A Hybrid CPU-GPU Scalable Strategy for Multi-resolution Rendering of Large Digital Elevation Models with Borders and Holes

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Abstract: Efficient rendering of large digital elevation models remains as a challenge for real-time applications, especially if those models contain irregular borders and holes. First, direct use of hardware tessellation has limited scalability; although the graphics hardware is capable of controlling the resolution of patches in a very efficient manner, the whole patch data must be loaded in memory. Second, previous techniques restrict elevation data resolution and do not handle irregular border or holes. In this paper, we propose an efficient and scalable hybrid CPU-GPU algorithm for rendering large digital elevation models. Our proposal effectively combines GPU tessellation with CPU tile management, taking full advantage of GPU processing capabilities while maintaining graphics-memory use under practical limits. Our proposal also handles models with irregular borders and holes. Additionally, we present a technique to manage level of detail of aerial imagery mapped on top of elevation models. Both geometry and texture level of detail management run independently, and tiles are combined with no need to load extra data.

1 INTRODUCTION

Due to advances in acquisition technologies, large digital elevation models (DEM), with gigabytes of data, have been widely available. As a consequence, an efficient and scalable rendering technique for such models has been mandatory in different applications. Without any special treatment, the amount of data easily exceeds hardware limits in both memory and triangle throughput.

On the other hand, graphics hardware tessellation has evolved and is currently able to generate complex geometry on the fly (Schäfer et al., 2014), eliminating the need to generate the geometry on the CPU, and thus avoiding transferring a large amount of data to the graphics pipeline at each frame. In this paper, we present a hybrid CPU-GPU strategy for handling large elevation models. Previous works have also taken advantage of hardware tessellation for DEM rendering (Yusov and Shevtsov, 2011; Fernandes and Oliveira, 2012; Kang et al., 2015), trying different strategies for mapping CPU tiles to GPU patches and for avoiding cracks along patch interfaces. Our hybrid approach makes it possible to control both CPU and GPU memory and computational loads, by tuning CPU-tile and GPU-patch sizes, and avoids cracks by construction.

Furthermore, previous proposals on rendering digital elevation models restrict tile/patch resolutions, generally as $(2^n + 1) \times (2^n + 1)$, and do not handle irregular borders and holes. We present a new method for handling borders and holes in DEMs. We introduce a metric to compute horizontal errors due to border displacements, as tile/patch resolution is reduced, and ensure these errors are under control in our levelof-detail management. Our approach also imposes restrictions on tile/patch resolution; however, being able to deal with holes allows us to easily handle models in arbitrary resolutions by just filling the "blanks" with holes. As we shall demonstrate, we are then able to render very long terrain strips and large seismic surfaces with complex holes.

We then extend our proposal to also manage level of detail of aerial imagery mapped as textures on top of elevation models. The texture tiles are also stored in a quadtree structure and the active cut is mandated by the screen resolution of projected tiles. Both geometry and texture level-of-detail managements run independently. As a result, we may end up with a 1to-*n* or *n*-to-1 mapping between geometry and texture tiles; both cases are handled smoothly without any additional load of data.

The rest of this paper is organized as follows. In the next section, we discuss related work. Then we

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present our strategy, discuss how we handle irregular borders and holes, and describe how we combine aerial level of detail. Next, we present the results of several computational experiments. Finally, we draw concluding remarks.

2 RELATED WORK

Several researches have been done to efficiently render massive terrain data. In (Pajarola and Gobbetti, 2007), the authors presented a comprehensive survey on multi-resolution approaches for digital terrain rendering, analyzing different choices of data structures and error metrics. The general idea consists in structuring the data in an hierarchical way to manage adaptive level of detail.

Early multi-resolution approaches have opted for a triangle-based hierarchy. Binary tree hierarchies were proposed to control triangulation resolution based on a screen-space error evaluation (Lindstrom et al., 1996) (Duchaineau et al., 1997) (Lindstrom and Pascucci, 2001). While simple to implement, these techniques are limited by CPU-GPU memory transfer because the geometry has to be loaded to the GPU for every frame.

