

After simplifying, the relation:

$$x_2 \cos x_4 + 2x_3 \leq 800 \quad (1)$$

2. Limit point interference constraint

In the process of frame folding, there should be no interference between the hinge point A of lifting bar and the limit position point F of auxiliary frame, and the length of lifting bar should be longer than the length from point O to point F. The dimension constraint relation:

$$\sqrt{x_3^2 + (x_1 + x_2 \sin x_4)^2} - \sqrt{x_1^2 + (x_2 \cos x_4 + x_3 + 50)^2} \leq 0 \quad (2)$$

3. Frame interference constraint

After folding, the front and rear frames should not interfere. As the point K is not the limit position of the front frame, when the frame reaches the limit position, the clearance between the point K and the rear frame is reserved for 120mm. The dimension constraint relation:

$$|x_K| \geq x_2 \cos x_4 + x_3 + 120$$

After simplifying, the relation:

$$\frac{x_2 \cos x_4 + x_3 + 120}{\sqrt{(1200 - x_2 \cos x_4)^2 - (x_1^2 + (x_2 \cos x_4 + x_3 + 50)^2 - x_1)^2}} \leq 0 \quad (3)$$

4. The battery interference constraint

Due to the use of hub motor drive technology, the space of the front and rear frame is mainly occupied by the battery pack, so the interference of the battery pack should be considered in the design of the frame.

The equation of the straight line EF can be get from the point E(-x₂cosx₄ - x₃, x₁) and point F(-x₃, x₁ + x₂sinx₄).

The liner equation:

$$y = \tan x_4 (x + x_2 \cos x_4 + x_3) + x_1$$

To ensure that the limit position point P (-520, 180) of the battery pack does not interfere with the ramp of the auxiliary frame, point P should be below the right of the linear EF in the coordinate. The constraint relation can be obtained from the position relation:

$$200 - \tan x_4 (-260 + x_2 \cos x_4 + x_3) - x_1 \leq 0 \quad (4)$$

5. Front and rear frame size constraint

Considering the size of battery pack and folding mechanism of vehicle size, the outer profile height of auxiliary frame is preliminarily determined to be 300-500mm. Constraint relation:

$$\begin{aligned} x_2 \cos x_4 + x_3 - 500 &\leq 0 \\ \text{and } 300 - x_2 \cos x_4 - x_3 &\leq 0 \end{aligned} \quad (5)$$

The length of the front and rear frame is 400-600mm. And the constraint relation:

$$\begin{aligned} x_1 + x_2 \sin x_4 - 600 &\leq 0 \\ \text{and } 400 - x_1 - x_2 \sin x_4 &\leq 0 \end{aligned} \quad (6)$$

6. Constraint of the lifting bar inclination

Rotation of the rocker plays a major role in frame folding. In order to ensure that the pressure angle of the rocker is not too large, its inclination angle relative to the X-axis of the coordinate system is set within 10-30°. The constraint relation:

$$\begin{aligned} \frac{x_1}{x_2 \cos x_4 + x_3 + 50} - \tan 30^\circ &\leq 0 \\ \text{and } \tan 10^\circ - \frac{x_1}{x_2 \cos x_4 + x_3 + 50} &\leq 0 \end{aligned} \quad (7)$$

3. MATLAB OPTIMIZE DESIGN AND MODELING SIMULATION

3.1 Multivariable Optimization

The mathematical model of frame folding optimization belongs to the problem of single objective multivariable optimization.

The normalized form[4]:

$$\begin{aligned} \min F(X) \\ \text{s.t} \\ AX \leq b \\ \text{Aeq}X = \text{beq} \\ C(x) \leq 0 \\ \text{Ceq}(X) = 0 \\ \text{lb} \leq X \leq \text{ub} \end{aligned}$$

The function fmincon is invoked to solve the problem. The basic format of the function command :

$$[x, fval, \text{exitflag}, \text{output}] = \text{fmincon}(@\text{objfun}, x_0, A, b, \text{Aeq}, \text{beq}, \text{lb}, \text{ub}, @\text{confun})$$

By writing the M file of the objective function and the constraint function, the optimization results can be obtained by establishing the main program solution:

x =149.2821 400.0000 226.7949 0.5236
 fval = -778.9473
 exitflag =1

The result (exitflag =1) shows that the first-order optimality condition of variable satisfies the tolerance range. According to the optimized result, the folding length of the frame will reach 778.95mm, which will reach one-third of the length of the whole vehicle. The summary results of design variable optimization are shown in Table.3.

Table.3: Optimization results of designing variable.

Design variable	Length, mm			Angle, °
	X1	X2	X3	X4
Initial value	150	290	290	45
Optimum value	149	400	226	30
Range of optimization,%	0.67	37.9	22.1	33.3

3.2 3D Modeling

According to the requirement of light weight and strength of the frame, the standard channel steel is adopted for the assembly modeling, and the rigid point factor of the suspension is ignored in the preliminary modeling. The virtual prototype modeling of the whole frame of the frame is carried out with SOLIDWORKS software, as shown in Figure.3a and Figure.3b. The lifting of frame rocker depends on the extension of actuator's pushing.

