Secure Key Distribution based on Meteor Burst Communications

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Abstract: The paper discusses possibility of secure encryption keys distribution based on stochastic properties of meteor burst radio propagation. Unlike wireless key distribution, this method provides much greater channel length and key distribution distances, which is up to 2000 km. Another important advantage is an ability of meteor burst communications to operate in severe climate, under conditions of polar and other remote areas. The paper also considers various physical factors ensuring stochastic variations in characteristics of received radio signal, which are applicable for the secret key generation. The simulation results revealing the most important randomizing factors within meteor burst channel are presented.

1 INTRODUCTION

Over the last 25-30 years there is an active discussion in the publications of a large number of researchers about the possibility of secure key distribution based on stochastic properties of physical layer of data channels. Historically, the first method to realize this idea was the quantum key distribution proposed in the mid-1980s (Bennett, 1984). Ten years after, the idea of encryption keys distribution based on physical properties of reciprocal radio channels was proposed (Hershey, 1995). In many subsequent works, such as (Mathur, 2008; Madiseh, 2008; Madiseh, 2009), the multipath fading effect within indoor environment and its unpredictability have been considered as a common source of randomness to create a shared secret key at two parties (say, Alice and Bob). The channel reciprocity ensured symmetry of the key instances at Alice and Bob. The secret key was generated based on random signal characteristics (e.g. phase, amplitude and quadrature components), whose measurements were identical at both sides of the link. A rapid spatial decorrelation of multipath signal characteristics ensured inability of key interception even at small spatial diversities.

A short-range radio is the main drawback of multipath channel, which typically limits key distribution distances by 1 km only. However, the years of research and development in the field of meteor burst communication systems have shown that, like the multipath channels, the meteor radio propagation has all properties necessary for the key distribution.

The purpose of this paper is to show that the stochastic properties of meteor radio propagation (MRP) provide encryption keys generation and their secure distribution over the distances up to 2000 km.

2 METEOR PHENOMENA AND “METEOR CRYPTOGRAPHY”

Every second a countless number of meteor particles invade into the Earth's atmosphere at the speed of 12 to 72 km/s. These particles are so small that their weights range from 0.01 mg to several grams only. Under the influence of a high atmospheric drag the meteor particles burn at altitudes of 70-120 km leaving ionized trails behind them. These trails scatter incident radio waves acting as natural retranslators. Thus, emitted by Alice radio signal is reflected from a meteor trail and will be eventually received by Bob. So, a meteor burst communication link is established between Alice and Bob. In fact, only a small part of all meteor trails is suitable for the communication between the given locations of Alice and Bob to arise. To be more specific, the communication will come only if a trail provides...
desired geometry of scattering and sufficient signal strength.

Typically, only 50-350 suitable meteor trails are observed within 1 hour. This is a small number, which naturally leads to a small (a few hundreds bps) capacity of meteor burst communication systems. However, the meteor burst channel (MBC) has a number of particular properties that can be used for the secure generation and distribution of encryption keys. According to experimental studies (Desourdis, 1993) the MBC can be considered as a reciprocal channel with a satisfactory approximation. Just like in the case of multipath fading channels, it allows detection of identical values of random signal characteristics both by Alice and Bob.

The scattering by meteor trails can be approximately regarded as a specular reflection from a certain point $M$ lying on its surface (McKinley, 1961). This leads to a limited area around the communication point where the scattered signal can be received. Obviously, the strongest signal will be received at the direction of specular reflection and a rapid spatial decorrelation will be observed with the rise of diversity. Such decorrelation makes key interception almost impossible at practice.

Finally, a significant randomness exists within the MBC. The invasion of meteor particles into the Earth's atmosphere along with its ablation and formation of ionized trail, emergence of the reflecting point $M$ are mostly unpredictable processes. Specifically, the coordinates of the reflecting point $M$ are also random. This causes randomness of the $A-M-B$ path for the signal transmitted from Alice to Bob. As a result, random values of the carrier phase $\varphi$, time delay $\tau$ and amplitude $U$ will be detected at the signal receiving. These values should be identical at both sides of the link due to channel reciprocity: $\{U_{AB}, \varphi_{AB}, \tau_{AB}\} = \{U_{BA}, \varphi_{BA}, \tau_{BA}\}$. Thus, the MBC channel can be considered as a common source of randomness for Alice and Bob. This allows them to create a shared secret key by performing at both sides a series of measurements of random characteristics of radio reflections from the meteor trails. The authors called such an approach to encryption keys distribution the “meteor cryptography”.