In order to overcome this limitation, techniques such as BDAM (Cignoni et al., 2003a) and P-BDAM (Cignoni et al., 2003b) opted for a tile-based hierarchy: each hierarchical node represents a precomputed triangle surface tile instead of a single triangle. The elevation data, which is encoded using a wavelet-based compression technique, can be placed into the GPU memory for future use. The use of a tile-based hierarchy is scalable and efficient, at the cost of decreased adaptivity, processing more triangles than needed. Geometry clipmaps (Losasso and Hoppe, 2004) use a mipmap pyramid as the terrain representation and a compression technique to reduce the storage requirements; however, they simplified the evaluation of the screen-space error to choose the appropriate level of detail, thus affecting resulting image quality.

Recent approaches have tried to explore the GPU tessellation to speedup mesh generation. A crack-free terrain surface generation with a continuous LOD triangulation algorithm is presented in (Fernandes and Oliveira, 2012). The method simply estimates the size of a patch in screen-space and tessellates it accordingly, producing a constant triangle size in pixels. In (Cervin, 2012), a density map is used, which encodes the terrain curvature, to choose the appropriate level of detail in the GPU tessellation stage, creating more triangles for a high density area (bumpy land) and few

triangles for low density areas (flat land). However, these techniques do not accurately evaluate geometry errors in the final triangulation.

The approach proposed in (Yusov and Shevtsov, 2011) is similar to ours. They also subdivide the model in patches (we call tiles) and then in blocks (we call patches). However, their approach is not able to ensure, by construction, crack-free surface along tile interfaces. To hide gaps along tile interface, they exploit "vertical skirts" as proposed in (Ulrich, 2000). Also, no analysis is performed to justify the choice of tile and patch resolutions. On another hand, Kang et al. (Kang et al., 2015) have presented an strategy for avoiding cracks by construction, annotating four edge LODs for each quadtree node (tile), determined by using the inner LODs of the current node and its neighbors. As in their approach each tile is mapped to a single patch, all tessellation levels are computed in CPU. We use a similar strategy to avoid crack along tile interfaces, but our approach maps each CPU tile to a set of GPU patches, minimizing CPU load. As a consequence, we also need to avoid cracks along patch interfaces.

3 GEOMETRY LOD

The proposed algorithm to render multi-resolution elevation models is a hybrid CPU-GPU approach. The CPU is responsible for managing a quadtree of tiles. Each tile is subdivided into a set of patches that are sent to the GPU, as illustrated in Figure 1.

3.1 Pre-processing Phase

In a pre-processing phase, the quadtree is built applying a bottom-up procedure. First, the tile resolution is chosen, and different choices of resolution affect memory footprint and performance, as we shall see. The whole elevation data is subdivided into tiles representing the quadtree leafs. Then, for each four neighbors, a parent tile is created with half of the children's resolution, filling the quadtree top levels. For simplicity, we do not apply any filter for reducing tile resolution; we only eliminate each other line/column of data, avoiding discontinuities along tile interfaces.

The resolution of each patch, and consequently the number of patches per tile, also affects performance. The maximum resolution is limited by the graphics hardware. In Section 6, we present the computational test we ran to test different resolutions. Once tile and patch resolutions are chosen, we are ready to compute the errors in object space associated to each tile and each patch.



Figure 1: Geometry tiles are selected to honor a predefined screen-space error limit; each tile is subdivided into a fixed number of patches to the GPU.

Tile and patch resolutions must be of dimension $(2^n + 1) \times (2^n + 1)$, because neighbor tiles (or patches) share the same border pixels. For simplicity, we mention dimension values by power of two $(2^n \times 2^n)$. To illustrate the discussion that follows, let us consider that tile's resolution is 512×512 and patch's is 64×64 . So, each tile is subdivided into 8×8 patches.

