A Novel Approach for Handling Discontinuities in Non-iterative Co-simulation

Daniela Dejaco and Martin Benedikt
VIRTUAL VEHICLE Research Center, Inffeldgasse 21A, Graz, Austria

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Abstract: In this work, a novel approach for the co-simulation of systems with discontinuities is presented. Currently, an extensive literature exists on the simulation of distributed systems as well as on the proper discontinuity handling during simulation. The not trivial task is to design a simulation platform that is able to do both at the same time.

The proposed algorithm, which extends an existing non-iterative co-simulation strategy, administrates the mutual communication between two subsystems to assure that events are propagated correctly within the distributed system. Based on a prediction of future event triggering, the co-simulation sequence is chosen and thus the discontinuities are handled with no need of “rolling-back” or of iterating.

A simulation example demonstrates the efficiency of the outlined algorithm.

1 INTRODUCTION

A hybrid system is a dynamic system where a continuous time behavior is combined with a discrete time behavior. This means that the system is both capable of flowing and of jumping. The continuous character of the system is described by a differential equation, while the discrete time part is modeled by an automaton. Hence, the current state of the overall system is described by both the continuous state $x(t)$ and the current discrete mode (Henzinger, 1996).

The jumps between the various modes of the system are associated to so called “events”. We distinguish between two types of events:

- Time events, triggered at a previously known time;
- State events, triggered if a condition associated to the continuous state $x(t)$ is satisfied, i.e. if the continuous state $x(t)$ reaches a certain threshold.

The time-discretization paradigm for simulating physical systems is nowadays a well known and established field of studies; its origins can be attributed to the deeper studies of system theory (see for example (Zadeh and Desoer, 1963)). For this simulation paradigm, the simulation of time events is straightforward. The simulation across state events is a bit more challenging, because whenever the solution crosses through a state event, the exact time instant of the discontinuity must be detected. For real-time simulation, interpolation methods of low order are preferable, while for a more accurate detection of the exact event time iterative methods are applied (Cellier and Kofman, 2006). Although there is a huge variety of methods for both discontinuity detection and exact event localization (see for example (Park and Barton, 1996) or (Zhang et al., 2008)), no current method can guarantee the proper functioning for all possible systems to be simulated. Hence, the task is to find the method that applies best to the specific use case.

A more recently developed numerical simulation strategy, termed Quantized State Simulation (QSS) (Cellier and Kofman, 2006) (Cellier et al., 2008), proposes to discretize the state values instead of discretizing the time. While the time-discretization algorithms convert Ordinary Differential Equation (ODE) systems to equivalent difference equation systems, the QSS algorithms convert the continuous-time model to an equivalent discrete-event model. The obtained discrete-event model can then be simulated using a discrete-event simulation engine, for example the Discrete Event System Specification (DEVS) (Zeigler et al., 2000). The asynchronous nature of this algorithm makes it a very powerful method for state event handling; detecting if the continuous state $x(t)$ reaches a threshold is exactly what QSS algorithms are designed for. Hence, as no iteration is needed at discontinuities, it is well suited for real-time simula-
tion. However, only for QSS of first order the event localization is exact; for higher orders, the localization is based on a linearization of the derivatives at the current point (Cellier et al., 2008).

The numerical simulation problem gets more intricate if the system to be simulated is a large-scaled cyber-physical system (CPS). Due to the increased complexity, the hybrid character and the different areas of engineering covered, it is typically necessary to split the overall system in separated subsystems. Each subsystem is modeled with a specific domain and is solved separately by a tailored solver. An efficient coupling of these subsystems is thus necessary in order to simulate the CPS properly. A commonly used methodology is the so called co-simulation, where each subsystem is solved independently over a certain time interval (macro-step), at the end of which the subsystems are allowed to exchange information. For this purpose, the functional mock-up interface (FMI) (Blochwitz et al., 2012) was established as a tool independent standard to support the exchange and the (protected) integration of various subsystems even if different simulation tools are used. In terms of co-simulation, iterative and non-iterative numerical schemes are available for adequate subsystem integration. Iterative approaches strictly require resetting of subsystems (and of their solvers) and can therefore be applied only to a very limited set of tools. On the other hand, non-iterative approaches state marginal requirements on simulation tools and can be applied in general. In case of closed loops, estimation of the future output of dedicated subsystems is performed by extrapolation.

