Meaning of Cause-and-effect Relations of the Topological Functioning Model in the UML Analysis Model

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Abstract: Topological Functioning Model specifies functional and structural characteristics of a system in the holistic manner. Cause-and-effect relations link cause and effect functional characteristics of the system, illustrating causality in it. The Unified Modelling Language (UML) provides its own relationship kinds among elements. Traditionally, a use of UML relationships depends on analyst’s experience in UML and knowledge about the system. However, after TFM transformation meaning of cause-and-effect relations in UML model is not always clear. The paper summarizes research results on this matter and provides mapping guidelines from TFM causal relations to often used UML relationships. These guidelines can be applied in further (manual or automated) refinement of UML diagrams.

1 INTRODUCTION

Principles of Model Driven Architecture (MDA) has opened a very interesting perspective of automated software model transformations from analysis models to code. In MDA terms analysis and design models are called platform independent and platform specific models correspondingly. There are plenty researches of code generation from platform specific models and transformations from platform independent to platform specific models. But the question about automated transformation of domain knowledge to the analysis/design model, i.e. from a computation independent model to a platform independent or platform specific one is still open.

According to (Miller and Mukerji, 2001), a computation independent model (CIM) represents a system in a form of domain models, business models, domain vocabulary, or system requirements. Usually, it is expressed as structured or unstructured text or semi-formal modelling languages (Singh and Sood, 2010; Siqueira and Silva, 2012) such as Unified Modelling Language (UML) and Business Process Model and Notation (BPMN) that could cover several or all viewpoints on the system, i.e. static, behavioural, and functional (Kriouile et al., 2013).

Speaking about dedication of the CIM to software development, one of its major goals is to bridge a real (business, problem) domain with its corresponding software solution. Achievement of this goal is difficult (but not impossible), since requires a use of formal languages or formal models instead of semiformal models and text at the very beginning of development. This goal could be achieved by using a Topological Functioning Model (TFM) that bridge the problem and solution domains via formalism provided by the algebraic topology and system theory, it is discussed in detail in (Osis et al., 2007a).

The TFM is a formal mathematical model that allows modelling and analysing functionality of the system (Osis and Asnina, 2011c). The system could be a business system, software, biological system, mechanical system, etc. The TFM represents its functionality as a digraph \((X, \Theta)\), where \(X\) is a set of inner functional characteristics (called functional features) of the system, and \(\Theta\) is a topology set on the characteristics in a form of a set of cause-and-effect relations. TFM models can be compared for similarities using continuous mapping mechanism (Asnina and Osis, 2010).

The open question is about transformation of cause-and-effect relations into associations between classes in analysis/design models, since as it is illustrated in (Osis and Asnina, 2011c; Donins et al.,
2011; Asnina et al., 2013) the causality semantics is of many forms that create two types of a flow, namely, a control flow and a data flow. The continuous mapping mechanism can drive discovering of structural relationships between domain objects.

This paper summarizes several research results and gives guidelines on transformation of cause-and-effect relations to control flows and structural relationships between domain objects modelled using UML types of relationships.

Section 2 describes the related work in CIM to PIM transformations. Section 3 discusses findings in transformation of cause-and-effect relation within Topological Functioning Modelling for MDA (TFM4MDA), TopUML and Integrated Domain Modelling (IDM) approaches, and provides mapping guidelines from TFM causal relations to UML relationships. At the end, conclusions and further directions for research are outlined.

2 RELATED WORK

The CIM can be presented in the form of Data Flow Diagram (DFD) and transformed to use case diagrams, activity diagrams, sequence diagrams and domain diagrams, which are the base for further obtaining of class diagrams (Kardoš and Drozdoňová, 2010). In this research, the transformation to behaviour diagrams allows correct mapping to control flows between activities, messages between objects, but a mapping to domain diagrams is incomplete. It allows defining concepts and navigations among them, but information about structural relationships and multiplicity must be added by the modeler.

