

Exposing Design Mistakes During Requirements Engineering by Solving Constraint Satisfaction Problems to Obtain Minimum Correction Subsets

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Abstract: In recent years, the complexity of production plants and therefore of the underlying automation systems has grown significantly. This makes the manual design of automation systems increasingly difficult. As a result, errors are found only during production, plant modifications are hindered by not maintainable automation solutions and criteria such as energy efficiency or cost are often not optimized. This work shows how utilizing Minimum Correction Subsets (MCS) of a Constraint Satisfaction Problem improves the collaboration of automation system designers and prevents inconsistent requirements and thus subsequent errors in the design. This opens up a new field of application for constraint satisfaction techniques. As a use case, an example from the field of automation system design is presented. To meet the automation industry's requirement for standardised solutions that assure reliability, the calculation of MCS is formulated in such a way that most constraint solvers can be used without any extensions. Experimental results with typical problems demonstrate the practicalness concerning runtime and hardware resources.

1 INTRODUCTION

The design of an automation system is already a complex and time-consuming task, today. Additionally, the complexity of these systems will increase in the future even more due to a higher degree of automation and an increasing amount of their constituent parts and environmental constraints (Fay et al., 2015). In (Vogel-Heuser et al., 2014) it is stated that today's design methods are not keeping pace with the rising complexity and it is shown that designers lack tools for efficiently designing automation systems.

In order to create suitable tools it becomes necessary to have a formalised description of design and configuration knowledge in industrial contexts. The knowledge can be accessed by automatic configuration tools that are able to execute certain (lower-level) design tasks and thus reduce the work for human designers. This enables designers to focus more on the specification of requirements. By making use of this formalised knowledge the design process becomes independent of single persons that have highly specialised skills because the knowledge is formalised in software and thus every designer can make use of it. Furthermore, when the software is able to design

the implementation specific details, repetitive and error prone tasks are automated. This also includes that different design variants of a system can be generated without additional engineering effort. Therefore, it enables users to find the best variant to a given use-case.

To devise such design methods it is necessary that the initial requirements can be specified in a formal way, because these are the basis for the subsequent automatic design.

This paper describes a method to specify requirements for an automation system formally with an emphasis on cooperation between different professions and support of interdisciplinary conflict resolution. This is done by dividing the design work into different categories like mechanics, visualization, security etc. If conflicts arise during the requirements specification the presented approach attributes each conflict to the corresponding category and tells the user which requirements need to be changed. For the underlying model, extended feature models (EFM) are used.

An EFM symbolizes requirements as a tree of required entities and a set of constraints over these entities and their attributes. Besides the ideal suitability of this model for industrial needs, a main benefit is

the representational duality as a constraint satisfaction problem (CSP) and as a rooted acyclic graph (Moriz et al., 2014; Böttcher et al., 2014).

That is beneficial because graph-based representations of design knowledge are very natural for engineers (Chakrabarti et al., 2011; Maher, 1990). The representation of design rules as changes of a graph perfectly reflects that the design rules specify how components can and need to be connected (Gruner et al., 2014). Feature models are a bridge from the requirements to the design (Czarnecki and Eisenecker, 2000) and they precisely fulfil industries' needs concerning formalisation and reuse of requirements (Benavides et al., 2010; Czarnecki and Eisenecker, 2000).

In order to resolve conflicting requirements that hinder the subsequent design process, corresponding unsatisfied constraints in the EFM need to be identified. The presented approach uses minimum correction subsets (MCS). Given a set of constraints (in form of an EFM, for example) which is not satisfiable, the MCS encompasses those constraints that need to be removed from the set to achieve satisfiability. Therefore, the MCS is the ideal choice to show only those requirements to the user that correspond to a constraint in the MCS. The users can subsequently decide how the conflicting requirements can be resolved. This approach improves the overall design efficiency since only those designers need to be involved in conflict resolution that entered the requirements originally. Furthermore, designers are aided in their designs because they focus on the requirements specification while the implementation specific details are generated by the system.

Our contribution is a method for efficiently finding MCSs by translating an EFM into a MaxCSP. The translated model can be solved by a standard CSP solver. The method is validated through implementation in a real-world demonstrator and used for increasing the usability for automatic design tools.

This paper is structured as follows. In the next section, current approaches are discussed and basic principles are introduced. Section 3 describes a use-case to illustrate the presented approach. To show how the minimum number of unsatisfiable constraints can be found and attributed to different categories, Section 4 introduces a technique for finding a minimum correction set of a CSP. At the end of the paper, empirical results are presented and the work is summarised.