For each tile, we first compute the error in object space associated to each patch for different resolutions. For the leaf tiles, the error for each patch at maximum resolution is zero. We denote this by $\varepsilon_{i_{64}}^l = 0$, where *i* represents the patch, *l* the tile quadtree level, and 64 the patch tessellation level. For each patch, we then annotate the errors associated to smaller tessellation levels: $\varepsilon_{i_{12}}^l$, $\varepsilon_{i_{12}}^l$, \cdots , $\varepsilon_{i_1}^l$.

smaller tessellation levels: $\varepsilon_{i_{32}}^l, \varepsilon_{i_{16}}^l, \dots, \varepsilon_{i_1}^l$. The error in object space associated to a tile is given by: $E^l = \max_i \varepsilon_{i_{64}}^l$, being naturally zero for the leaf tiles. The errors of patches at upper quadtree levels are inherited from the lower levels with half of the maximum tessellation:

$$\varepsilon_{i_{64}}^{l-1} = \max_{i \in N} \varepsilon_{i_{32}}^l \tag{1}$$

where *N* represents the set of associated four neighboring patches. This error is then propagated to smaller tessellation levels and, again, the tile error is $E^{l-1} = \max_i \varepsilon_{i_{64}}^{l-1}$. For each tile, all patch errors are annotated and stored in a texture to be accessed in the GPU-tessellation stage. Figure 2 illustrates this object-space error computation.

3.2 Rendering Phase

At run time, the error in screen space ρ is computed in the usual way, either to select tiles on the CPU or to determine patch tessellation level on the GPU:

$$\rho = \lambda \frac{E}{d}$$
, with $\lambda = \frac{w}{2\tan\frac{\theta}{2}}$ (2)

where E, w, θ and d represent, respectively, the error in object space, the viewport resolution, the camera field of view and the distance from the camera to the closest point of the tile's (or patch's) 3D bounding box.



Figure 2: Computed object-space errors: at leaf tiles, for each patch at maximum tessellation level, the associated error is zero; errors are then propagated to other possible tessellation levels. Errors of patches at upper quadtree level are inherited from the lower levels. The error associated to each tile is the maximum annotated to patches at maximum tessellation level.

On the CPU, we use two threads to process the data. The *loading thread* is responsible for predicting camera movement and loading tiles in advance from disk. The *rendering thread* is responsible for selecting tiles, among the loaded ones, necessary to render the terrain honoring a prescribed error tolerance for the current frame. Both threads use the conventional top-down approach, subdividing the tile if the screen space error exceed the prescribed tolerance.

Once the frame tiles are selected, the CPU is responsible for issuing rendering commands for the corresponding patches. In the tessellation shader, the level of detail of each patch is determined. The inner tessellation level is given by evaluating the screenspace error of the patch, choosing the lowest possible resolution. The choice of the outer tessellation level must avoid T-junctions between adjacent patches. There are two cases, denoted here by the *patch-patch case*, for interfaces between two patches of a same tile, and the *tile-tile case*, for interfaces between patches of different tiles.

The patch-patch case is easily handled, because all the needed data are available within the tile. The outer tessellation level is given by the maximum subdivision requested by the interfacing patches, as in (Yusov and Shevtsov, 2011). So, the coarsest patch gets refined along the border:

$$n_{outer} = \max(n_i, n_j) \tag{3}$$

where n_i and n_j represents the computed inner level of the interfacing patches.

The challenge lies on the tile-tile case; data are not available within a tile and additional information is necessary. To overcome this problem, on the CPU, after performing the LOD algorithm (tile selection), for each tile, we annotate the difference in level between adjacent selected tiles; one value for each tile edge. If the level of the adjacent tile is equal or higher (the adjacent is more refined), we annotate the value zero; if the level of the adjacent tile is lower (it is less refined), we annotate the difference in level: $l_{tile} - l_{adj}$. Figure 3 illustrates the values annotated for a sample active quadtree. In the tessellation shader, the outer tessellation level of a tile-tile interface is given by:

$$n_{outer} = \frac{n_{max}}{2^{\delta}} \tag{4}$$

where n_{max} is the maximum possible subdivision for the patch and δ is the annotated level difference. This imposes a limit in the unbalance level of adjacent tiles equals to $\log_2 n_{max}$, which, in practice, tends not to be a problem. For instance, for a 64×64 patch resolution, the unbalance between adjacent tiles cannot exceed a factor of six. If this limit is reached, it is imposed a subdivision on the less refined tile. All patch borders along the tile edge get the same outer tessellation level. Note that this approach makes all interface between tiles refined to the most possible resolution. This induces a small increase in the number of generated triangles but makes it simple to avoid T-junctions. As we shall demonstrate, this approach to ensure crack-free surface does not impact performance. Moreover, there is no need to employ additional procedures for crack filling, such as to add flanges, to join tiles with special meshes, or to generate vertical ribbon meshes(Ulrich, 2000).



