Data Aggregation and Distance Encoding for Interactive Large Multidimensional Data Visualization

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Abstract: Visualization of unlabeled multidimensional data is commonly performed using projections to a 2D visual space, which supports an investigative interactive analysis. However, static views obtained by a projection method like Principal Component Analysis (PCA) may not capture well all data features. Moreover, in case of large data with many samples, the scatterplots suffer from overplotting, which hinders analysis purposes. Clustering tools allow for aggregation of data to meaningful structures. Clustering methods like K-means, however, also suffer from drawbacks. We present a novel approach to visually encode aggregated data in projected views and to interactively explore the data. We make use of the benefits of PCA and K-means clustering, but overcome their main drawbacks. The sensitivity of K-means to outlier points is ameliorated, while the sensitivity of PCA to axis scaling is converted into a powerful flexibility, allowing the user to change observation perspective by rescaling the original axes. Analysis of both clusters and outliers is facilitated. Properties of clusters are visually encoded in aggregated form using color and size or examined in detail via local scatterplots or local circular parallel coordinate plots. The granularity of the data aggregation process can be adjusted interactively. A star coordinate interaction widget allows for modifying the projection matrix. To convey how much the projection maintains neighborhoods, we use a distance encoding. We evaluate our tool using synthetic and real-world data sets and perform a user study to evaluate its effectiveness.

1 INTRODUCTION

Raw representations of multidimensional data points are traditionally found in the form of large numerical matrices in which each column corresponds to an attribute or dimension (Bache and Lichman, 2013). In order to allow for an effective visual presentation of the data, however, a mapping from the original high-dimensional data space into a lower-dimensional visual space needs to be discovered. The sufficient dimensionality reduction is generally accompanied by an equally significant loss of information. Dimensionality reduction mappings often aim at exploiting the intrinsic dimensionality of the set, which can be much smaller than that of the original data space (Bennett, 1965). The second, more user-oriented phase of the data visualization process is the production of an aesthetic and insight-stimulating representation to display or interact with. Cognitive Psychology and Information Visualization research has demonstrated that representations of multidimensional data generated with the aid of computer-based visualization tools improve human cognition (Parsons and Sedig, 2013). In order to achieve that, many dynamic and static visualization techniques draw on aspects of human perception such as distance perception, shape identification, color recognition, size differentiation, motion detection (Healey, 1996). Although data attributes can in principle be mapped to various properties of representation glyphs (position, color, size, etc.), a typical cap is reached after the fifth or sixth dimension. Thus, for datasets of higher intrinsic dimensionality, it is important that adequate dimensionality-reduction and interactive-display techniques are employed in combination.

Our goal was to design, implement, and evaluate an easy-to-use data visualization tool through which spatially-accurate representations of large, unlabeled multidimensional data sets can be interactively examined. The qualitative study of correlations, clusters and exceptional points is empowered.
For the development of the application, the best characteristics of Principal Component Analysis (PCA) and K-means clustering are drawn upon. The fact that both methods provide for rapid computation and process data in an unsupervised manner makes them highly suitable for our purposes. Our tool aims at enabling the user to investigate spatial relations between data points via a distance-preserving representation, so PCA is an adequate approach. Since the tool visualizes large amounts of data in a limited screen space, measures are taken to minimize visual clutter and maximize cluster definition. One half of this is achieved via the PCA projection matrix which is further modifiable through the star-coordinates widget and with which data points are projected in as much of a spread-out manner as possible.

Regions where still many data points are accumulated then benefit from a summarization procedure developed on the basis of K-means clustering. By running this new adjustable-parameter clustering algorithm, small aggregations of data points can be unraveled and displayed at customizable levels of granularity. Important cluster properties, such as area, density and population profiles (in circular parallel coordinates) are visually encoded and displayed.

2 BACKGROUND

Dimensionality reduction approaches can be separated into two big families. Supervised methods operate on labeled data sets in which all data points are preliminarily assigned to a class based on the objective truth or an expert’s opinion. In applications where vast amounts of unlabeled data need to be compressed into a lower-dimensional space unsupervised techniques are preferred. With respect to distortion of relations within the original set, distance-preserving versus non-distance-preserving maps are differentiated between. Often distance-preserving projections aim at the arrangement of codomains whose local geometrical characteristics reflect the characteristics of the original set (Zhu et al., 2013).

