1 STAGE OF THE RESEARCH

Current work is at the third (final) year of the planned research period. The first year consisted of the formulation of the problem and the study of existing work in order to discover possible solutions. It concluded with a thorough literature review, an experimental evaluation of the state of the art technologies, suitable for the continuous-time (CT) aspect of our hybrid modelling approach, and an outline of objectives with a research path that linked the gathered knowledge together.

The second year has focused on the integration of the tools, discovered in the first year, and the Rodin platform for Event-B modelling. Based on the chosen research path – integrating Event-B and CT aspect via co-modelling and simulation – first, a widely used standard for co-simulation has been selected. Further work evolved around the study of the standard and co-simulation principles, the definition of the simulation semantics for both Event-B and CT models and the implementation of a proof of concept using a trivial hybrid system model.

The third year focuses on the technical aspects and includes formalisation of the simulation algorithm and its semantics, experimentation with alternative semantics, implementation of the actual co-simulation tool called Rodin Multi-Simulation (RMS) and its validation using a number of hybrid system examples from different domains.

2 OUTLINE OF OBJECTIVES

The foremost objective of this research is to develop a solid framework that is capable of formal modelling, verification and simulation of hybrid (also known as cyber-physical) systems with respect to their discrete and continuous aspects. Our attention is concentrated on an open and extensible platform, suitable for both academic research and industrial application, and a simple, yet powerful formal language that fits well with the task of safety-critical systems development and supports essential features of abstraction, modular development and refinement, as well as facilitates the difficult task of formal verification and validation.

The main goal is broken down into a number of subgoals:

- To develop an open integrated solution for the formal modelling, verification and co-simulation of discrete-event (DE) models of controllers and the interacting physical environment;
- To provide a generic simulation orchestration mechanism called master that can simulate deterministically an arbitrary number of interconnected DE and CT subsystems;
- To produce an open and extensible co-simulation tool, which is seamlessly integrated into an existing formal modelling framework, is efficient for the simulation-based analysis of real-scale systems and is simple and easy to use;
- To conduct a comparison between the proposed co-simulation approach and traditional simulation techniques;
- To create a development pattern for hybrid systems based on the produced co-modelling and co-simulation toolset.

3 RESEARCH PROBLEM

The heterogeneous nature of hybrid systems, which consist of interleaving computational and physical domains, often represented by a hierarchy of different components, makes it difficult to use a single development tool (Lee, 2008). It is also coming into practice that an application of some formal method is required for the rigorous analysis and assurance of the safety of a developed system (Gnesi and Margaria, 2013). This leads to a evident conclusion that a means of integrating the existing domain-specific tools and technologies with the emphasis on formal methods is required (Marwedel, 2010). In this work we focus on the idea of integrating formal modelling/verification
4 STATE OF THE ART

The existing work and literature includes a number of examples of the integration approaches. The most notable are the co-simulation between Simulink and clocked data flow in Signal (Tudoret et al., 2000), the DESTECS project for modelling the DE aspect of a hybrid system in VDM formal language and CT aspect in the 20-sim physical modelling environment (Fitzgerald et al., 2010), and the Ptolemy project that focuses on the heterogeneous composition of components and different models of computation that define particular semantics (Brooks et al., 2005). Although these technologies are very promising, they do not address the key problem of the lack of integration between multiple development approaches and environments. To tackle this issue we propose a generic integration solution, which is based on a widely supported tool-independent standard for model exchange and co-simulation called Functional Mock-up Interface (Blochwitz et al., 2011), an open physical modelling language Modelica (Fritzson and Engelson, 1998) and a powerful and open toolset Rodin (Abrial et al., 2010) for the rigorous analysis of Event-B (Abrial, 2010).

