Extraction of Conservative Rules for Translation Initiation Site Prediction using Formal Concept Analysis

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Abstract: The search for conservative features that define the translation and transcription processes used by cells to interpret and express their genetic information is one of the great challenges in the molecular biology. Each transcribed mRNA sequence has only one part translated into proteins, called Coding Sequence. The detection of this region is what motivates the search for conservative characteristics in an mRNA sequence. In eukaryotes, this region usually begins with the first occurrence of the sequence of three nucleotides, being Adenine, Uracil and Guanine, the nucleotide set that it is called Translation Initiation Site. One way to look for conservative rules that define this region is to use the formal concept analysis that can have implications that indicate a coexistence between the positions of the sequence with the presence of the translation start site. This paper analyzes the use of this technique to extract conservative rules to predict the translation initiation site in eukaryotes.

1 INTRODUCTION

The use of computational techniques for the molecular biology analysis information has contributed significantly to the area of bioinformatics. Among the main processes that have received attention are those of translation and transcription, which are mechanisms used by cells to interpret and express their genetic information (Tzanis et al., 2007). The entire mRNA sequence transcribed only a part called Coding Sequence (CDS) is translated into proteins. One of the main problems of molecular biology corresponds to the search for conservative characteristics in an mRNA sequence that allows the detection of a CDS region. In eukaryotes, this region usually starts at a AU/G (sequence of 3 nucleotides Adenine (A), Uracil (U) and Guanine (G)), with a nucleotide set that we call Translation Initiation Site (TIS).

The extraction of conservative characteristics can be done by exploiting dependencies in sequences containing TIS. In this paper, it will be considered the Formal Concept Analysis (FCA), which is a mathematical technique introduced in the early 1980s by Rudolf Wille (Wille, 1982). The FCA has been applied in different areas of knowledge (Poelmans et al., 2010; Poelmans et al., 2013; Kuznetsov and Poelmans, 2013). The application of the FCA depends on the construction of the formal context to represent a specific problem. From this context, it is possible to apply a specific algorithm for the extraction of knowledge from formal concepts it is possible to obtain rules of implication (commonly called implications), which are rules indicative of a relation between subsets of attributes related to objects. In this work, the formal context is constructed from the mRNA sequences, where the objects are the sequences themselves and each position is transformed into a multi-valued attribute of 4 positions: Adenine (A), Uracil (U), Cytosine (C) or Guanine (G). The extracted implication rules are given in the form \( Y \rightarrow Z \), where \( Y \) and \( Z \) attribute subsets, when its found the subset \( Y \) it has \( Z \) with confidence of 100%. In this way, could achieve new conservative characteristics that determine the TIS, besides those found by (Kozak, 1984).

The purpose of this article is to verify if the conservative characteristics obtained from implications extracted using FCA can improve the prediction of TIS using the Support Vector Machine (SVM) classi-
This paper is organized as follows: Section 2 gives a brief introduction to the formal concept analysis. In section 3 a review about related work is presented. Section 4 presents the description of the methodology and the experiments carried out. Finally, discussion of results obtained is showed.

2 FORMAL CONCEPT ANALYSIS

This section presents the main concepts of formal concept analysis (FCA). The notation and terminology are based on the formulations of Ganter and Wille (Ganter and Wille, 1999).

2.1 Formal Context

**Definition 1.** A formal context consists of two sets and a binary relation between them. Generally speaking, a formal context is a triple \((G, M, I)\) where \(I \subseteq G \times M\), the elements of the set \(G\) are called objects, the elements of the set \(M\) calls for attributes and \(I\) called incidence relation. In other words \((g, m) \in I\) or simply \(gIm\) should be read as "object \(g\) contains attribute \(m\)".

Table 1 shows an example of formal context. Each row of the table represents a sequence (TIS or non-TIS), the columns represent the positions of the sequence, and each position can assume one of the four nucleotides \(A, C, G\) or \(U\), each marking \((X)\) indicates if there is a nucleotide in that position. To demonstrate the nucleotide present in a multivalued position is used the notation \(P.N\), where \(P\) is sequence’s position and \(N\) is the nucleotide’s identifier.