Moreover, computational complexity and ease of implementation can be considered. Linear as opposed to non-linear dimensionality reduction methods have notably low computational costs and can be effectively implemented by reductions to matrix factorization and/or multiplication. Nonlinear methods have been empirically established to produce better results on artificial tasks but in many real-life applications linear methods prove equally reliable (von der Maaten et al., 2008). Therefore, the advantage of their computational simplicity should not be discounted.

Principal Component Analysis (Pearson, 1901) is an unsupervised, feature-transforming and linear dimensionality reduction procedure which maps an original data space with possibly correlated axes into a target space where no linear correlation between dimensions is observed. The basis of the new space is formed by the principal components of the data, which is a set of vectors existing in the original space, but along which the variance of the data is maximal. Geometrically, this corresponds to computing an n-dimensional ellipsoidal container for the data points, whose axes lie in the directions of optimal data variance. The eigenvectors of a symmetric matrix are by default pairwise orthogonal. Therefore, as the extraction of ellipsoid axes is based on eigen-decomposition of the data’s covariance matrix, the resulting vector set is also orthogonal. Three common approaches of centering, scaling and standardization are discussed in literature (Flury, 1997). Centering, the least intrusive of the three, refers to the shifting of data points to mean 0 along each axis before the eigen-decomposition on the covariance matrix is computed, and is what the majority of advanced linear algebra programming libraries implement to ensure minimization of the mean squared error. Scaling divides the point entries along each axis by the standard deviations in the data-matrix columns representing the axes. This results in all attributes having unit variance and ensures that variables are treated with equal weight. Standardization is the application of first centering and then scaling and, like scaling alone, is recommended only when information about differences in measuring scales is available.

An intuitive and computationally effective method of modifying the data projection matrix (and thus the observation perspective) is discussed by Kandogan in his work on Star Coordinates (Kandogan, 2000). In a star-coordinates system the position of a data point is computed as a vector sum of the unit vectors representing each axis, scaled by the point’s corresponding attribute-measurement. The unit vectors all lie in a 2D plane, distributed by the same angle and sharing a common origin.

The objective of clustering is the partitioning of a dataset into groups such that intragroup variance is minimized. Traditionally used in data mining and statistical analysis, clustering has an alternative application as a partial summarization procedure of
Data when visual clutter in graphical applications is to be avoided. A variety of clustering techniques exists, belonging to one out of four organizational branches, according to cluster model. Hierarchical cluster analysis is a greedy approach aiming at the establishment of a ranked sub-structure of the original data set. Hierarchical algorithms employ a predefined cluster-similarity measure according to which sub-clusters are merged or super-clusters are split. Decisions about cluster treatment are based on the local optimization criterion entailed by the measure. Data set representations obtained through agglomerative or divisive clustering are especially appropriate when a dendrogram-based final depiction is required (Long and Linsen, 2009). When a distance-preserving representation of the data is required however, more suitable choices exist.

Distribution clustering takes advantage of statistical knowledge of data distribution models. It assumes that objects generable under the same distribution parameters must share a deeper commonality. The arrival at suitable distribution-based procedures can be guided by Expectation Maximization but it often demands the solution of a non-trivial maximization problem, presented by the M-step (Dempster, 1977).

Density-based clustering defines a cluster as a regional density maximum in the original data space and uses density drops to delineate cluster boundaries. To identify a point as belonging to a cluster most density-based algorithms employ a reachability or a linkage relation whose asymmetry guarantees the termination of successive point inclusion (Dempster et al., 1977). The main advantage of density-based methods is the ability to recognize irregular cluster shapes. Disadvantages manifest in computational speed and with highly high-dimensional data sets where the Curse of Dimensionality (Bellman, 1957) interferes with the notion of density.

In centroid-based clustering, convex formations of data points are sought such that each group is centered around a prototype, which may or may not be a member of the original set. Common choices of representative points are the cluster’s mean or median. Therefore, optimization of cluster center as opposed to cluster border is performed. Since the decision (simpler) version of this problem is already NP-complete, effort has been focused on the development of approximate solutions. Centroid-based clustering is straightforward and efficient to implement in an iterative fashion and has an empirically fast convergence rate.