The main idea is to estimate the future output of a subsystem by extrapolation. This estimation is then used as an input to simulate the subsequent subsystem over the next macro-step. This co-simulation strategy is termed weak coupling, as each subsystem can be treated as a black-box and no information about its internal structure is needed for co-simulation purposes.

Up to date, co-simulation platforms, as well as the “FMI for Co-Simulation” 2.0 (Blochwitz et al., 2012), are currently focusing on continuous system simulation, limiting simulation accuracy. The purpose of this work is to propose a solution of how non-iterative co-simulation can be extended in order to be able to simulate properly hybrid systems.

The aforementioned QSS simulation paradigm can easily be extended to the simulation of distributed systems (Bergero et al., 2013). As previously mentioned, the QSS converts the various subsystems to discrete-event models. In literature, there are quite a lot of solutions for the simulation of distributed discrete-event models. In general they can be categorized into so called optimistic approaches (see for example (Jefferson, 1985)) and conservative approaches (see for example (Chandy and Misra, 1979)).

Besides the lower accuracy in comparison to the well known time-discretization simulation, the biggest drawback of applying QSS to co-simulation is that most of the co-simulation platforms and integrated tools are currently designed for numerical simulation with time-discretization.

In this work, a novel approach of non-iterative co-simulation of hybrid systems is proposed. The non-iterative and time-discretizing nature will be preserved, but some additional knowledge of the internal structure of the models is needed. However, only slight modifications on the FMI standard would be necessary. The need of adapting the FMI standard to hybrid systems is currently discussed in the FMI working group “Clocks and Hybrid Co-Simulation” (Broman et al., 2015).

Section 2 is devoted to non-iterative co-simulation and presents a simple hybrid system. Furthermore, extensions of common non-iterative co-simulation approaches are briefly discussed. In Section 3, the proposed algorithm is exposed. The algorithm is then applied and the results are discussed in Section 4. Finally, in Section 5 two important extensions to the algorithm are proposed.

## 2 PROBLEM DESCRIPTION

### 2.1 Non-iterative Co-simulation

Most integration platforms use a non-iterative coupling approach to co-simulate distributed systems. Each subsystem is solved independently using a suitable fixed or a variable micro-step $\delta T$. At predefined points in time, the simulations are paused and data can be exchanged between the subsystems. The time intervals between these points are termed macro-steps $\Delta T$. As shown in Figure 1, in order to solve the
closed loops in the distributed networks, the output of subsystem 2 is extrapolated (based on the history of simulation data) and fed into subsystem 1. Subsystem 1 can then be simulated over the macro-step and its output allows to simulate subsystem 2. The choice of the scheduling, the order of extrapolation as well as of the macro-step size is crucial and is discussed in (Benedikt et al., 2013a).

In this example, the subsystems within the co-simulation are scheduled in sequential order, i.e. the subsystems are not simulated in parallel. Of course, this is more time consuming in general, but significantly increases accuracy as well as numerical stability. For real-time applications, at the price of decreasing accuracy, it is possible to extrapolate the outputs of both subsystems and hence simulate the subsystems in parallel.

A recently proposed extension to the classical non-iterative co-simulation scheme, called NEPCE (Benedikt and Hofer, 2013), estimates the error committed by extrapolation for the current macro-step and compensates it during the subsequent steps in terms of energy preservation. This approach is extended for application of smoothing filters, effectively reducing aliasing effects. In (Drenth, 2016) the benefit of filtering techniques is demonstrated along very stiff stiff system integration. Recently, in (Sadjina and Pedersen, 2016), an extension of NEPCE for incorporation of direct feedthrough was done. For handling stiff systems linearly-implicit schemes are proposed (Arnold et al., 2007).

However, these mechanisms are not adequate to simulate distributed systems with discontinuities described by state events. An extension to the non-iterative approach that is able to do so is proposed in this paper.

Note: For the proposed algorithm to work, it is mandatory that the solvers of each subsystem are capable of simulating across discontinuities.

