Large Scale Petrol Station Replenishment Problem with Time Windows: A Real Case Study

Pablo A. Villegas and Víctor M. Albornoz
Departamento de Industrias, Universidad Técnica Federico Santa María, Av. Santa María 6400, 7660251, Santiago, Chile

Keywords: Petrol Station Delivery Problem, Time Windows, Trip Packing, Scheduling, Heuristic.

Abstract: In this study we deal with a real case of the problem known as Petrol Station Replenishment Problem with Time Windows arising in Chile. The company involved is one of the biggest actors in the country, and every day must schedule a series of trips from their depots to their clients, delivering different kinds of fuel. This specific case has some differences from prior formulations of this problem (e.g. trucks works in shifts with hard time windows). Also, another challenge is the high number of orders and trucks involved in everyday planning. To solve this problem in reasonable computing times we propose a sequential insertion heuristic. Finally, we present results over a month of data.

1 INTRODUCTION

Oil companies have the duty to supply their clients (gas stations and industrial clients) with different kinds of fuel, that is why every day they are confronted with the challenge of arranging a schedule program for the next day. This work is motivated by the challenge that one of the biggest oil companies in Chile faces when dealing with this scheduling program.

The problem known as Petrol Station Replenishment Problem with Time Windows (Cornillier et al., 2008a; Cornillier et al., 2012) or PSRPTW, corresponds to a specific multi-compartment vehicle routing problem or MCVRP, which includes time windows constraints. This problem consists in assigning a series of products demanded by clients to available truck compartments and schedule their delivery time. Thus, trips must be defined and assigned to trucks considering time windows constraints.

In this case we deal with trucks that are without flow meters, thus, every truck compartment must be delivered to no more than one client. Also, trucks are able to make more than one trip during their work shift.

The contribution of this work comes in two aspects. First, we deal with a real case which has some slight differences over the ones previously worked, for instance, trucks works in shifts with defined time windows. Shift starting and ending times vary from truck to truck, different from prior formulations (Benantar and Ouafi, 2012; Cornillier et al., 2009; Cornillier et al., 2012; Surjandari et al., 2011) that considered either maximum work time or closing time windows at the depot. Here, the final objective is to maximize compliance with customer orders, following a certain priority, with a limited heterogeneous fleet. Also, costs do not change based on the lapsed time from the start of the first trip till the end of the last, as every trip has its own cost. Client priority could have been addressed by forcing orders fulfillment, however, orders may focus on a certain time lapse making it an infeasible problem, while posing this problem as the maximization of dispatched product by priority enable us to get the best possible solution, assuming the possibility that not every order will be delivered in the agreed time window. Our second contribution consists on a proposed heuristic for this specific case, which main feature is getting a relatively good operational solution in a short time frame, so that people in charge of scheduling can work over this proposal. This heuristic consist on an adapted version of the insertion heuristic proposed by (Solomon, 1987) for a vehicle routing or scheduling problem with time windows.

The view from the standpoint of compliance with customer brings a wider view than just minimizing costs, as there is value associated with each client that is not necessarily reflected by the net profit of a transaction. This is very important in the case of fuels, as the profit per transaction is relatively low, and the gain is in the quantity sold. Therefore, it may be important...
to give preference to a client making large quantities of orders.

The remainder of this paper is organized as follows. In Section 2, we address some relevant literature related to previous works dealing with this problem. In Section 3 we formally define the problem addressed in this work and introduce some assumptions and characteristics that have impact in our solution approach. In Section 4 we introduce the solution strategy, including our proposed heuristic. In Section 5 we present results obtained over a month of data on one of the company's depots. In Section 6 we provide some final conclusions and future research.

2 LITERATURE REVIEW

In this section we provide a brief overview of published literature concerning the Petrol Station Replenishment Problem (PSRP) over the last few decades.

(Brown and Graves, 1981) were the first to publish an article dealing with the PSRP. They were faced with a situation involving more than 80 depots and 300 tank trucks. The main features of the problem was that all the orders corresponded to full truckloads, so each trip could only reach one customer. To solve this case, they proposed an integer programming model to assign commands to different trucks, in order to minimize the amount of travel costs, establishing a penalty if the need for overtime or idle time existed.