The authors in (Kriouile et al., 2013) have investigated results of several research papers on CIM to PIM transformations. The presented results showed that transformation to class diagrams requires additional refinements, since usually after the transformation it provides “a first sketch of the system structure” and lacks such important details as class operations, multiplicities in associations, structural relation types as well as relations. The authors underline that the CIM must cover all three aspects of the system, namely, behavioural, functional and static. Their research of transformation from the BPMN model to use cases (Kriouile et al., 2015) to behavioural and domain classes models resulted in complete acquisition of control flows and message flows, however, the domain classes model contains only aggregation relationships obtained from the BPMN pools and lanes (Kriouile et al., 2014). The same source and target models are presented in (Bousetta et al., 2013), and the transformation to the domain classes model is supported by using of structural business rules that allow keeping knowledge about terms and facts, as well as relations among them. This allows getting necessary static knowledge such as names of classes, compositions and aggregations among them, generalization/specialization relationships, navigations, and multiplicity in associations in semi-automatic way. Additionally, the knowledge about a list or a set of some terms can be expressed as a constrain in Object Constraint Language (OCL). The business rules are presented using a subset of natural languages, thus trying to avoid ambiguity.

Authors in (Rhazali et al., 2015; Rhazali et al., 2016) transform CIM represented in form of use case and activity diagrams to the class diagram, where control flows of the activity diagrams are transformed to bidirectional navigations with many-to-many multiplicity in the class diagram. Further refinement requires human participation.

Transformation from BPMN diagrams to UML class diagrams and state diagrams for each class presented in (Mokrys, 2012) also requires additional participation of a modeler in order to refine relationships among classes.

Authors in (Kherraf et al., 2008) have proposed application of patterns to structure of a CIM and a set of four archetypes that drive generation of a PIM. In their approach, a CIM model consists of the business process model (manual and automated) and the requirements model that specifies activities that should be automated to support the business activities. The business process model contains also data objects. The requirements model is a model of use cases expressed by means of UML activity diagrams. A use case is transformed into a process component that is linked with various entity components. Links are bidirectional without any additional information but roles. The roles are presented as four archetypes: Moment-Interval that usually corresponds to a process component, and PPT (Party, Place, Thing), Role and Description that correspond to an entity component.

The authors in (Essebaa and Chantit, 2016) similarly to (Bousetta et al., 2013) formalize business rules and requirements that allow them getting constraints in OCL, but instead of a subset of a natural language they use SBVR (Semantic of Business Rules and Vocabulary) standard. The CIM consists of a use case model extended with data objects and business rules in SBVR. The static viewpoint of the PIM is represented by a class diagram, however elements in it are linked with bidirectional associations, and requires additional refinement.
Summarizing results of related work, the conclusion is that static viewpoint of the system represented as a [domain] class diagram in many approaches proposed is limited with relationships obtained from control flows at the CIM level. It is possible to derive aggregation and composition (from BPMN models), and (intuitive) bidirectional navigation between domain classes. More advanced characteristics such as a specific navigation, multiplicity and roles in associations as well as generalization/specialization must be added manually or explicitly defined in business rules specified in formalized natural language, i.e. by using a predefined subset of a natural language or in the form of SBVR statements.

3 MEANING OF CAUSE-AND-EFFECT RELATIONS

3.1 Topological Functioning Model

The TFM is a formal mathematical model that has been first introduced by Janis Osis in 1969 at Riga Technical University (RTU), Latvia (Osis, 1969). Several decades this model has been dedicated for mathematical specification of functionality of complex mechanical systems (Osis and Asnina, 2011c), but since 1990s it is being elaborated for software development (Solomencevs, 2016).