2.2 A Simple Example

The hybrid system on which the algorithm is tested is shown in Figure 2. It consists of a mass \( m_1 \) connected to the ceiling by a spring and a damper with coefficients \( k_1 \) and \( d_1 \), respectively. Similarly, a second mass \( m_2 \) is connected to the first mass by a spring-damper element with coefficients \( k_2 \) and \( d_2 \). Let \( x_i(t) \) and \( v_i(t) \) be the position and velocity, respectively, of the mass \( i \) with respect to the ceiling.\(^1\) The continuous time behavior of the hybrid system can then be described by the following set of differential equations:

\[
\dot{z} = A z + g = \begin{bmatrix} A_1 & B_1 & B_2 \\ B_1 & A_2 & B_2 \\ 0 & 0 & A_2 \end{bmatrix} z + g, \tag{1}
\]

where the matrix \( A \) is composed of

\[
A_1 = \begin{bmatrix} 0 & -\frac{d_1}{m_1} & -\frac{d_1}{m_1} \\ \frac{k_1}{m_1} & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \tag{2}
\]

\[
A_2 = \begin{bmatrix} 0 & -\frac{d_2}{m_2} & -\frac{d_2}{m_2} \\ \frac{k_2}{m_2} & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}, \tag{3}
\]

\[
B_1 = \begin{bmatrix} \frac{k_1}{m_1} & 0 & 0 \\ 0 & \frac{d_1}{m_1} & 0 \\ 0 & 0 & 0 \end{bmatrix}, \quad B_2 = \begin{bmatrix} \frac{k_2}{m_2} & 0 & 0 \\ 0 & \frac{d_2}{m_2} & 0 \\ 0 & 0 & 0 \end{bmatrix}, \tag{4}
\]

and the vector \( g \) is given by

\[
g = \begin{bmatrix} g_1^T \\ g_2^T \end{bmatrix} = \begin{bmatrix} 0 & -g & 0 & -g \end{bmatrix}^T, \tag{5}
\]

with \( g \) being the gravitational acceleration. The state space vector of the overall system is:

\[
z = \begin{bmatrix} z_1^T \\ z_2^T \end{bmatrix} = \begin{bmatrix} x_1 \\ v_1 \\ x_2 \\ v_2 \end{bmatrix}. \tag{6}
\]

This hybrid system is composed of only one mode, but there are two events that can cause a discontinuity in the state vector:

- The mass \( m_1 \) hits the ceiling
  \[ \text{IF} \ (x_1 \geq -\Delta x) \quad \text{&} \quad (v_1 \geq 0) \]
  \[ \text{RESET} \quad v_{1,\text{new}} = -v_1 \]
- The two masses collide
  \[ \text{IF} \ ((x_1 - x_2) \leq 2\Delta x) \quad \text{&} \quad ((v_1 - v_2) \leq 0) \]
  \[ \text{RESET} \quad v_{1,\text{new}} = \begin{bmatrix} (m_1 + m_2)v_1 + 2m_1v_2 \\ (m_1 + m_2)v_1 + 2m_1v_2 \end{bmatrix} \]

As shown in Figure 2, the overall system is split into two subsystems, each one corresponding to one of the two masses.

Thus, the continuous time dynamics of subsystem 1 are described by

\[
\dot{z}_1 = A_1 z_1 + B_1 u_1 + g_1, \tag{7}
\]

\[\text{Figure 2: Test case: two-mass-spring-damper system connected to the ceiling. The system is split into two subsystems, each one corresponding to a single mass and its position and velocity as state variables.}\]
where the input $u_1$ corresponds to the state vector of subsystem 2:

$$u_1 = \begin{bmatrix} u_{1x} \\ u_{1v} \end{bmatrix} = z_2.$$  

(8)

Similarly, the continuous time dynamics of subsystem 2 can be written as

$$\dot{z}_2 = A_2 z_2 + B_2 u_2 + g_2.$$  

(9)

with input

$$u_2 = \begin{bmatrix} u_{2x} \\ u_{2v} \end{bmatrix} = z_1.$$  

(10)

But what about the state events that cause the jumps in the state variables? We can clearly see that the condition corresponding to the mass $m_1$ hitting the ceiling only depends on the state variables of subsystem 1. Even the jump in the state variables only affects this subsystem. Hence, this event will be termed **Private state event**.

The state event corresponding to the collision of the two masses, instead, depends on the state variables of both subsystems and the reset condition affects both. Thus, these events will be referred to as **Shared state events**.

