A Necessary Test for Fixed-Priority Real-Time Multiprocessor Systems based on Lazy-adversary Simulation

Romulo Silva de Oliveira, Andreu Carminati and Renan Augusto Starke

Department of Automation and Systems, UFSC, Florianopolis, Brazil

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Abstract: Many embedded systems have real-time requirements which are sometimes hard and must be guaranteed at design time, although most embedded systems have soft deadlines in the sense that they can be missed without any catastrophe being caused by that. Scheduling simulations can be used as a necessary but not sufficient schedulability test that is useful for both hard and soft real-time systems. They help to assess the pessimism of formal analysis applied to hard real-time systems and they can be used as test-case generators during the design of soft real-time systems. In this paper, we present a new adversary simulator for multiprocessors with global task queue and fixed-priority scheduling. We consider sporadic tasks with constrained deadlines (\(D \leq T\)). An adversary simulator uses the non-determinism in the arrivals of sporadic tasks to stress the system scheduler with valid arrival patterns. The simulator proposed in this paper applies a lazy approach that delays the arrival of high-priority tasks in order to form gangs that will preclude the execution of a victim task. We show that the new lazy-adversary simulator presented in this paper outperforms the previously existing necessary schedulability tests.

1 INTRODUCTION

Many embedded systems interact directly with the physical world and present real-time requirements. In hard real-time systems, there may be catastrophic consequences associated with missing a deadline. Most embedded applications however are soft real-time systems in the sense that they have timing requirements but there is no catastrophic consequence associated with missing a deadline.

Schedulability analysis is used to prove that a hard real-time system will never miss a deadline. It is based on sufficient tests that produce pessimistic upper bounds on task response times. While many schedulable task sets fail these sufficient but not necessary tests, those that pass the test are guaranteed to never miss a deadline. This kind of analysis is not appropriate for soft real-time systems since it would lead to over-designed systems and unnecessarily increased costs.

Schedulability analysis is generally based on identifying the worst possible sequence of arrivals. Details of different task models give rise to different possibilities, with various scenarios. In the case of multiprocessors with a single global task queue, there are several types of anomalies (Andersson and Jonsson, 2002) and that makes the determination of the worst sequence of arrivals a combinatorial problem.

One difficulty in evaluating the efficacy of sufficient schedulability tests is to distinguish the cause when a task set fails the test. The task set may not be schedulable, or it may actually be schedulable but the test itself was too pessimistic. Necessary schedulability tests are used to distinguish between these two possibilities. A necessary but not sufficient schedulability test is such that if a task set fails the test then there is a non-zero probability of it missing deadlines, while nothing can be said when it passes the test. Many papers use necessary tests when empirically evaluating new schedulability tests. Examples can be found in (Bertogna et al., 2009), (Cirinei and Baker, 2007), (Davis and Burns, 2011), (Bertogna and Baruah, 2011), (Lee et al., 2011), (Burns et al., 2012), and (Back et al., 2012).

The deadlines of soft real-time systems are usually not guaranteed at design time. Test cases are used instead to assess the timing behaviour of the system. The generation of appropriate test cases to stress the system scheduling is not an easy task due to the combinatorial nature of the problem. In this context, a necessary but not sufficient schedulability test is useful since it can be seen as a test-case generator capable
of generating stressing loads to the system scheduler.

Regarding multiprocessors, probably the most used necessary test is the one described in (Baker and Cirinei, 2006) for the feasibility of sets of sporadic tasks executed on globally scheduled multiprocessor systems. It is a feasibility test in the sense that if a task set fails the test then it is not possible to guarantee its deadlines regardless the scheduler used.