K-means clustering is an unsupervised centroid-based clustering algorithm, developed in response to the cluster-center optimization problem. Random initialization of a predetermined-cardinality centroid set is performed and upon convergence a Voronoi partitioning of the data space is returned. Although there exist synthetic data sets for which convergence is exponential, empirical tests have established that runtime on real-life data is polynomial (Har-Paled and Sadri, 2005). A disadvantage of K-means is that due to its approximative nature, it is susceptible to local solution optima. Also, while running the algorithm the correct number of random prototypes might produce inconsistent results, an ill-informed number of centroids will almost always result in under- or oversegmentation. Another concern is centroid-based algorithms’ sensitivity to outliers. One strategy to improve the reliability of K-means is the removal of outliers (Hautamäki et al., 2005). We argue though that outliers are of relevance for many application scenarios.

3 APPROACH

The main idea guiding the standard workflow of the developed visualization tool is to first lay the examined dataset out in a maximally distance-preserving fashion and display a low-detail summary of it in the form of a small number of representation glyphs encoding point-group area and relative density. The user is then allowed to toggle the visibility of observation points belonging to each glyph or of the entire dataset and to further refine the level of presented detail by modifying the tool’s algorithm parameters.

If the user wishes to recompute the projection by using different measurement units for a certain data attribute, he/she is allowed to rescale the attribute values in the original data matrix by operating one of the tool’s widgets. Additionally, the attribute values (in the currently used units) of points summarized by each glyph can be plotted in circular parallel coordinates upon request.

Observation of the dataset from various perspectives is encouraged via an interactive application of translations and rotations. Animated transitions between layouts and detail-level states are computed at interactive rates. Since viewing the dataset from a non-distance-preserving perspective can lead to the distortion of spatial information, a customizable number of helper links can be output between glyphs, encoding the represented group-centers’ actual proximity.
In the following, the individual steps of our approach are detailed.

### 3.1 Dimensionality Reduction

In order to obtain a matrix with which to transform the data into a simpler (fewer-dimensional) representation, we perform a PCA. Correlations between axes indicate that the data set possesses a much lower intrinsic dimensionality than the space in which it was originally recorded. To describe it in terms of this lower-dimensional space, the tool multiplies its original representation by the PCA matrix. The resultant contains a sufficiently large amount of spatial information about the data, recorded in its first few columns (determined by the intrinsic dimensionality). Principal components of lesser contribution are dismissed as the descriptive power they hold is typically negligible and a reduced matrix representation of the dataset is obtained.

### 3.2 Density Maxima Localization

The study of outliers finds various practical applications in performance, anomaly, and behavior monitoring. Therefore, an approach which not only preserves exceptional points in the dataset but also devotes equal attention to their handling as to the processing of other internal data-set structures, is advised. As an additional benefit, the undeterministic properties of the original K-means algorithm are ameliorated, since the number and the locations of initial centroids can be pre-informed.

A method for capturing both compact groups and outliers while minimizing distortions in the data representation and stabilizing the K-means clustering output, is developed, based on the analysis of local density maxima. Therefore, the discovery of high-density regions as a procedure prerequisite is performed.

Firstly, the columns of the reduced matrix are rescaled to the interval [0,1]. This is equivalent to fitting the transformed and simplified data points into a multi-dimensional hypercube, which is rasterized according to the number of desired dimensions and a fixed cell-size along each of the considered axes. This leads to a raster with \( N_c = S^d \) cells, where \( S \) is the cell size and \( d \) is the number of considered dimensions. The exponential growth in the number of raster cells with increasing the number of dimensions (cf. Curse of Dimensionality (Bellman, 1957)) justifies the decision to keep only the leading principal components.

Secondly, data points lying in each cell are counted with the purpose of identifying cells of high-density levels as compared to others in their d-dimensional neighbourhood (equivalent to a 3D 8-neighborhood). In Figure 1, a two-dimensional data set containing two natural clusters and one outlier point is presented with the purpose of illustrating the process of density-maxima discovery and the way in which the K-means centroid number/placement decision is taken.

Note that we only store non-empty cells during the processing to avoid exploding memory space.

![Figure 1: Example computation of local density maxima in an 8-neighbourhood comparison area, performed on a small two-dimensional dataset. The cell raster has been created by using 2 considered dimensions and cell size = 1/10. a) A color-coding of cells based on the number of points they contain. b) Density-maximum (centroid-placement) cells emphasized by keeping their original color. All non-maximum cells have been colored in gray.](image)

### 3.3 Aggregation

If thousands of points from a data set are projected to the screen individually, perceptual overload might ensue. In order to reduce visual clutter in the final visual representation, points with similar characteristics are grouped and displayed as a single appropriate-characteristics entity.

