Verifiable Parameterised Behaviour Models
For Robotic and Embedded Systems

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Abstract: Logic-labeled Finite-State Machines (LLFSMs) are Communicating Extended Finite State Machines that execute concurrently but with a predefined sequential schedule. This capacity has enabled effective formal verification. Moreover, LLFSMs are very powerful tools for Model-Driven Software Engineering of the behaviour of robotic and embedded systems. Although existing schedulers are capable of executing several instances of the same model, the challenge is to provide mechanisms for creating parameterised models akin to function calls. Since recent task planning algorithms can synthesise behaviours as LLFSMs with parameters and recursion, it becomes necessary to have a useful operational tool that produces compiled executables for such behaviours. Moreover, parameterisation allows replication of generic system components, reducing overall design complexity. We produce safe mechanisms to set actual and formal parameters for multiple, concurrent instances of the same behaviour. We achieve the parameterisation of behaviour models analogous to a procedural abstraction and discuss its advantages and disadvantages on formal verification.

1 INTRODUCTION

The prominent role of Model-driven software engineering (MDSE) for robotics derives from industry profiting from the promise of combining soft and physical robots with emerging technologies and platforms, e.g., for the Internet of Things (IoT), the Internet of Services (IoS), and the Internet of Data (IoD); and is propelled further by the promises of ubiquity and scalability of Cloud Computing. The challenge, thus, is to apply the power of abstract behaviour models in a systematic, reliable, and scalable form. Moreover, this kind of scalability has prompted modular robots (Arney et al., 2010), that is, a robot that can be composed of several physical parts. In such a system, the number of copies or parts of the same kind can be flexibly adjusted, not only prior to deployment, but even during operation. Therefore, it is natural to consider that the specified behaviour of modular components should also be modular and would utilise MDSE (Arney et al., 2010).

Logic-labeled finite-state machines (LLFSMs) are a comprehensive mechanisms for modelling behaviour in robotics and embedded systems. LLFSMs can be considered to be inspired by the Timed Finite-State Machines (t-fsms) that work as building blocks of Brooks’ subsumption architecture (Brooks, 1986) as they can very well represent the LISP-based textual language in which t-fsms were described (Mataric, 1992; Brooks, 1990). A similar type of robotic behaviour description has been presented for Teleo-reactive systems (Nilsson, 2001) and Situated Automata (Rosenschein and Kaelbling, 1995). LLFSM concurrent execution offers deterministic scheduling and allows the design of time-triggered systems (Kopetz, 1993). Such deterministicism has several advantages. In particular, the behaviour of a system composed of LLFSMs is much more predictable, ensuring reliability. In fact, the predictive schedule reduces the state explosion of uncontrolled concurrency enabling formal verification and model checking. It also enhances the confidence in any validation performed. Therefore, LLFSMs can naturally be incorporated into a test-driven-development framework, making test failures significantly more reproducible. Moreover, this sequential execution liberates the designer of challenges related to concurrency, such as race conditions, as at any given point in time, only one LLFSM in the arrangement is executing, making the execution of its ringlet atomic. The alternative to LLFSMs are event-driven statecharts derived from Harel’s State Charts (Harel and Naamad, 1996; Harel and Politi, 1998). This were incorporated into OMT and later into UML. In these even-driven
finite-state models transitions are labeled by events. We note that an event-driven system is typically based on a software architecture built around stimuli-driven call-backs or interrupts, a subscribe mechanism and listeners that enact such call-backs. Reacting to stimuli in this way implies uncontrolled concurrency (e.g. using separate threads or event queues). Lamport (Lamport, 1984) provided fundamental proofs of the limitations of event-driven systems. Reactive-systems are responsive systems without much processing, as opposed to deliberative systems (which reason, plan, learn). Real-time systems are required to meet time-deadlines in response to stimuli and time-triggered systems have been shown very effective for this (Kopetz, 1993). Therefore, although closely related, these terms are not the same, our preference for LLFSMs is supported by the work of Lamport (Lamport, 1984) that provides solid reasons why real-time systems may be better served by time-triggered systems and pre-determined schedules, rather than the unbounded delays that may occur in event-driven systems.

The $\text{clfsm}$ scheduler executes an arrangement of compiled LLFSMs, with the capacity to upload and suspend LLFSM that represent behaviours during runtime (Estivill-Castro and Hexel, 2016). The $\text{clfsm}$ scheduler offers very efficient, in-memory, data-centric communication between different behaviour modules. This works very well if the number of listeners for a message are known well before compile-time, but does not work so well if the role of consumer and producers is to be decided at run-time.