3 PREVIOUS WORKS

The concept of meteor cryptography was proposed by researchers from Kazan Federal University (Russia) in 2001. This idea was preceded by almost 50 years of active theoretical and experimental studies in the field of meteor radio propagation and system development for the meteor burst communication and time synchronization. As a result of this hard work, the prototypes of meteor burst synchronization systems with sub-nanosecond accuracy were created (Sidorov, 1993; Korneyev, 2003; Korneyev, 2007). Such accuracy allows synchronous detection of received signal carrier phase at both sides of the meteor burst communication link. It was experimentally shown (Desourdis, 1993) that the phase values measured at both sides of the link are very close to each other.

It should be noted, that in typical meteor burst communication link signal propagates over the distances of hundreds kilometers. Besides, due to randomness of coordinates of the reflecting point at meteor trail the propagation path is also random. As a result, the carrier phase of received signal is a random variable which could be used for the encryption keys generation.

In previous works (Karpov, 2005; Sidorov, 2007) on meteor cryptography the main efforts were focused at the discussion of technical aspects of implementation of encryption key distribution systems. However, we feel that a very important part of the research work has been missed. It was not taken into account that the meteor burst communications is a very specific technical field familiar only to a limited number of specialists. The basic principles of meteor cryptography were not disclosed properly in the prior works. In particular, the sources of randomness within the meteor burst channel have not been indicated.

The following sections of this paper are devoted to discussion of basic mechanisms of the MBC randomness. A significance of different randomizing factors will also be investigated for the values of carrier phase $\varphi$ and propagation delay $\tau$ of meteor radio reflections.

4 RESEARCH METHODS

Meteor burst channel is difficult in understanding. Its performance is influenced by many factors of different nature: by equipment, astronomical, atmospheric conditions, etc. All these factors have a complex impact on the measured signal parameters.
Unfortunately, we can’t separate them in an experiment, which makes a study of individual influence of each randomizing factor impossible. Moreover, the scattering from meteor trails takes its place at random coordinates at altitudes of 80-110 km. Thus, immediate observation and control of propagation of radio signals is very difficult to implement. For this reason, all the experimental study of meteor burst propagation is based on indirect measurements only.

That’s why simulation is the only solution. The simulation makes it easy to enable and disable various randomizing factors while monitoring changes in the statistical characteristics of received signal parameters.

The vast majority of MBC simulation models is based on simple mathematical models developed in the 1950-60s (McKinley, 1961). These models can’t simulate complex electrodynamic effects taking place at the scattering off ionized meteor trails. At the same time, these effects are vital for the studies of encryption keys distribution. The KAMET simulation model (Karpov, 2001) based on rigorous diffractional theory of radio waves scattering (Khuzyashev, 1984) includes and adequately reproduces all necessary effects.

We used the Moscow-Kazan MBC link for the simulation purposes. The following technical specifications were used during simulation:

- Link length: 720 km;
- Carrier frequency: $f = 50$ MHz;
- Transmitted power: $P_T = 2000$ W;
- Required signal-to-noise ratio: 20 dB;
- Threshold level: $U_0 = 0.5$ μV (which corresponds to SNR=20 dB);
- Standard deviation of turbulent wind velocity: $\sigma_V = 25$ mps.

5 BASIC RANDOMIZING FACTORS OF METEOR BURST CHANNEL

An analysis of meteor radio propagation reveals following basic randomizing factors in the meteor burst channel:

1. Random spatial orientation of each meteor trail;
2. Random coordinates $M(x,y,z)$ of the reflecting point on the meteor trail;
3. Random mass $m$ of meteor particle which produces the ionized trail;
4. Random moment of occurrence of signal fading (Weitzen, 1987);
5. Random direction and magnitude of the turbulent wind velocity blowing in the vicinity of the reflecting points of meteor trail (Weitzen, 1987);
6. Channel noise and measurement errors.

We used the Pearson correlation coefficient $R_1$ between the adjacent measurements of observable signal parameter as a measure of randomness. Since it characterizes statistical relationship between the parameters of two successively detected meteor radio reflections, the value of $R_1$ can be considered as an indicator of predictability of generated keys. We consider the carrier phase $\phi$ and propagation delay $\tau$ of received signal as observed random parameters implied for the key generation.