Another approach is to simulate the system and to observe the simulated response times of each task. One cannot guarantee that during the simulation it will be observed the worst-case response time of each task. But scheduling simulations can be used as a necessary but not sufficient schedulability test since any task set that misses a deadline shows that its deadlines are not guaranteed. It is impossible to simulate the entire space of possibilities even for systems of moderate size. Any non-determinism must be resolved during simulation. For example, it is necessary to define when sporadic tasks arrive, although with a minimum time interval between arrivals. Classic scheduling simulators simply generate as much load as possible, as soon as possible, but that is not necessarily the worst case for multiprocessors. An example of the classic approach can be found in (Davis and Burns, 2011).

In (de Oliveira et al., 2013), an adversary simulator was used as a necessary but not sufficient schedulability test. The adversary simulator generates a pattern of arrivals that is valid, but that also increases the response time of tasks, acting as an adversary to the scheduler. The adversary simulator stresses the system in such a way that it is a much tighter necessary but not sufficient schedulability test than the classic scheduling simulator. In (de Oliveira et al., 2013) it was described an adversary simulator for multiprocessors with a single (global) task queue and FP (fixed priority) scheduling. It applies a greedy approach that works well with small systems, but that is not very stringent as the number of tasks and processors increase.

In this paper, we present a new adversary simulator for multiprocessors with global task queue and fixed-priority scheduling. We consider sporadic tasks with constrained deadlines \((D \leq T)\). This new simulator applies a lazy approach that is much more effective for large systems than both the classic simulator and the greedy-adversary simulator from (de Oliveira et al., 2013). We compare the three simulators using both deadline monotonic priority ordering (DMPO) and deadline minus computation time monotonic priority ordering (DCMPO).

The remainder of this paper is organized as follows. Section 2 lists the related work. The task model is described in Section 3. In Section 4 we describe three existing necessary but not sufficient schedulability tests for sporadic-task sets running on multiprocessors. Section 5 describes a new lazy-adversary simulator. Its performance is evaluated in Section 6. Conclusions are presented in Section 7.

2 RELATED RESEARCH

In (Baker and Cirinei, 2007), Baker and Cirinei considered the schedulability of a set of sporadic hard-deadline tasks on a multiprocessor. The test is based on modelling the arrival and scheduling as a finite-state system, and enumerating the reachable states. The computational complexity of the test is too high to be practical for most real systems.

In (Baker and Cirinei, 2006), it is described a necessary test for the feasibility of sets of sporadic tasks. It has pseudo-polynomial complexity and any task set that fails this test is proved to be infeasible in globally scheduled multiprocessor systems. This test is based on concepts originally presented in (Fisher et al., 2006). This is a feasibility test in the sense that if a task set fails the test it is not possible to guarantee its deadlines regardless the scheduling algorithm used.

In (Samii et al., 2008), it is proposed a simulation-based method for worst-case response time estimation of distributed real-time systems. The simulator chooses the execution times of the jobs by exploring the space of execution times so that it maximizes the response times. In order to guide the execution-time space exploration, the authors developed optimization strategies based on three meta-heuristics: Simulated Annealing, Tabu Search, and Genetic Algorithms (GAs) (Reeves, 1993). The authors used the GA-based approach to estimate the pessimism of two response-time analysis approaches for distributed embedded systems considering two automotive communication protocols: CAN and FlexRay. The parameters of the heuristic were tuned experimentally.

In (G. Thaker and Price, 2004), it is used simulation to estimate the pessimism in different schedulability tests for end-to-end distributed periodic tasks. They compared values observed in simulation with values computed using multiple scheduling theory techniques. Regarding the simulations, the only decision was the phase for the first release of each periodic task in a system.

An early work on a similar problem was presented in (Baruah et al., 1991), but it considers the upper bound for the cumulative value obtained through the on-line scheduling of soft real-time aperiodic tasks.
running on uniprocessor and dual processors.

