Evaluation and Optimization of Adaptive Cruise Control Policies Via Numerical Simulations

Clement U. Mba and Carlo Novara

1Department of Mechanical and Aerospace Engineering, Politecnico di Torino, Corso Duca degli Abruzzi, 24, Torino, Italy
2Department of Control and Computer Engineering, Politecnico di Torino, Corso Duca degli Abruzzi, 24, Torino, Italy

Keywords: Adaptive Cruise Control, Test Simulation, Performance Optimization.

Abstract: Adaptive Cruise Control (ACC) makes the driving experience safer and more pleasurable. Several appealing ACC policies have been introduced so far. However, it is difficult in general to understand which is the actual performance that can be guaranteed on a real vehicle. Another relevant issue is that no systematic methods can be found for the optimization of a control policy performance. The first aim of this paper is to compare different ACC policies by means of extensive simulations, considering different realistic road scenarios. This kind of study is important to analyze which policies can be more effective in view of their implementation on real vehicles. The second aim is to develop an optimization method based on a multi-objective Pareto criterion, finalized at designing high-performance policies. The method is tested by means of extensive simulations.

1 INTRODUCTION

Driving can be defined as a set of operations aimed at controlling a motor vehicle, where control is typically performed by a human driver. However, the human driver behavior may tend sometimes to cause undesirable vehicle behaviors. In modern vehicles, to avoid or prevent these kinds of behaviors, control is usually done by the human driver with the help of some Driver Assistance Systems, one of the most important of which is the Cruise Control.

Cruise Control (CC) has the task of maintaining the vehicle speed at a desired value. However, a drawback of CC is that it cannot vary the speed of the vehicle: whenever a vehicle in front of the vehicle equipped with CC is traveling slower than the latter, the driver has to step on the brakes in order to deactivate the Cruise Control and step on the accelerator when the preceding vehicle speeds up, (Howard, 2013). As a result, Cruise Control has to be reset from time to time. This drawback is overcome by the more advanced Adaptive Cruise Control (ACC), which is able to adjust the speed of the vehicle, depending on various factors influencing it without manual intervention from the driver, (Howard, 2013; Shakouri et al., 2012, 2014). Some of them, like the “stop and go”, can bring the vehicle to a stop and start it moving, (Shakouri et al., 2012, 2014).

In general, the design of an ACC begins with an ACC policy. Different ACC policies have been proposed: Constant Time Gap (CTG), Constant Distance, Constant acceptance, Constant Stability and Constant safety factor (Xiao et al., 2010). ACC policies specify the desired steady state distance between two vehicles in succession. Note that ACC policies can be either autonomous, (Rajamani, 2012), cooperative, (Schakel et al., 2010; Oncu et al., 2010) or a combination of both, (Swaroop, 1995). Introducing and maintaining continuous inter-vehicular communication, which is the main feature of cooperative policies causes network effects that can undermine the performance of the ACC (Oncu et al., 2010). Moreover, maintaining continuous inter-vehicular communication is costly (Yanakiev et al., 1995, 1998). Thus, the autonomous operation seems like the most preferred choice at present, and it is the area of focus in this paper.

The performance of an ACC system is based on the particular control policy that it employs. The basic control policies are the Constant Spacing Policy (CSP), Constant Time Gap (CTG) and Variable Time Gap (VTG). All the other policies are usually variants of these basic policies. However, even though all these policies are appealing from a methodological point of view, it is difficult in general to understand which is the actual performance that can be guaranteed on a real vehicle. Another relevant issue is that, to the best of our knowledge, no systematic methods...
can be found for the optimization of the control policy performance.

In this perspective, the main contributions of the paper are two. First, the control policies employed by the “standard” ACC systems are compared by means of extensive simulations, considering different realistic road scenarios. This kind of study is important to understand which control policies and, more in general, which control approaches can be more effective in view of their implementation on real vehicles. Second, an optimization strategy based on a multi-objective Pareto criterion is proposed, finalized at designing high-performance control policies. The strategy is tested by means of extensive simulations, involving different realistic road scenarios. These simulations show that the method allows the design of control policies able to perform significantly better with respect to the “standard” policies, in terms of safety and fuel consumption.