**Definition 2.** Given a set \(B \subseteq G\), of objects of a formal context \((G, M, I)\), we can identify which attributes of \(M\) are common to all objects of \(B\). Similarly, that can be identified for a set \(D \subseteq M\), which are the objects of \(G\) that have the attributes of \(D\). These questions are answered by the derivation operators, defined by Equations 1 and 2.

\[
B' = \{ m \in M \mid \forall g \in B\} \quad (1)
\]

\[
D' = \{ g \in G \mid \forall m \in D\} \quad (2)
\]

2.2 Formal Concepts

The formal concepts obtainable from a formal context \((G, M, I)\) are ordered pairs \((B, D)\), where \(B \subseteq G\) and \(D \subseteq M\). Each object in \(B\) has all the attributes in \(D\) and each attribute in \(D\) is the attribute of all objects in \(B\). In other words, \((B, D)\) is a formal concept if and only if \(B' = D\) and \(D' = B\). The sets \(B\) and \(D\) are denominated extension and intention of the concept, respectively.

**Example 1.** Following the formal context of Table 1, it can be made the formal concept \((2, 3, 4, -9.G, -8.C)\) where the elements of the subset \(D\) are \{-9.G, -8.C\}. Hence, by derivation (Equation 2), \(B = 2,3,4\) represents the subset of the sequences having as characteristics the nucleotide \(G\) in the position 9 and the nucleotide \(C\) in the position 8. It should be noted that the formal concept corresponds to any aspect within the domain of the problem, represented by attributes and objects, where there may be an understanding or a comprehension.

2.3 Concept Lattice

When the set of all formal concepts of a formal context is hierarchically ordered, it receives the denomination of concept lattice. Its formal concepts are related as \((A1,B1) \leq (B2,D2)\), when \(B1 \subseteq B2\) and \(D2 \subseteq D1\), where \(B1, D1\) is called subconcept and \(B2, D2\) is called superconcept.

Figure 1 shows the diagram of the concept lattice obtained from the TIS prediction problem (presented in a simplified way in the table 1). We can observe that all object that has the attributes -7.G and -6.G also has -8.C and -9.G.

While a formal context is represented by a table, such as the Table 1, a concept lattice is represented by a diagram shown as a graph, where each vertex is a formal concept and the edge shows its relations \((B1, D1) \leq (B2, D2)\). When two concepts relate as subconcept and superconcept without any other formal concept between them, their vertices must be connected by an edge in the diagram. The highest vertex of the diagram represents the formal concept whose extension contains all objects, while the lowest vertex contains all the attributes in its intention.
Table 1: Example of a formal context.

<table>
<thead>
<tr>
<th>Sequences</th>
<th>Position of nucleotides in sequence</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>-9</td>
</tr>
<tr>
<td></td>
<td>A       U     C     G</td>
</tr>
<tr>
<td>1</td>
<td>X       X     X     ...</td>
</tr>
<tr>
<td>2</td>
<td>.       .     X     X</td>
</tr>
<tr>
<td>3</td>
<td>.       .     X     X</td>
</tr>
<tr>
<td>4</td>
<td>.       .     X     X</td>
</tr>
<tr>
<td></td>
<td>-8</td>
</tr>
<tr>
<td></td>
<td>A       U     C     G</td>
</tr>
<tr>
<td></td>
<td>...     X     X     ...</td>
</tr>
<tr>
<td></td>
<td>TIS     ...     ...</td>
</tr>
<tr>
<td></td>
<td>1083    A       U     C     G</td>
</tr>
<tr>
<td></td>
<td>...     X     X     ...</td>
</tr>
</tbody>
</table>

2.4 Implication Rules

Definition 3. In a formal context whose set of attributes is $M$, one implication is an expression $P \rightarrow Q$, where $P, Q \subseteq M$.

An implication $P \rightarrow Q$, extracted from a formal context, must be such that $P' \subseteq Q'$. In other words, every object that has the attributes of $P$ has the attributes of $Q$.