Figure 3: Annotated level differences along tile edges. For each edge of a selected tile, the neighboring tiles are checked; if neighbor tile is at same or higher level, zero is annotated; if neighbor tile is at lower level, level difference is annotated.

4 BORDERS AND HOLES

We now extend our approach to deal with irregular borders and holes. In such models, there are *regular vertices* (\bullet) and *void vertices* (\circ). We then consider that there are borders along all the interfaces between regular and void vertices. Figure 4a (left) illustrates a 4×4 patch with four void vertices and the corresponding defined border. At first, void vertices have no associated elevation data. In order to render the border, in a pre-processing phase, we assign, to each void vertex, an elevation value given by its neighboring regular vertices.

For computing the error in object space when decreasing tile/patch resolution, we need to consider border displacements, which we identify as *horizon-tal error*. Figure 4 shows what happens when decreasing the resolution of the illustrative patch from 4×4 to 2×2 (Figure 4a). As each other line/column are eliminated, the border is displaced, and horizontal error, illustrated in Figure 4b, has to be considered.



Figure 4: Horizontal object space errors: (a) illustrative patch with void vertices and corresponding coarser level; (b) computed horizontal errors due to border displacement.

Table 1 summarizes all possible cases involving void vertices when reducing resolution. For each eliminated vertex in a patch, the error is computed considering removing the middle vertex of four edges: horizontal, vertical, forward diagonal, and backward diagonal. The maximum error is stored per patch considering all edges of all eliminated vertices. Let as take as example the second table entry, case A - C - B as $\bullet - \bullet - \circ$ (regular, regular, and void vertices), where vertex *C* is removed: originally, the border is in the middle of edge \overline{CB} ; after removing vertex *C*, the border is moved to the middle of edge \overline{AB} , representing a displacement equal to $\Delta/2$, where Δ is the length of edge \overline{AC} (or \overline{BC}).

Vertical errors are expressed in the usual way by:

$$E_{\nu} = \left| \frac{z_A + z_B}{2} - z_C \right| \tag{5}$$

where z_V represents the elevation value at vertex V. This is valid for all cases, except for the last table entry, involving only void vertices; in this case, both vertical and horizontal errors are zero.

In the pre-processing phase, both maximum errors are annotated. The combined error, expressed by:

$$E = \sqrt{E_{\nu}^2 + E_h^2} \tag{6}$$

is only computed in the rendering phase. The reason we do that is to allow applying a vertical scale factor when visualizing the model, which is commonly employed.

In the rendering phase, the combined error is projected to compute the error in screen space. Note that the whole patch is rendered, even triangles with void vertices. In order to correctly render the border, we assign an attribute equal to one for regular vertices and equal to zero for void vertices. This attribute is interpolated by the rasterizer and, in the fragment shader, fragments with attribute value less than 0.5 are discarded.

Patches with only void vertices are not rendered, and tiles with only void vertices are not even represented in the quadtree. This allows us to process rectangular elevation data using regular quadtree in a effective way. The rectangular data is completed with void vertices to get the required resolution $(2^n + 1 \times 2^n + 1)$ but, in the end, we get a noncomplete quadtree, as void tiles are discarded.