Task planning technology has advanced significantly. Now, generic plans that solve generic task planning problems can be synthesised as logic-labeled finite-state machines with parameters and recursion (Segovia-Aguas et al., 2016). This poses the challenge of executing these behaviours as compiled routines on board a robot, even where several instances are deployed recursively. Parameterisation brings the challenge that the middleware cannot statically determine senders and receivers. Moreover, the number of LLFSMs in an arrangement can dynamically vary, e.g., through recursive invocation. The missing link to improve communication, is that invocation of a behaviour (modelled by a LLFSMs) should be similar to a procedure or function call.

This paper provides such a model, demonstrated first with the original that $\text{clfsm}$ provides and then proposing the semantics that parameterised LLFSM invocations should have.

## 2 INSTANTIATING SUSPENDED MACHINES

An arrangement of parameterised LLFSMs can be defined dynamically. LLFSMs can be loaded and unloaded by request from another machine. This mechanism is similar to the suspend/restart mechanism. However, in the case of unload, the machine is removed from the arrangement, while the load mechanism adds the named LLFSM to the arrangement. We introduce a variant we name load suspended. The semantics of this new command is similar to the previous load command with the exception that rather than loading a LLFSM that executes from the initial state, with load suspended the child machine is set with its suspended state as the current state.

Because a LLFSM can be loaded more than once, LLFSM instances can be logically replicated in an arrangement to execute concurrently, but, as we mentioned earlier, this facility was limited to communication patterns where the total number of LLFSM was predictable at compilation time to create control/status communication messages.

We introduce the concept of setting parameters for a loaded LLFSMs from a caller LLFSM. With this facility, we can now treat LLFSMs as a function call or procedure invocation, precisely suitable to enact the Hierarchical Finite State Controllers inferable with task planning (Segovia-Aguas et al., 2016).

To demonstrate this facility and illustrate its semantics, we present an example where we recursively compute the factorial (Fig. 1). The initial state of this recursive LLFSM has two transitions. If the value of its parameter (the variable value) is zero, the returned value will be set to 1 (state END), and no further recursion will occur (the machine will pause in its RETURN state until its caller collects the return value and such caller unloads the machine).

More interestingly, when the value of the input parameter is greater than zero, the LLFSM will use the loadSuspended command to load a new instance of itself (in the $\text{OnEntry}$ section of the LOAD_MYSELF_SUSPENDED state). The $\text{SET INPUTS}$ state obtains a reference to the recently loaded and, importantly, suspended machine and sets the parameter to one less than the current value ($\text{OnEntry}$ section). The caller then requests that the child resumes ($\text{Internal}$ section) and once the child is running (is_running() predicate of the transition), it will transition to the state $\text{MONITOR\_STATE}$.

The state $\text{MONITOR\_STATE}$ retrieves the current state of the child machine, exiting if the child is in the RETURN state. Once that happens, the caller retrieves the returned value from the local variable of
the child LLFSM (accessible through the LLFSM reference `next_machine`). In the case of the factorial function, the value this instance returns is the product of `value` with the `returned_value` of the callees LLFSM. The subsequent state is the state `UNLOAD` where the child LLFSMs is removed from the arrangement. Once this succeeds, this invocation itself parks in its `RETURN` state.

The top-level LLFSM that makes the invocation is presented in Fig. 2 and its simpler but illustrates the particular steps of calling another LLFSM as a procedure or recursive function using the new `loadSuspended`. While the child is suspended, the formal parameters are filled with values. This was not possible previously, as the child machine would run concurrently after `load` with uninitialised parameters.

Correctness of the recursive factorial function can be established by induction (Wand, 1980). Establishing formally that the LLFSM model (Fig. 1) is a correct executable model can be achieved with techniques to verify recursive programs (Huang et al., 2009). Our tool does not currently implement control-flow graphs but produces the corresponding Kripke structure for the LLFSM except the `loadSuspended` instruction. Nevertheless, for this example, formal verification can proceed as we can establish LTL and CTL properties for the LLFSM in Fig. 1.

**Property 1** If the input `value` is zero, then all paths lead to the `RETURN` state and the variable `returned_value` is 1 for all future states.

