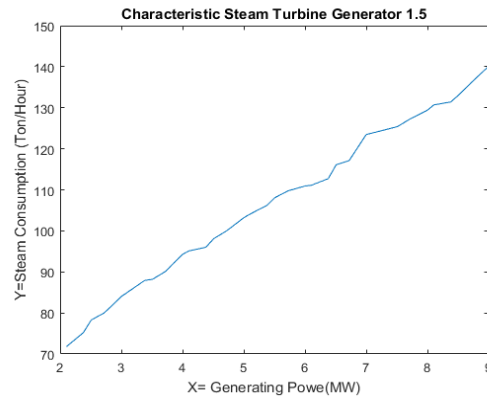


Figure 5: Characteristics STG 1.5

3.7 Cost Function STG 1.6

Based on Figure 6, the cost function of Steam Turbine Generator 1.6 can be established. In equation 18 is the result of forming a cost function from Steam Turbine Generator 1.6.

$$y = -0.16x^2 + 4.7x + 6.1 \quad (18)$$

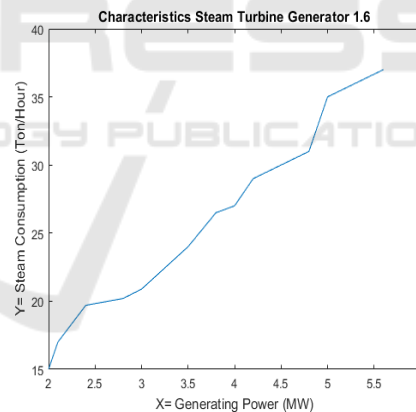


Figure 6: Characteristics STG 1.6

3.8 Cost Function STG 1.4

Based on Figure 7, the cost function of Steam Turbine Generator 1.4 can be established. In equation 19 is the result of forming the cost function of Steam Turbine Generator 1.4.

$$y = -2.5x^2 + 20x - 16 \quad (19)$$

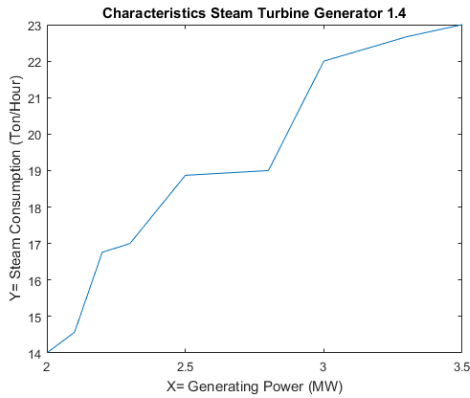


Figure 7: Characteristics STG 1.4

3.9 Cost Function STG 1.3

Based on Figure 8, the cost function of Steam Turbine Generator 1.3 can be established. In equation 20 is the result of forming the cost function of Steam Turbine Generator 1.3.

$$y = 3.1x^2 - 10x + 21 \quad (20)$$

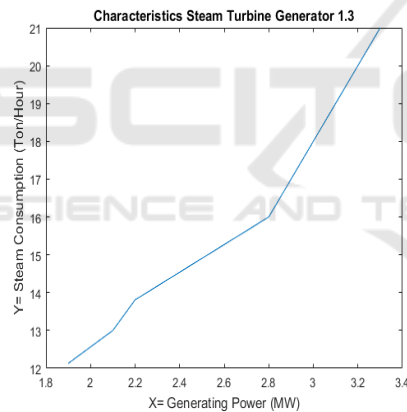


Figure 8: Characteristics STG 1.3

4 RESULT AND ANALYSIS

Economic dispatch simulation is performed using the bat algorithm method and the PSO algorithm. The simulation is carried out using MATLAB software.

4.1 Results of Simulations for 10 MW Loads

Determination of the bat algorithm convergence curve in solving economic dispatch is simulated with 1000 iterations, and the load requirement is 10 MW. The convergence curve of the economic dispatch

problem is shown in Figure 9, while in Figure 10 shows the simulation results of the PSO algorithm.