(Brown et al., 1987) described a decision-making support system, where they focused on the possibility to add more than one customer per trip to their previous work. The distribution network involved was 120 tanks and 430 tanker trucks.

(Van der Bruggen et al., 1995) in a counseling process to a Netherlands company, proposed some simple models: assign customers to depots, determining fleet size and composition, and restructure the network of depots. The problem considered five depots, 20-30 tanker trucks and about 800 customers.

(Ronen, 1995) described some of the features present in the operating environment of this problem and presented three models that can be applied to it: The set partitioning model, the elastic set partitioning model, and the set packing model.

(Taqqa allah et al., 2000) addressed the problem dealing with one tank and a homogeneous tank truck fleet. They proposed four original heuristics, three of which visited one client by lap while the fourth allows more than one client in every trip, and stations can receive multiple visits. They showed results for cases up to 75 clients with different evaluation horizons.

(Malèpart et al., 2003) worked with the problem of supply over a time horizon of several business days. This problem stems from the notion that in some cases the fueling stations are managed by the company, so they can decide at their convenience which day they will be supplied. They proposed four heuristics to solve this problem.

(Avella et al., 2004) studied the case of one depot and heterogeneous tank truck fleet, where orders were integral multiples of \( m^3 \) and truck compartments leave either full or empty. They proposed a set partitioning formulation and developed a branch-and-price algorithm that could solve the problem up to 6 trucks and 25 customers. They also proposed a heuristic to select a promising set of columns.

(Ng et al., 2008) studied two distribution networks in Hong Kong. The resulting problem corresponds to a model of supply over several working days, as stations inventories were managed by the company. They proposed a model to assign trips to trucks and stations simultaneously. The model does not guarantee that the stations are not left without fuel. Between the two areas studied, the number of stations was 48 and had a fleet of 8 tank trucks.

(Cornillier et al., 2008a) worked with the problem of one depot and unlimited heterogeneous fleet. They proposed an exact algorithm and conducted a test with an instance of 42 stations and 8 types of vehicles. Same year, (Cornillier et al., 2008b) treated the multi-period case with limited heterogeneous fleet, where they proposed a multiple phase heuristic. They conducted tests for this heuristic with instances up to 200 customers and a 28 days planning horizon.

(Cornillier et al., 2009) proposed two heuristics for the case of limited heterogeneous fleet and customer time windows. To verify the performance of these heuristics, they used instances of up to 50 clients.

(Boctor et al., 2011) addressed the trip packing problem arising in the PSRP. They proposed a formulation for the generalized version of this problem and four heuristics to solve it.

(Surjandari et al., 2011) worked a real case with time windows, multi-depot, split-deliveries and a limited heterogeneous fleet of tank trucks. As a solution they proposed a tabu search algorithm. In their work they show results for that particular case, which had two depots and a fleet of 76 tank trucks.

(Benantar and Ouafi, 2012) discussed the case with time windows, one depot and a limited heterogeneous fleet. They presented an algorithm based on tabu search, solving instances of over 100 customers and 20 trucks.

(Cornillier et al., 2012) proposed a heuristic for
the multi-depot problem with time windows. This heuristic included the generation of all possible trips visiting less than three clients and then selecting the most promising one and solve the allocation problem. In their work they show results of instances up to 6 depots, 10 trucks and 50 customers.

(Wang et al., 2014) presented the results of a meta-heuristic called “guided reactive tabu search” applied to the problem of a single depot with heterogeneous fleet. They addressed instances up to 200 orders.

(Coelho and Laporte, 2015) defined and compared four categories of the single period multi-compartment vehicle routing problem. This problem is one of the possible variants that appears when addressing the PSRP. For each of the particular cases they proposed a mathematical model and a “branch-and-cut” algorithm that is applicable to all of them. Largest instances that could be solved accurately contained 50 clients in the single period case and 20 for the multi-period version.

To the best of our knowledge there has not been addressed a real case with instance sizes bigger than the ones presented in this work or time windows associated with truck shifts. The challenge is to get an acceptable solution (proposal) for planners in a reasonably short time, as they will work over this solution. To this effect, we followed the strategy used by (Cornillier et al., 2012) separating routes creation, their allocation to the various truck shifts and finally defining their schedule.