5 TEXTURE LOD

On top of the multi-resolution elevation surface, we map aerial imagery as textures, also managing its

Table 1: Table of corresponding horizontal (E_h) errors when eliminating a vertex *C* in the middle of an edge \overline{AB} . The value of Δ corresponds to the horizontal length of \overline{AC} or \overline{CB} . Note that the edge \overline{AB} may be horizontal, vertical, forward diagonal, or backward diagonal, with respect to the patch.

| A-C-B | E_h |
|-------------------------------|------------|
| $\bullet - \bullet - \bullet$ | 0 |
| $\bullet - \bullet - \circ$ | $\Delta/2$ |
| $\bullet - \circ - \bullet$ | Δ |
| $\bullet - \circ - \circ$ | $\Delta/2$ |
| $\circ - \bullet - \bullet$ | $\Delta/2$ |
| $\circ - \bullet - \circ$ | Δ |
| $\circ - \circ - \bullet$ | $\Delta/2$ |
| 0-0-0 | 0 |

level of detail. The challenge here resides on combining both geometry and texture tiles without loading additional data. Each LOD manager has to independently select the tiles necessary to meet the desired quality in the final image.

In the preprocessing phase, a conventional quadtree structure is created to store the texture in different resolutions, using the box filter to reduce resolution of parent tiles. In the rendering phase, again, a separate thread is used to predict, select, and load texture tiles necessary for the next frames. The rendering thread selects the tiles needed for each frame, considering the loaded ones.

The selection of texture tiles also employ the conventional top-down procedure. For each visited tile in the hierarchy, we compute its longest edge in screen space, L_{proj} , and compute the magnification rate:

$$r_{mag} = \frac{L_{proj}}{w_{tile}} \tag{7}$$

where w_{tile} represents the maximum tile dimension. In our experiments, we use a limit of value 1.5: if the magnification rate is less than 1.5, the tile is selected; otherwise, its four children are processed.

As tile selection runs independently for geometry and texture, we end up having three cases of geometry-texture tile correspondences: 1-to-1, *n*-to-1, 1-to-*n*. Figure 5 illustrates these different correspondence cases.



Figure 5: Correspondence among geometry (in red) and texture (in blue) tiles: at the left quadrants, 1-to-1 correspondence cases are configured; at the upper right quadrant, there is a *n*-to-1 case and, at the lower right quadrant, there is a 1-to-*n* case, which requires the use of *virtual geometry tiles* to be rendered.

The 1-to-1 case is the direct one; we have one geometry tile for each texture tile: vertices defining the patches receive texture coordinates from 0.0 to 1.0. The *n*-to-1 case is also simple: there are *n* geometry tiles mapped into one texture tile. Texture coordinates are transformed accordingly, and all geometry tiles uses the same texture object.

The 1-to-n case is the one that requires a more elaborated solution: we have one geometry tile that must be rendered using different texture objects. It is needed to render the geometry tile multiple times, one for each texture tile. We see two approaches for doing this. In the first approach, for each render pass, we would select the patches covered by each texture tile. Although this solution seems straightforward, it presents two important drawbacks: (i) the correspondence factor, n, would be limited by the number of patches in a geometry tile; (ii) we would need a specialized algorithm to handle tiles with less patches.

We have opted for a second solution: we generate a *virtual geometry tile* for each texture tile. Each virtual tile is subdivided into the same number of patches as a regular tile, so there is no need to modify the algorithm. What differs is that a virtual tile uses a subset of the elevation data: all virtual tiles are rendering using the same elevation data; texture coordinates to access these data are assigned accordingly. Each patch of virtual tiles inherits the object-space errors annotated to the containing real patch.

6 RESULTS AND DISCUSSION

In this section, we describe a set of computational experiments we used to test and tune the proposed method. All experiments were run on a i7-3960X processor computer with 24GB of RAM, equipped with a NVIDIA Geforce GTX TITAN graphics card with 6GB of VRAM.

6.1 Tile and Patch Size Analysis

First, we analyze the influence of the geometry tile size. For this computational experiment, we used a high-resolution version of the Puget Sound Terrain. The elevation data has a resolution of $65K \times 65K$ with 4 meter pixel spacing, using the aerial imagery mapped as texture with $262K \times 262K$ in size and 1 meter pixel spacing. The dataset was obtained from (WU, 2017) and (USGS, 2017), totalizing 250GB of disk space. We set the screen resolution to 1920×1080 and the geometry error tolerance to 1.0 pixel.

