

Towards Real-Time Fleet-Event-Handling for the Dynamic Vehicle Routing Problem

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Abstract: This paper proposes an approach to real-time fleet event handling for the Dynamic Vehicle Routing Problem based on evolutionary computation. For this purpose, a communication protocol between a fleet of vehicles and an optimization back-end is presented and the related changes to the evolutionary algorithm are illustrated. This allows for information exchange and event-handling in real-time. Furthermore, this paper describes the adaption of benchmark files for the static Vehicle Routing Problem to a dynamic real-time scenario including time-dependent travel times, as well as dynamic travel and service times. The adapted benchmark files are then used for the evaluation of the proposed system.

1 INTRODUCTION

Transportation costs are one of the major cost drivers enterprises have to consider in their daily operations. The increasing complexity and multilateral dependencies of entire industrial ecosystems create challenging requirements for the supply chain and distribution management. Huge amounts of goods need to be planned and distributed within short time periods. Customers expect on-schedule deliveries in the B2B as well as in the B2C market. It is crucial to be able to react towards unforeseen events like traffic jams or service delays and to track the progress of delivery execution.

This paper presents a system for the Dynamic Vehicle Routing Problem (DVRP) and ensures an immediate reactivity towards events, by using an adapted evolutionary algorithm. The system includes a simulator, which is able to model entire delivery periods with lengths of up to one day. To validate the system, different realistic scenarios have been created, consisting of a static and a subsequent dynamic optimization process. By receiving the customer requests a day in advance, the static optimization process is running over night, providing a proper solution. With the start of the actual delivery period, dynamic optimization is initiated in order to be able to react to changing traffic conditions or fluctuating service times. As the system is running in real-time, it provides real-world feedback to the optimization process.

The steering process is based on a newly developed two way communication protocol, which triggers information updates in an event-based fashion. Due to the implemented information protocol the simulator can be substituted by mobile devices, providing the same event-based information updates. The protocol is designed bilaterally. Status updates of the individual vehicles are sent to the optimization back-end, which in return provides routing updates to the vehicles. The information flow is steered by the so-called decision maker, which represents an information interface. Direct event processing enables an immediate reactivity towards dynamic travel and service times. The system aims at practical application.

The remainder of the paper is structured as follows: In Section 2, a literature-review is presented. Section 3 illustrates the general framework of the optimization scenario. In chapter 4, the architecture of the proposed DVRP-system is described while Section 5 explains the corresponding algorithmic aspects. In Section 6, the proposed system is evaluated. Finally, Section 7 and 8 conclude the paper and present future research possibilities.

2 RELATED WORK

As the Vehicle Routing Problem (VRP) is one of the most studied combinatorial optimization problems,

numerous papers were published in the last decades. A good overview of recent publications in the field of DVRP is given in the work of (Psaraftis et al., 2016). In this work, the authors deploy a taxonomy, consisting of eleven criteria, and classify 117 publications. The review published by Ritzinger et al. focuses on dynamic and stochastic VRPs (Ritzinger et al., 2015). For further surveys on the general DVRP, please refer to (Bektas et al., 2014) and (Pillac et al., 2013).

Out of the 117 reviewed papers of Psaraftis et al. eleven approaches can be classified as genetic or evolutionary algorithms. Whilst nine of the mentioned approaches exclusively address the processing of dynamic customer orders, only two refer to the processing of dynamic travel times or the processing of both dynamic elements. A major part of the mentioned approaches is based on the temporal segmentation of the optimization period into smaller sub-segments, which are processed with static solution approaches.

In (Barkaoui and Gendreau, 2013), a two-level genetic algorithm is used to handle problems with dynamic customer orders. (Créput et al., 2012), as well as (Elhassania et al., 2014) are based on static solution methods to process temporal sub-segments of the actual problem instance. In contrast to the work of Elhassania et al., which uses an ordinary GA, the paper of Créput et al. combines a GA with a self-organizing map approach. Furthermore, the two publications of Ghannadpour et al., are also based on the consecutive static processing of several temporal segments. Whereas the first paper can be used to process dynamic customer orders and dynamic travel times (Ghannadpour et al., 2013), the second one focuses on dynamic customer orders exclusively (Ghannadpour et al., 2014). A related approach, which is also based on the iterative processing of multiple time segments for dynamic customer orders can be found in (Hanshar and Ombuki-Berman, 2007). A differing concept is presented in (Taniguchi and Shimamoto, 2004) where the GA is applied to a newly developed road network and focuses on dynamic travel times. (Haghani and Jung, 2005) address dynamic optimization of customer orders, including time dependent travel times. A combined rolling horizon strategy in combination with an annealing GA is presented in the publication of (Gan et al., 2013).