Example 2. An example of an implication rule is given by $\{−4, C, −3, A, 4, G\} \rightarrow \{1, A, 2, U, 3, G\}$, whose premise is formed by the set of attributes $\{−4, C, −3, A, 4, G\}$ indicating that in positions $−4$, $−3$ and $4$ we have the nucleotides $C$, $A$ and $G$, respectively. The conclusion is represented by the set of attributes $\{1, A, 2, U, 3, G\}$ indicating the TIS. From the example we can infer that when this premise is found in the mRNA sequence we have the TIS, with a confidence rate of $100\%$.

3 RELATED WORKS

In (Curé et al., 2015), the authors used an approach based on FCA and on semantic query expansion to determine diseases from their symptoms. The approach proved to be efficient for the detection of diseases with greater sensitivity and support especially for cases of presence or absence of obesity.

The use of FCA was also addressed by (Hristoskovski et al., 2014) as a cluster analysis technique, derived from several sets of genetic microarrays. These data sets were initially divided into groups that have characteristics related to a predefined criterion. As result, the FCA proved to be a robust data integration technique capable of producing a good and representative grouping solution for the entire set of genetic expression matrices. In addition, the use of FCA enabled a subsequent analysis of the data, providing useful information about the biological role of genes contained in the same concepts of the FCA.

The biggest problem of mining of numeric data using FCA is caused by binarization of data. This can cause a loss of information or produce a large volume of data, difficult to process. In (Kaytoue et al., 2011), the authors studied two methods based on FCA for the mining of numerical data in contexts of genetic data expressions. The first uses interordial scaling, encoding all possible attribute ranges in a formal context without losing information, but ends up producing a large and dense volume of data. The second constructs a concept lattice directly from the original data. The author shown that the two methods are equivalent, but the second method was shown to be computationally more efficient.

After an exhaustive search, it was not possible to find papers using FCA in the biological domain considered in this work. Thus, we intend to show that this theory can be used to improve the performance of methods and techniques in the context of TIS prediction.

4 MATERIALS AND METHODS

4.1 Materials

The used databases in our experiments were extracted from the NCBI RefSeq (Pruitt and Maglott, 2001) repository on April 22, 2014. The extracted data refer to four organisms Rattus Norvegicus (1383 molecules), Mus musculus (1097 molecules), Homo sapiens (21528 molecules) and Drosophila melanogaster (27764 molecules).

In this work, each molecule is identified according to the level of inspection, and classified as: Model, Inferred, Predicted, Provisional, Reviewed, Validated and WGS. In this work only mRNA molecules with inspection level reviewed were used. Table 2 shows the sequence amount for each species. Positive sequences are those that synthesize proteins (TIS) and the negative sequences do not synthesize proteins (Non-TIS).

<table>
<thead>
<tr>
<th></th>
<th>Positives</th>
<th>Negatives</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rattus Norvegicus</td>
<td>66</td>
<td>101</td>
<td>167</td>
</tr>
<tr>
<td>Mus musculus</td>
<td>398</td>
<td>632</td>
<td>1030</td>
</tr>
<tr>
<td>Homo sapiens</td>
<td>9716</td>
<td>16085</td>
<td>25801</td>
</tr>
<tr>
<td>Drosophila melanogaster</td>
<td>10122</td>
<td>25725</td>
<td>35847</td>
</tr>
</tbody>
</table>
4.2 Window Size Definition

The size of the nucleotide sequence used in training has a direct influence on the quality of the prediction model (Silva et al., 2011; LIU and WONG, 2003). Extraction windows can be symmetric, with the same number of nucleotides in the upstream regions (region of the sequence before TIS) and downstream (region after of TIS), or asymmetric, with a number other than nucleotides for each region. Preliminary studies indicate that asymmetric-sized windows provide greater accuracy (Silva et al., 2011). We will adopt asymmetric windows in this work being the region upstream with the lowest number of nucleotides.