To form observation groups, a small number of pre-informed-centroid K-means clustering iterations are executed. This summarization procedure aims to capture small regions of stable or radially-decreasing concentration, reducing the discretization effects induced by the rasterization. Due to the local rise in density they constitute, outlier points are assigned to their own centroids and are later on separately projected. In this manner, outliers are prevented from distorting the representations of more compact structures, yet an in-depth exception analysis is facilitated.

At the level of granularity defined in Figure 1, the 2D dataset is summarized on the screen as follows: one glyph for the single-point group containing the outlier, two glyphs for two multipoint...
groups of close relatedness, arisen by the left cluster, and three more glyphs for the multipoint groups comprising the core, the upper tail, and the lower tail of the right cluster, respectively. Each of the pre-informed prototypes typically result in a group unless no points have remained in its closest proximity due to the iteration. The segmentation level in cluster representations depends on the raster-cell size / the number of considered dimensions and is customizable by the user.

3.4 Intra-group Properties

In order to encode characteristic information about each of the delineated groups into the visual properties of its representation glyph the following two measures are computed: group spread and group relative density.

The multidimensional area equivalent of each group (the group’s spread) is estimated by an intragroup measure $\beta_i$, similar to a statistical variance. First, the divergence $\delta_i$ is the divergence of point $j$ in group $i$ is computed by:

$$\delta_{ij} = \sqrt{\sum_{k=1}^{d}(e_{ijk} - \mu_{ijk})^2}$$

where $e_{ijk}$ is the $k$th entry of point $j$ in group $i$, $\mu_{ijk}$ is the analogous entry in the representation of the group’s centroid, and $d$ is the number of considered dimensions. The measure $\beta$ of a group is then defined by

$$\beta_i = \frac{\sum_{j=1}^{n_i} \delta_{ij}^2}{n_i}$$

where $n_i$ is the number of points assigned to group $i$.

For display and comparative purposes, the area of each group is converted to a percentage of total groups area and is proportional to the size of the group’s representation glyph to be output to the screen. Thus, the total area $A_i$ of the representation glyph of group $i$ is given by:

$$A_i = \omega \frac{\beta_i}{\sum_{j=1}^{n} \beta_j}$$

where $n$ is the total number of groups computed by the K-means-like summarization procedure and $\omega$ is a scaling factor which can differ depending on the size of the screen.

The second important property encoded in a group’s glyph representation is group density, as compared to the densities of other dataset structures presented on the screen. A straightforward computation of group density by the formula $D_i = n_i / A_i$, where $D_i$ is the density of group $i$, is bound to result in division-by-zero errors, due to the fact that the standard deviation of 1-point groups is equal to 0, i.e., the point’s position in space coincides with that of the centroid. To avoid this caveat and any arbitrary threshold numerically delimiting zero and non-zero values, the relative density of group $i$ is computed by

$$\Delta_i = 1 - \frac{D_i^{-1}}{\max_{j=1}^{n} D_j^{-1}}$$

3.5 Inter-group Distances

Since the large number of small groups output by the summarization procedure at higher levels of granularity can be perceived as broad-structures oversegmentation, it is important to keep track of which glyphs encode detail in a more complicated formation and which should indeed be considered as separate. To achieve this, the distance between each pair of groups is computed and the option to display links between logically-connected groups is provided to the user. Moreover, encoding these distances provides information that is important, if the data are projected to a 2D layout that cannot fully preserve distances.

We compute the distance between the closest two points belonging to different groups as a measure of the groups’ logical connectedness (similar to the procedure in single linkage clustering). Since we have to compute pairwise distances of $n$ groups and need to consider in each pairwise test all samples of both groups, which can each be $O(N)$ samples, if $N$ is the number of all samples, the time complexity is $O(n^2N^2)$, which is rather expensive for large $N$. We approximate the result by finding for a group the point with minimal distance to the centroid of the other group and vice versa. Since centroid computations are expensive in a high-dimensional space, we operate in the dimensionality-reduce space (cf. Section 3.1). The final distance is computed in the original data space though. Time complexity drops to $O(n^2N)$.