4.1 Event-B

Event-B is a formal method for modelling and rigorous analysis of complex systems. The language is inspired by Action Systems (Back, 1990) and B Method (Abrial et al., 1991), and is based on the simple mathematical formalisms of set theory and first-order logic. A system is modelled in Event-B as a collection of state variables and guarded events that act upon those variables, while the system properties are modelled by invariants that must hold and can be verified by deductive proof. The key feature that distinguishes Event-B from other methods is the iterative modelling via proof-based refinement, which lets a modeller introduce the details and increase the complexity of the model in small steps (refinements), whilst ensuring the correctness of the model with respect to its specification through refinement proofs. The other key feature is a powerful and extensible Rodin platform, which offers automatic proof obligation generation and automatic/interactive proving capabilities, and, thanks to a collection of available plug-ins, provides additional automatic provers, a mechanism for extending the existing language by defining new theories (Butler and Maamria, 2013), model checking (Leuschel and Butler, 2008), modular development via decomposition (Silva et al., 2011), UML modelling (Snook and Butler, 2008), code generation (Edmunds and Butler, 2011), etc.

A typical model in Event-B consists of a static context, which defines the constants, sets and axioms, and a dynamic machine, which contains the variables and invariants that model system properties, and the events that model the behaviour. An event may have a number of input parameters, guards (event-enabling predicates) and actions (variable modifiers), which all happen at the same time (atomically) as the event gets executed. If a number of events are enabled, execution is performed non-deterministically.

Besides the machines and context there may be the following relations: a machine can see a context to be able to use its definitions, a context can extend another context with new static information, a machine can refine another machine to introduce new data (vertical refinement) or behaviour (horizontal refinement).

4.2 Modelica

Modelica is an open-source object-oriented language for modelling and simulation of complex heterogeneous systems that may span a number of domains. The language was designed to allow the tools to automatically generate efficient simulation code without the specification of causality (relationship between inputs and outputs). This enables high reusability and readability of declarative (acausal) models, as opposed to context-sensitive procedural approaches where causality is fixed (e.g. Simulink). On the other hand equation-based models are not oriented to solution and therefore require more sophisticated symbolic analysis capabilities from the tools. Nevertheless, Modelica is largely supported by the open-source and commercial simulation tools, offers numerous domain-specific libraries of reusable components and continuously evolves as a language. Following is a list of the basic modelling constructs in Modelica (Association et al., 2000):

- Basic data type components, such as Real, Integer, Boolean and String;
- Structured components (classes), to enable hierarchical structuring;
• Component arrays, to handle real matrices, arrays of submodels, etc.;
• Equations and/or algorithms (assignment statements);
• Connections;
• Functions.

In the context of hybrid systems a particularly interesting feature of the language is the capability to model intermixed continuous and discrete dynamics. The discrete and sampled systems can be modelled in Modelica using discrete state variables (whose values are changing only at specific points in time) and a when clause that activates equations instantaneously on the event occurrence. A built-in function sample(start, interval) can be used as a condition of a when clause to trigger it when time = start + n × interval, n ≥ 0, which is particularly useful for modelling sampling. Some of these constructs are demonstrated in a hybrid model of the classical example of a bouncing ball that involves both the continuous motion of the ball and discrete changes in velocity at the bounce times:

```model BouncingBall
  parameter Real g=9.81;
  parameter Real c=0.50; // elasticity constant
  Real height(start=0); // height above ground
  Real v(start=10); // velocity
  equation
    der(height) = v; // derivative of v
    when height<0 then // when bounce happens
      reinit(v, -c*v); // reset v to -c*v
    end when;
end BouncingBall;
```

### 4.3 Functional Mock-up Interface

Functional Mock-up Interface (FMI) is an open standard for tool-independent model exchange and co-simulation. It provides a cross-platform API that comes as a specification document, a set of C header files to be implemented by an individual model and a model description file schema for describing state variables and capabilities of the model (Blochwitz et al., 2012). The model code is built as a dynamic/shared library for the target platform and bundled with the model description file into a Functional Mock-up Unit (FMU) that can be used for modelling and simulation in any FMI-compliant tool.