2 VEHICLE MODEL AND CONTROL POLICIES

In this section, we introduce the vehicle and control models that will be used in the simulations, first to compare the “standard” ACC systems, then to test our optimal control policy design method.

The following assumptions were made:

- All vehicles are identical and move in a straight line.
- Before the maneuver of the lead vehicle, all the vehicles were moving at the same steady state speed.
- The lead vehicle takes a finite amount of time to perform a maneuver prior to reaching steady state speed.

The longitudinal dynamics of each vehicle (plant) can be approximated by the following model (see Rajamani, 2012; Santhanakrishnan et al., 2003; Swaroop et al., 1994):  

\[ \tau \ddot{p} + \dot{p} = u \]  

where \( p \) is the vehicle longitudinal position, \( u \) represents a “desired” longitudinal acceleration and \( \tau \) is the vehicle time constant.

The desired acceleration \( u \) is the control input, which can be used to improve the vehicle performance in terms of safety, comfort and fuel consumption. This task can be accomplished by a proper control policy, as shown schematically in Fig. 1, where the block “Vehicle” is a dynamic system described by (1) and \( \varepsilon \) is the spacing error to be defined subsequently.

Usually, the control policies should satisfy string stability requirements in order to give a good performance. String stability is defined as stability with respect to the spacing between vehicles. It ensures that the spacing error, defined as the difference between the actual and desired spacing, do not get larger as it propagates upstream in a string of Adaptive Cruise Control vehicles using the same control law (Rajamani, 2012; Santhanakrishnan et al., 2003; Swaroop, 1995; Swaroop et al., 1994; Yanakiev et al., 1998; Chi-Ying et al., 1999). The CSP policy requires inter-vehicular communication if string stability is to be guaranteed (Swaroop et al., 1998; Yanakiev et al., 1998), while the CTG and VTG policies overcome this limitation (Yanakiev et al., 1995; Swaroop et al., 1994; Yanakiev et al., 1998). Since we are only considering the autonomous operation, our tests are conducted only on the CTG and VTG policies.

The CTG policy is defined by the control law

\[ u = \frac{(\dot{p} - \dot{p}_f + k \varepsilon)}{h} \]  

where \( p \) and \( p_f \) are the positions of a vehicle and the preceding vehicle respectively, and \( \varepsilon \) is the deviation from the desired spacing, otherwise known as the spacing error, (Rajamani, 2012; Santhanakrishnan et al., 2003; Swaroop et al., 1994; Zhao et al., 2009). \( \lambda, L_{des} \) and \( h \) are design parameters, to be chosen in order to obtain the desired longitudinal dynamics performance. \( \lambda \) is a control gain, \( L_{des} \) is the desired spacing between the vehicles and \( h \) is called the time gap (it represents the time distance between the two vehicles).

Combining the vehicle equation (1) with the control equations (2), we obtain an Linear Time Invariant (LTI) system, with input \( p_f \) and output \( y = \varepsilon \). Note that, on a vehicle equipped with an ACC systems, \( p_f \) is typically measured by a radar.

The VTG has several variants (Zhou et al., 2004; Santhanakrishnan et al., 2003; Yanakiev et al., 1995; Zhao et al., 2009; Wang et al., 2004, 2002; Zhou et al., 2005), which are similar to each other. The Nonlinear Range Policy (NRP) (Zhou et al., 2004, 2005) is considered here because of its simple structure. This policy is defined by the control law

\[ u = (1 - \frac{\tau k}{h} - \frac{\tau k}{h^2} \dot{h}^2) \dot{p} + (\frac{\tau k}{h}) p_f - \dot{p} \]  

where \( k \) is a design parameter, called the scaling factor (Zhou et al., 2004, 2005).

As for the VTG policy, combining the vehicle equation (1) with the control equations (3), we obtain an LTI system, with input \( p_f \) and output \( y = \varepsilon \).
3 ACC POLICIES COMPARISON

The two ACC policies described in Section 2 are tested considering three different scenarios:

Scenario 1. Constant Number of Vehicles Traveling in a Line
In this scenario, 10 vehicles are traveling in a line and the lead vehicle makes some critical manoeuvre. Three kinds of critical manoeuvres are simulated:
- Manoeuvre 1: The lead vehicle suddenly increases its speed; this manoeuvre was obtained simulating $u_1$ (the input of the leading vehicle) as a filtered positive step. Manoeuvre 2: The lead vehicle suddenly increases its speed and then goes back to the original speed; this manoeuvre was obtained simulating $u_1$ as a filtered positive impulse. Manoeuvre 3: The lead vehicle decelerates continuously; this manoeuvre was obtained simulating $u_1$ as a filtered negative ramp.