The discontinuities of subsystem 1 can thus be written as:

- **Private State Event:** The mass $m_1$ hits the ceiling

  $\text{IF } (x_1 \geq -\Delta x) \land (v_1 \geq 0)$

  $\text{RESET } v_{1,\text{new}} = -v_1$

- **Shared state event:** The two masses collide

  $\text{IF } ((x_1 - u_{1x}) \leq 2\Delta x) \land ((v_1 - u_{1v}) \leq 0)$

  $\text{RESET } v_{1,\text{new}} = \frac{(m_1 + m_2)v_{1} + 2m_1u_{1v}}{m_1 + m_2}$

while the only event that can be triggered in subsystem 2 is:

- **Shared State Event:** The two masses collide

  $\text{IF } ((u_{2x} - x_2) \leq 2\Delta x) \land ((u_{2v} - v_2) \leq 0)$

  $\text{RESET } v_{2,\text{new}} = \frac{(m_1 + m_2)v_{2} + 2m_1u_{2v}}{m_1 + m_2}$

In order for the proposed algorithm to work, there must exist a link between the shared state events of the two subsystems. In an object-oriented programming paradigm, for example, the events can be treated as objects and include a pointer to the corresponding event in the other subsystem. Due to this necessary change, the subsystems can no longer be seen as "black boxes" as it is state-of-the-art in common co-simulation platforms.

Figure 3 summarizes the hybrid behavior of both subsystems and shows the necessary links between the two subsystems.

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**2.3 Necessary Extensions**

A significant problem arises when a shared event is triggered only in one of the two subsystems. In our test case this means that for example the upper mass changes direction due to a collision with the lower mass, while the lower mass does not recognize the occurrence of the event. This violates the laws of physics.

Alternatively, it can happen that a shared event is triggered in subsystem 1 and the reset on the state variables is done accordingly. If the same shared event is triggered in subsystem 2 with a small delay, the reset of the state variables proves to be completely wrong. As stated, the reset condition depends on $u_2 = z_2$. For a correct implementation, the reset condition should be calculated based on $u_1 = z_1$. For the upper mass, this means that for example the upper mass becomes inactive only after the jump in subsystem 1.

Finally, private state events cause abrupt changes in the state variables of one subsystem. This jump propagates to the second subsystem according to its ordinary differential equation. If no changes are applied to the co-simulation paradigm, however, the information about the jump is sent only after the end of the macro-step. This delay in the loop can cause oscillations.

In order to avoid these unpredictable errors, an algorithm for the correct co-simulation of hybrid systems is proposed in the following section.
3 ALGORITHM

3.1 Requirements and Main Idea

Summarizing, the requirements on the co-simulation platform to apply the proposed algorithms are:

- Each subsystem must be capable of simulating across discontinuities. That means that it must be able to detect discontinuities and it must be able to locate them accurately either by interpolation or by iteration.
- There must be a (bilateral) link from a shared state event to its corresponding shared state event in the other subsystem.
- Each subsystem must be capable of interrupting its own simulation even within a macro-step. After such an interruption it can notify this occurrence to the co-simulation platform. Note that it is not demanded that a subsystem be able to stop the simulation of the other subsystem, but merely to interrupt its own simulation procedure.

The proposed algorithm is designed for sequential co-simulation and cannot be completely extended to a parallel paradigm. In section 5, however, it is briefly discussed how the algorithm could be redesigned to switch between a sequential and parallel co-simulation mechanism.

The main idea behind the algorithm is that, as soon as an event is detected in one subsystem, the simulation should be stopped and the occurrence of the event should be notified to the other subsystem. As one subsystem is only capable of stopping its own simulation and as it is not possible to “roll back”, the first system to be simulated must be the one where a private state event is more likely to occur within the next step. If the event is a shared state event, instead, after interrupting the simulation of the first subsystem, the exact event time must be notified to the second subsystem. Furthermore, the bilateral links between the shared state events serve to communicate to the second subsystem which event was triggered.

For our test case, the upper mass (subsystem 1) is the only one where private state events are possible, hence the co-simulation sequence will be, for each macro-step $\Delta T$:

1. Extrapolate subsystem 2
2. Simulate subsystem 1

In section 5 it will be shown how the simulation sequence is chosen at the beginning of each macro-step if it is not trivial.