The $\tau$ variable is mainly determined by the geometric path of received signal:

$$\tau = \frac{(AM + MB)}{c}$$

In formula (1) $c$ means speed of light, $AM$ and $BM$ are the distances between the reflecting point of meteor trail and communication points of the link. Therefore, randomness of the $\tau$ variable is almost completely determined only by the second randomizing factor (random coordinates of the reflecting point). Factor no.5 also gives a small contribution. However, the total shift of the reflecting point made by turbulent winds during signal detection rarely exceeds 100 m (or several $\lambda$). This is much lesser than the contribution of geometric path (1), which typically is of hundreds kilometers or more.

The variable $\phi$ consists of two components: the path length shift $(2\pi f \cdot \tau)$ and polarization phase shift added by the scattering of radio wave from a meteor trail. For this reason, the phase value $\phi$ is affected by greater number of randomizing factors. For example, factor no. 5 is very significant for the carrier phase and we should not neglect it. This is due to wind shift of the reflecting point at several $\lambda$ leads to large changes in the carrier phase.

6 SELECTION OF MEASUREMENTS

During the detection of meteor radio reflection its amplitude and phase are changing in time. These
changes are recorded as the Amplitude-Time Response (ATR) and the Phase-Time Response of radio reflection, respectively. In fact, only approximate channel reciprocity is observed for the meteor burst propagation. Calculations and experiments show that the Phase-Time Response $\phi_{AB}(t)$ recorded in point $B$ is slightly different with the Phase-Time Response $\phi_{BA}(t)$ recorded in $A$. Such difference occurs due to non-absolute reciprocity of MBC. Figure 1 shows an example of simulated Phase-Time Responses observed synchronously in communication points $A$ and $B$. We should outline that no noise effect was enabled for these curves. Figure 2 shows differential PTR for the above example, which indicates presence of some channel non-reciprocity. This reciprocity is a consequence of non-identical scattering of radio waves transmitted by the opposite communication points. It occurs every time the reflecting point is located non-symmetrically relative to the communication points $A$ and $B$.

In this approach, only a single value of the carrier phase $\phi$ and propagation delay $\tau$ should be extracted from each meteor radio reflection.

![Figure 1: Examples of Phase-Time Responses of the same meteor radio reflection observed at both sides of the link](image1)

The profiles of PTR and differential PTR are unpredictable and individual for every specific meteor radio reflection. For the keys generated in points $A$ and $B$ to be identical, the moment of minimum absolute value of channel non-reciprocity should be used to make phase measurements. Such point ($t^* = 0.13s$) is marked in Figure 2 with a circle.

![Figure 2: Example of MBC non-reciprocity.](image2)

7 SIMULATION RESULTS

To evaluate significance of various randomizing factors, a simulation of the test Moscow–Kazan radio link has been carried out. Step by step, we reduced the number of randomizing factors at each stage of the simulation. For each set of randomizing factors a sample of $N = 5000$ meteor radio reflections was simulated. This allowed the points $A$ and $B$ to collect 5000 measurements of the carrier phase $\phi$ and propagation delay $\tau$ implied for the key generation purposes. For each simulated radio reflection a PTR consisting of $M = 2000$ points with sampling interval $\Delta t = t_{i+1} - t_i = 5ms$ has been calculated.

The simulation results are summarized in the Table 1. The second column of the table contains short symbolic notation of enabled (“+”) and disabled (“–”) randomizing factors. The symbol (“x”) denotes that this factor is not significant, i.e. its activation and disabling did not affect at the simulation results. It was found at the stage no.5 that the factor no. 4 should be classified as non-significant. At the subsequent stages of simulation this factor was ignored.

<table>
<thead>
<tr>
<th>Stage No.</th>
<th>Enabled randomizing factors</th>
<th>$R_1(\phi)$</th>
<th>$R_1(\tau)$</th>
<th>$R_1(PTR)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1+</td>
<td>2+</td>
<td>3+</td>
<td>4+</td>
</tr>
<tr>
<td>2</td>
<td>1–</td>
<td>2+</td>
<td>3+</td>
<td>4+</td>
</tr>
<tr>
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<td>1–</td>
<td>2+</td>
<td>3–</td>
<td>4+</td>
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<tr>
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<td>1–</td>
<td>2+</td>
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<td>4+</td>
</tr>
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<td>4–</td>
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<td>2–</td>
<td>3–</td>
<td>4x</td>
</tr>
<tr>
<td>8</td>
<td>1–</td>
<td>2–</td>
<td>3–</td>
<td>4x</td>
</tr>
</tbody>
</table>
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\[
R_i(q) = \frac{1}{N-1} \sum_{i=1}^{N-1} \sum_{j=1}^{N-1} \frac{\sum_{k=2}^{N} \Phi_k \cdot \Phi_{k+2} - \sum_{k=2}^{N} \Phi_k}{\sqrt{\sum_{j=1}^{N-1} \sum_{k=2}^{N} \Phi_k}}
\]

