Towards Rhythmicity Analysis of Text using Empirical Mode Decomposition

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Abstract: The rhythmicity characteristics of the written text is still an under-researched topic as opposed to the similar research in the speech analysis domain. The paper presents a method for text deconstruction into text modes using Empirical Mode Decomposition (EMD). First, the text is encoded into a numerical sequence using a mapping table. Next, the resulting numerical sequence is decomposed into Intrinsic Mode Functions (IMFs) using EMD. The resulting text modes provide a basis for further analysis of a text as well as specific characteristics of the language of the text itself. The text modes are used further to derive the measures of text complexity (cardinality) and rhythmicity (frequency) as well as the visual representations (scalograms, convograms), which can provide important insights into the structure of the text itself. The application of EMD to text analysis allows to decompose text into basic harmonics, which can be attributed to the structural units of the text such as syllables, words, verses and stanzas. Higher order harmonics however can be observed only in the rhymed types of the text such as poetry.

1 INTRODUCTION

The rhythmicity characteristics of the written text is an under researched topic as opposed to the similar research in speech analysis domain. Rhythm arises as a result of letters, syllables or words, which are perceived as similar. In speech, these elements are syllables, or stressed syllables in particular.

Metrics for comparing the linguistic rhythm of speech have been proposed previously such as the proportion and standard deviation of vocalic and consonantal intervals within (Ramus et al., 1999) and pairwise variability indices (Grabe and Low, 2002), which reflect the specific phonological characteristics of the text. Speech rhythm reflects the phonological structure of a language (see, e.g., Roach, 1982; Dauer, 1987). For example, languages that allow complex consonant clusters have a rhythm with more variability in consonant length (Keane et al., 2010).

Larger-scale structures such as meter and rhyme are also important for cognitive processing of language and influence the aesthetic and emotional response of the subject (Obermeier et al., 2013).

Here, however, we analyse the rhythmicity of written text rather than voiced text (speech).

The tune-text relationships have been researched by Gussenhoven (2004) and Xu (2003). Xu (2003) proposed three levels of timing relations: underlying association of linguistically functional components (consonants, vowels, lexical tones, pitch accents, etc. combined into syllables), target synchronization (coordination of phonetic targets, the smallest articulated units associated with phonological elements), and surface alignment (e.g., consonant closure onset and release, vowel onset and offset, etc.).

The potential applications of text rhythmicity analysis may be the authorship analysis, i.e. the statistical study of linguistic and computational features of texts written by individuals (Venckauskas et al., 2015). It involves analyzing the writing styles or stylistic features from the document content. Writing style is an unconscious habit of a person, which varies from one author to another in the way uses words, grammar and other elements of a language to communicate. Writing style can be identified using semantical information extracted from the text features (Napoli et al., 2015).
The rhythmical characteristics of a text alongside with other stylometric features such as patterns of word usage (e.g., lexical richness), composition and writing, such as particular syntactic and structural layout traits, patterns of vocabulary usage, unusual language usage could be used for authorship attribution (Kapociute et al., 2015) or profiling (Kapociute et al., 2014).

In this paper, we analyze the rhythmicity (or periodicity) characteristics of the written text. To analyze rhythmicity characteristics we convert text fragments into numerical sequences and use the Empirical Mode Decomposition (EMD) (Huang et al., 1998) method to deconstruct numerical sequences into the empirical modes of frequency (empiquencies), or in our case text modes, which provide unique stylistics features of the text message.

The remaining parts of the paper are as follows. Section 2 discusses the related work on the numerical representation of text. Section 3 describes the proposed method. Section 4 presents an illustrative example in Lithuanian language. Finally, Section 5 presents conclusions and discusses future work.

2 RELATED WORK

The numerical processing of the text requires it to be converted into a digital representation. Transformation of text messages to number series is a widely researched topic.

Traditionally, documents are represented as feature vectors (e.g., in Vector space model (Salton et al., 1975), word embeddings (Bengio et al., 2000), word2vec (Mikolov et al., 2013), which do not preserve the sequential information contained in the text message. For example, common features such as the number of words in a text document with some specific linguistic property (e.g., ending in ‘-ing’) will not change if the words in a text are randomly permuted. Therefore, important stylistic and sub-stylistic information in bag-of-words models is lost. Other text features such as the frequency of n-grams preserve only local sequential information, but still do not allow reconstruction of the original text from its n-gram frequencies.

Text fingerprinting using similarity preserving hash functions have been used for plagiarism detection. It involves generation of a unique numerical representation of a document or a text segment. Then, these representations are used in the comparisons against a corpus of documents to find a matching copy (Palkovskii et al., 2010).