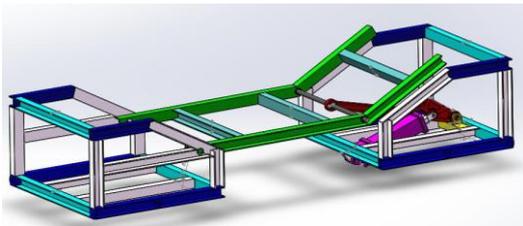


Figure. 3a: The working condition of the frame.

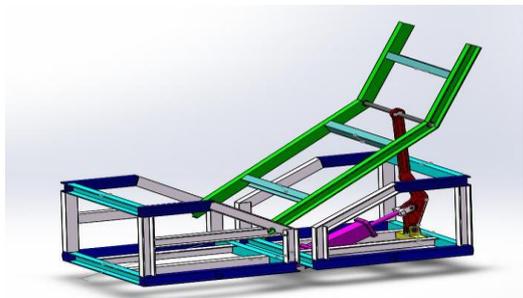


Figure.3b: The folded state of the frame when parking.

The 3D modeling of frame is imported into ADAMS software and the source part model is divided into front frame, main frame, rear frame, connection, rod, linear actuator and connection first-class parts by Boolean operation.

The ADAMS model in Figure.4 is obtained after pre-processing.

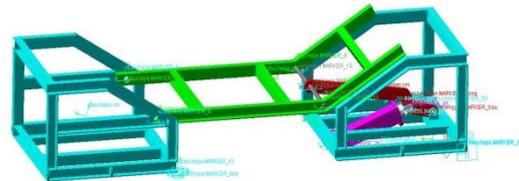


Figure.4: ADAMS model of the car chassis.

3.3 Simulation Settings

In order to achieve the frame from acceleration start to slow down the stillness of the folding process, the ADAMS built-in STEP function is added in the simulation of linear actuator and the connection to simulate the movement speed. The movement simulation time is set to 6 seconds.

The STEP function is shown below:

step(time,0,0,2,36.4)+step(time,2,0,4,0)+step(time,4,0,6,-36.4)

The STEP Function meaning: The moving pair accelerates from static to 36.4mm/s in 0-2s time, moves at a constant speed of 36.4mm/s for 2-4s, and the speed is reduced to 0 in 4-6s.

3.4 Simulation Results and Analysis

3.4.1 Frame Folding Analysis

The center of mass of the front frame is used to be the reference point to measure its displacement in the folding direction. The displacement of the front frame under the initial size is compared with that of the optimized front frame. The comparison results are shown in Figure.5.

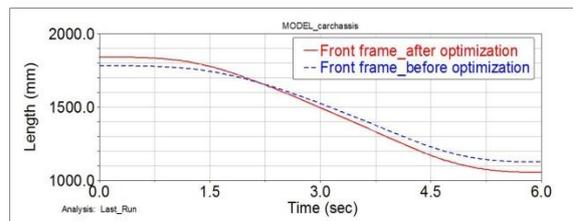


Figure.5 :Displacement of the front frame.

As can be seen from the Figure 6, the folding length of the frame, that is, the displacement of the front frame increases from 657mm to 775mm. Compared with the results of MATLAB model, the error after optimization is less than 1%, indicating that the virtual prototype modeling meets the requirements.

3.4.2 Linear Actuator Motion Analysis

The linear actuator stroke, rocker rotation angle and angular velocity images are shown in Figure.6.

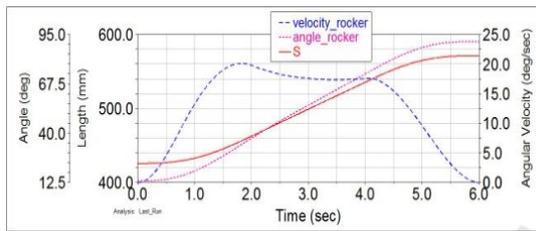


Figure.6: The angular, velocity of the rocker and the elongation of the line actuator.

As can be seen from the image, the maximum displacement of the linear actuator S is 145mm, which satisfies the maximum stroke of the selected linear actuator of 152mm. The maximum rotation angle of the rocker is 91, which is similar to the 90 rotation angle of the rocker in the mathematical model. At the beginning and ending of the motion, the displacement of the linear actuator changes gently and the angular velocity of the rocker is not accelerated or decelerated rapidly.

4 CONCLUSIONS

1. The folding length optimized by MATLAB has increased by 18% compared with that before optimization and is more than one third of the length of frame. The folding effect of frame meets the design requirements.

2. The comparison between MATLAB calculation results and ADAMS simulation results shows that the modeling error is less than 1%, which reflects the reliability of this model.

3. The variation of motion parameters of key components of folding mechanism shows the stability of the designed mechanism at a certain speed.

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