2 STATE OF THE ART

In (Moriz et al., 2014) and (Benavides et al., 2010) extended feature models (EFM) have been formally

related to CSPs. These models are used to represent configurations of products or other complex systems i.e. cars, phones etc. According to (Czarnecki et al., 2006) they can also be used for modelling ontologies. The most important fact is that EFMs help to represent how different entities are organised hierarchically. Each feature in an EFM has a number of attributes which can specify the details of a feature. Furthermore, each attribute can be limited in its range of possible values by a set of constraints. To illustrate this, think of a feature representing a motor. The attributes could then be values for torque, weight, power consumption etc. Constraints would be used to specify that for an imaginary use-case, the weight must not exceed 10 kg and the power consumption must be less than 500 W. That means, the ranges (from here on called the domains) of the attributes are limited to values below 10 and 500, respectively.

In contrast to the approaches discussed in (Moriz et al., 2014; Böttcher et al., 2014) and (Moriz et al., 2014), which describe the implementation of the EFM, this paper focuses on solving conflicts in EFMs by using solutions to constraint satisfaction problems.

In order to solve the EFM with a standard constraint solver, the EFM has to be formulated as a CSP (Benavides et al., 2004; Mendonca et al., 2009). According to (Kumar, 1992) and (Bartak, 1999) the CSP can be defined as follows. Given a set of variables, with each value of a variable being in a certain domain D and a set of constraints over these variables, find a solution which satisfies all of the constraints.

In (Ansotegui et al., 2013) and (Gu et al., 1999) a definition of the satisfiability problem (SAT) is presented. A SAT formula is a boolean formula consisting of a conjunction of clauses C . Each of these clauses in turn consists of a disjunction of literals. The SAT problem defines the task of finding values x , with $x \in V = \{TRUE, FALSE\}$, so that the formula is satisfied. According to (Tamura et al., 2009), a CSP can be defined as a SAT problem by substituting literals for constraints and setting $V = D$ i.e. the domain. Different approaches have already been introduced by (Tamura et al., 2009; Tamura et al., 2008).

With this information it is possible to formulate a generalization of the SAT problem which is called the MaxSAT problem (Ansotegui et al., 2013; Kuegel, 2010). Given a set of SAT clauses, begin to solve the SAT problem by trying to satisfy the maximum number of clauses. When this is solved, the output \mathcal{M} can be split into two sets $\mathcal{M} = \mathcal{S} \cup \mathcal{C}$. One set $\mathcal{S} \subseteq \mathcal{M}$ will then be used to denote the clauses which can be satisfied, whereas $\mathcal{C} \subseteq \mathcal{M}$ denotes the clauses which could not be satisfied. This gives the overall

solution of the MaxSAT problem.

As yet, many approaches have been proposed for solving MaxSAT problems. The approaches mentioned in (Ansotegui et al., 2013; Kuegel, 2010; Boffill et al., 2012) focus on computing the subsets from SAT formulas. The work in (Koshimura et al., 2012) finds all minimal unsatisfiable subsets of a boolean constraint system. In (Ansotegui et al., 2013) an overview for solving a SAT problem by its corresponding MaxSAT problem is given, whereas the work in (Jiang et al., 1995) is about a stochastic approach for solving the MaxSAT problem. All these approaches have in common, that they focus on boolean values. In practice, however, it is often necessary that constraints take on numerical values. Examples are the speed of a conveyor belt or the maximum available bandwidth. A partial constraint satisfaction problem is equivalent to a MaxSAT problem (Freuder and Wallace, 1992).

A major area of application for automatic design is Product Line Engineering (PLE) (Nie et al., 2013). PLE has been identified to deal with the increasing complexity and variation in product lines. For dealing with inconsistencies within product lines the use of Minimum Correction Subsets is proposed by (Felfernig et al., 2013) and (Rincón et al., 2015). Minimum Correction Subsets contain the smallest possible number of constraints that, when removed, guarantees that all remaining constraints are free of logical contradictions. While (Felfernig et al., 2013) suggests a brute-force algorithm for finding such sets, (Rincón et al., 2015) propose a binary-search based algorithm that finds conflicting constraints but no Minimal Correction Subsets. In this work the MaxSAT problem described above forms the base for a more general and complete calculation of inconsistent constraints in PLE.