The TFM represents system functionality in a holistic manner as a CIM (Asnina and Osis, 2011). It describes the functional and structural aspects of the software system in the form of a directed graph \((X, Q)\), where a set of vertices \(X\) depict functional characteristics of the system named in human understandable language, while \(Q\) is a set of edges that depict causal relations (topology) between them. Such specification is more perceived, precise and clearer than the large textual descriptions. The TFM is characterized by the topological and functioning properties (Osis and Asnina, 2011b). The topological properties are connectedness, neighbourhood, closure, and continuous mapping. The functioning properties are cause-and-effect relations, cycle structure, inputs, and outputs. The composition of the TFM is presented in (Osis and Asnina, 2011c).

Rules of composition and derivation processes within TFM4MDA from the textual system description is provided by examples and described in detail in (Asnina 2006b; Osis et al. 2007b; Osis et al. 2008). The TFM can also be generated automatically from the business use case descriptions, which can be specified in the IDM toolset (Šlihte and Osis, 2014). It also can be manually created in the TFM Editor from the IDM toolset.

Speaking about TFM element, a functional feature represents some system’s functional characteristic, e.g., a business process, a task, an action, or an activity (Osis and Asnina, 2011b). It can be specified by a unique tuple (1) (Osis and Asnina, 2011c).

\(<A, R, O, PrCond, PostCond, Pr, Ex>\)  \( (1)\)

Where (1):
- \(A\) is object’s action,
- \(R\) is a set of results of the object’s action (it is an optional element),
- \(O\) is an object that gets the result of the action or a set of objects that are used in this action,
- \(PrCond\) is a set of preconditions or atomic business rules,
- \(PostCond\) is a set of post-conditions or atomic business rules,
- \(Pr\) is a set of features providers, i.e. entities (systems or sub-systems) which provide or suggest an action with a set of certain objects,
- \(Ex\) is a set of executors (direct performers) of the functional feature, i.e. a set of entities (systems or sub-systems) which enact a concrete action.

The cause-and-effect relations between functional features define the cause from which the triggering of the effect occurs.

The formal definition of the cause-and-effect relations and their combinations are given in (Asnina and Ovchinnikova, 2015). It states that a cause-and-effect relation is a binary relationship that links a cause functional feature to an effect functional feature. In fact, this relation indicates control flow transition in the system (Figure 1).

Figure 1: The execution of the functional feature instance (Nazaruka et al., 2016).

The cause-and-effect relations (and their combinations) may be joined by the logical operators, namely, conjunction (AND), disjunction (OR).
(OR), or exclusive disjunction (XOR). The logical relation denotes system execution behaviour (e.g., decision making, parallel or sequential actions).

The TFM can be manually (but according to the precise rules) transformed into most used UML diagram types: use cases (Osis and Asnina, 2011a) and others (Donins et al., 2011).

3.2 Cause-and-Effect Relations in TFM4MDA, TopUML and IDM

The TFM4MDA has been developed as an approach for computation independent modelling within the MDA. The main idea is that the TFM can serve as a foundation for domain knowledge modelling, software requirements verification according to them, and identification of a use case model and a conceptual class diagram (Osis et al., 2008).

The TFM4MDA gives a set of characteristics of a cause-and-effect relation (Asnina et al., 2013; Asnina & Osis 2010): time dimension, causal connections allow exceptions in operation, sufficiency and necessity for generation of effects, a series of parallel or serial factors involved, and the universality.

During transformation from the TFM to a use case model, cause-and-effect relations of the TFM are transformed to control flows between activities in UML activity diagrams that serve as use case specifications (Osis and Asnina, 2011a).

The TFM4MDA provides also transformation to a conceptual class diagram. However, the conceptual diagram holds relations between classes, but it is assumed to be bidirectional. In order to make these relations more accurate, the topological graph can be transformed into a sketch (a special form of representation for Universal Categorical Logic (Diskin et al., 2000)), then refined, and represented as a refined conceptual class diagram.