(Branke et al., 2005) implemented various vehicle waiting strategies for the purpose of anticipating future customer orders. The goal is to maximize the success rate of including additional customer orders without violating any constraint. Another concept was published by (AbdAllah et al., 2017). Again, the dynamic VRP instance is modeled as a sequence of static VRP instances. By enhancing the underling

GA, the authors try to increase the population diversity and the capability to escape from local optimas.

The paper at hand progresses beyond the state of the art as the proposed system provides an immediate reactivity towards incoming information. Instead of the partitioning into temporal segments, the optimization period can be processed in a continuous, holistic way. While other papers consider only few different event types, the communication protocol proposed in this work results in various event types. These are considered in a dynamic real-time delivery scenario with changing traffic conditions and stochastic service times to model different real-world scenarios. Furthermore, delivery plans are evaluated economically by a cost-based fitness function, since this is the basis of decision making for transportation companies.

3 SCENARIO DESCRIPTION

3.1 Problem Description

In the static VRP optimization, delivery plans are calculated regardless of any real-time information like status updates on fleet events, even though this information is easily available nowadays. Hence, the proposed delivery plan is likely to become obsolete rather instantly. This is due to changes in traffic flows or other unexpected changes of the environment.

One first step to overcome this issue is to monitor the whole delivery period. Therefore, we have established a communication protocol between the individual vehicles and the optimization back-end. Each vehicle is represented by a state machine (Figure 1), submitting status updates in terms of event data, whenever the corresponding event occurs. One important assumption (A), that can directly be derived from the definition of the state machine, is that for each vehicle en route the next customer is fixed and cannot be altered. This is due to the fact that the optimization back-end receives the next status update at the arrival at the next customer location.

The defined model can simulate an arbitrary amount of vehicles, using predefined mathematical distributions for the generation of dynamic travel and service times.

Unlike other work on the dynamic VRP, the proposed communication protocol leads to the integration of various event types (*Ready for Departure, Started, Arrived, Unloaded, Departed*) into the VRP, which result from simulation in this work, but could easily be obtained from mobile devices in real-world applications. These events trigger different algorithmic actions which also include changes and correla-

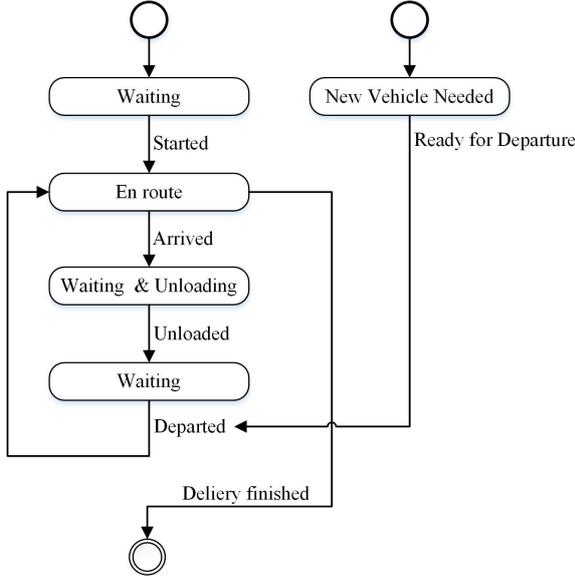


Figure 1: State machine model for individual vehicle.

tions to solution representations. The interaction of event data and optimization process is explained in detail in Section 5.

3.2 General Setting and Simulation

Unfortunately, exploring dynamic VRPs in real-time lacks the availability of compatible benchmarks, whereas benchmarks for static VRPs are very common. Hence, one solution to generate an appropriate setting for the real-time dynamic VRP is to adapt static benchmark files to suit a real-time implementation. Foundations to our work are the well-known Gehring & Homberger benchmarks for the static capacitated VRP with time windows (Gehring and Homberger, 1999).

3.2.1 Description of the Benchmark Files

Besides the maximum number of vehicles K and a uniform maximum capacity q of each vehicle, the Gehring & Homberger benchmark files consist of a list of N customers. Note, that the first customer c_0 is the depot. Each customer can be considered a 7-ary-tuple containing the values listed in Table 1.

Distances between customers are calculated as Euclidean distances. Commonly, these benchmarks suppose that one time unit equals one distance unit. As this assumption is contradictory to realistic use-cases, our approach differentiates between time and distance by using average speed values to calculate travel times from the given distances.