(Törngren et al., 2014) has identified the need for different views, since products are often configured by stakeholders working at different organisations, departments, or professions. They state that for efficient development of products it is necessary to provide different viewpoints to a system at the level of people, models, and tools.

Beside the concept of views, the work in (Nie et al., 2013) also mentions the necessity to provide consistency checking between all requirements. Furthermore, five functionalities for automated configuration of software solutions are identified:

1. The need to infer decisions automatically through relevant information such as constraints
2. Consistency checking to verify that certain properties hold, especially between different views
3. The ordering of decisions towards reducing the configuration effort

4. The possibility of collaborative configuration
5. A way to revert decisions made by users

The approach presented in this paper mainly deals with the first four points as section 5 will show. Point 5 is left to future work.

3 DEMONSTRATION USE-CASE

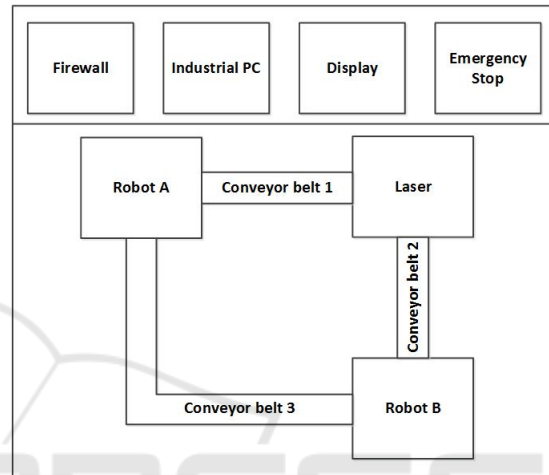


Figure 1: The demonstration use-case consisting of different components belonging to several categories (i.e. mechanics, visualization, security etc.).

To illustrate the implemented techniques Figure 1 depicts a demonstration use-case. The use-case consists of a manufacturing system with two robots and a laser connected by three conveyor belts. Robot A is used to place items into carriages on conveyor belt 1. The filled carriages are then transported to the laser and subsequently transferred to Robot B through conveyor belt 2. Robot B takes the lasered items from the carriages. The empty carriages themselves are then transported back to Robot A by conveyor belt 3. Overall, the manufacturing system is controlled through an industrial PC attached to a firewall. For interaction with the operator, a display is connected to the industrial PC. Additionally, human operators are protected by an emergency stop functionality.

In this example, views are utilized to divide the manufacturing system into distinct parts e.g. Mechanics, Visualization, Security etc. The robots, conveyor belts and the laser as well as the industrial PC all need mechanical structures in order to be placed in a production plant. The planning and installation of these components is done by mechatronic engineers. On the other hand, the robots and the industrial PC run a certain kind of software. Thus, the programming and

administration of this software is done by software engineers. Visualisation (i.e. user interface design) is a completely different discipline and requires experts familiar with human machine interfaces. Contrary to that, security or safety related components must be installed by personnel especially trained for these kinds of tasks.

When the automation system depicted in Figure 1 is designed, each member of the design team starts by specifying the initial requirements of his subsystem. This is done by choosing abstract entities from a list of templates (seen in Figure 1). Each template may have some attributes like power consumption, maximum weight, maximum temperature, speed etc. After all abstract entities have been selected, the details and relations between those must be specified. This is the point where constraints are added. In this case, constraints could be the speed of the conveyor belts, cycle time of the underlying fieldbus or the available bandwidth.

It follows from this example that the design of an automation system is very complex. The present approach can greatly simplify the effort required. This is done by finding conflicted constraints during the specification and point those out to users. It is conceivable that the security expert requires that the firewall has a maximum bandwidth of 100 Mbit/s. Conversely, the expert for the industrial PC might require a bandwidth of 1 Gbit/s (see Figure 2).

When a number of unsatisfiable constraints are encountered, the goal is to display only the absolute minimum number of necessary changes to the user. This entails that only a minimum number of views, and thus persons, are affected. To accomplish this, the next section shows how minimum correction subsets can be found.

4 MINIMUM CORRECTION SETS

In order to attribute all unsatisfiable constraints to a certain view, a method is needed to determine exactly which constraints could not be satisfied. This is accomplished by the use of Minimum Correction Subsets (MCS) and Maximum Satisfiable Subsets (MSS). The MCS, formally defined below, contains all unsatisfied constraints. This section describes how each constraint is augmented with an additional boolean variable which is used to determine the MCS.

