CSP Formulation for Scheduling Independent Jobs in Cloud Computing

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Keywords: Scheduling Algorithms, Cloud Computing, Job Scheduling, Resource Allocation, CSP Formulation.

Abstract: This paper investigates the use of Constraint Satisfaction Problem formulation to schedule independent jobs in heterogeneous cloud environment. Our formulation provides a basis for computing an optimal Makespan using job and machine reordering heuristics based on Min-min algorithm result. The combination of these heuristics with the weighted constraints allows improving the efficiency of the tree search algorithm to schedule jobs with considerable space search reduction. The proposed CSP model is validated through simulation experiments against clusters of 10 virtual machines. The results demonstrate that our model is able to efficiently allocate resources for jobs with significant performance gains between 18% - 40% compared to the Min-Min heuristic results to optimize the Makespan.

1 INTRODUCTION

Nowadays heterogeneous cloud computing is expanding its services to data-intensive computing on cloud platforms because each job (application) of users runs on a separate virtual machine. In these platforms, the jobs are independent and different from one another and it needs an optimal maximal completion time (Makespan). Hence the Scheduling process in cloud computing systems is useful for several different user needs. Static or dynamic heuristics are proposed for cloud to find an optimal solution to the scheduling. Static heuristics define a schedule at compiled time based on the knowledge of the processors availability and tasks to be executed. Dynamic heuristics, on the other hand, are applied when the tasks arrival time is not beforehand known and therefore the system needs to schedule tasks as they arrive (Barbosa and Moreira, 2009). The scheduling strategy defines the instants when the scheduling algorithm is called to produce a schedule based on forecasting resources performances and independent tasks to be executed. The aim of task scheduler in cloud computing environment is to determine a proper assignment of resources to the tasks of jobs to complete all the jobs received from clients. Large numbers of jobs scheduling heuristics are available for maximizing profit via resources allocation in cloud computing systems (Kuribayashi, 2011; Abirami and Ramanathan, 2012; Gouda et al., 2013; Iruigurala and Chatrapati, 2013).

The challenge that needs to be addressed is how efficiently schedule jobs in cloud computing based on the job completion time’s optimization to increase resource utilization. In this paper, we consider the problem of resource allocation in heterogeneous cloud environment. The proposed solution in this work is based on the computing power parameter for resources allocation in cloud environment. Clients in our case are jobs decomposed into various tasks where each task should be assigned to one of the resources, which is best suited for its execution to maximize the profit. The proposed approach uses constraint satisfaction problem formulation to schedule independent jobs in heterogeneous cloud environment. Our formulation provides a basis for computing an optimal Makespan using job and machine reordering heuristics based on Min-min algorithm result. The combination of these heuristics with the weighted constraints allows improving the efficiency of the tree search algorithm to schedule jobs with considerable space search reduction. The proposed CSP model is validated through simulation experiments. Our evaluation shows that the proposed approach can improve efficiency and effectiveness of heterogeneous cloud computing systems with significant performance gains between 18% - 40% compared to the Min-Min heuristic results to optimize the Makespan.

This paper is organized as follows. Related works...
2 RELATED WORK

There has been a large amount of work focusing on static scheduling approaches on cloud computing platforms and are currently prevalent in clouds. These approaches use static heuristics which are suitable for known prior time execution of jobs. Yuan et al. (Yuan et al., 2011) propose an intelligent scheduler which can handle heterogeneous resources, and be able to allocate resources according to user needs. The proposed intelligent scheduler shows an improved scheduling algorithm for making efficient resources allocation in cloud. Zhang et al. (Xie et al., 2012) uses the a dynamic constraint programming to solve the problem of virtual cloud resource allocation model. This approach takes into account both users’ QoS requirements and the cost of virtual cloud resources. The simulation results show that the proposed approach can efficiently allocate and manage the virtual resources of the cloud platform, and are in agreements with those of (Zhang et al., 2013). Goudarzi and Pedram (Goudarzi and Pedram, 2011), address the Service Level Agreements (SLA)-based resource allocation problem for cloud and a distributed solution for this problem is proposed. The response time of the request based on the different allocation of resources for different servers and the cluster is modeled and used in the profit optimization problem.