Yang and Lee (2009) investigate if mapping between text and time series data is feasible so the methods for time series analysis could be applied for solving relevant data mining problems in text and vice versa. They present the T3 (Text To Time series) framework that is based on different combinations of granularity (e.g., character or word level) and n-grams (e.g., unigram or bigram). To assign appropriate numeric values to each character, the T3 method applies the space-filling curves (e.g., linear, Z orders, Hilbert), which are mostly based on the keyboard layout.

Finally, one can assign fuzzy logic scores to texts or parts thereof and apply fuzzy algebra to evaluate the relations of text fragments with a specific keyword or a tag (Damasevicius et al., 2016).

Text conversion to semi-numerical sequences have been used in the phonetic coding algorithm, called Soundex (Odell and Russel, 1922) in the information retrieval task to match American English names. Soundex converts each name into a four-character code using a mapping scheme based on the sound of each letter. The first letter of the name is retained while each remaining letter in the input word is assigned a numeric value.

There are extensions and adaptations of the Soundex, such as Phonix (Gadd, 1999). While Soundex only removes certain letters and duplicate code characters, Phonix applies a much larger set of rules to transform the name before it is mapped to a set of codes. A number of variants of Soundex have been proposed for non-English languages such as SoundexPL (Kosmulski, 2005), LT-Soundex (Palijuonis, 2009), Polyphphon (Paramonov et al., 2016), Arabic Soundex (Ousidhoum and Bensaou, 2013), D-M Soundex and its adaptation for texts in Slavonic languages (Kawulak, 2009). Pinto et al. (2012) present an adaptation of the Soundex phonetic algorithm for representing SMS texts (or so called textese language).

There has been several efforts in establishing the taxonomy of rhythm-based units of the language such as the prosodic hierarchy (McCarthy and Prince, 1986), which includes the prosodic word, foot, syllable, mora, phonome, and features.

The decomposition of a text into structurally different text fragments and semantically different text themes has been analyzed by Salton et al. (1996).

In the context of analysis of text messages, Empirical Mode Decomposition (EMD), as far as we know, has not been used. The only known similar application is the use of EMD for visual stylometry in image recognition (Hughes et al., 2012).
3 METHOD

The proposed text decomposition method consists of the following steps as explained as detailed below.

1) Text Pre-processing and Mapping to Numerical Sequence

First, the text is pre-processed to remove all punctuation symbols and other non-alphabetic symbols such as digits.

Next, all remaining true letters of the language are assigned the numerical codes as follows: vowels are assigned 1, semivowels (glides or approximants) are assigned 0, and consonants are assigned -1.

An example of the coding tables for English and Lithuanian languages are presented in Tables 1 and 2, respectively. Lithuanian is one of Baltic languages. It has a Latin-based alphabet with additional letters with diacritics (in total, 32 letters).

Table 1: Coding table for English language.

<table>
<thead>
<tr>
<th>Letter</th>
<th>Numerical code</th>
</tr>
</thead>
<tbody>
<tr>
<td>A, E, I, O, U</td>
<td>1</td>
</tr>
<tr>
<td>Y, W</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 2: Coding table for Lithuanian language.

<table>
<thead>
<tr>
<th>Letter</th>
<th>Numerical code</th>
</tr>
</thead>
<tbody>
<tr>
<td>A, Ą, E, Ė, Ė, I, Ė, Y, O, U, Ū, Ū</td>
<td>1</td>
</tr>
<tr>
<td>V, J, L, M, N, R</td>
<td>0</td>
</tr>
</tbody>
</table>

2) Empirical Mode Decomposition (EMD) of a Numerical Sequence

Next, EMD (Huang, 1998) is applied to the obtained numerical sequence. EMD is a signal processing method based on local characteristics of data in the time domain. EMD allows decomposing a multicomponent signal consisting of many composite signals with different frequencies into its constituent mono-component signals, called Intrinsic Mode Functions (IMFs).