3 PROBLEM DEFINITION

The PSRPPTW used in this real case can be defined as follows. Let \( G = (\{0, n + 1\} \cup C, A) \) be a directed graph, where \( \{0, n + 1\} \) corresponds to the depot, \( C = \{1, ..., n\} \) is the set of clients, and \( A = \{(i, j) : i, j \in \{0, n + 1\} \cup C, i \neq j\} \) is the set of arcs. Every arc \( (i, j) \) has associated a travel time \( t_{ij} \). Also, service time \( s_i \) at depot or station \( i \), where \( i \in \{0, n + 1\} \cup C \), is known. The set of trucks associated to the depot is denoted by \( K \). Client \( i \) orders are composed of \( P_i \) order lines, where every line specifies a different kind of product and which type of compartment will be filled with that order, also, every order specifies an ideal time window. Trucks must get to the client \( i \) inside the proposed time window \([a_i, b_i]\). Furthermore, every truck must comply with their shift time window \([\alpha_x, \beta_x]\).

The real nature of the problem leads to many situations where theory differs from reality, so it is important to make a balance between which elements of reality we will model and those we will simplify through assumptions.

One of the most important simplifications of the model is present in the step of route generation. Clients are grouped by zones, so travel time is directly associated to the zone they are into. As a rule of thumb, routes visiting more than one client shall only visit clients inside the same zone. For this and some other restrictions, orders may be grouped in a way so that they will be assigned to one and just one possible route. Resulting routes will have just one kind of truck assigned (capacity related), letting us solve the problem for every truck type separately. Orders that do not comply to these rules are left outside this problem, as the compliance decision is in the schedulers’ hands. As an interesting fact, volume of discarded orders is often below 1% of total volume transported during a work day.

Next, other important assumptions are noted for this particular problem:

- Orders are composed of order lines, every client may generate orders lines till they fill a truck. This orders may contain more than one kind of product, but no more than one by compartment.
- Every client is free to generate more than one order. Every one of such is treated separately as they have their own requirements and time windows.
- Every order must be complied with just one trip.
- A route may include more than one client, but no more than two.
- Trucks may have more than one shift during the working day. As they are independent, they are treated as different trucks.
- There exists relevance associated to the priority of an order, this will be represented by constant \( p \).

4 SOLUTION STRATEGY

To solve this problem in reasonably low computing times, we have separated this problem in two phases, addressed separately:

- Phase I: Route generation
- Phase II: Route assignment & Scheduling

We have developed a heuristic which follows the same idea used by the sequential insertion heuristics proposed by (Solomon, 1987). It also shows some similarities with the construction heuristics proposed by (Boctor et al., 2011).

In addition to parameters already defined, the following notation will be used:


\begin{align*}
\text{Minimize:} & \quad \sum_{r \in V} d_r (2) \\
\text{Subject to:} & \quad \sum_{r \in V_k} x_{t,v} = 1, \quad \forall t \in T_k (3) \\
& \quad \sum_{t \in T_k} x_{t,v} = 1, \quad \forall v \in V_k (4) \\
& \quad \sum_{t \in T_k} \alpha_t x_{t,v} \leq d_v \leq \sum_{t \in T_k} \beta_t x_{t,v}, (5) \\
& \quad \forall v \in V_k \\
& \quad d_v \geq d_{v-1} + \sum_{r \in T_k} \lambda_{r,x_{r,v-1}}, (6) \\
& \quad \forall v \in V_k \mid v \neq 1 \\
& \quad d_k' \leq d_1 (7) \\
& \quad d_{n(v_i)} \leq \beta_k' - \sum_{r \in T_k} \lambda_{r,x_{r,n}(v_i)} (8) \\
& \quad x_{t,v} \in \{0, 1\}, \quad \forall t \in T_k, \forall v \in V_k (9) \\
& \quad d_v \in \mathbb{R}, \quad \forall v \in V_k (10)
\end{align*}

Objective function (2) minimizes starting times while privileging shorter trips before longer ones if possible, this function corresponds to a secondary optimization criteria. Restrictions of type (3) ensures that every route assigned to truck $k$ will be performed once. Type (4) restrictions states that every trip position will host one route, no more, no less. Restrictions of type (5) ensures that every route must comply their time window if they correspond to the $v$-th trip. Type (6) restrictions states that $v$-th trip starting time will occur after the end of the previous one. Restriction (7) ensures that the first trip must comply with truck’s starting time. Restriction (8) states that the last trip must finish before the ending time window of truck $k$. Finally, restrictions of type (9) and (10) show variables’ nature.