In (Santos et al., 2002), the authors propose a mathematical formulation for the resource allocation problem in clusters. The authors describe a method to find the best resource assignment in a cluster in the case that the application has certain resource requirements. Experimental results proved that the proposed method was able to realize best load balancing and reasonable resources utilization. In (Li et al., 2010), an adaptive resource allocation algorithm for the cloud system with preemptable tasks is considered. The proposed algorithms adjust the resource allocation adaptively based on the updated of the actual task executions. A. Kundu et al (Kundu et al., 2010) proposed the memory utilization method in cloud computing environment based on transparency. The proposed mechanism enables users to access memories depending on the predefined criteria. The resource allocation is made based on the selection criteria which will improve the efficiency of the cloud environment. The memory manager is responsible for allocating memory resources to the clients. The authors introduced a cloud service based memory utilization which is an effective mechanism for allocating memories in cloud computing environment. A scheduling algorithm named as Linear Scheduling for Tasks and Resources (LSTR) is designed in (Abiri and Ramanathan, 2012). This algorithm performs tasks and resources scheduling respectively. The combination of Nimbus and Cumulus services are imported to a server node to establish the IaaS cloud environment. The virtualization technique used with the scheduling algorithm will yield higher resource utilization, and improve the performance of the cloud resources.

Chen et al. (Chen and Tseng, 2012) introduced an Improved Load Balanced algorithm on the ground of Min-Min algorithm to reduce the Makespan and increase resource utilization. Another optimal joint multiple resource allocation method based on the above resource allocation model is presented in (Kuribayashi, 2011). The Author develops a resource allocation model for cloud computing environments, assuming both processing ability and bandwidth are allocated simultaneously to each service request and rented out on an hourly basis. Gouda et al. (Gouda et al., 2013) proposed a new approach that allocates resource with minimum wastage and provides maximum profit. This approach used priority algorithm which decides the allocation sequence for different jobs requested among the different users after considering the priority based on some optimum threshold decided by the cloud owner. An innovative admission control and scheduling algorithms for efficient resource allocation to maximize profit by minimizing cost and improving customer level is introduced in (Irugurada and Chatrapati, 2013). The authors showed that the algorithms work well in a number of scenarios and give the maximum profit among all proposed algorithms by varying all types of QoS parameters.

Silva et al. (Silva et al., 2008) presented a heuristic for optimizing the number of machines that should be allocated for processing an analytical task so that maximum speedup can be achieved within a limited budget. The traffic of web applications is dynamic and random; hence predicting the optimal number of machines for the completion of the client applications in real time and within budget is not a trivial task. Gomathi and Karthikeyan (Krishnasamy and Gomathi, 2013) proposed Hybrid Particle Swarm Op-
timization (HPSO) based scheduling heuristic to balance the load across the entire system while trying to minimize the makespan as well as to utilize the resources in an efficient way in cloud environment. In addition, the results are in agreement with those of (Guo et al., 2012).

In (Katyal and Mishra, 2014), authors have discussed a selective algorithm for resources allocation in cloud environment to end-users on-demand basis. The proposed algorithm is based on min-min and max-min conventional task scheduling algorithms. The selective algorithm uses certain heuristics to select between the two algorithms so that overall makespan of tasks on the machines is minimized. In (Han et al., 2013), the authors presented a QoS guided task scheduling model based on Sufferage-Min-Min heuristic algorithm. An efficiency improvement has been obtained by dividing the tasks and resources into two groups of high QoS level.

3 RESOURCES ALLOCATION STRATEGY

To meet the increasing computational requirements of scientist needs, cloud computing environments are promising platforms which ensure the resources allocation with high quality of service. Therefore the essential challenge of cloud computing scheduler is to provide an optimal scheduling of the jobs based on Makespan optimization to allocate jobs on suitable resources.

The scheduling problem of finding the optimal Makespan is a known NP-complete problem. The scheduling problem that we consider can be stated as follows. Let \( J = \{j_1, j_2, \ldots, j_n\} \) denote the set of jobs which are independent and let \( M = \{m_1, m_2, \ldots, m_n\} \) be the set of machines in the cloud computing environment. We assume that each machine can estimate how much time is required to perform each job. In (Minarolli and Freisleben, 2011), Expected Time to Compute (ETC) is an \( m \times n \) matrix, used to estimate the expected execution time of the job \( j_i \) on the machine \( m_i \). In ETC matrix, \( n \) is the number of jobs and \( m \) is the number of machines. One column of the ETC matrix contains the estimated execution time for a given job on each machine. Similarly one row of the ETC matrix contains the estimated execution time of a given machine for each job. Hence, for a given job \( j_i \) and a given machine \( m_i \), \( ETC_{ij} \) is the estimated execution time of job \( j_i \) on machine \( m_i \). For this problem, we assume take the hypothesis that the computing capacity of each resource and the running time of each job are known.