For the definition of the nucleotide number of the upstream region, we use the ribosome scanning model and the Kozak’s consensus (Kozak, 1984), that identifies a conservative pattern at the −6, −5, −4, −3, −2, −1, 1, 2, 3, 4 positions with the sequence (GCC[A or G]CCAUGG), where predominance of the nucleotides [A/G] and [G] in the positions of −3 and 4, respectively. A greater number of nucleotides in the upstream region was used by (Tzanis et al., 2007), where the conservation of the −7 position was also identified. For the experiments of this work, we adopted a window with 9 nucleotides in the upstream region, since the mRNA scanning model is done by codon and, besides that, we guarantee the conservative positions identified in other works.

For the downstream region, it was found in (Pinto et al., 2017) that the larger the region the greater the accuracy achieved by the SVM classifier, thus adopting the size of 1081 nucleotides in the downstream region, so that we can have a better fit in the classifier. For the extraction of the conservative rules, we used the 20 nucleotide downstream size to ease the computational time of extraction, due to the high computational cost of the algorithm used in rule extraction.

4.3 Extraction of Conservative Characteristics

In this work, we used the ‘Find Implications’ algorithm, proposed by (Carpineto et al., 1999). This algorithm allows to extract implications using formal concept analysis for the extraction of all rules. Given a formal concept (X, Y), and a concept lattice, the algorithm looks for implications of (X, Y) where there are implications P → Q, with P ∩ Q = Θ, R ⊆ Y, = Y − P, so that this implication can not be obtained from the concept (W, Z). This algorithm requires a large computational effort due to its complexity that is proportional to O(|C|k²|M| q), where C is the concept number, k is the largest number of attributes in the premise, M is the number of attributes and q is the largest number of relation per concept. Since the database was very large, causing a great computational effort, we divided the base into groups of 500 sequences and, in the end, we made an intersection between the implications generated for each analyzed organism.

Since the TIS attribute is common to all positive sequences, it was possible to observe rules where TIS is the conclusion of a certain premise as exemplified in the 2.4 section. After obtaining the implications of each organism, the common rules among all organisms were collected. This extraction was made through the intersection between the sets of rules acquired from each organism. We also consider that rules with support greater than or equal to 30%, within all bases, should be used as conservative characteristics to increase classifier performance (25% would be considered random since they are four nucleotides).

It were added characteristics as supporting vector $G$ in our base as binary values demonstrating the existence of that rule in the sequence. The vector $G$ is formed by Equation 3.

$$G(n) = \begin{cases} 1 & \text{if } V(n) == N(n) \\ 0 & \text{Otherwise} \end{cases} \quad (3)$$

where $V$ is a vector with the values of the sequence in the positions of the conservative characteristics found and $N$ is the vector with the values that each position must have according to the implications found.

4.4 Support Vector Machines Classifier

SVM is a machine learning technique capable of solving linear and non-linear classification problems. It separates examples using a linear decision surface and increasing the distance between training points (Silva et al., 2011).

The efficiency of SVM classifier depends on the proper selection of the parameters of the kernel function used and the smoothing parameter of the optimal hyperplane separation margin, represented by symbol $C$. In this work, the Gaussian RBF (Radial Basis Function) kernel function was used, which acts as a structural regulator. The RBF function is defined by the Equation 4 and its parameter is represented by the symbol $\gamma$.

$$K(x_i, x_j) = \exp(-\gamma ||x-x'||^2) \quad (4)$$

To define the parameters $C$ and $\gamma$, was used the ‘Grid Search’ method, implemented for the class lib-
SVM\(^1\). This method defines the best set of parameters through an exhaustive search within a predefined range of values for each of the parameters. The execution time of this tool can be prohibitive. To decrease this time, the grid search method was executed in a cluster, consisting of 12 machines\(^2\).