Our proposed sequential insertion heuristic can be expressed as follows:

For every truck:

1. Fill a list with the set of unassigned routes.
2. Sort routes in descending order by priority.
3. Filter routes by truck’s time window compatibility.

4. Assign a route from the list, which complies to a certain starting criteria, to the truck and extract it from the list.

5. For every element in the list:
   (a) Verify compatibility with current routes assigned. If verification is positive, then solve the scheduling problem including the current route. Else, move onto the next element of the list.
   (b) If scheduling problem is correctly solved, assign current route to the truck, extract it from the list and check for potential remaining routes. Else, move onto the next element of the list.
   (c) If there are potential routes, move onto the next element of the list. Else, move onto the next truck.

The process ends once we have been through every truck or all routes have been assigned.

5 RESULTS

We tested our heuristic against a month of real data. Each day presented different number of orders and trucks involved, so a wide variety of possibilities are covered. The route start criteria used was: any route that holds the highest priority on the list. As for the main parameters used, we set the maximum number of trips per shift to 4, and \( \rho(i) \) takes values from table 3.

Our heuristic was coded in AMPL language, using CPLEX 12.1, in a computer with O.S. Windows 8, Intel Core i5-4200U 1.6 - 2.3 GHz processor and 8 GB of RAM.

As shown in table 1, the objective function obtained by our heuristic (OF) outperforms the ones...
Table 2: Detailed Compliance Level.