3.6 Visual Encoding

For generating the layout of our visual encoding, the locations of group centroids in the reduced data space are projected to a 2D visual space, where the circular glyphs are placed.
Group spread as a percentage of total groups spread is encoded via the size of the circular glyphs, where the total screen area covered by glyphs sums up to scaling factor $\omega$ introduced in Section 3.4.

To encode relative group density a glyph color along the linear-interpolation gradient (Figure 2a) between the two RGB colors (210, 230, 250) and (75, 0, 110) is selected. The choice of the two colors is considered appropriate due to the fact that differences in all three HSV components of the colors are present ($dH = 71$, $dS = 84$, $dV = 55$), yet the location of an intermediate color on the resultant gradient can be easily estimated. Additionally, tritan-related anomalies in the general population have the lowest documented incidences of all color-related vision disorders (Rigden, 1999), giving color-shades in the blue-violet end of the spectrum the highest chance of being recognized by the average human individual.

As possessing a maximum comparative density of 100%, single-point groups, likely containing an outlier, are encoded with a distinct blue color (Figure 2b), combined with a hollow-circle appearance of their representation glyphs. In contrast, multi-point groups exhibiting the same density (i.e., all points lie exactly at the group’s centroid), are encoded as normally – by a small-size filled-circle glyph drawn with the darkest color of the density-encoding gradient.

There are two less aggregated views for each group available when hovering over or clicking at a glyph, respectively. When hovering over a glyph, a planar plot of the points belonging to its corresponding group according to the current projection is rendered. The number of assigned points, the group’s area, and relative density are output in textual form in the lower left corner of the screen. If the glyph is clicked, a circular parallel coordinates plot of all points belonging to the cluster is rendered.

To reduce overplotting in groups with large number of members, the color of each line is chosen according to the point’s entry value along the original dataset axis with maximum variance. The examination of the circular-parallel-coordinates signature of each group can provide qualitative information on the group’s homogeneity, the intragroup ranges along axes, and the presence of outstanding points, which at a higher level of granularity may have been captured as outliers.

The option of visualizing intergroup connectedness is provided via the concept of neighborhood links, which improves the coherent interpretation of larger structures presented as multiple glyphs and will convey truthful information on group-pairs’ proximity, regardless of chosen projection. When hovering over a glyph, connections in the form of colored straight lines to the centers of other groups’ glyphs are depicted. The neighborhood criterion according to which the links are drawn is of a k-closest nature, where k is between 0 and 10 and is modifiable via a slider in the visualization tool’s interface. Furthermore, the visibility of a user-defined maximum number of links, in the same interval, can be permanently enabled, while the links are additionally interactively filtered by the strength of the relation they represent.

For color-computation purposes the strength of each connection is expressed in relative terms. Naturally, links of close-to-0 lengths encode the strongest relations among groups in the dataset and are drawn in the darkest possible intergroup-connectedness-encoding color. Conversely, neighboring groups possessing closest points further apart are paired by a less visually salient connection, using again the color map in Figure 2a.

Figure 3: Visual encodings: (a) LargeSpread low-density group. (b) Group scatterplot appearing when the group’s glyph is hovered over. (c) Hint reporting number of points (426), area (10.161), and relative density (87.97) of hovered-over group. (d) Smaller-spread, high-density group. (e) Circular parallel coordinates plot of the group in (d). (f) Outlier. (g,h) High-relation-strength intergroup links, produced by a 2-closest criterion applied on the group in (b).
Figure 3 provides an example image showcasing the visual encodings. To produce this image, the visualization tool was run on a synthetically-generated six-dimensional dataset containing three easily-distinguishable clusters, polluted with approximately 1% of noise objects each, and one outlier point marked with blue in f). The clusters, each of which has been captured as a single group at the current low level of granularity, have different equivalents of multidimensional area, as encoded in their glyphs’ colors. The cluster in b) is currently the densest multipoint object presented on screen, having a relative density value of 87.97 (the outlier has 100.0) and a color towards the right end of the density-encoding gradient, which would have been visible if the glyph had not been hovered over. The circular-parallel-coordinates plot of the points assigned to the group in e) reveals a homogeneous cluster nature. Similar ranges along all axes are observed, alluding to the almost hyper-spherical shape of the cluster. The signatures of three foreign (noise) points can be seen as one line crossing through Axis 3 (green) and two lines crossing through Axis 4 (pink) closer to the center of the plot compared to the majority of intersections.