The Makespan is equal to maximum completion time of all jobs and can be estimated using the following equation (Eq.1):

\[
makespan = \max_{i \in \{1, \ldots, m\}} \left\{ \sum_{j \in J_{m_i}} ETC_{ij} \right\}
\]  

(1)

where \( J_{m_i} \) is the set of the jobs mapped on the machine \( m_i \).

4 OUR STATIC SCHEDULING AS CSP FORMULATION

In this study we start with a presentation to the practical part of our Constraint Satisfaction problem modelling for independent tasks scheduling to improve the Min-Min algorithm result. Thereafter we show that this problem can be described using this formalism using the Min-Min developed job and machine ordering heuristics. These heuristics aim to minimize the total completion time (Makespan).

4.1 SCSP Problem Formulation

The Constraint Satisfaction Problem model is widely used to represent and solve various AI related problems such as Scheduling or Optimization. A SCSP (Scheduling CSP) is defined by a set of jobs, a set of allowed estimated execution time of machines (the domain) is associated to each job and a Global Completion Time constraint (GCT). Solving a SCSP means finding an assignment for each job on one machine that satisfies a GCT constraint.

Based on the Min-min scheduling results, we present a formal model for minimizing the completion time obtained by this algorithm. Using this model, we formulate the static scheduling problem for independent job scheduling in heterogeneous environment as a constraint satisfaction problem (CSP). Our formulation provides a basis for computing an optimal completion time based on several CSP search strategies to refine the Makespan obtained by Min-min algorithm.

The SCSP consists of:

- \( N \) jobs \( J_1, J_2, \ldots, J_n \), and \( M \) machines \( M_1, M_2, \ldots, M_m \).
- \( D = \{D_1, \ldots, D_n\} \) is a set of \( n \) domains where each \( D_n = \{ETC_{n1}, ETC_{n2}, \ldots, ETC_{nm}\} \) is associated with \( J_n \).
- \( GCT_m = \sum_j ETC_{jm} < (1 - \alpha) \times C_{max} \) for all \( m \in \{1, \ldots, M\} \). GCT is the global completion time constraint on the machine \( m \). The parameter \( \alpha \in [0, 1] \) represents the improvement of the \( C_{max} \) obtained by the Min-Min algorithm. The search
Table 1: An ETC matrix example.

<table>
<thead>
<tr>
<th>Machines</th>
<th>$j_1$</th>
<th>$j_2$</th>
<th>$j_3$</th>
<th>$j_4$</th>
<th>$j_5$</th>
<th>$j_6$</th>
<th>Completion Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_1$</td>
<td>129</td>
<td>109</td>
<td>42</td>
<td>218</td>
<td>113</td>
<td>168</td>
<td>779</td>
</tr>
<tr>
<td>$m_2$</td>
<td>89</td>
<td>73</td>
<td>33</td>
<td>178</td>
<td>83</td>
<td>106</td>
<td>562</td>
</tr>
<tr>
<td>$m_3$</td>
<td>164</td>
<td>141</td>
<td>45</td>
<td>305</td>
<td>148</td>
<td>221</td>
<td>1024</td>
</tr>
</tbody>
</table>

Table 2: Execution results of Min-Min algorithm.

<table>
<thead>
<tr>
<th>Machines</th>
<th>$j_1$</th>
<th>$j_2$</th>
<th>$j_3$</th>
<th>$j_4$</th>
<th>$j_5$</th>
<th>$j_6$</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>$m_1$</td>
<td>0</td>
<td>0</td>
<td>218</td>
<td>113</td>
<td>0</td>
<td>331</td>
<td></td>
</tr>
<tr>
<td>$m_2$</td>
<td>0</td>
<td>73</td>
<td>33</td>
<td>0</td>
<td>0</td>
<td>106</td>
<td>212</td>
</tr>
<tr>
<td>$m_3$</td>
<td>164</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>164</td>
</tr>
</tbody>
</table>

space can be reduced by applying this parameter as mentioned in experimental section. If $\alpha = 0$ we use the $C_{max}$ of the Min-Min algorithm to avoid the systematic search assignment which explores systematically the whole search space. So using this GCT constraint, we minimize the maximum completion time for all machines. Note that the $C_{max}$ value is modified in the search process according to the obtained maximal completion time.