Such transformation also indicates possible inheritance relations among types and common operations, which can be further transformed into interface classes (Osis nd Asnina, 2008). The underlying logic is discussed in (Asnina, 2006a), where it is stated that while refining simplified functional features of the topological functioning model \( G(X, \Theta) \) to the specialized ones of the \( G^*(X^*, \Theta^*) \) the following significant case can occur: “If a functional feature \( x_i \) of the \( G(X, \Theta) \) is continuously mapped onto functional features \( x_1^*, \ldots, x_n^* \) of the \( G^*(X^*, \Theta^*) \), they specify the same action over objects of different types and do not have cause-and-effect relations between them, then this case indicates a possible inheritance relation between an object of the \( x_i \) and objects of the specialized functional features \( x_1^*, \ldots, x_n^* \).

For example, if there is a part of the TFM for some actions on the report (Figure 2) that has a functional feature 2 “Generate a report” with action “generate” on an object of type “Report”. During modelling, functional feature 2 is continuously mapped onto both functional features 2.1 “Generate a UserReport” and 2.2. “Generate a AdminReport” in the refined TFM (Figure 3). Feature 2.1 and 2.2 do not have cause-and-effect relations among them. Therefore, it could be assumed that types UserReport and AdminReport are subtypes of the type Report.

![Figure 2: The TFM for modelling some actions on reports.](image)

![Figure 3: The refined TFM for modelling some actions on reports.](image)

Otherwise, if there are functional features \( x_{21}, \ldots, x_{2n} \) of the \( G(X, \Theta) \) which specify the same action over objects of different types and may have cause-and-effect relations between them, then this case indicates a possible interface class that can be realized by objects of these types. For example, if only the TFM in Figure 3 exists, then objects of types UserReport and AdminReport could realize the same interface class with operation generate().

In the TFM4MDA, the decision about other structural relations (aggregations, dependencies, directed associations) among object classes must be made by an analyst in accordance with the problem domain description and some additional analysis. The sketch approach that implements the Universal Categorical Logic can serve as a formal background for that decision making. For example, in case of the TFM defined in two levels of abstraction (Figure 2 and Figure 3), the produced class diagram would look like in Figure 4.

The Topological UML (TopUML) is a language that extends UML metamodel with the concept of a
topological relation and a topological functioning model, and modifies a use case diagram and a class diagram to the topological use case diagram and topological class diagram correspondingly. The TopUML approach explicates the idea of getting behavioural and structural diagrams from the TFM and uses TopUML language for modelling the system in the prescribed order (Donins, 2012).

In contrast with the TFM4MDA, the TopUML considers that cause-and-effect relations in the TFM are not equal to associations in the UML class diagram (Table 1). The TopUML extracts a topological relation as a separate type of relations between UML constructs (Donins et al., 2011; Donins et al., 2012). Table 1 summarizes how topological relations are defined in TopUML diagrams in comparison with the UML diagrams as it is stated in (Donins, 2012). It approves the statement made in the TFM4MDA that a topological relation should be mapped to the control flow (a control flow, a message, and a transition) when analyse behaviour of the system. The topological relation in the use case diagram indicates the direction in which triggering occurs. The unclear is how to define meaning of the topological relation in the class diagram.

Let us consider definitions of the topological relationship and operation stated in (Donins, 2012):

- The topological relationship is “a binary relationship that shows a cause-and-effect relation between two elements – the source element and the target element. A topological relationship is assertion that indicates that the effect element can be triggered only by the cause element thus showing that effect element is executed only after the cause element executes”.

- Topological operation is a “behavioural feature of classifier that specifies the name, type, parameters, and constraints for invoking an associated behaviour, and related functional features and topological relationships for specifying cause-and-effect relations within system, thus allowing cause-and-effect relations to be modelled within the system by means of behavioural”.

Table 1: Cause-and-effect relations in UML and TopUML.