The third and fourth columns of the Table 1 show values of the Pearson correlation coefficient \( R_i \) between the adjacent measurements of the phase \( \phi \) and propagation delay \( \tau \). Each of the 5000 simulated measurements has been selected according to the selection criterion discussed in the section 6. The simulation results show that the samples of phase and propagation delay measurements remain to be random up to exclusion of all the MBC randomizing factors. Therefore, the values in the third and fourth columns do not allow indication of the significance of individual randomizing factors.

To get more indicative measure of statistical relationship between the successively detected meteor radio reflections, we should consider a correlation between the whole Phase-Time Responses but not the correlation between their single counts, as we did before. The \( R_i(PTR) \) values calculated according to the formula (3) are presented in the last column of the Table 1.

\[
R_i(PTR) = \frac{1}{N-1} \sum_{i=1}^{N-1} \left( \frac{M-1}{\sqrt{\sum_{j=1}^{M-1} \sum_{k=2}^{M} \Phi_j \cdot \Phi_{k}}} \right)
\]

At the first and the second simulation stages the mass \( m \) of meteor particles was a random variable with the inverse-power probability distribution. At the third stage masses of all the simulated meteor particles were fixed at value \( m = 5 \times 10^{-4}g \). The same value was also used at the simulation stages no. 4, 5, 7 and 8.

The simulation showed that the factor no. 2 “random coordinates \( M(x,y,z) \) of the reflecting point” is the most significant randomizing factor in meteor burst channel. Even if all the simulated meteor trails have the same spatial orientation (i.e. factor no. 1 is disabled) there is still a great randomness in the characteristics of received signal due to presence of the factor no. 2. This allows considering the factor no. 2 as the most basic randomizing factor. As it can be traced out from the last column of the Table 1, the shapes of Phase-Time Responses for the successively detected meteor radio reflections are becoming mostly identical as we reduce the number of enabled randomizing factors.

The simulation also showed that the Phase-Time Response of radio reflection produced by an underdensed meteor trail typically has a smooth shape with no sharp phase discontinuities. Conversely, the Phase-Time Response of radio reflection produced by an overdensed meteor trail typically reveals much more intensive variation of the carrier phase in time. In other words, the phase measurements produced by the overdensed meteor trails are more stochastic.

8 CONCLUSIONS

Based on the simulation results, we can rank the randomizing factors of meteor burst channel in order of their significance as follows:

1. Random coordinates \( M(x,y,z) \) of the reflecting point on the meteor trail (factor 2);
2. Random spatial orientation of each meteor trail (factor no. 1);
3. Random direction and magnitude of the turbulent wind velocity blowing in the vicinity of the reflecting points of meteor trail (factor no. 5);
4. Random mass \( m \) of meteor particle which produces the ionized trail (factor no. 3);
5. Random moment of occurrence of signal fading (factor no. 4);
6. Other randomizing factors.

Enabling the factors no.1, 2 and 5 ensures unpredictability of the carrier phase \( \phi \) and propagation delay \( \tau \) of received signal. No any immediate influence of the number of enabled randomizing factors on the statistical and probabilistic properties of observed random variables have been identified during the simulation. The only exception is the factor no. 2, which is the most basic in randomizing the observed parameters of received signal. It was also found that the factor no. 4 barely affects on the probabilistic and statistical properties of observed variables.

Radio reflections produced by the overdensed meteor trails have less predictable variations of the signal amplitude and phase. However, a serious drawback of the overdensed trails is a higher value of the channel non-reciprocity. Rise of the channel non-reciprocity results in a higher probability of bit mismatch between the keys generated by Alice and Bob. Thus, the use of radio reflections produced by the overdensed trails provides higher entropy of
encryption key but reduces a key generation rate due to increased channel non-reciprocity.

The future research work should be aligned at the performance evaluation and security analysis of the meteor cryptography systems. Non-reciprocity effects of meteor radio propagation and spatial correlation features of meteor burst channel should be considered to address the above problems.

REFERENCES