3.7 Interaction Mechanisms

When the visualization tool is initially launched on a dataset, the default observation perspective provided to the user is based on the data points’ transformation by the PCA eigenvector matrix. The first two principal components of data are used to arrange observation points, i.e., they define the projection matrix to the 2D visual space.

In case relevant features of the examined structures are not immediately visible in the default projection plane, an opportunity to dynamically apply transformations to data points and centroids alike is enabled via the manipulation of the star-coordinates widget included in the visualization tool’s interface. The columns of the projection matrix represent the tips of the dimension axes in the star-coordinates plot. One operates on the star-coordinate widget by translating the tips of the coordinate axes. When changing the tip’s position of the ith dimension, the projection matrix is updated by replacing the ith column with the new coordinates of the tip. The same projection matrix is used for both the global layout and the layout of group as in Figure 3(b). In the global layout the glyphs are placed at the centroid of the projected group rather than the projection of the group’s centroid. Figure 4 shows the interaction widget.

Statistically, rescaling one of the original data axes results in an increase/decrease of relative variance as considered by PCA. This can be used to redefine attribute relevance or reduce the undesirable effects of inappropriate unit selection or PCA’s outliers sensitivity. In order to regroup points, based on his/her personal understanding of property importance, an axis-rescale widget is provided to the user. The widget is similar in appearance to the projection-modification star-coordinates widget. However, variations in the length of a ray resulting from changing its tip’s on-screen position leads to proportionate rescales along the corresponding original data axis. Manipulation of the angles at which widget rays are presented has no effect on axis-scaling but is supported such that rays can be closely placed to each other and the relationships among scaling factors visually assessed. When the scaling of an original data axis is altered, the PCA, summarization, and display procedures are re-executed and the axis’ representation in groups’ circular parallel-coordinates plots is adjusted accordingly.

Figure 4: Star coordinate interaction widget for a 7-dimensional data set (here showing PCA outcome).

Other interaction mechanisms are concerned with changing the granularity of the clustering mainly by adjusting the cell size of the density-based clustering. To maintain the mental map and observe changes of assigned samples to clusters, we provide an animated transition that first splits the groups into fractions, which then move and reassemble themselves to the new clusters. Figure 5 shows an example.

Figure 5: Animation for tracking cluster changes when modifying level of granularity: original clusters (a) are split to fractions (b), which translate (c), and re-assemble (d) to form the modified clustering result (e).
4 RESULTS AND DISCUSSION

To have a known ground truth, we first apply our data to a synthetic data set. The Fake Clover data set (Ilies, 2010) contains 1,211 samples in 7 dimensions that has been labeled to 6 similarly sized clusters plus 7 outliers. Figure 6 shows the outcome of the PCA algorithm without our visual encodings. We observe that the clusters overlap pairwise such that 3 instead of 6 clusters are observed when not color-coding the labeled classes.

Figure 6: PCA of Fake Clover dataset leads to non-separated cluster pairs (a,b), (c,d), and (e,f).

Figure 7 shows our visual encoding of the PCA view with data aggregation using two iterations of the K-means-like procedure and density-estimation cell size 1/49. We show the 2-nearest neighborhoods with edges. The 7 outliers stay as separate clusters and the other samples merge to three groups of somewhat close clusters.

Figure 7: Aggregated visual encoding of PCA view on Fake Clover data set with 2-nearest neighborhoods.

In Figure 8, we use the circular parallel coordinate plots to examine an outlier and its 2-nearest neighbors. It can be observed that the outlier is close to one of the clusters (the lower one) in all dimensions except for one (the 6th dimension when counting clockwise from top).

Figure 8: Circular parallel coordinate plots to examine the properties of an outlier in comparison to the 2 nearest clusters.

Figure 9 documents how the edges can help to understand whether the projection is maintaining well distances. It shows the 6-nearest neighbors of a selected cluster. While the projection on the left maintained neighborhoods well, the projection on the right did not maintain it well, which becomes obvious with our visual encoding.