As example, consider a simple SCSP of 3 machines $m_1$, $m_2$ and $m_3$ and 6 jobs $J_1$, $J_2$, …, $J_6$. A scenario of ETC (duractions) is given in Table 1. First, Min-Min algorithm determines that the minimum completion time for $J_3$ will be achieved on $m_2$, and makes this assignment. After the first assignment, Min-Min algorithm continues to schedule the jobs $J_2$, $J_3$, $J_1$, $J_6$ and $J_4$ as well on $m_2$, $m_1$, $m_3$, $m_2$, $m_1$ machines respectively. Consequently, this algorithm finds that the maximum completion time is 331 seconds on $m_1$ as reported on Table 2. The scheduling, like the following can be expressed as SCSP:

- (06) Jobs $J_1$, $J_2$, $J_3$, $J_4$, $J_5$ and $J_6$ as variables
- (06) Domains $D_1 = \{89, 129, 164\}$, $D_2 = \{73, 109, 141\}$, …, and $D_6 = \{106, 168, 221\}$.

$GCT < (1 - \alpha) \times 331$

Most algorithms for solving CSPs search systematically through the possible assignments of values to variables. These algorithms seek any solution or all solutions of a CSP. Or they try to prove that no solution exists. In the present work, we have adapted the Forward Checking (FC) algorithm to find all SCSP solutions because the original algorithm aimed simply at finding a feasible solution. So we use FC algorithm with an incremental and modified maximal completion time process. However, the order in which jobs are considered for allocation on machines (instantiation) has a dramatic effect on the time taken to solve our SCSP, relatively to the order in which each job’s ETC are considered. There are general principles which are commonly used in selecting the jobs and their ETC values on the machines ordering. The job and machine ordering may be either a static or dynamic ordering according to the current state of the search. In our approach, we use both job and machine ordering heuristics. The job ordering uses the inverse job order obtained by the Min-Min algorithm. The machine ordering heuristic is based on the global completion time of each machine under hypothesis that all jobs are affected to the same machine.

The SCSP formalism allows defining the space of a combinatorial search as a tree. To cut branches in the search tree based on our adapted FC algorithm, we add job and machine ordering heuristics with the incremental maximal completion time as follow:

- The job ordering heuristic uses the order $J_4 \ll J_5 \ll J_3 \ll J_2 \ll J_1$ which is the inverse order obtained by Min-Min algorithm. (see Fig.1)
- The value (machine) ordering heuristic uses the completion time reported in Table 1. So we obtained $m_2 \ll m_1 \ll m_3$ for $J_4$. (see Fig.1)
- Modification of the maximal completion time $C_{max}$ in the GCT constraint in the search tree process.

Applying our search algorithm, more work per node but, presumably, the extra effort will be compensated by the reduction on the number of visited nodes. Fig. 2 shows an example of search space reduction obtained by our FC algorithm. As can be seen the use of the $C_{max}$ modification in the search process offers more reduction of the visited nodes to skip the instantiations with no possible $C_{max}$ improvement. For instance, the new obtained $C_{max} = 260$ allows to cut practically the whole branches in the rest of the search tree. So for this example, our algorithm visited only 117 nodes instead of 1093. For example, our algorithm FC has detected that the partial assignment with $GCT_{m_3} = 305$ is inconsistent with the global constraint ($GCT_{m_3} > C_{max} = 260$), and the algorithm will
therefore backtrack immediately.

In order to make our search algorithm more efficient, another preprocessing treatment can be added that initially introduces the $\alpha$ parameter value for the global completion time constraint. Hence, if we fix $\alpha = 0.2$, the space of a combinatorial search tree will be reduced to only 66 visited nodes (Fig. 3).

5 SIMULATION RESULTS

Simulation evaluations of our formalism have been
performed. The SCSP resolution uses the inverse of the obtained total order from the Min-Min algorithm to optimize the maximum completion time. The details of the simulation setting are presented in the following. In the literature, many heuristic-based techniques have been proposed for independent job scheduling in heterogeneous environment. The Min-Min heuristic algorithm is the most efficient and used one.