Scenario 2. Vehicles Joining and Leaving the Line
In this scenario, 10 vehicles are traveling in a line and one or more vehicles join or leave the line at different times; this manoeuvre was simulated just by suddenly increasing or decreasing the number of vehicles in the line with the gap between the vehicles taken into consideration to prevent collision. Note that this simulation is more challenging than a real situation, where the process of joining or leaving the line is “more continuous”. We considered up to 5 vehicles joining or leaving the line.

Scenario 3. Traffic Flow
In this scenario, 10 vehicles are traveling in a line and one or more vehicles join or leave the line at different times. We considered up to 5 vehicles joining or leaving the line. As an additional complication, the line may stop at different times due to the presence of traffic lights; the stop at the light was obtained simulating $u_1$ as a filtered negative ramp that, after a certain time, becomes constant.

We considered different combinations of the values of the parameters characterising the vehicle model and the control policies. In particular, the following parameter ranges were assumed:

$$\tau \in [0.5, 0.95] \text{ s}$$
$$\lambda \in [0.4, 0.95]$$
$$h \in [0.1, 2]$$
$$k \in [2, 15]$$
$$L_{des} = 40 \text{ m.}$$

For each manoeuvre of scenario 1 and for each parameter combination, we performed one simulation. This simulation was long enough to reach steady-state conditions. For each of scenarios 2 and 3 and for each parameter combination, we performed a sufficiently long simulation, in order to capture all relevant situations that can occur in a real road scenario. In particular, the duration of the simulated road scenarios was about 107 hours, corresponding to about 4 hours of Matlab run time. The simulations were done using Matlab R2014a and its simulink environment.

To evaluate the performance of an ACC control policy, we considered the following indexes:

- **Recovery Time**: The recovery time of a vehicle is defined
  $$T_R = T_{ss} - T_c$$
  where $T_c$ is the time at which a critical event occurs (e.g., a critical manoeuvre, a vehicle joining or leaving the line, or a stop at the light) and $T_{ss}$ is the 2% settling time (that is, the time after which the system output is always within an interval with center at the steady-state value of the output and amplitude 2% of this value).

- **Input Signal Root Mean Square Value**:
  $$RMS_u = ||\tilde{u}|| / \sqrt{N}$$
  (4)
  where $\tilde{u}$ is the (discrete-time) command input signal of a vehicle acquired from the simulation, $||.||$ is the vector 2-norm and $N$ is the length of $\tilde{u}$.

- **Output Signal Root Mean Square Value**:
  $$RMS_y = ||\tilde{y}|| / \sqrt{N}$$
  (5)
  where $\tilde{y}$ is the acquired (discrete-time) output signal of a vehicle.

The recovery time measures the capability of the control policy to promptly bring the vehicle back to its “normal” operation conditions. $RMS_u$ essentially measures the mean deviation of the output from the desired value (hence, it is also an indirect measure of the recovery time). $RMS_y$ is related to the energy spent by the control policy in order to obtain the desired performance.

Tables 1-6 show the performanceindexes obtained in the simulations, averaged over all the vehicles composing the line, all the critical events (i.e., vehicles joining and leaving the line and stops at the lights)
and all the parameter combinations. The averages are indicated with a bar. In Figures 2-6, we can observe the performance indexes obtained in the simulations, averaged over all the vehicles composing the line and all the critical events.

Tables 1, 2 and 3 show that the NRP generally recovers faster when subjected to critical conditions, involving also lower values of $RMS_y$. However, the required command activity, measured by $RMS_u$, is higher. Similar results are shown by Tables 4, 5 and 6.