For this, the proposed approach introduces a technique using a Constraint Satisfaction Optimisation Problem (CSOP) to find MCSs for an unsatisfiable CSP. As opposed to approaches discussed in (Ansotegui et al., 2013) and (Kuegel, 2010) this work

proposes to augment a CSP in such a way, that it can be transferred into a CSOP subsuming the CSP and a MaxSAT problem for maximizing the number of satisfied constraints. The result of solving the CSOP are value assignments to all problem variables and truth assignments to boolean variables indicating which constraints can and which cannot be satisfied, as well as the constraints themselves.

A MCS is a set of constraints which needs to be omitted from a CSP in order to make it satisfiable. Conversely, the maximum satisfiable set contains the maximum amount of clauses which can be satisfied without making the CSP unsatisfiable. Therefore, the MSS is the inverse of the MCS. The minimum unsatisfiable set (MUS) describes the so called cause of the unsatisfiability. A MUS consists of a set of constraints from which one constraint needs to be omitted to achieve satisfiability. In this work, the MUS is not necessary because the focus is to find the minimum set of unsatisfiable constraints (MCS) in order to make the CSP satisfiable. To illustrate the approach described in this paper, the following definitions are necessary (Marques-Silva et al., 2013; Liffiton and Sakallah, 2005).

Definition 1. *The subset $\mathcal{U} \subseteq \mathcal{C}$ is a MCS, iff $\mathcal{C} \setminus \mathcal{U}$ is satisfiable and $\forall c \in \mathcal{U}, \mathcal{C} \setminus (\mathcal{U} \setminus \{c\})$ is unsatisfiable.*

Definition 2. *The subset $\mathcal{S} \subseteq \mathcal{C}$ is a MSS, iff \mathcal{S} is satisfiable and $\forall c \in \mathcal{C} \setminus \mathcal{S}, \mathcal{S} \cup \{c\}$ is unsatisfiable.*

The MaxSAT problem can be stated as follows (Kuegel, 2010). Given a formula in conjunctive normal form (CNF), try to satisfy as many clauses as possible. A CNF of a boolean formula can be expressed as $\bigwedge_{l=0}^n C_l$ where $n \in \mathbb{N}$, $l \in \mathbb{N}$ is the number of clauses. With $C_l = \bigvee_{k=0}^{m_n} (\neg)x_{lk}$, where $m_n \in \mathbb{N}$ is the number of literals and x can be either *true* or *false*. $\neg x_{lk}$ is therefore the negation of x_{lk} . Each C_l will henceforth be called a clause. If the maximum number of satisfiable clauses can be determined, it is also possible to determine the MCS, since this set consists of all the clauses which are left unsatisfied. Subsequently the MSS can be determined, since it is the difference of all constraints \mathcal{C} and the MCS. In this case, one MCS is used to notify the user which constraints do not match and need to be removed or relaxed. By replacing clauses by arbitrary predicates which are boolean functions of arbitrary constraints a MAX-CSP is obtained. This is realised as follows.

Upon validation of the constraints during the design process, every constraint $c_m, c \in \mathcal{C}, m \in \mathbb{N}$ is a predicate that is the logical consequence of a boolean indicator variable, $b_m \in \mathcal{B}, m \in \mathbb{N}$, so that b_m implies constraint c_m . This means, any CSP solver is able to find solutions where c_m must hold (b_m is true)

and solutions where c_m is not required to be satisfied (b_m is false).

In order to convert the CSP to a CSOP problem which objective is maximum satisfiability the following objective function is used. The set $B^* = \{\text{true}, \text{false}\}^{|B|}$ is the set of all possible value assignments for all $b \in B$. The function

$$val(b^*, i) = \begin{cases} b_i = \text{true} \rightarrow 1 \\ b_i = \text{false} \rightarrow 0 \end{cases} \quad (1)$$

gets a value assignment $b^* \in B^*$ and the index of a variable $b_i \in B$ and returns 1 if b_i is assigned the value *true* and 0 otherwise. The objective is to maximize the number of satisfied constraints. This is equal to finding the value assignment out of B^* with a maximum number of variables in B that are assigned the value *true* and for which the CSP is satisfiable:

$$\begin{aligned} & \operatorname{argmax}_{b^* \in B^*} \sum_{m=0}^{|B|} val(b^*, m) \\ & \text{where } \bigwedge_{m=0}^{|C|} b_m \rightarrow c_m = \text{true}, b_m \in b^* \end{aligned} \quad (2)$$

The optimisation is realised by applying a constraint solver which maximises the objective function. As the input for the solver, the FlatZinc (Becket, 2015) format is used. This format is a solver independent modelling language for constraints. Besides the obvious standard predicates for specifying constraints, the FlatZinc format also allows to specify global predicates. These are used to optimize certain tasks which would be too inefficient when performed without global predicates. Examples for those tasks are counting, set operations, or sorting. All global constraints are solver specific extensions to FlatZinc. Thus not all global constraints are available on all solvers which support FlatZinc.