We can establish that, in this case (`value=0`), all paths only use `END` once and followed by the state `RETURN`, and they do not use any other state. For a small illustration, Fig 3 shows the LTL formula we used in NuSMV to verify that in no more than 3 Kripke states, the LLFSM of Fig. 1 reaches the state `END` from the initial state. Similarly, with our current compiler that generates Kripke structures, we can use NuSMV to establish that if the input `value` is greater than zero, then the states executed are those on the path and in the path’s sequence shown by the model.

However, the new `loadSuspended` offers a non-blocking execution, much more general than the vanilla invocation of a sub-routine with the semantics for recursion of an invocation stack. In traditional, imperative languages, the invocation of a subroutine blocks the calling code at the point of invocation until the subroutine terminates and returns. We demonstrate the additional versatility of a non-blocking call in the following examples.

![Figure 1: Recursive LLFSM for computing the factorial function $f(n) = n!$.](image1)

![Figure 2: The LLFSMs that invokes the recursive LLFSM from Fig. 1.](image2)

![Figure 3: NuSMV coding of the property that, when `value=0`, the next state after Initial is state `END`.](image3)
2.1 Hexapod Walk

We alluded earlier to the capacity to achieve scalability using MDSE on modular robots. The gaits’ rhythmic motion for an hexapod is a good example of the generality of the behaviour model for legs. Although our illustrations are for 6 legs, but they are applicable to an arbitrary number of n legs placed around the center of mass of the robot. In particular, when all the legs are placed equidistant from the center of the robot as if they were on a regular n-gon, it is easy to imagine the gait that spins the robot clockwise. First, the even numbered legs raise. In the second stage, odd legs use their body joint to push the robot clockwise as they actually do a counter-clockwise turn of the body joint. Simultaneously, the even legs are raised and turn clockwise, advancing in the direction of the spin. The third phase lowers the even legs while raising the odd legs and roles are reversed between these groups of legs. In the fourth phase, it is now the legs on the ground (the even legs) that push the robot clockwise, while the odd ones (the odd ones) rotate clockwise. An equivalent gait for counter-clockwise rotation would simply reverse the direction of joint rotations.

How does the robot walk in a particular orientation? Once more, the fundamental movement uses the same four-stage leg movement. But, as opposed to spinning, legs are now partitioned into two sides. Those on the left will be performing motions to spin clockwise, while those on the right of the center line of motion will spin counter-clockwise. The robot will walk because odd legs and even legs will have a phase shift of two stages. So the robot will ‘row’ in the direction of motion with even legs pushing back on the ground, while the odd legs are raised and move forward, again, with the odd group of legs replaced by the even in their role of pushing or advancing.

There are many more possible gaits. The point we are illustrating is that linear and rotational leg movements can be modelled as the fundamental parameterised motion. Fig. 4 shows the fundamental four states of a leg, RAISE_LEG, LEVEL_LEG, SPIN_AGAINST_DIRECTION_OF_MOVEMENT, as well as PUSH_OPPOSITE_DIRECTION. However, deciding what is a push motion when the leg is down or what is rotating back the leg when the leg is up depends on three factors: (1) whether the hexapod is walking or spinning, (2) whether this particular leg is to the left or right of the direction of movement; and (3) if we are spinning, then whether the motion is a clockwise or counter-clockwise spin. Finally, the phase of a leg motion depends on whether it is an odd numbered leg or an even numbered leg. Fig. 4 shows the parameterised executable LLFSM for the motion of a leg. The motion starts raising a leg or levelling a leg according to the group of the leg (even or odd). From there on, all legs loop through the same four states, and adjust the move
Figure 6: Section of the LLFSM that numbers the legs and sets the parameters based on the new action (and new direction) the driver of the hexapod wants to take. All LLFSMs are then invoked concurrently (non-blocking).

when the leg is down or up according to the described calculation. A video of a hexapod driven around an area with spinning and walking can be seen at https://youtu.be/60FgjRvZqsc. The parameterised LLFSM in Fig. 4 are launched as concurrent, non-blocking calls with the corresponding parameters. That is, the behaviour that conforms to the gait in the case of the Hexapod invokes six instances of Fig. 4 with the appropriate parameters.