Table 1: Definition of customer c_i .

| Customer Number | i |
|-----------------|-------|
| x-Coordinate | x_i |
| y-Coordinate | y_i |
| Demand | d_i |
| Ready Time | e_i |
| Due Date | l_i |
| Service Time | f_i |

3.2.2 Introduction of Real-Time

To further enhance the benchmark towards real-time scenarios, three additional parameters are introduced: the start time of the delivery period is denoted as t_{start} , its planned duration is denoted as l_{period} and the average velocity of a vehicle is represented by v . Due to the fact, that the presented approach runs in system time, all relevant time parameters must be converted into milliseconds. Based on these parameters and the due date of the depot l_0 , which marks the end of the delivery period in the static benchmark, two basic coefficients can be derived:

$$f_{time} := \frac{l_{period} \cdot 60 \cdot 60 \cdot 1000}{l_0} \quad (1)$$

$$f_{distance} := \frac{v \cdot l_{period}}{l_0} \quad (2)$$

Using these coefficients, time and location data of the benchmark files can be adapted to create a real-time environment. The time and location data of every customer c_i is adapted as shown below.

$$x_{i,new} := x_i \cdot f_{distance} \quad (3)$$

$$e_{i,new} := e_i \cdot f_{time} + t_{start} \quad (4)$$

All other relevant parameters are adapted accordingly.

3.2.3 Time-Dependent Travel Times

Time-dependent travel times are crucial as they embody changing traffic conditions. Based on the concept of (Ichoua et al., 2003), the calculation period is divided into discrete, equidistant time intervals with predefined speed factors. The total travel distance results as sum of the iteratively calculated partial distances in each time interval. The travel time can then be calculated based on the total distance. One advantage of this method is the straightforward implementation of the FIFO principle, which guarantees, that a later departure at a specified destination cannot lead to a sooner arrival at another.

3.2.4 Dynamic Travel and Service Times

In real-world applications, traffic conditions underlie dynamic changes due to accidents, construction sites, congestion and more. To represent this adequately, we apply a gamma distribution on the time-dependent speed factors of the model. Specific parametrizations then allow the simulation of different traffic scenarios (Chiang and O. Roberts, 1980).

Additionally, staffing problems and occupied loading zones e.g. by delay of preceding unloading processes are only exemplary reasons that cause delayed service times in real-world scenarios. For this, queuing theory proposes the gamma distribution to generate dynamic service times (Liebermann et al., 1997). More details on the specific parametrizations are provided in Section 6.

3.2.5 Time Windows and Penalty Function

In the Gehring & Homberger benchmarks, each customer c_i is associated with a time window (e_i, l_i) , in which the delivery should be started. Time window violations are taken into account by a penalty function, which assigns a penalty cost value p_i to each customer. Depending on the end of the time window l_i and the arrival time s_i at customer c_i , this is calculated as follows:

$$p_i = \begin{cases} c_{penalty} + c_{fpenalty} \cdot (s_i - l_i) & \text{if } s_i > l_i, \\ 0 & \text{else.} \end{cases} \quad (5)$$

In this context, $c_{fpenalty}$ is a cost factor rating the time of delay and $c_{penalty}$ is the fixed cost part in case of time window violation.

3.2.6 External Vehicles

For each of the Gehring & Homberger benchmark files, a maximum number of vehicles K is specified. However, real-time reaction to dynamic events may require the use of additional vehicles in order to serve all customer requests, preferably in the given time windows. Hence, it is possible that K needs to be exceeded. In this case, our model assumes the possibility to hire different transportation companies by renting external vehicles (and drivers) which then carry out some of the customer requests. Certainly, this implies additional costs. These are assumed to be 20% higher than the costs in case all customers could be served by vehicles of the own fleet.

4 ARCHITECTURE

The proposed DVRP-system consists of three main components, which are reflected in Figure 2. The optimizer represents the core component of the system and is responsible for the actual optimization process. The simulator executes delivery plans in real-time and produces event data of the simulated fleet. Events for each vehicle are raised according to the state machine introduced in Figure 1. The decision maker handles those events in real-time by updating the information-base of the optimizer. A further responsibility of the decision maker is to decide whether it is economically viable to realize new delivery plans in case a new plan is proposed by the optimizer.

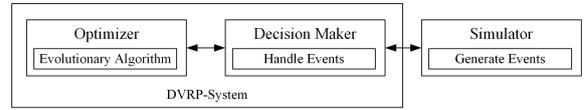


Figure 2: Architecture of the DVRP-system.