The proposed scheduling algorithm has been applied on simulated data, with 3 different types of ETC matrices up to 3 heterogeneous machines, and up to 20 randomly generated heterogeneous jobs used in (Ibarra and Kim, 1977). These different types of ETC matrices are generated based on the following properties (Inomata et al., 2011):

- **Job Heterogeneity** – represents the amount of variance among the jobs execution times for a given machine. The job heterogeneity is defined as: \( J(l) \): Job low and \( J(h) \): Job high.

- **Machine Heterogeneity** – represents the variation among the execution times for a given job across all machines. The machine heterogeneity is defined as: \( M(l) \): Host low and \( M(h) \): Host high.

- **Consistency** – an ETC matrix is said to be consistent (c) whenever a machine \( m \) executes all jobs faster than another machine and the inconsistency (i) if the machine \( m \) may be faster than another machine for some jobs and slower for others. Partially-consistent (s) matrices are inconsistent matrices that include a consistent submatrix of a predefined size and are a combination of consistent and inconsistent matrices (Minaroli and Freisleben, 2011). Instances are labeled as \( J(x)M(y)C(z) \) as follows: \( x \) indicates the job heterogeneity, \( y \) represents the machine heterogeneity and \( z \) shows the type of consistency.

Table 3 shows the results of the maximum completion times compared to the Min-Min algorithm for scheduling 20 jobs (\( J(l)M(l)c(c) \)) based on the \( C_{max} \) of this algorithm (\( \alpha = 0 \)). The results are based on the computation of job completion times across explored nodes. As can be seen the search space can be reduced by applying our heuristics where the total explored nodes are widely lower compared to the total nodes of the search space. Moreover, we obtain minimal completion times with the improvements 9%, 7%, 18% and 16% for 2, 3, 4 and 5 machines respectively.

Table 4 reports the speed-ups for the same instance with different values of \( \alpha \) parameter. The efficiency observed is very good where the computation time’s decrease for all instances compared to the above results from 1 to 5 machines. Also, it is observed that for 6, 7, 8, 9 and 10 machine instances, the execution times are considerably reduced. For example, for the last instance (20 jobs on 10 machines) the execution time 2748 seconds and is reduced to 3.79 seconds with \( \alpha = 40.45 \). It is interesting to note that the execution time is reduced by 99.85% for 10 machines and we note that the resulting Makespan of Min-Min heuristic is constant starting from 571 because the Min-Min algorithm does not maximize the use of resources. Overall, our results demonstrate that where there is a consistency for low jobs, and having large number of machines, we obtains an efficiency superior to 95% with \( \alpha \geq 30 \% \).

Finally, Table 5 presents the results of the completion times compared to Min-Min heuristic using maximal values of the parameter \( \alpha \). It is interesting to note that our heuristic outperforms the Min-Min algorithm in all cases (job heterogeneity, machine heterogeneity and consistency) by obtaining the minimal Makespan. Clearly, with the use of an adequate \( \alpha \) value, our algorithm performs well in all cases and reduces the tree space search and the execution time to schedule these instances from many hours to a few minutes. A remark has to be made on the computation time irregularity observed for the inconsistent cases for high jobs and low machines. So a major drawback of \( \alpha \) values determined by our simulations is that the execution times for the same scheduling problem can be very different from an execution to another for different types of ETC matrix up to 10 heterogeneous machines, and up to 20 randomly generated heterogeneous jobs of the same instance category. An important point to notice is that our approach cannot considered as very effective for large scheduling problems. To be efficient we remedied the poor performance of
Table 4: The computation time reduction using different values of $\alpha$ parameter for 20 jobs.