The aspect of the standard that describes Co-Simulation is designed for coupling models and simulators in a co-simulation environment, where each subsystem called Slave (an FMU representing either a model or a coupled simulation tool) is solved by its individual solver. The simulation is coordinated by the algorithm called Master (see Figure 1), which breaks the simulation interval [t<sub>start</sub>, t<sub>stop</sub>] into discrete communication steps t<sub>c</sub>→t<sub>c+1</sub>, at which it synchronises Slaves and performs the data exchange. The standard is designed to support a number of FMU capabilities and a general class of simulation algorithms, although it does not define the algorithm itself.

![Figure 1: FMI master-slave architecture.](image)

### 5 METHODOLOGY

Our approach of integrating simulation into the Rodin platform is comprised of several steps. First, we are defining the semantics of a simulation step of both discrete (Event-B models) and continuous (FMUs) components, and derive a simulation API along with a meta-model of the simulation composition graphs, according to the FMI specification. Then, specifically for the Event-B components, we design a mapping from Event-B modelling constructs to our FMI-compliant API. Next, we define our simulation master algorithm. The final (current) stage consists of the implementation of all developed ideas into a Rodin plug-in and the following empirical validation on a number of case studies.

#### 5.1 Semantics

In our co-simulation approach, which is based on the master-slave architecture of the FMI for Co-Simulation v1.0 standard (MODELISAR, 2010), we distinguish the simulation step of a DE component, represented by an Event-B machine, and a CT component that denotes an FMU.

The semantics of a continuous step (CStep) is defined by the FMI standard and the underlying FMU’s simulator, which is responsible for simulating the model for a specified period of time.

The discrete step (DStep) is defined by a single or a number of Event-B events, executed sequentially...
according to the language semantics. To avoid the explicit definition of the constituting sequence of events we introduce the notion of a Wait event, which signifies the end of the step. Essentially, Wait must be the only executable event(s) at synchronisation points, whereas the sequence of events within a step can be arbitrary and is defined by the individual model’s logic. This offers a generic simulation solution and a flexible model of refinement of the DE components.

The state of an individual component with respect to simulation time can be defined as a function:

\[ F: Time \rightarrow V \]

(1)

where \( V \) is the state of the component’s internal variables. The evolution of each variable and its component over time can be represented on a graph:

![Graph of state over time](image)

Figure 2: The state of a slave over time.

where \( g \) is a state function defined over time interval \( time \ldots time + t \). If \( t \) equals the communication step of the master, the simulation semantics of a continuous component can be formally defined using Event-B notation as follows:

```
machine C
variables F, time

event CStep =
  any i, t, g
  where
  g \in [time \ldots time + t] \rightarrow V
  g(time) = F(time)
  P(g,i,F,time,t)
  then
    time := time + t
    F := F \cup g
```

where parameter \( i \) is the component’s inputs and \( P \) is the model properties, or properties that \( g \) must satisfy. This formal model specifies the semantics of CT components, as it depends on time and the continuous function \( F \). For the DE components we derive a simpler definition that depends on the input and internal variables:

```
machine D
var V, O

event DStep =
  any i
  where
    i \in T
    V, O := S(V, O, i)
```

where \( i \) is the input, \( O \) is the internal variables that are also outputs, and \( S \) is a discrete state function.

Besides the notion of a Wait event we introduce a similar concept of a Read event, which maps the component’s inputs to Event-B input parameters and enables the exchange of signals between DE and CT components. Hence, Wait and Read events are the only meta-constructs, required to provide the defined co-simulation semantics.

### 5.2 Event-B Mapping

A representative mapping of an Event-B machine that models a water tank controller (controls the water level in a leaking tank by switching the input valve) to a discrete simulation component is demonstrated below.

```
machine tankController0
variables valve

events
  SwitchOn \equiv \text{any } l \text{ where } l < LT
  then
    valve := on end
  NoSwitch \equiv \text{any } l \text{ where } l \geq LT \land l \leq HT
  then
    skip end
  SwitchOff \equiv \text{any } l \text{ where } l > HT
  then
    valve := off end
end
```

All three events of this abstract machine would map to Read events and Wait events, thus simulation will progress by executing one of the events, depending on the value of \( l \), which is an input signal of the sensed water level from the environment.