3.2 Detailed Description

Having chosen a proper co-simulation sequence, a suitable macro-step $\Delta T$ and interruption time $eT$ (see subsection 3.2.1), the algorithm can be written in detail as follows.

For each macro-step $\Delta T$:

I EXTRAPOLATE SUBSYSTEM 2: The output of subsystem 2 is extrapolated with a polynomial of first order (zero-order for the first iteration).

II SIMULATE SUBSYSTEM 1: Using the extrapolated output of subsystem 2 as an input, subsystem 1 should be simulated till the next macro-step point, unless an event is detected within the current step, i.e.:

- If a private state event is detected at time $t_e$, the simulation should be interrupted at $t_{stop} = t_e + eT$.
- If a shared state event is detected at time $t_e$, a link to its co-event $e$ should be created and the simulation should be interrupted at $t_{stop} = t_e + eT$.

It is necessary to extend the simulation by a small time lap $eT$ to assure that there are at least two samples available if an extrapolation of first order is demanded.

III SIMULATE SUBSYSTEM 2:

- If the simulation of subsystem 1 was not interrupted by any event, simulate subsystem 2 without allowing it to trigger events.
- If the interruption in subsystem 1 was due to a private state event, simulate subsystem 2 till $t_e$, and then simulate it till $t_{stop}$.
- If the interruption in subsystem 1 was due to a shared state event, simulate subsystem 2 till $t_e$, trigger event $e$ and continue simulation till $t_{stop}$.

IV CHECK: The state vector of both subsystems must now be visible within the co-simulation platform. In very rare cases it can happen that:

- A private state event in subsystem 1 was not detected during the simulation, but is detected now. In that case trigger the event in subsystem 1.
- A shared state event was not triggered properly and is recognized now. Trigger the event in both subsystems.
- Due to a wrong setting in the simulation sequence a private state event is recognized in subsystem 2; trigger the event now.
After having triggered the event, extrapolate subsystem 2, simulate subsystem 1 till \( t_{\text{stop}} = t_{\text{stop}} + \varepsilon T \) and then simulate subsystem 2 till \( t_{\text{stop}}^* \). No event triggering is allowed in none of the systems during this short time \( \varepsilon T \); if a state event is detected, don’t trigger it, but repeat step \( \text{CHECK} \).

**V ITERATE:** Go back to I unless simulation time is over.

### 3.2.1 Choice of Interruption Time \( \varepsilon T \)

The interruption time \( \varepsilon T \) must be chosen small enough to ensure that no two consecutive events happen within this time. Obviously, zeno-chattering phenomena, which cannot be simulated properly neither in a mono-simulation, cannot be handled in the co-simulation paradigm (Lunze and Lamnabhi-Lagarrigue, 2009). Furthermore, \( \varepsilon T \) must be at least as large as the minimum step-size in each internal solver and must be large enough to avoid discontinuity sticking (Park and Barton, 1996).

### 4 SIMULATION EXAMPLE

To demonstrate the efficiency of the proposed algorithm, it is tested on the mass-damper system described in 2.2. The results of the co-simulation are then compared to a mono-simulation, i.e., where the overall system is simulated within a single solver. Neglecting numerical errors, we can assume that the results of the mono-simulation are correct.

To simulate the dynamic behavior of the system, for both co-simulation and mono-simulation, a Runge-Kutta-algorithm of 4th order is used. If a discontinuity is detected, it is located accurately using a bisection algorithm.

The physical parameters used for the simulation are \( m_1 = 0.2 \text{kg}, m_2 = 0.3 \text{kg}, d_1 = d_2 = 0.01 \text{kg/s}, k_1 = k_2 = 1 \text{kg/s}^2 \) and \( \Delta x = 0.55 \text{m} \), while the initial values are set:

\[
\begin{bmatrix}
  x_1 \\
  v_1
\end{bmatrix}_{(i=0)} = \begin{bmatrix}
  -0.7 \\
  3.5
\end{bmatrix},
\begin{bmatrix}
  x_2 \\
  v_2
\end{bmatrix}_{(i=0)} = \begin{bmatrix}
  -8.8 \\
  3
\end{bmatrix}.
\]

Figure 4 shows the simulation results using a macro-step size of \( \Delta T = 0.1 \text{s} \) and an interruption time of \( \varepsilon T = 10^{-4} \). We can see that even for a quite long macro-step, the algorithm performs very well as the trends of co-simulation and mono-simulation are identical.