<table>
<thead>
<tr>
<th>Day</th>
<th>NR</th>
<th>NT</th>
<th>T (sec)</th>
<th>C</th>
<th>CC</th>
<th>CC1</th>
<th>CCCL</th>
<th>CCCL1</th>
<th>CCT</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>195</td>
<td>142</td>
<td>44.9</td>
<td>97.9%</td>
<td>77.4%</td>
<td>79.0%</td>
<td>90.3%</td>
<td>92.8%</td>
<td>86.2%</td>
</tr>
<tr>
<td>2</td>
<td>207</td>
<td>97</td>
<td>42.6</td>
<td>89.9%</td>
<td>81.2%</td>
<td>86.0%</td>
<td>91.3%</td>
<td>98.1%</td>
<td>87.9%</td>
</tr>
<tr>
<td>3</td>
<td>47</td>
<td>50</td>
<td>5.8</td>
<td>87.2%</td>
<td>83.0%</td>
<td>85.1%</td>
<td>93.6%</td>
<td>95.7%</td>
<td>89.4%</td>
</tr>
<tr>
<td>4</td>
<td>272</td>
<td>142</td>
<td>67.6</td>
<td>93.4%</td>
<td>83.5%</td>
<td>87.1%</td>
<td>94.1%</td>
<td>92.8%</td>
<td>85.6%</td>
</tr>
<tr>
<td>5</td>
<td>238</td>
<td>150</td>
<td>50.0</td>
<td>97.1%</td>
<td>81.9%</td>
<td>84.9%</td>
<td>93.3%</td>
<td>96.6%</td>
<td>88.2%</td>
</tr>
<tr>
<td>6</td>
<td>294</td>
<td>158</td>
<td>51.7</td>
<td>99.2%</td>
<td>87.3%</td>
<td>91.5%</td>
<td>92.4%</td>
<td>96.6%</td>
<td>94.9%</td>
</tr>
<tr>
<td>7</td>
<td>297</td>
<td>156</td>
<td>86.8</td>
<td>98.0%</td>
<td>84.2%</td>
<td>84.8%</td>
<td>96.3%</td>
<td>97.3%</td>
<td>87.5%</td>
</tr>
<tr>
<td>8</td>
<td>260</td>
<td>111</td>
<td>59.2</td>
<td>98.1%</td>
<td>85.0%</td>
<td>88.1%</td>
<td>94.2%</td>
<td>98.8%</td>
<td>89.2%</td>
</tr>
<tr>
<td>9</td>
<td>62</td>
<td>47</td>
<td>7.8</td>
<td>72.6%</td>
<td>82.3%</td>
<td>87.1%</td>
<td>93.5%</td>
<td>98.4%</td>
<td>88.7%</td>
</tr>
<tr>
<td>10</td>
<td>279</td>
<td>150</td>
<td>86.8</td>
<td>93.9%</td>
<td>83.5%</td>
<td>86.4%</td>
<td>94.6%</td>
<td>98.3%</td>
<td>87.1%</td>
</tr>
<tr>
<td>11</td>
<td>286</td>
<td>154</td>
<td>77.2</td>
<td>99.3%</td>
<td>83.9%</td>
<td>87.8%</td>
<td>93.0%</td>
<td>96.9%</td>
<td>90.6%</td>
</tr>
<tr>
<td>12</td>
<td>299</td>
<td>156</td>
<td>99.6</td>
<td>97.3%</td>
<td>85.3%</td>
<td>87.0%</td>
<td>96.3%</td>
<td>98.3%</td>
<td>88.6%</td>
</tr>
<tr>
<td>13</td>
<td>268</td>
<td>154</td>
<td>98.8</td>
<td>99.3%</td>
<td>83.6%</td>
<td>84.3%</td>
<td>96.3%</td>
<td>97.4%</td>
<td>86.6%</td>
</tr>
<tr>
<td>14</td>
<td>312</td>
<td>157</td>
<td>100.6</td>
<td>98.4%</td>
<td>86.5%</td>
<td>88.1%</td>
<td>96.2%</td>
<td>98.1%</td>
<td>89.4%</td>
</tr>
<tr>
<td>15</td>
<td>261</td>
<td>111</td>
<td>53.3</td>
<td>98.1%</td>
<td>82.8%</td>
<td>85.4%</td>
<td>94.6%</td>
<td>97.7%</td>
<td>87.4%</td>
</tr>
<tr>
<td>16</td>
<td>58</td>
<td>48</td>
<td>7.3</td>
<td>77.6%</td>
<td>81.0%</td>
<td>86.2%</td>
<td>93.1%</td>
<td>98.3%</td>
<td>86.2%</td>
</tr>
<tr>
<td>17</td>
<td>287</td>
<td>141</td>
<td>78.8</td>
<td>94.8%</td>
<td>81.9%</td>
<td>89.2%</td>
<td>88.9%</td>
<td>93.8%</td>
<td>89.9%</td>
</tr>
<tr>
<td>18</td>
<td>273</td>
<td>148</td>
<td>60.6</td>
<td>96.7%</td>
<td>81.7%</td>
<td>87.9%</td>
<td>90.1%</td>
<td>96.3%</td>
<td>91.6%</td>
</tr>
<tr>
<td>19</td>
<td>318</td>
<td>152</td>
<td>101.5</td>
<td>93.7%</td>
<td>83.3%</td>
<td>87.4%</td>
<td>92.1%</td>
<td>96.2%</td>
<td>91.2%</td>
</tr>
<tr>
<td>20</td>
<td>190</td>
<td>148</td>
<td>37.3</td>
<td>100.0%</td>
<td>83.7%</td>
<td>85.8%</td>
<td>95.3%</td>
<td>97.4%</td>
<td>88.4%</td>
</tr>
<tr>
<td>21</td>
<td>255</td>
<td>155</td>
<td>58.7</td>
<td>99.2%</td>
<td>85.5%</td>
<td>86.7%</td>
<td>96.5%</td>
<td>98.0%</td>
<td>88.6%</td>
</tr>
<tr>
<td>22</td>
<td>251</td>
<td>112</td>
<td>39.7</td>
<td>96.8%</td>
<td>85.7%</td>
<td>90.4%</td>
<td>92.8%</td>
<td>99.2%</td>
<td>91.2%</td>
</tr>
<tr>
<td>23</td>
<td>58</td>
<td>53</td>
<td>8.5</td>
<td>96.6%</td>
<td>89.7%</td>
<td>91.4%</td>
<td>94.8%</td>
<td>96.6%</td>
<td>94.8%</td>
</tr>
<tr>
<td>24</td>
<td>282</td>
<td>144</td>
<td>81.0</td>
<td>90.8%</td>
<td>81.9%</td>
<td>86.5%</td>
<td>92.2%</td>
<td>98.2%</td>
<td>87.2%</td>
</tr>
<tr>
<td>25</td>
<td>280</td>
<td>154</td>
<td>58.3</td>
<td>99.6%</td>
<td>82.1%</td>
<td>86.8%</td>
<td>91.4%</td>
<td>97.1%</td>
<td>88.9%</td>
</tr>
<tr>
<td>26</td>
<td>300</td>
<td>152</td>
<td>89.7</td>
<td>99.0%</td>
<td>84.7%</td>
<td>87.0%</td>
<td>93.7%</td>
<td>96.0%</td>
<td>91.0%</td>
</tr>
<tr>
<td>27</td>
<td>260</td>
<td>153</td>
<td>56.2</td>
<td>99.2%</td>
<td>83.8%</td>
<td>87.3%</td>
<td>93.1%</td>
<td>96.9%</td>
<td>90.0%</td>
</tr>
<tr>
<td>28</td>
<td>310</td>
<td>158</td>
<td>105.5</td>
<td>97.7%</td>
<td>81.0%</td>
<td>84.2%</td>
<td>94.8%</td>
<td>98.1%</td>
<td>85.8%</td>
</tr>
<tr>
<td>29</td>
<td>282</td>
<td>105</td>
<td>58.1</td>
<td>94.7%</td>
<td>78.4%</td>
<td>81.2%</td>
<td>92.9%</td>
<td>96.5%</td>
<td>84.4%</td>
</tr>
<tr>
<td>30</td>
<td>80</td>
<td>56</td>
<td>15.9</td>
<td>92.5%</td>
<td>85.0%</td>
<td>90.0%</td>
<td>91.3%</td>
<td>96.3%</td>
<td>92.5%</td>
</tr>
</tbody>
</table>