The concept of an adversary simulator was used by (de Oliveira et al., 2012) to stress the system in such a way that the simulation will generate tighter lower bounds for the maximum response time. This concept was applied to multiprocessors using global scheduling and fixed priority. The adversary simulator resolves any non-determinism against a victim task, which results in a valid timeline with a high response time for the victim task. The adversary algorithm is specific to each scheduling solution. In (de Oliveira et al., 2012), an adversary for global fixed-priority scheduling was presented for two priority assignment policies: deadline minus computation time monotonic priority ordering (DCMPO) and deadline monotonic priority ordering (DMPO). In (de Oliveira et al., 2013), an adversary simulator for global fixed-priority until zero-laxity scheduling was also described.

In this paper we present a new adversary simulator for fixed-priority multiprocessor systems that applies a lazy approach and is more effective for large task sets than those presented in (de Oliveira et al., 2012) and (de Oliveira et al., 2013).

3 TASK MODEL

We assume a homogeneous multiprocessor system comprising \( m \) identical processors. There is a static set \( \tau \) of \( n \) sporadic tasks \( \{\tau_1, \ldots, \tau_n\} \). Each task gives rise to a potentially infinite sequence of jobs. Each job of a task may arrive at any time once a minimum inter-arrival time has elapsed since the arrival of the previous job of the same task. Tasks are independent and can not voluntarily suspend themselves.

Each task \( \tau_i \) is characterized by its relative deadline \( D_i \), worst-case execution time \( C_i \), and minimum inter-arrival time or period \( T_i \). The utilization \( U_i \) of each task is given by \( C_i/T_i \) and we assume \( D_i \leq T_i \). The worst-case response time \( R_i \) of task \( \tau_i \) is defined as the longest time from a job of the task arriving to its complete execution.

A global queue exists for all processors. According to global fixed priority pre-emptive scheduling (FP), the jobs with the \( m \) highest priorities execute. As a result of pre-emption and subsequent resumption, a job may migrate from one processor to another. The cost of pre-emption, migration, and the run-time operation of the scheduler is assumed to be either negligible, or subsumed into the worst-case execution time of each task.

We will consider two popular priority assignment policies for the fixed-priority global scheduling of multiprocessors: deadline monotonic priority ordering (DMPO) and deadline minus computation time monotonic priority ordering (DCMPO).

4 EXISTING NECESSARY BUT NOT SUFFICIENT TESTS

In this section we briefly describe the three most used necessary but not sufficient schedulability tests for multiprocessor systems when fixed-priority global scheduling is applied. These three tests will be compared to the new test described in Section 5.

4.1 Feasibility Test

We use as baseline the necessary feasibility test described in (Baker and Cirinei, 2006), which is often used in empirical evaluations in order to eliminate task sets that are certainly not schedulable. It uses the concepts of processor demand bound function and processor load.

The processor demand bound function \( h(t) \) corresponds to the maximum amount of task execution that can be released in an interval \([0,t]\) and also has to complete in that interval.

\[
h(t) = \sum_{i=1}^{n} \max_{i}( \left\lfloor \frac{D_i - t}{T_i} \right\rfloor + 1)C_i
\]

The processor load is the maximum value of the processor demand bound divided by the length of the time interval.

\[
\text{load}(t) = \frac{h(t)}{t}
\]

Baruah and Fisher observed in (Baruah and Fisher, 2005) that a task set cannot possibly be schedulable according to any algorithm if the total execution that is released in an interval and must also complete in that interval exceeds the available processing capacity. The processor load provides a simple necessary condition for task set feasibility: \( \text{load}(\tau) \leq m \), where \( m \) is the number of processors.

In 2006, Baker and Cirinei (Baker and Cirinei, 2006) defined the modified processor load \( \text{load}^m(t) \) as the processor load including task execution that must unavoidably take place within an interval \([0,t]\), even though the release time or deadline is not actually within the interval. The necessary feasibility test becomes \( \text{load}^m(t) \leq m \).