In contrary, using the macro-step \( \Delta T = 0.3 \text{s} \), the co-simulation for hybrid system does not give good results for this test case. In Figure 5, we can clearly see that at \( t = 0.9 \text{s} \), a private state event (The mass \( m_1 \) hits the ceiling) is detected in the co-simulation, whilst this is not the case in the mono-simulation. This event error is then propagated throughout the simulation and leads to totally wrong and unpredictable results.

Although these two examples show that the choice of the macro-step size is crucial for the co-simulation, it is shown in (Benedikt et al., 2013b) how NEPCE could significantly improve the simulation even for larger macro-steps.
5 EXTENSIONS

5.1 Automatic Co-simulation Sequence

As previously explained, for the test case the co-simulation sequence is trivial. Only subsystem 1 triggers private state events and is hence the subsystem to be simulated first. If both subsystems can trigger private state events, the co-simulation sequence must be set at the beginning of each macro-step. The setting is based on a prediction of which subsystem is more likely to trigger a private event within the next macro-step. The proposed procedure is likely to work properly, but in some very rare cases it can fail. If it fails, however, it will be recognized with a small delay during the CHECK phase in the algorithm proposed in 3.2.

For the first iteration, the co-simulation sequence must be set randomly. For the following iterations the technique is the following (the assumption is that currently subsystem 1 is simulated first):

- Set $\Delta T^* = 1.5\Delta T$.
- Extrapolate subsystem 2 till $\Delta T^*$ and check if a private event is triggered.
- IF no private event is triggered, keep the co-simulation sequence.
- IF a private event is triggered, extrapolate subsystem 1 till $\Delta T^*$ and check if a private event is triggered.
  - IF no private event is triggered in subsystem 1, switch the simulation sequence.
  - IF a private event is triggered in subsystem 1, do some iterations to find out which subsystem is supposed to trigger its private event first. This subsystem is the subsystem to be simulated first.

To prove the correctness of this idea, a co-simulation example is shown in Figure 6. It refers to the usual test case, but in this case the ceiling is not standing still anymore. In addition, the mass $m_2$ can hit the floor, which is moving as well. This means that both subsystems are capable of jumping due to a private state event.

Here, the gray dashed lines show the extrapolated outputs that are used for co-simulation purposes. We can see that till $t = 2.4s$ subsystem 2 is extrapolated (default co-simulation sequence). At $t = 2.4s$, the co-simulation sequence is switched because a private state event in subsystem 2 is predicted. The sequence is switched again at $t = 3.55s$ and at $t = 4.75s$.

Figure 6: Co-simulation vs. mono-simulation for the test case extended to both subsystems capable of performing private state events. The graphic shows only the state variables describing the positions $x_1$ and $x_2$ of the two masses. Macro-step $\Delta T = 0.05s$.

5.2 Parallel Co-simulation

Due to real-time requirements, in many applications it is preferable to simulate the two subsystems in parallel. In dynamical systems without discontinuities, the simple procedure is:

1. Extrapolate both subsystems in parallel
2. Simulate both subsystems in parallel

This strategy is less time-consuming, but even less precise.

It is not possible to extend the proposed algorithm to work in parallel for all iterations, but with a similar approach as in 5.1, it can be predicted if any kind of discontinuity is likely to occur within the next macro-step. If it is stated that no event will occur, we can switch to parallel co-simulation for the next macro-step.

6 CONCLUSION

In this work, an approach for handling discontinuities in sequential non-iterative co-simulation was addressed. Currently, most of the co-simulation platforms focus on continuous dynamic systems and experience various problems if abrupt changes in the state variables occur. Thus, the developed algorithm aims to administrate the communication between two subsystems in order to handle discontinuities properly. It was stated in the paper that first of all, the co-simulation sequence is crucial, i.e. which of the two subsystems is to be simulated first. During the simulation of the first subsystem, the simulation has to be
stopped as soon as an event occurs and the event must be communicated to the second subsystem. In order to apply the proposed algorithm, slight changes to the Functional Mock-Up Interface are demanded, but the non-iterative character of the co-simulation platform will be preserved. Finally, it was shown with a simple simulation example that, provided suitable settings, the approach leads to accurate simulation results.

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