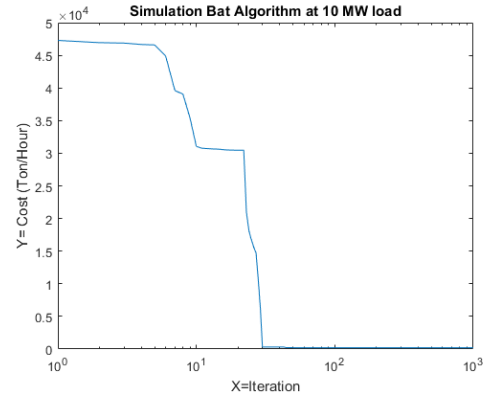


Figure 9: The result of simulation bat algorithm at 10 MW load

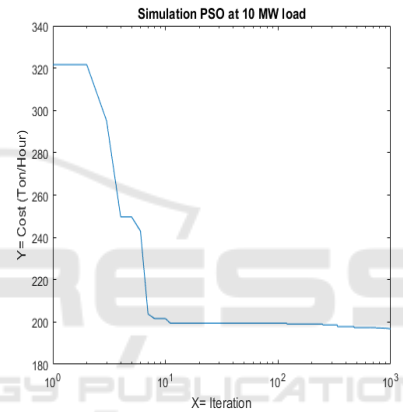


Figure 10 The result of simulation PSO at 10 MW load

Based on Figure 9, the bat algorithm can converge at 865 iterations with a total expenditure of 195.88 Tons/hour. Figure 10 shows that the PSO algorithm can converge at 956 iterations, while the generation cost is 196.83 tons/hour. Based on the speed of the algorithm to reach the convergence point, the bat algorithm is better than the PSO algorithm and to obtain the minimum expenditure costs obtained by the bat algorithm with a difference of 0.95 Ton / Hours. Table 4 shows the distribution of load on the generator at a power requirement of 10 MW.

Table 4: Distribution load generator at 10 MW load

Load (MW)		10	
Algorithm		PSO	BA
Load distribution (MW)	STG 2.1	0	0
	STG 2.2	4,83	0,16
	STG 2.3	1,48	7,61
	STG 2.4	1,50	0,04
	STG 1.5	0	0,01
	STG 1.6	0	0

	STG 1.4	0	0
	STG 1.3	2,20	2,18
Cost (ton/h)		196,83	195,88
Iteration		956	865

4.2 Results of Simulations for 20 MW Loads

This simulation is carried out using a power requirement of 20 MW. Figure 11 shows the convergence curve of the bat algorithm at a load of 20 MW, while in Figure 12 shows the convergence curve of the PSO algorithm.

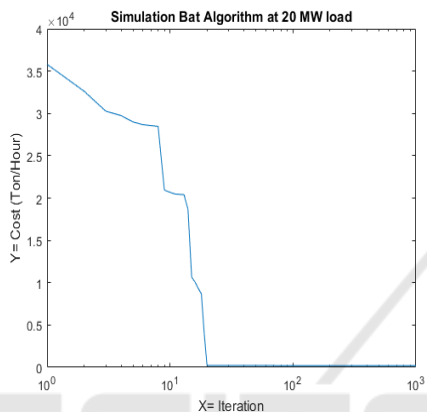


Figure 11: The result of simulation Bat Algorithm (BA) at 20 MW load

Based on Figure 3, the bat algorithm convergence curve is obtained at 669 iterations while the required cost is 201.95 Tons / Hour. Figure 4 shows that PSO can converge at 976 iterations with a cost of 203.23 ton/hour. By comparing the simulation results, it is obtained that from the speed of the superior bat algorithm with converging at 669 iterations while PSO converges at 976 iterations. From the results side, the bat algorithm is better than the PSO algorithm. Table 5 shows the distribution of generator power at a load of 20 MW.

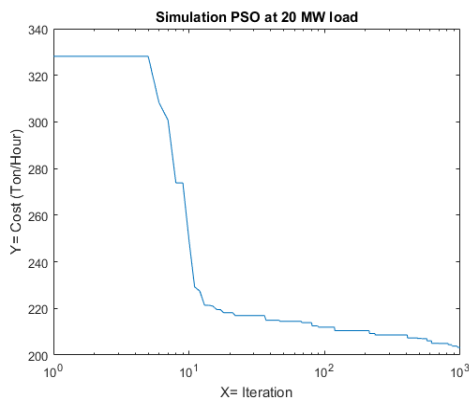


Figure 12: The result of simulation PSO at 20 MW load

Table 5: Distribution load generator at 20 MW load

Load (MW)		20	
Algorithm		PSO	BA
load distribution (MW)	STG 2.1	0	0
	STG 2.2	4,00	4,66
	STG 2.3	4,93	5,13
	STG 2.4	0,38	0
	STG 1.5	0	0
	STG 1.6	0,50	0,01
	STG 1.4	8,00	8
	STG 1.3	2,20	2,20
Cost (ton/h)		203,23	201,96
Iteration		976	669

4.3 Results of Simulations for 30 MW Loads

Figure 13 shows the results of the bat algorithm simulation in the form of convergent curves, while in Figure 14 shows the simulation results of the PSO algorithm.