The steps comprising the EMD method are as follows:

1. Identify local maxima and minima of signal \( S(t) \), where \( t \) is a sample number in the data sequence.
2. Perform cubic spline interpolation between the maxima and the minima to obtain the envelopes \( E_{\text{max}}(t) \) and \( E_{\text{min}}(t) \).
3. Calculate the mean of the envelopes as:
   \[
   M(t) = \frac{E_{\text{max}}(t) + E_{\text{min}}(t)}{2}.
   \]
4. Calculate \( C_i(t) = S(t) - M(t) \).
5. If the number of local extrema of \( C_i(t) \) is equal to or differs from the number of zero crossings by one, and the average of \( C_i(t) \) is close to zero, then \( C_i(t) \) is an IMF; else repeat steps 1-4 on \( C_i(t) \) instead of \( S(t) \), until the new \( C_i(t) \) satisfies the conditions of an IMF.
6. Compute the residue \( R_i(t) = S(t) - C_i(t) \).
7. If the residue \( R_i(t) \) is above a threshold value of error tolerance, then repeat steps 1-6 on \( R_i(t) \) to obtain the next IMF and a new residue.

As a result, \( n \) orthogonal IMFs are obtained from which the original signal may be reconstructed as follows:

\[
S(t) = \sum_n \text{IMF}_n(t) + R(t) \tag{1}
\]

here \( R(t) \) is the final residue.

The first IMF consists of the highest frequency components present in the original signal. The next IMFs contain progressively lower frequency components of the signal, and the final residue exhibits any general trends followed by the original signal. Hereinafter, for further analysis, only three first IMFs (modes) can be used.

3) Spectral analysis of IMFs using Short Time Fourier Transform (STFT)

Next, for each \( \text{IMF}_n(t) \) we calculate its Short Time Fourier Transform (STFT) and a power spectral density (PSD) estimate of each window as follows. Given a signal \( \text{IMF}_n(t) \), the discrete STFT for harmonic \( h \) at time \( n \) is defined as follows:
where, \( \nu(n) \) is a suitably chosen window function (e.g., a rectangular window) of size \( L \) and

\[
w_i = \frac{2\pi h}{N}, \quad h = 0, 1, 2, \ldots, N - 1
\]

(3)

is the digital harmonic frequency in radian, and \( N \) is the total number of harmonics.

The spectrogram of a signal can be estimated by computing the squared magnitude of the STFT of the signal as follows:

\[
spectrogram(t, \omega) = |STFT(t, \omega)|^2
\]

(4)

### 4) Calculation of Scalograms

Next, we calculate scalograms (Fargues and Brooks, 1995) as a squared multiplication of a STFT with a real part of a Power Spectral Density (PSD) matrix as follows:

\[
scalogram(t, w) = (STFT(t, w) \cdot \text{real}(PSD(t, w)))^2
\]

(5)

Scalograms are visual plots that represent the percentage energy for each coefficient of STFT on a time-scale dimension.

### 5) Calculation of Convograms

Convograms (Li and Nábělek, 1996) are calculated as convolutions of different scalograms as follows:

\[
g(i, j) = \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) h(x_i, y_j)
\]

(6)

As a result of steps 4 and 5 we can obtain 3 scalograms for each of 3 modes and 3 convograms for each combination of modes (1-2, 2-3, and 1-3).

### 6) Feature Dimensionality Reduction using Principal Component Analysis (PCA)

To reduce feature dimensionality of the scalogram and convogram images, Principal component analysis (PCA) (Pearson, 1901) may be applied. PCA is a statistical method that transforms a set of observations of original variables into a set of values of linearly uncorrelated variables called principal components. The number of principal components is less than or equal to the number of original variables. The first principal component has the largest possible variance.

\[
E = \sum_{i=1}^{N} |x_i|^2
\]

(7)

Cardinality – the number of IMFs’ derived from the numerical representation of the text fragment. Cardinality represents the complexity of the structural component hierarchy of the text.
5 ILLUSTRATIVE EXAMPLE

As an illustrative example we analyse a line from the classical Lithuanian poem The Seasons (“Metai”, in Lithuanian) written by Kristijonas Donelaitis around 1765–1775.

The original text fragment is given below:

\[ Jau saulelė vėl atkopdama \\
\quad \text{budino svietq} \\
\quad \text{Ir žiemos šaltos trūsus} \\
\quad \text{pargriaudama juokės.} \]

The Lithuanian language has 32 letters, of which 12 are vowels, 6 are semivowels and 14 are consonants.

The above given poetry line contains 14 words (all unique and occurring only once), 86 characters (73 without spaces) and 27 syllables. The average word length is 1.93 syllables (6.14 letters), and the average syllable length is 3.18 letters. This short fragment was chosen deliberately as it is shorter than 140 characters that can be sent over Twitter.