2.2 Formal Verification of the Executable Model

Formal verification of the behaviour for all legs in Fig. 4 (which is an executable model) can be performed with standard tools. Recall that the LLFSM compiler derives the Kripke structure from the executable model (Estivill-Castro and Hixel, 2013) as input to NuSMV. We can readily verify that each state is necessarily followed by the corresponding state shown in Fig. 4 and no other state before that. For example, for the state LEVEL_LEG, Fig. 5(a) shows the LTL expression for the following property.

Property 2 It is globally true that, after the OnEntry of state LEVEL_LEG, in the next 3 Kripke states the OnEntry of the state PUSH_OPPOSITE_DIRECTION is executed.

Also, we need to show that no other part of any other state is executed. A particular case is the following property.

Property 3 It is globally true that, after the OnEntry of state LEVEL_LEG happens, none of the next 3 Kripke states are the OnEntry of the state RAISE_LEG.

Fig. 5(b) shows the NuSMV for Property 3. To completely verify the model, we would need an analogue to Property 2, and all the analogous LTL expressions to Property 3. However, the point is that, with our tools, we can formally verify that, after initialisation, the states of the executable LLFSM in Fig. 4 belong to the regular language (LEVEL_LEG PUSH_OPPOSITE_DIRECTION RAISE_LEG SPIN_AGAINST_DIRECTION_OF_MOVEMENT)⁺.

2.3 Run-time Verification of the Executable Model

As the purpose of this example was to show the flexible non-blocking invocation of parameterised LLFSMs, we only show the most relevant states of the controller LLFSMs that enable driving around of the hexapod as illustrated in the video mentioned earlier. Setting of parameters is shown in NUMBER_LEGS and RESTART_LEG_MACHINES, where the former state assigns a number to each invoked LLFSM (Fig. 6) and the latter actually performs the non-blocking invocation.

However, since each LLFSM for the legs is launched separately, there is a need to ensure synchronisation. That is, the driver LLFSM needs to check that all launched LLFSMs are running and then synchronise them, before reading a new action (and new direction) from the driver. For example, all even legs (and similarly, all odd legs) must be in the same state. This verification is rather different from the verification performed with NuSMV earlier. In theory, one could write the corresponding temporal logic formula, but this would be particularly laborious. Therefore, we illustrate the virtue by presenting an LLFSM that verifies this aspect at run-time. The new monitoring LLFSM will watch the state changes of the six instances of LLFSMs for the hexapod. Recall that all these are instances of the LLFSM of Fig 4, with common parameters for the action (walking vs spinning), but with a different leg number. The monitoring LLFSM (different from the controlling LLFSM)
Figure 7: A monitoring LLFSM that inspects the states of the instances in Fig. 4 and checks the leg groups.

is shown in Fig. 7. The important aspect to notice is that the transition from MACHINE_STATE_CHANGES happens if any of the six LLFSMs has a state change (the transition is whether the first, second, or third odd-labelled leg LLFSM has a state change or the first, second, or third even-labelled LLFSM has a state change). In case not all machines involved had a state change, the transition to the ERROR state fires. This is also the virtue of LLFSMs' deterministic schedule, as all LLFSMs in the arrangement are guaranteed to receive the execution token before the monitoring LLFSM in Fig. 7 executes again. All LLFSMs are executing concurrently, and despite non-blocking calls that re-launched the leg controllers, synchronisation is achieved without requiring explicit coordination (as required with open concurrency, e.g., through semaphores, monitors, or other explicit synchronisation mechanisms that often render formal verification impossible (Estivill-Castro and Hexel, 2013)). The monitoring LLFSM in Fig. 7 is not necessary to control the hexapod. We use it for validation and incorporate it as part of a suitable software architecture (Estivill-Castro and Hexel, 2016).

3 FUNCTIONAL DECOMPOSITION

Functional decomposition is a major technique in software design (Aggarwal and Simgh, 2008). Algorithmic decomposition is a necessary part of object-oriented analysis and design (Booch, 1994). Functional decomposition is naturally used for algorithmic-based system, where a problem is decomposed, broken into subproblems, whose solution is then integrated into a final solution. This approach to problem-solving and algorithm creation is exemplified by divide and conquer (Cormen et al., 2009). Any algorithm is fundamentally built from sequencing, selection, and iteration of earlier defined algorithms (recall Structured Diagrams from Jackson's Structured Programming). The process of building abstractions as subroutines is regularly practiced to build even more sophisticated functions. We now illustrate that our proposed parameterised behaviours act as building blocks of more sophisticated behaviour.