Given that $\tau \geq 0.5$ and $\lambda = 0.4$, the NRP is more flexible than the CTG, in the sense that $h$ can be varied from 0.1 to more than 1.8 without the spacing errors getting larger as they propagate upstream in vehicles using NRP. When $h = 0.1$, for the NRP the recovery time as well as the $RMS_y$ value is “small”, with a high value of $RMS_u$ on the command input activity.

The average recovery time increases a little for vehicles using the NRP as $\tau$ gets higher. In the case of the CTG, the average recovery time increases considerably as $\tau$ gets higher. Accordingly, it can be said that higher values of $\tau$ for each of the vehicles do not have as much influence on vehicles using the NRP as they do on vehicles that use the CTG. This is most likely to be a result of the high value of $h$ that is required in the CTG when $\tau > 0.5$, to prevent the spacing errors from getting larger as they propagate upstream.

The simulation results obtained from scenario 2, as shown in Figures 2 and 3, and scenario 3, as shown in Figures 4 and 5, show that the NRP has lower $RMS_y$ than the CTG for the same values of $h$ and $\tau$. The two lines with the same $h$ in Figures 2 and 3 correspond to the vehicles either joining or leaving the line. It should also be noted that similar results are obtained when $\tau$ is different for each vehicle in the stream.

Low values of the time gap as well as low values of $RMS_u$ are desirable but these act in contrast to each other. As stated earlier, lower values of the time gap

<table>
<thead>
<tr>
<th>Strategy</th>
<th>$\bar{T}_R$ [s]</th>
<th>$RMS_u$</th>
<th>$RMS_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTG</td>
<td>33.14</td>
<td>12.508</td>
<td>1.1199</td>
</tr>
<tr>
<td>NRP</td>
<td>4.5</td>
<td>14.7154</td>
<td>0.1833</td>
</tr>
</tbody>
</table>

Table 2: Scenario 1, Manoeuvre 2. Average performance indexes.

<table>
<thead>
<tr>
<th>Strategy</th>
<th>$\bar{T}_R$ [s]</th>
<th>$RMS_u$</th>
<th>$RMS_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTG</td>
<td>36.7</td>
<td>0.0228</td>
<td>0.0286</td>
</tr>
<tr>
<td>NRP</td>
<td>5.14</td>
<td>0.0820</td>
<td>0.0237</td>
</tr>
</tbody>
</table>

Table 3: Scenario 1, Manoeuvre 3. Average performance indexes.

<table>
<thead>
<tr>
<th>Strategy</th>
<th>$\bar{T}_R$ [s]</th>
<th>$RMS_u$</th>
<th>$RMS_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTG</td>
<td>6.7</td>
<td>35.3265</td>
<td>1.5331</td>
</tr>
<tr>
<td>NRP</td>
<td>0.55</td>
<td>45.1805</td>
<td>0.0996</td>
</tr>
</tbody>
</table>

Table 4: Scenario 2, Vehicles joining. Average performance indexes.

<table>
<thead>
<tr>
<th>Strategy</th>
<th>$RMS_u$</th>
<th>$RMS_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTG</td>
<td>117.7</td>
<td>6.9109</td>
</tr>
<tr>
<td>NRP</td>
<td>115.3</td>
<td>5.8677</td>
</tr>
</tbody>
</table>

Table 5: Scenario 2, Vehicles leaving. Average performance indexes.

<table>
<thead>
<tr>
<th>Strategy</th>
<th>$RMS_u$</th>
<th>$RMS_y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CTG</td>
<td>109.6</td>
<td>7.1459</td>
</tr>
<tr>
<td>NRP</td>
<td>114</td>
<td>6.0608</td>
</tr>
</tbody>
</table>

Table 6: Scenario 3. Average performance indexes.
Figure 4: Scenario 3 (CTG with $\tau = 0.5, \lambda = 0.4$).

Figure 5: Scenario 3 (NRP with $\tau = 0.5, \lambda = 0.4, k = 4$).

4 OPTIMIZATION STRATEGY

As discussed in the previous section, in the design of an ACC system there is a trade-off between two contrasting requirements. On the one hand, the ACC system must provide a satisfactory performance in terms of safety and prompt answer to external disturbances. On the other hand, the ACC system must not require too large command activity, which may lead to a high consumption of fuel and/or electrical power.