To run the experiment, we defined a camera path over the terrain, crossing flat and bumpy regions along the way. We run the same experiment with two different patch size $(32 \times 32 \text{ and } 64 \times 64)$ and tested different tile sizes. Figures 6 and 7 show the achieved frame rate. In this experiment, we got better performance with 128×128 tiles for patches of 32×32 and with 256×256 tiles for patches of 64×64 , what suggests an ideal relation of 4×4 patches per tile on this machine. As we increase tile size, we reduce the height of the quadtree, thus alleviating CPU workload and increasing performance. On the other hand, as we increase tile size, we reduce LOD granularity, requiring more GPU memory and processing. Tests with smaller patches resulted in worse performance.



Figure 6: Achieved frame rate along camera path for patch size of 32×32 .



Figure 7: Achieved frame rate along camera path for patch size of 64×64 .

The following figures show different measurements along the camera path for the 32×32 patch; similar results were achieved for the 64×64 patch. Figure 8 shows the required GPU memory for different tile sizes. The 128×128 , which delivered better performance, presents a good compromise between performance and requested memory resource. Figure 9 shows the required CPU time to process the frames along the camera way. As expected, small tiles increases CPU workload, degrading performance. Figure 10 shows the observed error in screen space; recall that the used tolerance was set to 1 pixel. Small tiles do not honor the requested image quality, since the application becomes CPU limited, not being able to assure the quality in real time.

6.2 Comparison with Other Methods

We compared the rendering performance of our method with the implementation of the chunked LOD



Figure 8: Required GPU memory (in MB) per frame along camera path (patch 32×32).



Figure 9: Required CPU processing time (in milliseconds) per frame along camera path (patch 32×32).

approach provided by (Ulrich, 2000). The available code uses the Puget Sound data with $16k \times 16k$ of resolution. In the experiment, we set the screen error tolerance to one pixel and use a similar camera paths. Figure 11 shows the achieved performance along the camera path: our approach was in average 6.5x faster than the chunked LOD approach. This relative gain is higher than the one reported by (Yusov and Shevtsov, 2011) but our experiment was ran on a different equipment (they reported their proposal run 3.5x faster than the chunked LOD approach, using two pixel tolerance on a NVidia GTX480).

6.3 Terrain Strip

In order to demonstrate the ability of our system to handle terrain with irregular border, we run a second experiment using a dataset that represents the elevation model of 1,000 kilometers of a terrain strip that is the site a natural gas/oil pipeline, as shown in Figure 12. This model is used in an application to monitor emergency situations along the pipeline. The raw dataset consists of several partially overlapping terrain patches, one for each kilometer of the pipe, resulting in 86 GB and 130 GB of elevation and aerial imagery data, respectively. To pre-process this dataset, we compose all files into a virtual raster file, using a common GIS format (Virtual Raster). The final virtual image resolution was $2^{22}x2^{22}$. However, since this virtual image contains large amount of void data, the pre-processing is performed in rea-



Figure 10: Observed maximum screen space error (in pixels) per frame along camera path (patch 32×32). Recall we request an error of at most 1 pixel; values above this number signalize the system is not capable of delivering the requested quality in real time.



Figure 11: Comparison on performance of our approach and the chunked LOD approach.

sonable time, only persisting tile with valid data. The proposed system is capable of rendering such model smoothly, from overview to zoom-in shots.



Figure 12: A rendered image of an actual terrain strip along a gas/oil pipeline of 1,000 kilometers.

6.4 Seismic Surface

This last experiment demonstrates our system dealing with internal holes in the surface. We used a horizon surface resulted from an actual seismic data processing. This surface is represented by an elevation model but contains a large amount of void data, and correctly rendering the holes is crucial for an accurate interpretation of the model. Figure 13 shows a rendered image. Again, the proposed system was capable of rendering the model smoothly ensuring image quality even for the complex structure of such a model.



Figure 13: A rendered image of an actual horizon surface from a seismic data.