In the use-case described in this paper, the FlatZinc script is built as follows: The objective in formula 2 is realised by mapping all boolean values of the variables b_m to integer variables that are arranged in an array. The summing up of the array is done by the global predicate *count(.)* and constrained to equal the integer variable *Out*, where *Out* is assigned the outcome of formula 2. This variable's value is maximized by constructing a FlatZinc script with the solve options

"solve maximize Out"

The keyword *solve* specifies that all lines above the statement will be used for the solution. *Maximize* states that the goal is to maximise the variable indicated by the next word (*Out*).

To summarise, a robust method has been devised in which it suffices to let a help-variable (b_m) imply each constraint. Subsequently, an aggregation function can be employed, whose output is a single variable *Out*. This output can be maximised by a standard off-the-shelf constraint solver that, for example, uses branch and bound techniques for optimisation.

5 IMPLEMENTATION

The presented technique was implemented in an application called "assisted design for automation systems (AD4AS)". The software, developed as a prototype, realises an iterative, holistic design approach for automation systems. One major focus of the work is to divide elicitation of requirements into different categories, called Views. These were first mentioned in (Törngren et al., 2014) and (Nie et al., 2013). They state that any complex system will involve multiple stakeholders and multiple views. Additionally, the relationship between different stakeholders in a project is evaluated with the goal of an optimal integration of each stakeholder. It is stated that stakeholders with backgrounds in different disciplines may have diverse vocabularies and understandings of the same concepts. From this follows that in design software it is necessary to include support for helping users with different professions collaborate.

As indicated in the introduction, in the present approach each view displays components of a certain requirements category. One category could be the mechanical structure of the automation system. Other categories are the visualisation of process parameters or security related components. These different views help to divide the requirements elicitation into parts. Each part can be designed by experts in the appropriate discipline.

Figure 2 shows the prototype's user interface. At the top, different design steps can be selected. In the next line the views are visible as well as the button to start the validation of the design. The currently implemented views are: system (overview), mechanics, visualisation, security, process and product. Below, the list of selected abstract components, i.e. templates, can be seen.

By taking advantage of the compartmentalisation made possible by the views, each member of a design team can concentrate on his own speciality. This means, when unsolvable constraints are encountered during the automated design, the solution of these constraints can be delegated to the specific team member in whose subject area the unsatisfied constraints fall. This way, each area of an automation system can

be covered by domain experts. Thus, design time can be reduced and the quality of the design is improved.

The process simplifies the work by enabling the design team to focus on abstract, conceptual ideas (i.e. specifying the requirements) instead of having to work out every detail. The advantage is that the software is able to find inconsistencies among the requirements of the system. With this information, each inconsistency can be attributed to a specific subject by using the concept of views. Additionally, the presented prototype frees users of the tedious work to select products from a range of different vendors to conform to every requirement in the system’s specification. Instead, a catalogue of permitted components can be supplied and the software will decide which components can be used and how those should be ordered hierarchically. As section 6 shows, the presented approach scales sufficiently well for many automation systems.