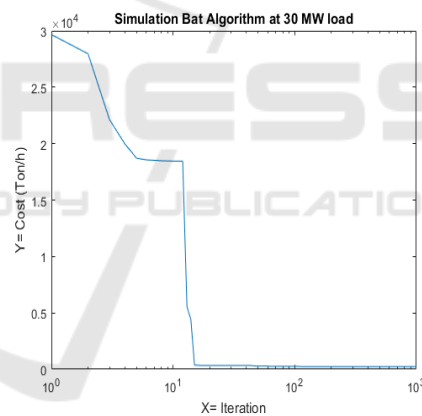


Figure 13: The result of simulation Bat algorithm at 30 MW load

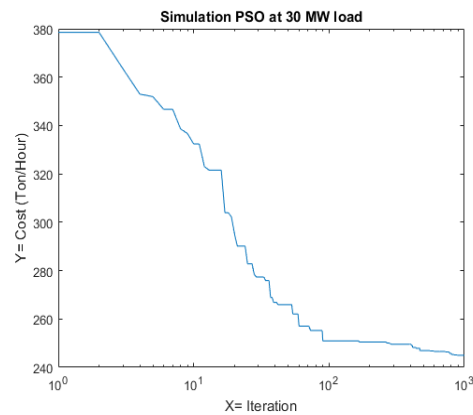


Figure 14: The result of simulation PSO at 30 MW load

From Figure 13 and Figure 14, it can be seen that in terms of speed, the bat algorithm is superior to the PSO algorithm. Based on Figure 13, the bat algorithm converges at 359 iterations. Figure 14 shows that the PSO algorithm converges at 967 iterations. In terms of the value generated, the bat algorithm is better than the PSO algorithm. The value generated by the bat algorithm is 242,765 Tons / Hour. In the PSO algorithm, the resulting value is 244.98 Tons/hour. From the two values, it can be seen that the results issued by the bat algorithm are smaller. Table 6 shows the distribution of generator power at a load of 30 MW.

Table 6: Distribution load generator at 30 MW load

Load (MW)		30	
Algorithm		PSO	BA
load distribution (MW)	STG 2.1	0	0
	STG 2.2	6,90	8
	STG 2.3	7,30	8
	STG 2.4	4,26	3,29
	STG 1.5	0	0
	STG 1.6	1,28	0,28
	STG 1.4	8	8
	STG 1.3	2,26	2,43
Cost (ton/h)		244,99	242,77
Iteration		967	359

4.4 Comparison of Algorithmic Statistical Data

Statistical data consists of the best value, the worst value, the average and the standard deviation of the cost of expenditure by carrying out five times the data collection with 1000 iterations and the load used is 32.7 MW. Statistical data is shown in table 7.

Table 7: Comparison algorithm at statistic value

Algorithm	Best value (ton/h)	Worst value (ton/h)	Average value (ton/h)	STD
BAT	256,20	256,45	256,26	0,10
PSO	256,50	258,71	257,12	0,82

Based on statistical data in table 7, the minimum cost (best value) is obtained by the bat algorithm while the highest minimum cost (worst value) is obtained by the PSO method, on average the bat algorithm is superior compared to the PSO method fixed at the standard deviation algorithm bat at 5 times of data retrieval the data difference is very small

at 0.09 while the PSO method is very large for data differences in the data collection process that is equal to 0.82 standard deviations the more the value is close to zero then the better the program is made better.

5 CONCLUSIONS

Based on the results of experiments by comparing the bat algorithm with the PSO algorithm. A comparison of the two algorithms is made using three load variations. The variations used are 10 MW, 20 MW, and 30 MW. Statistical testing was carried out using a load of 32.7 MW. In the 10 MW load variation the bat algorithm produces a generation cost of 195.88 tons / h while the PSO algorithm generates 196.83 tons / h this shows that the bat algorithm can obtain a generation cost that is less than the PSO, whereas at the convergent convergence speed bats faster than the PSO algorithm this is shown from the 865 iterations to the bat algorithm can converge whereas the PSO requires an iteration to 956. At 20 MW load variations the bat algorithm is better than the PSO algorithm in terms of the cost of generation and speed it is shown from the value bat algorithm generation is 201.96 tons / h and iteration speed is 669 while the PSO algorithm is 203.23 tons / h and iteration speed is 976. At 30 MW load variation, the bat algorithm is also better on both sides. In the generation of 242.77 tons / h and for iteration speed is 359. While in the PSO algorithm, the generation rate is 244.99 tons / h, and the iteration speed is 967. Based on the static test conducted by the bat algorithm also obtained good values with STD of 0.1 while the PSO algorithm of 0.82.

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