7 CONCLUSION

We presented a new hybrid CPU-GPU strategy to render large digital elevation models with aerial imagery mapped as textures. Level of detail managements, for geometry (elevation) and texture (aerial imagery), run independently. On the CPU, a multi-threaded implementation is responsible for selecting, loading, and transferring to the GPU active tiles. Geometry tiles are decomposed into patches, and tessellation shaders are used to determine tessellation levels for each patch. The proposed method avoids crack between patch and tile interfaces by construction. Geometry and texture tiles are combined with no extra data load, even in the case where one geometry tile is covered by a set of different texture tiles.

We also extended the proposal for handling terrain with irregular borders and surfaces with holes, introducing the concept of horizontal errors. Dealing with irregular borders mitigates the constraint of power of two (plus one for the border) on terrain dimensions; supporting surfaces with hole has an important application on rendering interpreted seismic surfaces of large datasets.

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REFERENCES

Cervin, A. (2012). Adaptive Hardware-accelerated Terrain Tessellation. PhD thesis, Linköpings Universitet, Tekniska Högskolan.

- Cignoni, P., Ganovelli, F., Gobbetti, E., Marton, F., Ponchio, F., and Scopigno, R. (2003a). BDAM — Batched Dynamic Adaptive Meshes for High Performance Terrain Visualization. *Computer Graphics Forum*, 22(3):505–514.
- Cignoni, P., Ganovelli, F., Gobbetti, E., Marton, F., Ponchio, F., and Scopigno, R. (2003b). Planet-Sized Batched Dynamic Adaptive Meshes (P-BDAM). In *Proceedings of the 14th IEEE Visualization 2003* (VIS'03), VIS '03, pages 20–, Washington, DC, USA. IEEE Computer Society.
- Duchaineau, M., Wolinsky, M., Sigeti, D., Miller, M., Aldrich, C., and Mineev-Weinstein, M. (1997). ROAMing terrain: Real-time Optimally Adapting Meshes. In *Visualization '97., Proceedings*, pages 81– 88.
- Fernandes, A. and Oliveira, B. (2012). Gpu tessellation: We still have a lod of terrain to cover. In Cozzi, P. and Riccio, C., editors, *OpenGL Insights*, pages 143–160. CRC Press.
- Kang, H., Jang, H., Cho, C.-S., and Han, J. (2015). Multiresolution Terrain Rendering with GPU Tessellation. *Vis. Comput.*, 31(4):455–469.
- Lindstrom, P., Koller, D., Ribarsky, W., Hodges, L. F., Faust, N., and Turner, G. A. (1996). Real-time, continuous level of detail rendering of height fields. In *Proceedings of the 23rd annual conference on Computer graphics and interactive techniques*, pages 109–118. ACM.
- Lindstrom, P. and Pascucci, V. (2001). Visualization of large terrains made easy. In *Visualization*, 2001. VIS'01. Proceedings, pages 363–574. IEEE.
- Losasso, F. and Hoppe, H. (2004). Geometry Clipmaps: Terrain Rendering Using Nested Regular Grids. In ACM SIGGRAPH 2004 Papers, SIGGRAPH '04, pages 769–776, New York, NY, USA. ACM.
- Pajarola, R. and Gobbetti, E. (2007). Survey of semi-regular multiresolution models for interactive terrain rendering. *The Visual Computer*, 23(8):583–605.
- Schäfer, H., sner, M. N., Keinert, B., Stamminger, M., and Loop, C. (2014). State of the Art Report on Real-time Rendering with Hardware Tessellation. In *Eurograph ics*, pages 93–117.
- Ulrich, T. (2000). Rendering massive terrains using chunked level of detail. ACM SIGGRAPH Course "Supersize it! Scaling up to Massive Virtual Worlds".
- USGS (2017). US geological survey USGS. https://www.usgs.gov/products/maps/gis-data.
- WU, G. R. G. (2017). Geomorphological research group - washington university. http://gis.ess.washington.edu/data/.
- Yusov, E. and Shevtsov, M. (2011). High-performance terrain rendering using hardware tessellation. *Journal of* WSCG, 19(3):85–92.