<table>
<thead>
<tr>
<th>Machines</th>
<th>Time (second)</th>
<th>Total nodes</th>
<th>Explored nodes</th>
<th>$\alpha$ (%)</th>
<th>$C_{max}$ Min-Min Algorithm</th>
<th>Proposed approach</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>01.53</td>
<td>2097151</td>
<td>24990</td>
<td>10</td>
<td>1074</td>
<td>973</td>
</tr>
<tr>
<td>3</td>
<td>11.50</td>
<td>5.23E+09</td>
<td>266832</td>
<td>8</td>
<td>744</td>
<td>692</td>
</tr>
<tr>
<td>4</td>
<td>39.75</td>
<td>1.47E+12</td>
<td>1167804</td>
<td>18</td>
<td>684</td>
<td>562</td>
</tr>
<tr>
<td>5</td>
<td>49.73</td>
<td>1.19E+14</td>
<td>1683660</td>
<td>15</td>
<td>571</td>
<td>480</td>
</tr>
<tr>
<td>6</td>
<td>51.92</td>
<td>4.39E+15</td>
<td>1945518</td>
<td>23.5</td>
<td>571</td>
<td>434</td>
</tr>
<tr>
<td>7</td>
<td>89.72</td>
<td>9.31E+16</td>
<td>3690876</td>
<td>30.29</td>
<td>571</td>
<td>398</td>
</tr>
<tr>
<td>8</td>
<td>27.67</td>
<td>1.32E+18</td>
<td>1215384</td>
<td>33.97</td>
<td>571</td>
<td>377</td>
</tr>
<tr>
<td>9</td>
<td>10.09</td>
<td>1.37E+19</td>
<td>469152</td>
<td>38.01</td>
<td>571</td>
<td>353</td>
</tr>
<tr>
<td>10</td>
<td>03.79</td>
<td>1.11E+20</td>
<td>185420</td>
<td>40.45</td>
<td>571</td>
<td>340</td>
</tr>
</tbody>
</table>

Table 5: Makespan results for all heterogeneity and consistency cases.

<table>
<thead>
<tr>
<th>Instance</th>
<th>Time (s)</th>
<th>$\alpha$ (%)</th>
<th>$C_{max}$ Min-Min Algorithm</th>
<th>Proposed approach</th>
</tr>
</thead>
<tbody>
<tr>
<td>J(l)M(l)C(c)</td>
<td>03.79</td>
<td>40</td>
<td>571</td>
<td>340</td>
</tr>
<tr>
<td>J(l)M(h)C(c)</td>
<td>35.1</td>
<td>32</td>
<td>17271</td>
<td>11627</td>
</tr>
<tr>
<td>J(h)M(l)C(c)</td>
<td>1029.4</td>
<td>13</td>
<td>10640</td>
<td>8167</td>
</tr>
<tr>
<td>J(h)M(h)C(c)</td>
<td>36.3</td>
<td>37</td>
<td>683030</td>
<td>427236</td>
</tr>
<tr>
<td>J(l)M(l)C(i)</td>
<td>1290.4</td>
<td>10</td>
<td>442</td>
<td>397</td>
</tr>
<tr>
<td>J(l)M(h)C(i)</td>
<td>62.7</td>
<td>35</td>
<td>22947</td>
<td>14734</td>
</tr>
<tr>
<td>J(h)M(l)C(i)</td>
<td>1304.2</td>
<td>38</td>
<td>11495</td>
<td>7109</td>
</tr>
<tr>
<td>J(h)M(h)C(i)</td>
<td>1265.9</td>
<td>38</td>
<td>1068180</td>
<td>654517</td>
</tr>
<tr>
<td>J(l)M(l)C(s)</td>
<td>7.3</td>
<td>18</td>
<td>341</td>
<td>278</td>
</tr>
<tr>
<td>J(l)M(h)C(s)</td>
<td>6.37</td>
<td>16</td>
<td>20025</td>
<td>14734</td>
</tr>
<tr>
<td>J(h)M(l)C(s)</td>
<td>3.86</td>
<td>22</td>
<td>10286</td>
<td>6992</td>
</tr>
<tr>
<td>J(h)M(h)C(s)</td>
<td>8.82</td>
<td>22</td>
<td>969294</td>
<td>654517</td>
</tr>
</tbody>
</table>

our FC search algorithm by avoiding the recursive tree traversal based on a parallel computation for global completion time constraint. This parallelization uses decomposition methods which distribute the search tree at a particular depth level (Habbas et al., 2005).

6 CONCLUSION

In this work, a static scheduling problem in cloud environment based on a combination of a CSP formulation and Min-Min job ordering heuristic. To improve the Min-Min algorithm result a refinement process uses the incremental maximal completion time as weighted global constraint.

We used various ETC matrixes to investigate efficiency of our approach based on different degrees of job and machine heterogeneities and consistencies. The results indicated that our CSP solver provides to reach an optimal completion time in very short time for small instances compared to Min-Min algorithm. However, our approach cannot considered as very effective for large instances.

For future work, there are still some aspects for further investigation in our CSP job scheduling algorithm especially for parallel CSP solver using decomposition strategy of the search tree in cloud environment and prediction model for the job completion time distribution that is applicable to making decisions in scheduling.

REFERENCES


Applications Workshops (WAINA), 2012 26th International Conference on, pages 1316–1319. IEEE.