Baker and Cirinei showed that an upper bound on the modified processor load \( \text{load}^m \) can be found by considering a synchronous arrival sequence, with the modified processor load calculated from the modified processor demand bound function for each task:
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\[ h^*(t) = h(t) + \sum_{i=1}^{n} \max(0, t - \max(0, \left\lfloor \frac{t-D_i}{T_i} \right\rfloor + 1)T_i - D_i + C_i) \]  (3)

4.2 Classic Scheduling Simulation

The task model based on sporadic tasks defines a minimum interval of time between two arrivals of the same task, but there is no maximum interval. The first arrival of each task is not defined. Also, the execution time of each individual job can be any value smaller than or equal to the worst-case execution time of the respective task.

When simulation is used to evaluate the schedulability of sporadic task sets running on multiprocessors, it is necessary to resolve issues of non-determinism of the system, since it is impossible to simulate the entire space of possibilities.

Most simulations in the literature employ a classic heuristic to define the behaviour of the system. The classic scheduling simulation assumes that the greater the workload offered to the system, the higher the response times. Thus, the simulator tries to increase the workload as much as possible, as quickly as possible. We will adopt the behavior described in (Davis and Burns, 2011) as an example of the classic approach.

In (Davis and Burns, 2011) each simulation runs for a time interval equal to ten times the longest period of any task in the task set. Each simulation starts with the synchronous release of the first job of each task. Subsequent jobs are released as early as possible. That means that the minimum inter-arrival time is always used. Each job requires its worst-case execution time. The simulation deems a task set schedulable by a given algorithm if it did not find a deadline miss during the time interval simulated, or any unavoidable deadline miss for any job that had execution time remaining at the end of the interval.

4.3 The Greedy-Adversary Simulator

In the classic approach, given the possibility of a job to arrive sooner or later, the simulator always opts for having the job arriving as soon as possible. It makes sense for uniprocessor but this heuristic does not always perform well on multiprocessors.

In the case of multiprocessors, the worst scenario for a victim job is obtained when jobs with higher priority than \( J_v \) occupy all processors. Since task priorities can not be manipulated by the simulator, the only way to manage the execution order is to control the arrivals. The goal of an adversary simulator is not to maximize the processing demand from higher priority tasks but to organize this demand so higher-priority tasks hold all processors simultaneously for as long as possible.

The adversary simulator designed for global fixed-priority multiprocessor scheduling presented in (de Oliveira et al., 2012) and (de Oliveira et al., 2013) chooses a specific job from a specific task to be the victim job. It manipulates non-determinisms in the task model in an attempt to generate the worst possible case for the victim. The only source of non-determinism explored is the arrival time of sporadic tasks, since the execution time of each task is always set to its worst-case execution time. Each task is tried once as the victim.

Let \( \tau_v \) denote the victim task and \( J_v \) the victim job. \( HP(\tau_v) \) represents the set of tasks with a priority higher than or equal to the priority of \( \tau_v \). The first job of the victim task is the victim job and it is the first job to arrive at \( t = 0 \). The adversary heuristic described in (de Oliveira et al., 2013) is based on the following ideas:

- The arrival of jobs associated with tasks in \( HP(\tau_v) \) is postponed until the arrival of \( J_v \).
- The arrival of jobs associated with tasks in \( HP(\tau_v) \) is postponed unless there are enough jobs from \( HP(\tau_v) \) to prevent the execution of \( J_v \).
- Jobs from a task in \( HP(\tau_v) \) arrive as soon as possible, as long as this task is capable of generating more jobs before the deadline of \( J_v \).
- When a task in \( HP(\tau_v) \) is such that it will be able to generate only a single last job before the absolute deadline of \( J_v \), this last job will arrive only when this is necessary to prevent the execution of \( J_v \). If there are more than one job that satisfies this condition, they arrive in the descending order of their execution times.
- Any arbitrary tie-break is against the victim task whenever possible.