4.1 Optimizer

An evolutionary algorithm is proposed, which enhances the hybrid multi-objective evolutionary algorithm (HMOEA) by (Tan et al., 2006). Major parts of the HMOEA have been adapted, enlarged or substituted to comply with the requirements of the environmental model. The genotype is encoded as visualized in Figure 3. According to the representation, a delivery plan consists of various tours, which represent all customers dedicated to a specific vehicle. A tour starts and ends at the depot c_0 . Besides all customers c_i are represented as integer values.

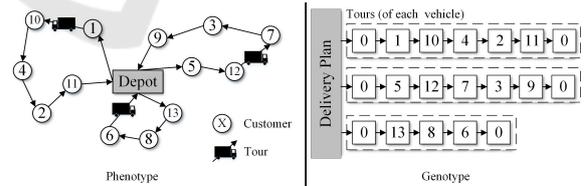


Figure 3: Encoding of a delivery plan.

The formerly used Pareto fitness ranking of the HMOEA was replaced by the restricted tournament selection (RTS) of Harik (Harik, 1995) and combined with a selection method as well as a simple elitism method. To enable the evaluation of the distance of different individuals as required in the RTS, the optimizer uses the Jaccard-Coefficient in combination with the 2-Gram method (Naumann and Herschel, 2010). Furthermore, we adopted the route-exchange-crossover, the three optional mutation methods (split-route-mutation, merge-route-

mutation, partial-swap-mutation), as well as all local search heuristics (intra-route-heuristic, lambda-interchange-heuristic, shortest-path-heuristic) of the original HMOEA, but adapted them to fit the requirements of the real-time model.

4.1.1 Cost Function

To evaluate the fitness of a solution, a newly developed cost function C_{total} was implemented. As costs are crucial for enterprises and their practical application of the VRP, the cost function aggregates three major cost drivers: distance-dependent costs $C_{distance}$, time-dependent costs C_{time} and penalty costs $C_{penalty}$. For that, the tour time of a vehicle (from start to end of its delivery) t_j is weighted with a time cost factor cf_{time} . Analogously, the tour distance of each vehicle d_j is weighted by $cf_{distance}$. The total time and distance costs are then both calculated as sum of the cost values of all K vehicles. The overall penalty costs $C_{penalty}$ result from the individual penalty costs p_i of all N customers.

$$C_{total} = C_{distance} + C_{time} + C_{penalty} \quad (6)$$

$$C_{distance} = \sum_{j=0}^K (cf_{distance} \cdot d_j \cdot \delta_j) \quad (7)$$

$$C_{time} = \sum_{j=0}^K (cf_{time} \cdot t_j \cdot \delta_j) \quad (8)$$

$$C_{penalty} = \sum_{i=0}^N p_i \quad (9)$$

To reflect the possibility of hiring external vehicles and the associated extra costs, δ_j is introduced and defined as follows:

$$\delta_j := \begin{cases} 1.0 & \text{if vehicle } j \text{ is part of fleet,} \\ 1.2 & \text{if vehicle } j \text{ is not part of fleet.} \end{cases} \quad (10)$$

4.2 Simulator

The simulator is responsible for the generation of the events, which includes the simulation of the dynamic travel and service times. Aligned to the approach of (Ichoua et al., 2003), the simulator generates individual speed factors for each road segment and each time interval. Based on the simulated speed factors the actual travel time can be calculated. The dynamic service times are simulated by applying the integrated gamma distribution directly to the updated service time values of the benchmark file. The flexible implementation of the simulator facilitates the modular exchange of different traffic/queuing models, as well as the integration of real traffic data. Furthermore,

it is possible to substitute the simulator for mobile devices or vehicle-based on-board devices, using the same event-based communication protocol.

4.3 Decision Maker

The decision maker represents the interface between the simulator and the optimizer. It is responsible for plan updates and the information flow towards the individual vehicles. For this purpose, the decision maker continuously compares the current best plan of the optimizer with the plan currently executed and decides whether a change should be realized. Thereby an real-time reactivity towards new information, as well as the alignment of the delivery plan towards the currently best solution is ensured throughout the entire optimization period.

As all information emerging from the simulator passes the decision maker, the decision maker is also responsible for the event handling process. This comprises the update of the information base, as well as the execution of repair routines. These are necessary in case the individuals of the HMOEA-population need to be adapted throughout the dynamic optimization process.