<table>
<thead>
<tr>
<th>TopUML Diagram</th>
<th>Extension to UML Diagrams</th>
</tr>
</thead>
<tbody>
<tr>
<td>Topological class diagram</td>
<td>Topological relationship is introduced for modelling cause-and-effect relations between classes</td>
</tr>
<tr>
<td>Activity diagram</td>
<td>Topological relationship is mapped to the control flow from one node to another</td>
</tr>
<tr>
<td>Topological use case diagram</td>
<td>Topological relationship is introduced to show “formally defined communication between a use case and an actor, showing who is triggering the communication” (Donins, 2012)</td>
</tr>
<tr>
<td>State diagram</td>
<td>Topological relationship is mapped to the transition relationship between states</td>
</tr>
<tr>
<td>Sequence diagram</td>
<td>Topological relationship is mapped to a message sending from one lifeline to another</td>
</tr>
<tr>
<td>Communication diagram</td>
<td>Topological relationship is mapped to a message sending from one lifeline to another (the same construct as in the sequence diagram)</td>
</tr>
<tr>
<td>Interaction overview diagram</td>
<td>Topological relationship is mapped either to the control flow or to the message between lifelines</td>
</tr>
<tr>
<td>Timing diagram</td>
<td>Topological relationship is mapped to the message sent between lifelines that cause changes in their states or conditions</td>
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</table>

Integrated Domain Modelling (IDM) is an approach that explicates the TFM4MDA and TopUML approaches (Šlihte and Osis, 2014). The main idea is to generate the TFM from structured text fragments, i.e. textual use case specifications, and validate knowledge obtained from use cases against domain ontology (Fernández Céspedes et al., 2015). Ontology must represent declarative domain knowledge in the form suitable for computer processing.

The IDM also provides guidelines for transformation from the TFM to the UML class diagram, however, this approach avoid defining any kind of relationships between classes (Solomencevs and Osis, 2015).
### 3.3 Mappings from Cause-and-effect Relations to UML Relationships

Summarizing results from all the three approaches, namely, TFM4MDA, TopUML and IDM, the following guidelines for determination of meanings of cause-and-effect relations in UML diagrams can be stated.

**UML behavioural diagrams (the behavioural view on the system):**
- Activity Diagram – a direct mapping to the control flow as it is defined in the TopUML;
- State Diagram – a direct mapping to the transition relationships as it is defined in the TopUML;
- Sequence Diagram – a direct mapping to the messages between lifelines as it is defined in the TopUML;
- Communication Diagram – a direct mapping to the messages between lifelines as it is defined in the TopUML;
- Interaction Overview Diagram – a direct mapping to the messages between lifelines or to the control flow as it is defined in the TopUML;
- Timing Diagram – a direct mapping to the message sent between lifelines that causes changes in their states or conditions as it is defined in the TopUML;

**Use case diagram** (in some approaches it is considered as the functional view on the system): here the topological use case model can serve as an intermediate model or transformation step that could help in determining a direction of communication between an actor and a use case as well as to identification of extensions and inclusions.

The transformation from the TFM in Figure 2 to the first four behavioural diagrams is illustrated in Figure 5. Fragments in ellipses show how a cause-and-effect relation from functional feature 2 “Generate a report” to functional feature 3 “Show a report” (part a) is transformed to the control flow between activities “Generate a report” and “Show a report” in the activity diagram (part b); to the transition relationship between two states of the object Report, namely, “generate” and “show” (part c); to the messages between lifelines calendar:Calendar and report:Report in the communication diagram (part d) and in the sequence diagram (part e).

**The UML class diagram** (the structural view on the system):
- Generalization/Specialization – a structural relationship that can be defined in case if there is a set of specialized functional features, which actions specify the same action over objects of different types as a functional feature at the higher level of abstraction does for its object and they do not have cause-and-effect relations between themselves (as it is stated in the TFM4MDA). The illustrating example was discussed in Section 3.2.

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![Figure 5: Transformation from the TFM to the activity, state, sequence and communication diagrams.](image-url)
Realization between classes and interfaces – it comes from the determination of generalization/specialization. If several functional features at the same level of abstraction have the same action for different types of objects, then this action can be extracted to the interface class. However, if these functional features are continuously mapped to the functional feature at the higher level of abstraction, then this indicates rather on different implementations of the superclass operation (the refined guideline stated in the TFM4MDA).