The model can be easily refined whilst keeping simulation semantics consistent with the abstract model. As new events are introduced, the Read and Wait events become distinct:

```
machine tankController1 refines tankController0
variables valve, level, state

events
  ReadLevel \equiv \text{any } l \text{ where state = 0}
  then
    level := l end
  DecideOn \equiv \text{where state = 1 \land level < LT}
  then
    state := 2 end
  DecideSkip \equiv \text{where state = 1 \land level \geq LT \land level \leq HT}
  then
    state := 3 end
  DecideOff \equiv \text{where state = 1 \land level > HT}
  then
    state := 4 end
  SwitchOn refines SwitchOn \equiv \text{witness } l = \text{level}
  then
    valve := on end
```
In the refinement the ReadLevel becomes a Read event and SwitchOn, NoSwitch and SwitchOff – Wait events. The flexibility of marking same/multiple events as Read or Wait events enables simulation of control behaviour alongside its refinement and verification, ensuring that developed models are correct by construction and interact with the environment as expected.

5.3 Master Algorithm

Our master is a fixed step size generic algorithm, based on a two-list simulation approach from the VHDL (Mazor and Langstraat, 1993) and designed to comply with the FMI standard, i.e. developed to reflect the recommended use of the FMI API. It divides the simulation into discrete steps and communicates the data between components at the step boundaries. At each simulation cycle an update list is checked for components that need to be evaluated according to their step size and progression in time. If a component is found in the update list, it is put into an evaluation list. All evaluated components then exchange the data and advance their simulation state. The outline of the algorithm (with API calls) is as follows:

1. Instantiate all components:
   Component.instantiate()

2. Initialise all components:
   Component.initialise(startTime, stopTime)

3. Set the simulation time to a start time, put all components into the update list (“time zero initialisation”) and begin the simulation loop.

4. Check the update list for the components to be evaluated at the current simulation time and put them into the evaluation list.

5. For each component in the evaluation list, write all outputs:
   Component.writeOutputs()

6. Read all inputs:
   Component.readInputs()

7. Perform the step:
   Component.doStep(time, stepSize)

8. Put evaluated components back to the update list increasing the next evaluation time by the corresponding step size.

9. If the time has reached the stop time then stop, otherwise progress the time and go back to step 4.

10. Terminate components:
    Component.terminate()

The step size is defined for each component individually at the master level, hence Event-B models do not have to be timed. In addition, the master uses our generic API and therefore does not rely on a particular implementation of the individual component type, making it possible to extend co-simulation capabilities by introducing other types of components without the need to modify the algorithm.

5.4 Co-simulation Environment

Our simulation environment RMS (Rodin Multi-Simulation) is currently being developed. It already implements the described master algorithm and an extensible component meta-model that supports both Event-B and FMI components. The environment enables import, configuration and diagrammatic composition of components via input/output ports, controlled simulation and real-time visualisation of the signals, simulation trace recording/playback, deadlock and invariant checking via ProB tool (Leuschel and Butler, 2008). The preliminary work and experiments are explained in more detail in (Savicks et al., 2014).

6 EXPECTED OUTCOME

The goal of this work is to provide a development solution, targeted at hybrid systems, that combines formal modelling, verification and physical simulation, in order to ensure the safety and reliability of constructed systems. We expect to implement and offer modellers a tool that enables both the rigorous analysis (using Event-B) of the discrete aspect of hybrid systems and the simulation-based analysis of the interaction with the physical environment. We hope that by integrating simulation and formal verification technologies system engineers will benefit in terms of clearer understanding of the intricate interactions between the discrete and continuous aspects of a hybrid system, be able to formally verify its safety and reliability properties and to analyse its behaviour in a realistic model of environment. This should ultimately reduce the cost and time of the development and improve the quality of implemented embedded software.
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REFERENCES