5 ALGORITHMIC ASPECTS

The communication protocol between the vehicles and the optimization back-end requires a thorough definition of the submitted event data and their algorithmic consequences. For this purpose, the decision maker is implemented as interface between the simulator and the optimizer to handle incoming events. The tasks of the decision maker can be divided as follows:

Update of Information-Base

To properly use the incoming information, it has to be embedded into the information base of the optimizer. This includes the real-time update of actual and expected travel/service times as well as the update of the customer base.

Adaption of Population

Some events also require an update on the population of the HMOEA to guarantee a consistent set of feasible individuals for the further execution of the optimization process. The importance of this will be explained subsequently.

5.1 Event Handling

Referring to Figure 1, this section describes all types of events and their inherent changes to the optimization process.

The *Arrived*-event marks the arrival of a vehicle at a customer and is handled with a simple routine. The decision maker processes the received information by replacing the expected arrival time at the corresponding customer (which was used by the optimizer for plan calculations until then) by the actual arrival time.

The same procedure is valid for the *Unloaded*-event which marks the end of the service period of a vehicle at a customer. In this case, the decision maker replaces the expected service time by the actual service time.

The *Departed*-event however requires more sophisticated routines. On the one hand the expected departure time has to be replaced by the actual departure time. On the other hand the served customer c_{old} , which the vehicle has departed from, has to be deleted from the representation. Due to (A) we obtain a fixed customer c_{next} as a next target for the considered vehicle. This causes the necessity to update the population of the HMOEA as c_{old} has to be deleted from each individual of the population. Each individual shall now contain one vehicle heading to c_{new} (which means one tour with c_{new} at first position).

The same adaptations have to be conducted for the *Started*-event, where c_{old} is considered as a substitute for the depot. Additionally, this event marks the beginning of the delivery period and therefore the shift from static to dynamic optimization.

In case the decision maker proposes the utilization of an additional vehicle, the *Ready for Departure*-event is triggered and a new vehicle departs at the depot c_{old} heading to a customer c_{new} . As a consequence, all individuals of the population have to be expanded by one vehicle also heading to c_{new} (A).

5.2 Repair Routines

To guarantee the individuals of the HMOEA-population to be feasible at all times, the events *Started* and *Departed* trigger repair mechanisms for the entire HMOEA-population. Each individual has to be adapted such that the new customer c_{new} is directly targeted by a vehicle, whereas the served customer c_{old} is deleted from all individuals. In some cases, it may be required to relocate several unserved customers within the individual. Therefore these customers are transferred to a so-called *relocation-list* (RL) and later reinserted by a special insertion method.

5.2.1 Repair Routine for the *Departed*-Event

In case c_{old} and c_{new} are scheduled to be served by the same vehicle, the corresponding tour will be cut before c_{new} , thus making sure that this vehicle serves c_{new} as next customer. Furthermore, the customers between c_{old} and c_{new} are put on the RL (Figure 4).

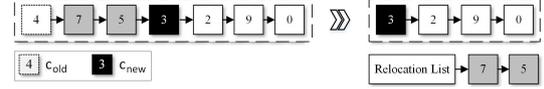


Figure 4: Repair routine for the *Departed*-event (case 1).

If c_{new} is contained in a different tour than c_{old} , all customers of the tour that contains c_{old} will be transferred to the RL. The customers of the tour containing c_{new} will be divided as visualized in Figure 5. This ensures that the considered vehicle keeps on heading to the customer that it is targeting (customer 6 in the example) while the vehicle, whose tour contained c_{old} , is now targeting c_{new} .

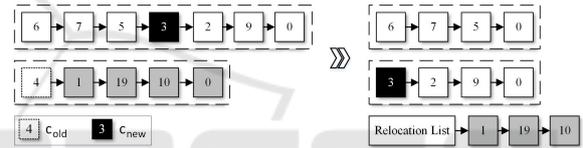


Figure 5: Repair routine for the *Departed*-event (case 2).

Repair Routine in Pseudo-Code:

```

Find tour containing c_old;
Delete c_old;
if(c_new is contained in same vehicle)
    Put customers before c_new on RL;
    Delete customers before c_new;
else
    Delete last customer (depot);
    Put remaining customers on RL;
    Find tour containing c_new;
    Divide tour at c_new;
    Replace vehicle that contained c_old;

```

5.2.2 Repair Routine for the *Started*-Event

In the case of the *Started*-event all scheduled vehicles leave the depot at the beginning of the delivery period. Thereby, each vehicle gets assigned a fixed first customer (c_{new}). In the following, the set containing these customers is denoted S . To update the individuals of the HMOEA-population, in a first step the depot at first position of each vehicle's tour is deleted. Subsequently, for each tour it is checked whether its first customer is contained in S . If so, this tour remains unchanged and the corresponding customer gets deleted from S . In the other case, the vehicle is put to a recombination list. In a third step, the remaining customers