Table 3: p values.

<table>
<thead>
<tr>
<th>Type A Order</th>
<th>Type A Client</th>
<th>Type B Client</th>
</tr>
</thead>
<tbody>
<tr>
<td>125</td>
<td>25</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

from the company (COF) in 30 out of 31 cases. There is a second acceptance criteria which states that any order may have plus/less one hour of error. Considering this criteria, our heuristic gets a higher objective function than the ones from the company (COF1) in 29 out of 31 cases. Looking deeper within these two cases, it is important to state that few of the routes were made by a truck with higher capacity, action that needs further confirmation and is not included in the set obtained in Phase I. Overall, our heuristic is able to find good solutions despite being simple and fast. The average increase in the objective function respect COF is of 22%.

The lowest computing times (T) are reported on days 3, 10, 17, 24 and 31, which corresponds to Sundays, where there is little movement compared to other working days. Time required to solve this problem on these days ranges from 6 to 16 seconds. Interestingly, the only two days where our heuristic’s resulting objective function was lower than the company’s one are present in this group. There is no clear difference between other days of the week.

Excluding Sundays, the number of routes (NR) ranges from 190 to 318, the number of trucks (NT) ranges from 97 to 158 and solution time ranges from 37 to 106 seconds. An increase in any of them, routes and trucks, have a negative impact in computing time, although it is expected that a higher number of routes encourages the company to try and get enough truck shifts to perform them, so they often grow together.

Breaking down total computing time in time used by CPLEX solver (T_{CPLEX}) and the rest of the phases (T_{AMPL}), it is possible to see that most of the time is used to solve the single truck scheduling problem with tentative sets of routes assigned. Any improve-
ment to the selection of routes to be included or to the model itself is expected to have a huge impact on total computing time.

Table 2 shows compliance levels. We can see that our heuristic is capable of obtaining a proposal with a really high number of trips while fulfilling all restrictions proposed, even outperforming the compliance of the company (CC), even considering the error acceptance criteria (CC1) in most of the cases. We can see that the compliance of the company with clients’ time windows is really high (CCCL), their main problem resides in being able to manage compliance with trucks’ time windows (CCT). If we go by the criteria of an acceptable error of plus/less one hour, the company compliance with the clients (CCCL1) is higher than our heuristic in 18 out of the 31 days.

In average our heuristic got a 95.1% compliance level, which correspond to an increase of 14% with respect of the current compliance level of the company over that month.