4.5 Evaluation Methods

The evaluation of the results was performed from the precision, sensitivity, and F-measure metrics. Precision evaluates among all the sequences classified as TIS those that are truly TIS (Equation 5).

\[
\text{Precision} = 100 \cdot \frac{TP}{TP + FP} \quad (5)
\]

The sensibility is relative to the hit rate in the positive class (TIS). It is also called rate of true positives (Equation 6).

\[
\text{Sensitivity} = 100 \cdot \frac{TP}{TP + FN} \quad (6)
\]

where TP, TN, FP and FN denote the number of True Positives, True Negatives, False Positives and False Negatives, respectively.

F-measure considers the precision and sensitivity metrics to evaluate the model, performing a harmonic average between the two metrics (Equation 7).

\[
F\text{−measure} = 2 \cdot \frac{\text{Precision} \cdot \text{Sensitivity}}{\text{Precision} + \text{Sensitivity}} \quad (7)
\]

For the validation of the proposed model, it was used the cross-validation (10-fold cross-validation) technique, which guarantees a statistical validation of the model. The procedure consists in subdividing the available dataset into ten folds of the same size, 9 of which folds are used for training and one fold for validation.

5 RESULTS

After determining the subset of implications of the intersection between the set of rules of each organism, the main rules for TIS prediction, in the range stipulated, were obtained (Table 3), while still retaining the characteristics demonstrated by Kozak. For example, the first line of Table 3 represents \(-8.C \rightarrow TIS\). This indicates that whenever there is a nucleotide C at the -8 position, the AUG begins the traduction. This occurs with a support of 34.3% of the base \(Rattus\; novergicus\) and 31.1% support when considering all species bases. The values of the brackets for each rule found in the positives sequences can be visualized in Figure 2.

It can be noted the predominance of the conservative Kozak characteristics in the \(-3\) positions, containing \(A\) or \(G\) and 4 containing \(G\), and \(T\) with the values of greater support among the bases analyzed. It is also observed 11 new conservative characteristics, besides those indicated by Kozak, among which the 9 position is a C nucleotide (with a support of 37%).

As for the negative sequences (Non-TIS), two conservative positions were identified: positions -2 and 4 with the presence of nucleotide A, with a support of 30.6% and 31.3%, respectively. This shows how negative sequences can be random and not follow a pattern, unlike positive sequences (TIS).

In preliminary tests, it was decided to add features with greater support within all the bases, positives and negatives, to value its main characteristics. Thus, the -3.A, -3.G, 4.G and 9.C, 1.C characteristics were added in the positives sequences and the -2.C and 4.C characteristics were added in the negatives sequences. However, in doing so, it was noted that there was an increase in noise in the data and an increase in classification error. Thus it was decided to add only the features that value the positive characteristics, shown in the Table 3.

Table 4 presents the parameters used for the SVM, obtained by ‘Grid search’ method.

The use of the implication rules found allowed a small increase in the metrics evaluated in this work (see Table 5). The biggest difference between the results with and without the characteristics happens in the organisms \(Mus\; musculus\) and \(Drosophila\; melanogaster\), where we see an increase around 1 %. This is due to the fact that in none of the rules found, the appearance of them in the negative sequence is greater than in the positive ones while this happens twice in the other bases. Even so, the organism \(Homo\)
Table 3: Implications rules extracted and their support.