Navigation and Association – a kind of behavioural relationship that can be obtained from the analysis of directions of cause-and-effect relations among functional features with the object of the concrete type and functional features with the objects of other types: in case if all cause-and-effect relations among the mentioned functional features have the same direction, this indicates the navigation; otherwise, it is the association. This statement is based on the results that come from the TopUML, namely, these two relationships indicates on calls of the operations which in case of sequence and communication diagrams are direct mappings from the cause-and-effect diagrams to the messages between object lifelines.

Roles – a characteristic that may come either from the domain knowledge or be just automatically created based on the domain object type (class name) and some automatic incremental number generator.

Aggregation and Composition – a structural relationship that should be obtained from the domain knowledge (as further elaboration of the idea proposed in the IDM).

Dependency – a kind of behavioural relationship for event-driven system, where an event is a special case of action. Thus, “event” is a characteristic of the action that may come from the domain knowledge (as further elaboration of the idea proposed in the IDM).

Multiplicity – a characteristics that should be obtained from the domain knowledge (as further elaboration of the idea proposed in the IDM).

In case of realization of interfaces, determination of navigations, associations and, partially, roles, the necessary knowledge can be obtained from the TFM as illustrated in Figure 6.

Here we have two object types UserReport and AdminReport (part a) that are transformed to two classes with the same names (part b). Functional features 3 and 7 of the TFM are feature sets that holds functionality for both these objects. Therefore, it is possible to extract this functionality to the interface class with operations `generate()`, `show()`, `print()`. However, operation `refresh()` can be assigned only to AdminReport. Certainly, further analysis can lead to including this operation to the same interface class.

Bold arrows denote directed cause-and-effect relations between classes. Their direction is applied to associations by indicating navigable ends of them, i.e. in case of topological relationship from Calendar to UserReport it is possible to map it to a navigation from Calendar to UserReport. In the presented example (Figure 6, part b) roles are generated from the names of classes related to each other by association or navigation.

**Figure 6:** The UML class diagram (b) obtained from the TFM (a).
Other structural characteristics of relationships between domain objects, i.e. aggregation, composition, multiplicity and dependencies, are pure declarative knowledge. Therefore, the idea of keeping them in domain ontology that could be proceeded during transformation is very promising.

Summarizing, the abovementioned mappings illustrate that it is possible to get most of the often-used types of UML relationships when transforming from the TFM to the analysis model. In case of structural relationships and characteristics of objects or actions, the declarative knowledge on the domain should be used. This knowledge can be represented as ontology according to the idea provided in the IDM.

4 CONCLUSIONS

The overview of the related work showed that in many proposed approaches the transformation to the behavioural diagrams is mostly successful, however structural diagrams are limited with the aggregation and composition obtained from the BPMN model for several data objects (mainly representing pools and lanes within it), and intuitive associations between domain classes. Other relationships that represent generalization/specialization, specific navigations, multiplicities and roles must be added manually or predefined in business rules.

The overview of three approaches, namely, TFM4MDA, TopUML and IDM, that make transformations to and from the TFM showed that there is the same weakness regarding to structural diagrams. Generalizations/specializations between classes and realizations between classes and interfaces can be generated after analysis of TFM abstraction levels. Besides that, transformation from the TFM to the class diagram suggests keeping the cause-and-effect relations between classes. Thus, navigations and associations could be obtained by analysis of directions of cause-and-effect relations. To get other structural information, there is a necessity to hold declarative knowledge about the domain in some computational format, e.g. ontology. The ontology should be useful for automated generation of aggregations, compositions, dependencies, multiplicities as well as roles that depend on the context.

The future research is dedicated to implementation and validation of automation of the proposed guidelines and domain ontology to get the more complete class diagram that should be in conformity to other (behavioural) diagrams of the system under consideration.

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