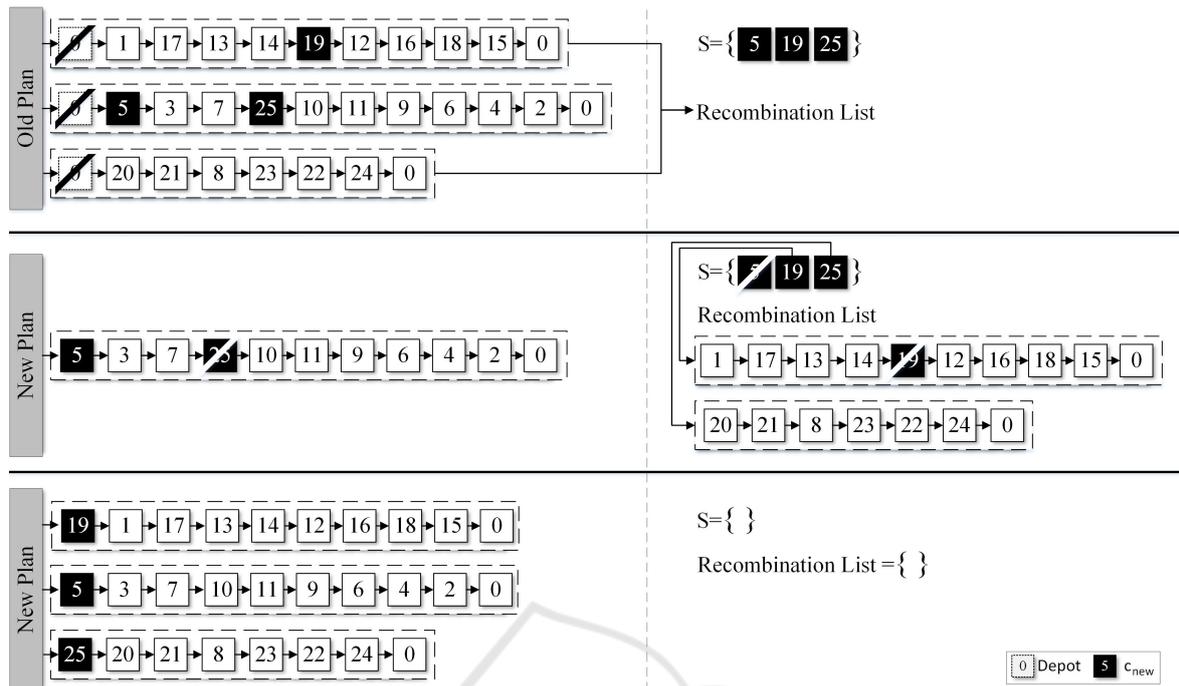


Figure 6: Repair routine for the *Started*-event.

in S are deleted from the tour. Finally the customers in S are recombined with the remaining tours in a cost efficient way to create a new individual that is feasible. For a short example on this repair routine see Figure 6.

In case no feasible way of recombination is found, customers of the remaining vehicle representations are transferred step by step to the relocation list until a feasible recombination is obtained. After this procedure, the customers of the RL are reinserted using the insertion method.

Repair Routine in Pseudo-Code:

```

Delete first customer of each individual;
for (each tour)
    if (first customer of tour is in S)
        Delete customer from tour;
        Delete customer from S;
    else
        Put tour on recombination list;
end
Delete customers in S from tours;
Recombine customers in S with remaining tours
of recombination list;
while (no feasible combination found)
    Put random customer (not contained in S)
    to relocation list;
    Recombine customers in S with remaining
    tours of recombination list;
end

```

5.2.3 Insertion Method

The insertion method is in charge of the reinsertion of the customers that were transferred to the relocation list by the repair routines. To minimize the loss of optimization knowledge, it is aspired to maintain the major parts of the customer-sequence. Therefore, this method randomly inserts (and instantly deletes) the first customer of the RL at a predefined number of positions in the genotype and calculates the corresponding cost value. Subsequently, the customer is inserted at the position, that causes minimal additional costs. If no feasible insertion position is found, a new vehicle is required to serve this customer. Thereafter, all following customers are inserted and deleted from the RL as long as there is no violation to the capacity limitation. In case of violation this procedure starts anew.