The example we chose is from the RoboCup Standard Platform League (http://spl.robocup.org), in particular, the entire soccer player behaviour, following a top-down design. The behaviour must, at the top level, maintain a few states, named Initial, Set, Ready, Play, and Penalised. Suffice it to say that the top behaviour therefore implements these states as an LLFSM with corresponding transitions reacting to the stimuli (e.g., UDP messages, a whistle, or even buttons on the robot being pushed). Here, we focus on the state of Ready, where a robot must reach a legal position (usually its own half of the field) before game resumes (after a goal has been scored or the first commencement of a period of play – see https://youtu.be/6bzyf5fhTAQ). Thus, the state of Ready is again broken down into sub-behaviours, namely, to find a landmark (a goal), and identifying whether that landmark is in the opponent’s or the player’s half. Finding a goal (if not visible) corresponds to scanning using the head, and if that is not enough, to spin the whole robot around a bit (on the spot). However, if the goal is visible, we need two sub-behaviours, one to track the visible object with the head, and one to align the body to the object.

Behaviour models are naturally designed using
Figure 8: Behaviour searching for an object. A Boolean (formal) parameter controls whether to only spin on the spot or to interleave a short walk. That parameter is passed along to a sub-behaviour to walk and/or spin.

Figure 8 demonstrates a parameterised model. The behaviour to search for a landmark uses 3 sub-machines, one to halt the walk, one to scan using the head, and one to walk about, trying to identify an object. The latter can be invoked using a parameter. When finding landmarks for the super-behaviour for *Ready*, it is only suitable to spin on the spot (the designated starting position for the robot). However, when finding the ball during *Play*, it is important to alternate with walking backwards or forwards to avoid missing the ball in a “dead spot”. Thus, Figure 8’s behaviour invokes its sub-behaviour, with a Boolean parameter to only spin or not.

This illustrates that parameterisation enables refactoring of behaviours, enabling their re-use for initially distinct sub-tasks in the hierarchy of decomposition. That is the *Seek* behaviour becomes a reusable structure. Refactoring improves the quality of the implementation (Fowler, 1999), ensuring that the generality of the code is extracted, and thus regularly used in all cases, leading to fewer potential faults (e.g., through cut-and-paste). Moreover, a generic behaviour needs to be formally verified only once.

The other aspect we illustrate with this example is the flexibility of behaviour invocation as a non-blocking call. Figure 9 shows the caller for Figure 8 that requests to focus on a goal. In fact, the *Seek* behaviour generic, taking a parameter as to what it is seeking for (a post, a ball, a goal, etc.). This behaviour uses several sub-behaviours in addition to *Seek*. When the landmark is visible, two sub-behaviours form what are essentially feedback-loop controllers. The first is a behaviour tracks the object with the neck of the robot, keeping the target object centred as much as possible in the camera’s field of view. The second sub-behaviour is a walk or spin, that keeps the torso of the robot aligned with the object (at the equilibrium point, the neck is centred looking straight and the torso is also facing the target object). The non-blocking nature of the invocation is exploited by the LLFSM in Figure 9 to abort the *Seek* behaviour as soon as the landmark (or ball) becomes visible. Similarly, if the landmark becomes invisible, the sub-behaviours to track and follow the landmark are aborted accordingly.

The SPL example illustrates the power of parameterised executable behaviours as LLFSMs. Sophisticated, complex behaviours can be build bottom-up, decoupled from an initial top-down design, thus allowing re-factoring. While LLFSMs have a whiteboard middleware as their default communication mechanism, it is overkill to create communication channels for every caller-callee pair, as that would result in many communication classes (or whiteboard identifiers), specially if the same message is being posted between several sender-receiver LLFSMs or multiple instances of the same LLFSM. The whiteboard is more suitable for a broadcast or knowledge repository between individual components.

4 CONCLUSION

We showed the use of the loadSuspended capability to create LLFSMs that can be invoked with parameters and enabling the construction of LLFSMs’s recursive functions. As such, we believe we have the only compiler for plans produced from new, generic task planners. Moreover, we can generate mechanisms for formal verification for all aspects of the LLFSM semantics, including the loadSuspended function. Also, our LLFSMs can themselves be used to build monitoring LLFSMs for runtime verification. This enables the generation of high level, executable
behaviour models for robotic and embedded systems that are modular and encapsulate design complexity.

REFERENCES