1) Pre-processing and Transformation into Numerical Representation

The string is pre-processed to remove all white characters and delimiters, and uppercase letters are replaced with lowercase letters. The resulting text string is converted into the numerical representation using the proposed scheme (see Table 2) (1 – vowels, 0 – semivowels, -1 – consonants). The result is a binary numerical sequence as follows:

\[ 0 1 1 -1 1 0 1 0 1 0 1 -1 -1 1 -1 1 \\
0 1 -1 1 -1 1 0 1 -1 1 -1 1 0 -1 1 0 -1 \\
1 -1 -1 0 -1 1 -1 -1 0 1 -1 -1 1 0 -1 \\
0 1 1 1 -1 1 0 1 0 1 1 -1 -1 \]

The same numerical sequence is depicted graphically in Figure 1.

2) Decomposition using EMD

Next, we perform decomposition of a numerical sequence as a time series into Intrinsic Mode Functions (IMFs) or text modes using the EMD method. The result of decomposition is presented in Figure 2.

The series has been decomposed into four IMFs and a residue. Therefore, the cardinality of the analysed text fragment is equal to 4. IMF_1 has the largest amplitude. The frequency of IMF_1 calculated using the zero-crossing method is f_1 = 2.76, and the frequency of IMF_2 is f_2 = 7.44, and the frequency of IMF_3 is f_3 = 14.04. These values are close to the average length of syllables and words in Lithuanian language (1.93 and 6.14 letters, respectively).

The periodicity of IMF_1 corresponds to a metrical line of verses K. Donelaitis used – the classical hexameter consisting of six feet, separated by caesurae, a complete pause in a line of poetry. The foot is the basic metrical unit that forms part of a line of verse. The unit is composed of syllables, the number of which is limited.

In our example, first five feet consist of a single syllable, while the last one has two syllables. Therefore, the average length of the verse is 7 syllables, i.e., 13.51 letters, a value close to periodicity of IMF_3.

The periodicity of IMF_4 (f_4 = 28.24) corresponds to the length of the stanza, which in case of hexameter is equal to 2 verses (27 letters). A stanza is a grouped set of lines within a poem, which can have a regular rhyme.

Note that in this example IMF_1 is responsible for 92 % of variance in a numerical sequence, while IMF_2 – for 4 %, and IMF_3 – for 2.6 %, and IMF_4 – only for 0.7 %. Therefore, for this kind of short texts, of text modes above 3 could be ignored.
3) Calculation of Scalogram

For IMFs 1-3 we calculate PSD using STFT with a rectangular filter and 128 sampling point. Having PSD, the numerical sequence can be represented visually as a spectrogram or a periodogram. A spectrogram is a visual representation of the frequency spectrum of a time-varying signal while a periodogram is an estimate of the spectral density of a signal, which describes how the variance of the data is distributed over the frequency components of the data. Having spectrograms and periodograms calculated, we compute scalograms as multiplication of the periodogram matrix with a real part of the spectrogram matrix as in Eq. 5. The obtained scalogram allows to reveal the intrinsic periodicity of a series. The results are presented as spectrograms in Figure 3. Note that sequence no. is used instead of time here, because numerical representations of text are not time series, and periodicity is used instead of frequency.
1) Calculation of Convograms

To reveal the relationship between different IMFs, convograms are calculated as convolutions of the scalogram matrices of the respective IMFs. The results are presented in Figure 4.

Note that the overlap of periodicities between IMF1 and IMF2 is the largest.

Convograms and scalograms contain information that describe the stylometric features of the analysed text and specifically may reveal any periodicities or rhythmicities at different scales present in the text. The obtained convograms can be analysed either manually by an expert in digital signal analysis or further analysed using PCA or other feature dimensionality reduction method, which is however, has not been applied in this paper.

6 CONCLUSIONS

The spoken languages have their own specific patterns of durational variation (or “rhythm”) (Loukina et al., 2011). In this paper, we claim that it is also valid for the written texts of languages, too.

The application of Empirical Mode Decomposition (EMD) to text analysis allows to decompose text into basic text harmonics or modes: syllables, words, verses and stanzas. Higher order harmonics however can be observed only in the rhymed types of text. While more extensive research and analysis is still needed, the proposed method still can identify the frequency characteristics of the short texts, which match well with statistically established characteristics of the considered language. Of course, one should note the limitations of the approach: the result depends upon the select method of mapping from a sequence of text letters to a numerical sequence. The presented approach to map letters according to their spoken sound category (vowel, semivowel, consonant) may not be the best one or the only one possible. The use of other text-to-sequence mapping methods and how it allows to reveal the rhythmicity of the text is a subject of further research.

In future work, we also intend to use the text modes for authorship identification and for language comparison.

REFERENCES


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