This adversary simulator is greedy in the sense that as soon as there are enough tasks to prevent the execution of the victim, all enabled tasks are immediately released. It might not be the best approach. For instance, by waiting a little longer, the adversary simulator might release a larger number of tasks that would keep all processors busy for a longer time interval, creating a worse scenario for the victim task. The exact arrival pattern that will lead to the worst-case response time of the victim is unknown due to the combinatorial nature of the problem.
5 THE LAZY-ADVERSARY SIMULATOR

In this section, we present a lazy-adversary simulator that also manipulates non-determinisms in the task model to generate the worst possible case for the victim task. The only source of non-determinism is again the arrival time of sporadic tasks, since the execution time of each task will always be its respective worst-case execution time. This adversary simulator also chooses a specific job from a specific task to be the victim job.

The lazy-adversary simulator postpones the release of enabled tasks in order to form larger gangs of tasks. A task gang is a set of tasks that have higher priority than the victim task and execute simultaneously in order to occupy all processors and prevent the victim job from executing. The collective release of the tasks of the gang creates a busy interval where task \( \tau_v \) cannot execute. It is important to notice that the same task may appear more than once in the gang when its period is smaller than the busy interval created by the gang.

Let \( \tau_v \) and \( J_v \) denote the victim task and the victim job, respectively. \( HP(\tau_v) \) and \( LP(\tau_v) \) are the sets of tasks with a priority respectively higher than or equal to and lower than the priority of \( \tau_v \). The first job of the victim task is released at time \( t = 0 \) and this is the victim job. \( D_v \) is the relative deadline of \( \tau_v \) and also the absolute deadline of \( J_v \) since it arrives at \( t = 0 \).

The lazy-adversary simulator is based on the following ideas:

- The arrival of tasks from \( HP(\tau_v) \) is organized in gangs.
- No task from \( HP(\tau_v) \) arrives until a gang is formed.
- No gang is formed until the arrival of \( J_v \).
- A gang is formed by at least \( m \) tasks from \( HP(\tau_v) \) that can release a job immediately.
- Even when \( m \) or more tasks from \( HP(\tau_v) \) can release a job immediately, the gang formation will be postponed if the following is true: the time until the next task from \( HP(\tau_v) \) completes its minimum time interval between arrivals is less than the remaining execution time of \( J_v \) and it is also less than the execution time of this task from \( HP(\tau_v) \).
- Once a gang is formed, tasks from this gang arrive only when this is necessary to prevent the immediate execution of \( J_v \).
- Tasks of the gang arrive in the descending order of their execution times.
- More tasks from \( HP(\tau_v) \) can be included in the gang while the gang is executing.
- When there are not enough tasks from \( HP(\tau_v) \) to prevent the execution of \( J_v \) then tasks from \( HP(\tau_v) \) are no longer released until a new gang can be formed.
- Any arbitrary tie-break is against the victim task whenever possible. The most obvious example is when two tasks have the same priority.

At each moment of the simulation, set \( waitingTasks \) contains all tasks that still have to wait for the minimum time interval between arrivals before generating a new job. Set \( enabledTasks \) contains all tasks capable of immediately generating a new job, because it already satisfied the minimum time interval between arrivals since its last arrival. All tasks enter set \( enabledTasks \) at \( t = 0 \). Set \( enabledTasks \) is kept sorted by decreasing execution times.

At any moment, \( availableProcessors(J_v) \) returns how many processors are available for job \( J_v \). That depends on the total number of processors and the number of jobs released but not finished that have a higher priority than \( J_v \). This value can be obtained from the global ready queue. Also, \( e_v \) represents the amount of processing time still needed to finish \( J_v \).

At any time \( t \), \( nextDelta \) represents the time interval until the next task from set \( waitingTasks \) will be capable of generating a new job and then be transferred to \( enabledTasks \). \( nextComp \) represents the execution time of that task. If \( waitingTasks \) is empty then \( nextDelta = \infty \) and \( nextComp = 0 \).