The CCT column in table 2 shows that truck compliance is fairly lower when comparing it to client compliance or our heuristic’s result. This means that truck compliance is one of the key points that can be drastically improved in practice.

6 CONCLUSIONS AND FUTURE RESEARCH

From the results obtained, we can say it is possible to include trucks shifts’ time windows in the scheduling problem faced by the company, as it is possible to reach at least the same compliance level the company already has without considering it, for most of cases.

The end result from our heuristic correspond to a proposal which schedulers usually request at the start of their day or along it, especially when big changes to the current schedule plan is required, so it must be able to present a good starting plan in a short span of time. As stated in results section, the heuristic is able to handle the biggest instances of this problem in at most 2 minutes, which is a fairly good time span considering the compliance yielded.

Future research will be focused on the impact of including more real life aspects to the two phases mentioned in 3, and test different aspects of the heuristic so it can solve them, such as: the efficiency of using a parallel insertion heuristic for this case; the impact on time solution of the secondary optimization criteria; and lastly, test different route starting criteria, as they might boost the heuristic performance.

ACKNOWLEDGEMENTS

This research was partially supported by Direcccion General de Investigacion y Postgrado (DGIP) from Universidad Tecnica Federico Santa Maria, Grant USM 28.15.20. Pablo Villegas also wishes to acknowledge the Graduate Scholarship also from DGIP.

REFERENCES


APPENDIX

Assignment Model

Variables:
- \( x_{tvk} \): binary that takes value 1 if route \( t \) corresponds to the \( v \)-th trip of truck \( k \); 0 otherwise
- \( d_{tvk} \): starting time of route \( t \) if it corresponds to the \( v \)-th trip of truck \( k \)

Maximize:
\[
\sum_{t \in T} \sum_{v \in V} \sum_{k \in K} \rho_t x_{tvk} \tag{11}
\]

Subject to:
\[
\sum_{v \in V} \sum_{k \in K} x_{tvk} \leq 1, \quad \forall t \in T \tag{12}
\]
\[
\sum_{v \in V} \sum_{k \in K} x_{tvk} \leq 1, \quad \forall v \in V, \quad \forall k \in K \tag{13}
\]
\[
\sum_{t \in T_k} x_{tvk} \geq \sum_{t \in T_k} x_{tv,k'}, \quad \forall v \in V \mid v \neq 1, \quad \forall k \in K \tag{14}
\]
\[
\alpha_k x_{tvk} \leq d_{tvk} \leq \beta_k x_{tvk}, \quad \forall t \in T, \quad \forall v \in V, \quad \forall k \in K \tag{15}
\]
\[
\alpha_k x_{tvk} \leq d_{tvk} \leq \beta_k x_{tvk} - \lambda_k x_{tv,k}, \quad \forall t \in T, \quad \forall v \in V, \quad \forall k \in K \tag{16}
\]
\[
d_{tvk} \geq \sum_{l \in T_k, l \neq t} \left( d_{l,v-1,k} + \lambda_k x_{l,v-1,k} \right), \quad \forall t \in T, \quad \forall v \in V \mid v \neq 1, \quad \forall k \in K \tag{17}
\]

Objective function (11) maximizes priority assigned. Restrictions of type (12) ensures that routes can be performed at most once. Type (13) restrictions ensures that at most one route can be performed as \( v \)-th trip of truck \( k \). Restrictions of type (14) ensures that in truck \( k \), the \( v \)-th trip exists just if trip \( v-1 \) also exists. Type (15) restrictions states that if route \( t \) is the \( v \)-th trip of truck \( k \), its departing time must be inside the route’s time window. Restrictions of type (16) states that if route \( t \) corresponds to the \( v \)-th trip of truck \( k \), its departing and arriving time must be inside truck’s time window. Type (17) restrictions states that starting time of route \( t \) in truck \( k \) must be higher than the arrival time of the previous trip. Finally, type (18) restrictions show variables’ nature.

\[
\rho_t = \sum_{i \in G_t} \rho_i \cdot Q_i \tag{19}
\]

Where \( G_t \) is the set of orders involved in route \( t \), \( \rho_t \) is the priority modifier of order \( i \), and finally \( Q_i \) is the quantity of product to be delivered in order \( i \).