<table>
<thead>
<tr>
<th>Pos</th>
<th>Neg</th>
<th>Pos</th>
<th>Neg</th>
<th>Pos</th>
<th>Neg</th>
<th>Pos</th>
<th>Neg</th>
</tr>
</thead>
<tbody>
<tr>
<td>-8</td>
<td>C</td>
<td>34.3%</td>
<td>21.6%</td>
<td>28.5%</td>
<td>22.3%</td>
<td>29.1%</td>
<td>26.7%</td>
</tr>
<tr>
<td>-7</td>
<td>C</td>
<td>35.8%</td>
<td>27.5%</td>
<td>29.7%</td>
<td>21.1%</td>
<td>30.6%</td>
<td>25.7%</td>
</tr>
<tr>
<td>-6</td>
<td>G</td>
<td>37.3%</td>
<td>17.6%</td>
<td>40.8%</td>
<td>31.3%</td>
<td>33.6%</td>
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</tr>
<tr>
<td>-5</td>
<td>C</td>
<td>23.9%</td>
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<td>31.3%</td>
<td>25.4%</td>
</tr>
<tr>
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<td>C</td>
<td>40.3%</td>
<td>18.6%</td>
<td>30.5%</td>
<td>25.4%</td>
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<td>24.8%</td>
</tr>
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<td>A</td>
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<td>23.5%</td>
<td>48.2%</td>
<td>26.9%</td>
<td>50.2%</td>
<td>25.4%</td>
</tr>
<tr>
<td>-2</td>
<td>G</td>
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<td>40.1%</td>
<td>25.7%</td>
<td>33.3%</td>
<td>28.3%</td>
</tr>
<tr>
<td>-1</td>
<td>C</td>
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<td>16.6%</td>
<td>42.5%</td>
<td>23.2%</td>
<td>40.5%</td>
<td>25.4%</td>
</tr>
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<td>C</td>
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<td>25.5%</td>
<td>46.9%</td>
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<td>50.2%</td>
<td>27.7%</td>
</tr>
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<td>1</td>
<td>G</td>
<td>52.2%</td>
<td>33.3%</td>
<td>45.0%</td>
<td>24.6%</td>
<td>53.7%</td>
<td>28.5%</td>
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<td>33.0%</td>
<td>24.6%</td>
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<td>3</td>
<td>C</td>
<td>31.3%</td>
<td>26.5%</td>
<td>33.2%</td>
<td>21.9%</td>
<td>35.3%</td>
<td>30.7%</td>
</tr>
<tr>
<td>4</td>
<td>G</td>
<td>26.9%</td>
<td>26.5%</td>
<td>38.2%</td>
<td>27.7%</td>
<td>34.5%</td>
<td>28.2%</td>
</tr>
<tr>
<td>5</td>
<td>A</td>
<td>29.8%</td>
<td>39.2%</td>
<td>28.2%</td>
<td>27.3%</td>
<td>20.6%</td>
<td>24.1%</td>
</tr>
<tr>
<td>6</td>
<td>C</td>
<td>42.2%</td>
<td>19.6%</td>
<td>37.5%</td>
<td>21.8%</td>
<td>35.6%</td>
<td>23.8%</td>
</tr>
<tr>
<td>7</td>
<td>A</td>
<td>34.3%</td>
<td>18.6%</td>
<td>33.9%</td>
<td>23.8%</td>
<td>20.9%</td>
<td>23.9%</td>
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<tr>
<td>8</td>
<td>G</td>
<td>35.8%</td>
<td>22.5%</td>
<td>34.7%</td>
<td>31.2%</td>
<td>29.3%</td>
<td>28.7%</td>
</tr>
<tr>
<td>9</td>
<td>A</td>
<td>32.9%</td>
<td>24.5%</td>
<td>31.7%</td>
<td>21.1%</td>
<td>24.6%</td>
<td>24.1%</td>
</tr>
<tr>
<td>10</td>
<td>A</td>
<td>32.8%</td>
<td>28.4%</td>
<td>30.6%</td>
<td>22.3%</td>
<td>24.6%</td>
<td>23.1%</td>
</tr>
</tbody>
</table>

sapiens had a small increase, while the Rattus norve-
gicus organism they continued with the same values, because of its low amount of data.

6 CONCLUSIONS

In this work it was proposed the extraction of conserva-
tive mRNA characteristics from eukaryotes organ-
isms to improve the prediction of TIS, using formal concept analysis. Using a downstream region of 20 nucleotides and 9 nucleotides upstream, it was possible to find a total of 19 rules of implication, including the rules of Kozak. The results show shows that the addition of conservative characteristics, even using a small window, improves SVM results, although the increase is little in this work.

In future works, it would be important to test larger windows, both in the upstream and downstream regions for rule extraction. In this work, by computational limitation, we use only 20 nucleotides in the downstream region. But for this, it is necessary to implement more optimized versions of the algorithm in order to consider more characteristics.

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REFERENCES