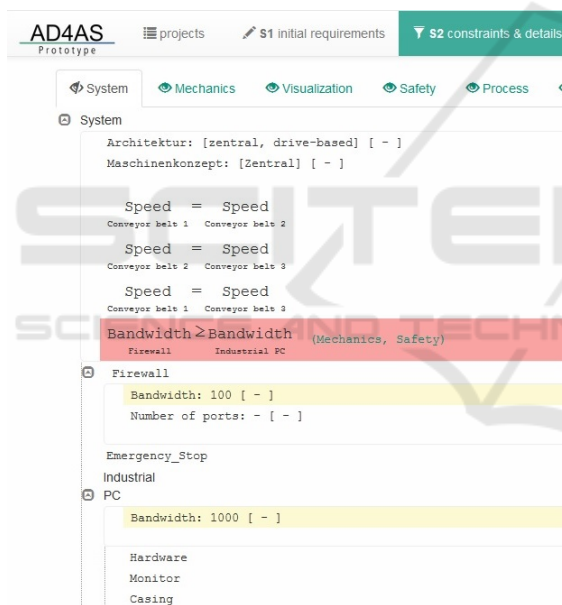


Figure 2: The AD4AS user interface when unsatisfied constraints are encountered

When the design from figure 1 is validated in AD4AS, the software will ensure that the maximum number of constraints can be satisfied. If it is assumed that in this case all other constraints are satisfied (for example conveyor speed, energy consumption etc.) the software will show, which constraint is left unsatisfied (i.e. bandwidth). Furthermore, the system determines that the unsatisfied constraint is located in the views mechanics and safety. Thus the security expert and the industry PC administrator can find a solution without affecting the designers of the user interface for example. When different MCSs with the

same number of conflicts are found, the user can decide which of the MCSs he wants to solve.

6 RESULTS

In (Fay et al., 2015) was established that in practice, automation engineers are often given no time to define requirements formally. The present approach works toward making the formal design of automation systems faster and more consistent. The provided platform incorporates techniques determined to be useful to increase the overall design efficiency (i.e. the concept of views and validation of constraints). Furthermore, the constraint validation has been extended to attribute each constraint to one or more views. To accomplish this, a way to transform the EFM into a CSOP problem and thus satisfying the maximum number of constraints has been implemented.

Table 1 shows the runtime of the proposed algorithm as performed on a 64-Bit PC with Intel Core i5 CPU with 2.67 GHz, 8 GB memory and Windows 7 operating system. The test set has been created from randomly generated extended feature models with a branching factor between 5 and 10 and each feature having two attributes. The branching factor describes how many child features each parent feature has. The maximum depth of an EFM was set to 6. One attribute a_{i1} is limited by a constraint c_i with $c_i : a_{i1} < r$, $r \in \mathbb{R}$ and a fixed domain size. Additionally, the second attribute a_{i2} of each feature is limited by a constraint of the same form, but with a randomly varying domain.

Table 1: Runtime (milliseconds) compared to the number of variables and constraints.

Variables	54	199	2021	2824	21379
Solvable Constraints	1	10	237	406	3111
Unsolvable Constraints	7	20	37	14	31
Runtime (ms)	1	2	20	35	2023

The AD4AS software is an assistance system which supports designers in specifying requirements for automation systems iteratively. The standard use-case is that designers enter requirements to achieve a functioning system. Therefore, the ratio of unsatisfied to satisfied constraints is small.

The work in (Nie et al., 2013) gives three examples of industrial applications. The examples illustrate the amount of variables and constraints commonly found in real-world applications. The first and second example describe a subsea production system

and a video conferencing system, respectively. These consist of approximately 500 variables. Whereas the third example, a vessel prognostics and health management system, consists of approximately 1000 variables. These examples illustrate the numbers in Table 1 which show that the proposed approach is sufficient for configuring today's automation systems. With the calculation of the minimum correction subsets integrated into the software described in section 5, a tool is created which enables engineers to design automation systems very efficiently. Furthermore, even systems with several thousand components can be easily formulated and checked for consistency.

7 CONCLUSION

In this paper a holistic approach to designing automation systems is presented. Based on the work introduced in (Törngren et al., 2014) and (Nie et al., 2013), it is shown that our work contributes to greatly simplify and speed up the design of an automation system. The most important point is that through the presented work system designers can concentrate on high-level specifications in their field of knowledge while certain details and implementation specific aspects are added automatically. Overall, the presented approach aides designers in two ways. On the one hand, the design is compartmentalised to accommodate the need that experts with different backgrounds and professions interpret designs in different ways (see (Törngren et al., 2014)). This means, in order to achieve maximum efficiency, each expert should be best put to work with a vocabulary and concepts he is most familiar with. On the other hand, the AD4AS prototype finds each unsatisfied constraint within a system and can attribute it to different views (i.e. experts). Furthermore, we showed in section 6, that finding unsatisfied constraints can be done in reasonable time for the amount of components usually found in automation systems. Therefore, the suggestions from (Fay et al., 2015) and (Törngren et al., 2014) were implemented and extended to construct a prototype which can contribute to close the gap between the increasing complexity of automation systems and automated design tools.

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