To quantify the ACC performance we hereby consider the $RMS_y$ index defined in (5). To quantify the command activity we consider the $RMS_u$ index defined in (4). We would like to minimise both these coefficients but clearly this cannot be done, since these indexes are in contrast with each other. In other words, we are dealing with a multi-objective optimization problem.

This kind of problems can be efficiently solved considering a Pareto optimality criterion, (B. Brownstein, 1980). Let $RMS_y(C)$ and $RMS_u(C)$ be respectively the performance and command activity indexes of a given ACC controller $C$. A controller $C^1$ is said to dominate another controller $C^2$ if

\[
RMS_y(C^1) \leq RMS_y(C^2) \text{ and } RMS_u(C^1) < RMS_u(C^2)
\]

\text{or}

\[
RMS_y(C^1) < RMS_y(C^2) \text{ and } RMS_u(C^1) \leq RMS_u(C^2).
\]

A controller $C^*$ is said Pareto optimal if it is not dominated by any other one. In other words, no other controller exists that can be overall better than an optimal controller. If a controller is better than an optimal one with regard to a single objective (e.g., $RMS_y(C)$), it is certainly worse with respect to the other (e.g., $RMS_u(C)$). The set of Pareto optimal controllers define a curve in the performance index space called Pareto front (see the green line in Fig. 6).

Based on these concepts, the optimization strategy that we propose is as follows:

- Perform a Monte Carlo simulation, consisting of $N_f$ trials.
- In each trial:
  - Choose random values of the parameters $h$, $k$ and $\lambda$ (clearly, these values must be reasonable from a physical point of view). Each parameter 3-tuple defines a controller $C^i$, with $i = 1, \ldots, N_f$.
  - For the chosen parameter 3-tuple, perform $N_3$ simulations considering realistic road scenarios.
  - Compute the averages $RMS(C^i)_y$ and $RMS(C^i)_u$ of the $N_f$ values of $RMS(C^i)_y$ and $RMS(C^i)_u$.
- Considering that the pairs $(RMS(C^i)_y, RMS(C^i)_u)$, with $i = 1, \ldots, N_f$,
define points in the two-dimensional performance index space, construct the Pareto optimality front, using (6) to individuate those controllers that are not dominated.

Note that \( \tau \) and \( L_{\text{des}} \) are assumed fixed but they can be included in the optimization process without significant modifications.

Following this strategy, a Monte Carlo simulation was performed, consisting of \( N_f = 4760 \). In each trial, random values of \( h, k \) and \( \lambda \) were taken from the intervals \([0.1, 2], [2, 15] \) and \([0.4, 2] \), respectively (a uniform distribution was considered for all the three parameters). The values \( \tau = 0.5 \) s and \( L_{\text{des}} = 40 \) m were also assumed. For each random 3-tuple (corresponding to a randomly generated controller), \( N_S = 10 \) simulations were performed considering Scenario 3 (traffic flow with 10 vehicles in a line and 5 vehicles randomly joining or leaving the line). Then, the performance averages \( RMS(C^i) \), and \( RMS(C^u) \) were computed. Finally, the Pareto optimality front was constructed.

The results of this procedure are shown in Fig. 6. We can distinguish a number of randomly generated controllers (blue dots) and the Pareto optimal controllers (green line). These are compared with the tested NRP controllers (red dots). The performance in terms of spacing errors of a set of “standard” vehicles and a set of Pareto optimal vehicles is plotted in Figures 7 and 8, respectively.

These results show that an improvement of about 30% can be obtained using a Pareto optimal controller with respect to using a “standard” controller, indicating that the proposed optimization strategy can lead to high-performance ACC systems.

5 CONCLUSIONS

In this paper, a systematic simulation procedure has first been developed for comparing different Adaptive Cruise Control (ACC) policies. Then, a multi-objective optimization technique, based on a Pareto efficiency criterion, has been proposed and tested. The optimal controller designed by means of this technique showed better results when compared with the “standard” ACC policies. Future activities will focus on extending the numerical simulations considered in this paper to curve situations where the radar is unable to sense the vehicle in front for a while, comparing the comfort indexes of the policies, and on developing a user-friendly performance ACC optimization toolbox.
REFERENCES