Our tool also allows for top-down and bottom-up analyses. In Figure 10, we follow the top-down strategy by starting with a highly aggregated view (left) that identifies three clusters in the PCA view, which correspond to the cluster pairs (a,b), (c,d), and (e,f) in Figure 6. When refining the aggregation level by changing the cell size from 1/15 to 1/25, we observe that the clusters split into two subclusters. When changing the projection with the star coordinate interaction widget, we obtain views that the subclusters are indeed separate structures. The projection in Figure 11 (left) shows that the upper left cluster in the PCA view actually consists of two clusters (corresponding to clusters a and b in Figure 6). The projection in Figure 11 (right) shows that the bottom cluster in the PCA view also consists of two clusters (corresponding to clusters e and f in Figure 6).
Figure 10: Top-down strategy starting with a highly aggregated view using cell size 1/15 (left) and refining the clusters using cell size 1/25 (right).

Figure 11: Changing the projection with the star coordinate widget allows us to separate clusters a and b from Figure 6 (left) as well as clusters e and f (right).

In a bottom-up analysis, we would start with each data sample being its own cluster and aggregate. In Figure 12, we show a projection where the neighbourhood structures at a barely aggregated level exhibit that the clusters c and d from Figure 6 are also separated structures. We reduce overplotting here by just showing the edges without the clusters.

Figure 12: Bottom-up strategy starting with each sample forming its own cluster and merging them. Here the clusters c and d from Figure 6 could be separated.

Figure 13: When applied to the Iris dataset we identified the three well-known clusters.

Figure 14: When applied to the Out5D dataset, we observe many distinct subclusters.

Figure 15: Example of a clustering result with a heterogeneous cluster and a more homogeneous cluster, which can be verified by switching to scatterplot visualizations of the clusters.

The main parameter to be chosen is the cell size. The perfect value cannot be known a priori and should be adjusted interactively. In fact in case of different cluster densities and sizes, it may have to be chosen differently when analyzing different regions of the data. However, our visual encoding supports the analysis, as homogeneous clusters typically do not need further refinement, while heterogeneous might do. In Figure 15 (left), we observe two clusters, but the left one is heterogeneous and may consist of further subclusters, which here can be easily confirmed by switching to the scatterplot views for selected

All the results presented so far were on the synthetic Fake Clover dataset. We also applied out methods to non-synthetic data like the well-known Iris (Bache and Lichman, 2013) and Out5D datasets [23]. Figure 13 shows the result on the Iris dataset revealing the known three clusters. Figure 14 shows the results on the Out5D data set with various distinct subclusters.
clusters (middle), while the cluster on the right is more homogeneous (right). Another issue with the cell size parameter is that clusters are not necessarily changing smoothly when smoothly varying the cell size parameter. To alleviate this issue we introduced an animation as in Figure 5.

5 EVALUATION

To evaluate the effectiveness of our tool, we performed a user study with 10 subjects with different professional background, gender, and age. We gave a short tutorial and subsequently asked 8 easy questions that should familiarize the subjects with the functionality of the tool. We asked about the number of dimensions, number of samples, the dimension with the broadest range, the dimension contributing most to the variance, the number of outliers in one dimension, the number of visible structures in the PCA view, a comparison between clusters in terms of size, are, and density, and correctness of an aggregated view. Afterwards, we asked them to perform actual analysis tasks like identifying the correct number of clusters, testing clusters on homogeneity, and finding the most similar observations to an outlier. All tasks were conducted on the Fake Clover dataset. The outcome was evaluated by computing the correctness of the answers. Time was not part of the investigation, but the study took on average 66 minutes (ranging between 29 and 98 minutes) per participant.

The outcome of the user study was that subjects were able to fulfill the tasks with a high average correctness rate of 90.0% (92.5% for easy questions and 83.3% for actual analysis tasks). There was no difference in performance between groups of different professional background.

6 CONCLUSIONS

We presented an interactive visual tool for effectively analysing unlabeled multi-dimensional data using data aggregation and distance encoding. Data aggregation is based on K-means clustering and a cell-based density clustering. The cell size allowed us to modify the granularity of the data aggregation. Cluster properties are visually encoded in aggregated form using color and size or in detailed form using circular parallel plots and scatterplots in a local layout. Distances are computed in an efficient way and conveyed by ending k-nearest neighborhoods with edges, which allows for analysing the neighbourhood preservation property of the chosen projection. Projections are based on PCA, but a dimension-scaling parameter allows for interactive weighting of axes and a star-coordinate widget allows for changing the projection. We have shown that our tool can be effectively applied to analyze multi-dimensional data.

REFERENCES