Insertion Method in Pseudo-Code:

```

while (customers contained in RL)
    for (counter < number of attempts)
        Insert first customer of RL at random
        position in genotype;
        if (feasible)
            Evaluate cost function;
            Delete first customer from genotype;
            Counter++;
        end
    end
    if (feasible position found)

```

```

        Insert first customer at best position;
    else
        Insert customer in new vehicle;
    while (no violation to capacity)
        Insert following customers from RL;
    end
end

```

6 EVALUATION

The aim of this chapter is a holistic evaluation of the repair routines. As a first step, this paper validates their general functionality and impact towards different dynamic problem instances. Future research should focus on a detailed analysis and the further enhancement of the approach. In order to evaluate the performance of the dynamic optimization, the evaluation concept is based on the comparison of the initial delivery plan and the actual plan. The actual plan P_{actual} results from the initial delivery plan $P_{initial,static}$ by constant changes through the continuous reactions of the optimization back-end to the dynamic environment, whereas the initial plan is the result of the static optimization at the beginning of the delivery period. Assuming this delivery plan is exposed to the dynamic events without online re-optimization, Figure 7 shows the respective cost as $P_{initial,simulated}$. To ensure the comparability of $P_{initial,simulated}$ with P_{actual} , it is crucial to use the same underlying traffic conditions and service times. Figure 7 shows the typical progression of the cost functions of the three considered plans.

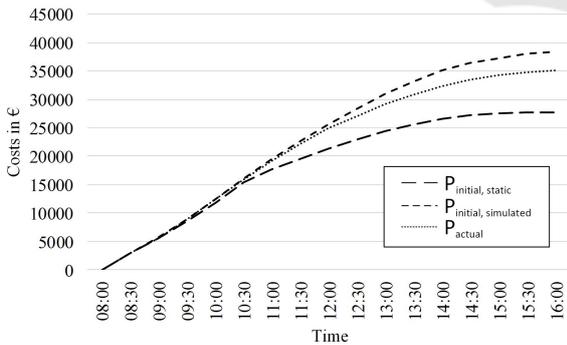


Figure 7: Typical progression of the cost functions.

6.1 Test Setup

The real-time test setup employs the C101 instances of the Gehring & Homberger benchmarks for 200, 400, 600, 800 and 1000 customers. Each of these instances was simulated using three different shifted gamma distributions. Every combination of the test

instances and the gamma distributions was repeated ten times with different random seeds, which resulted in 150 test runs. All instances model an entire real-time distribution period starting the static optimization at 8.00 pm the day before the actual delivery took place. Dynamic optimization starts with the beginning of the distribution period at 8.00 am and continues until 4.00 pm. All relevant parameters used in the test setup are shown in Table 2. For a detailed definition of the genetic parameters, please refer to (Tan et al., 2006).

Table 2: Test parameters.

| | |
|------------------|---------|
| Crossover-rate | 0.7 |
| Mutation-rate | 1.0 |
| Elastic-rate | 0.5 |
| Squeeze-rate | 0.7 |
| Population-size | 20 |
| Elitism-quantity | 3 |
| $c.f_{distance}$ | 1€/km |
| $c.f_{time}$ | 60€/h |
| $c.f_{penalty}$ | 50€/h |
| c_{base} | 100€ |
| t_{start} | 8:00 am |
| l | 8h |
| v | 70km/h |

The focus is set on evaluating different traffic conditions and their impact on the optimization process. Hence, one single parameter setting was used for the simulation of the dynamic service times. The service time is reflected by the gamma distribution (1, 0.25) which is shifted by 0.75. The three gamma distributions, which were used for the simulation of the dynamic service times are shown in Table 3.

Table 3: Parameter for the gamma distribution.

| | | |
|-----------------|---------------------|-------------|
| Distribution 1: | $\Gamma(1, 0.25)$, | Shift: 0.75 |
| Distribution 2: | $\Gamma(1, 0.50)$, | Shift: 0.5 |
| Distribution 3: | $\Gamma(1, 0.75)$, | Shift: 0.25 |

The distribution parameters have been chosen following the approach of (Russell and Urban, 2008) where the gamma distribution was applied to model dynamic travel times. The expected value equals 1 in all cases.

6.2 Test Evaluation

The final average results of all 150 test instances grouped by the number of customers are shown in Table 4. The results indicate the percentage, as well as the total deviation of P_{actual} from $P_{initial,simulated}$. In total, an average saving of 6.58% in the overall costs

Table 4: Test results on different instances of the adapted Gehring & Homberger C101 benchmark files.

| Number of Customers | | Total Costs [€] | Total Distance [km] | Total Time [h] | Number of Vehicles | Number of Time Window Violations | Penalty Costs [€] |
|---------------------|---|-----------------|---------------------|----------------|--------------------|----------------------------------|-------------------|
| 200 | Δ | -1687.98 | 214.10 | 8.64 | 1.23 | -18.67 | -2420.54 |
| | % | -7.66% | 11.30% | 5.66% | 3.89% | -25.69% | -25.08% |
| 400 | Δ | -3458.28 | 439.16 | 12.04 | 2.50 | -36.13 | -4620.11 |
| | % | -7.93% | 9.12% | 3.80% | 3.92% | -24.47% | -24.18% |
| 600 | Δ | -5446.20 | 678.78 | 14.41 | 2.93 | -53.07 | -6989.88 |
| | % | -7.23% | 6.61% | 2.59% | 2.88% | -22.33% | -22.16% |
| 800 | Δ | -5460.88 | 268.58 | 0.43 | 1.33 | -46.33 | -5755.30 |
| | % | -4.98% | 1.50% | 0.07% | 0.92% | -14.12% | -13.15% |
| 1000 | Δ | -8643.93 | -1318.35 | -26.63 | 2.17 | 40.50 | -5727.95 |
| | % | -5.07% | -3.73% | -2.19% | 1.03% | -9.27% | -9.09% |
| Total | Δ | -4939.45 | 56.45 | 1.78 | 2.03 | -38.94 | -5102.75 |
| | % | -6.58% | 4.96% | 1.99% | 2.53% | -19.18% | -18.73% |

could be achieved. The overall saving is primarily caused by a significant reduction of the penalty costs and usually results in an increase of the distance and time values. As shown in the table, the increase in the distance and time values seems to correlate with the number of processed customers. The instances with less customers generally indicate a higher increase in the corresponding values, than the instances with more customers. The number of additional vehicles is also increasing by 0.92% to 3.92% which means up to three additional vehicles in average. However, there was no test instance in which the number of vehicles exceeded the maximum fleet size K of the C101 Gehring & Homberger benchmarks. This implies that no external vehicle was needed in all test instances. The percentual reduction of time window violations is decreasing with the number of processed customers, whereas the total number reaches its peak at the test instances with 600 customers. As the number of time window violations is directly affecting the penalty costs, similar characteristics are reflected in these results. The achieved results indicate a reliable performance of the implemented repair routines in various test settings, by achieving overall average savings between 4.98% and 7.66%.

7 CONCLUSION

This paper proposed an approach to real-time fleet event handling for the DVRP based on evolutionary computation. In contrast to other approaches, the system allows for rapid responses to dynamic events and processes dynamic travel times as well as dynamic service times. The system is able to simulate real-time delivery periods lasting up to one day and is designed for further expansion like the inclusion of GPS-data or real event data. With the two newly developed repair routines, new innovative methods were imple-

mented to ensure a continuous creation of feasible delivery plans. The system runs a time-dependent travel time model and optimizes the total costs of the delivery plan including penalty costs for delayed delivery. In empirical studies the system and its repair routines could be validated in different test scenarios. Furthermore, the DVRP-system led to cost savings between 4.98% and 7.66% in all test scenarios.

8 FUTURE WORK

The flexible and modular system implementation, allows for easy extension and adaption. Even the substitution of essential parts such as the simulator is possible with little effort. This is enabled by a smart and lightweight system architecture with a clearly structured message exchange protocol between the system components. Therefore, the system could be extended by additional dynamic aspects such as dynamic customer orders. In order to test the system in a real-life scenario, the simulator is projected to be substituted and replaced by mobile devices and/or be connected to on-board vehicle-based systems. Such alternate edge devices would then be responsible for the information (event) transfer towards the optimization back-end. The adaption of the current system would require very little effort only. As a long-term goal, it is aspired to include GPS-data. Besides these structural adaptations of the system, it is crucial for further development to enlarge the test evaluation towards additional benchmark tests. Especially, more restrictive settings considering the fleet size would be preferable to evaluate the concept of external vehicles and the influence of the associated extra costs δ_j . Further research focuses on a detailed analysis of repair routines and their impact on the optimization process. Additionally, existing optimization algorithms like Ant Colony Optimization or Particle Swarm Optimization

and other solution strategies for the DVRP (Psaraftis et al., 2016) need to be adapted to the proposed dynamic real-time VRP-environment to ensure comparability. The gathered insights can then be used to gain optimization performance.

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