The lazy-adversary simulator alternates between two states: waiting the formation of a new gang (\( waitingGang \) is true) and releasing tasks from a formed gang (\( waitingGang \) is false). The first gang is formed at \( t = 0 \) and includes all tasks from \( HP(\tau_v) \).

Immediately, \( waitingGang \) is set to false, since the victim job has not arrived yet. The first time the victim job is about to execute, tasks from the first gang begin to be released. When there are no more tasks in set \( enabledTasks \) to preclude \( \tau_v \) from executing, this gang is finished and \( waitingGang \) is set to true. \( waitingGang \) is set to false again when a new gang is formed.

The heuristic described is used by the adversary simulator when it has to decide whether a task must be released or not. This happens when a task becomes capable of generating a new job (becomes enabled) and when the victim job is about to receive a processor. Algorithm 1 is used whenever a task \( \tau_v \) becomes enabled (job \( J_v \) may arrive). Algorithm 2 is used when job \( J_v \) is about to receive a processor.
Algorithm 1 When \( \tau_i \) becomes enabled

if \( \tau_i = \tau_j \) and \( r = 0 \) then
    \( J_j \) from \( \tau_i \) arrives now
    exit
end if

if \( \tau_i \) belongs to \( LP(\tau_j) \) then
    \{ Jobs of lower priority than \( J_i \) are just ignored \}
    exit
end if

\( \text{Task of higher priority than } J_i \) becomes enabled
insert \( \tau_i \) into set enabledTasks

if \( \text{waitingGang} > \text{size} \text{(enabledTasks)} \) \&\& \( m \) then
    if \( \text{nextDelta} < e_i \) \&\& \( \text{nextComp} \geq \text{nextDelta} \) then
        \{ Wait a little longer before starting a gang \}
        exit
    else
        \{ Start a gang right away \}
        while \( \text{availableProcessors}(J_i) > 0 \) do
            \( J_i \) from \( \tau_i \) arrives now
            end while
        set \text{waitingGang} to false
    end if
end if

Algorithm 2 When \( J_i \) is about to execute

if \( \neg \text{waitingGang} \) then
    if \( \text{size} \text{(enabledTasks)} \geq \text{availableProcessors}(J_i) \) then
        \{ Reload the necessary jobs from enabledTasks \}
        while \( \text{availableProcessors}(J_i) > 0 \) do
            extract \( J_i \) from set enabledTasks
            \( J_i \) from \( \tau_i \) arrives now
        end while
    else
        set \text{waitingGang} to true
    end if
end if

In this paper we assume a task model where \( D_j \leq T_j \). When the deadline does not have to be equal to the respective task period it is not simple to determine which task has the biggest chance of missing its deadline. In order to avoid having to choose a single victim task, each task is tried once as the victim. Once a task misses its deadline, it is proved that the task set is not schedulable. The algorithm of the lazy-adversary simulator is very fast, so it is feasible to run the simulator once for each task.

6 EVALUATION OF THE LAZY ADVERSARY

In order to evaluate the lazy-adversary described in Section 5, we implemented using the programming language C all three simulators: the classic, the greedy-adversary and the new lazy-adversary. The scheduling of many task sets with different system utilizations were simulated considering different numbers of processors. This empirical experimentation attempts to compare how many systems are declared schedulable by each simulator.

Since all three simulators are driven by heuristics, they can only obtain a lower bound for the maximum response time of each task. The main goal is to determine which one is the more challenging, the one that will be more effective as a necessary schedulability test by generating the most demanding test cases. We also implemented the necessary feasibility test described in (Baker and Cirinei, 2006) as a baseline.

6.1 Simulation Conditions

In order to evaluate the proposed lazy-adversary simulator, we use here the same conditions described in (Davis and Burns, 2011) as a representative example of the conditions generally used in empirical investigations of this kind.

Task utilization’s were generated using the UUnifast Discard algorithm (Davis and Burns, 2009), giving an unbiased distribution. It is based on the UUnifast algorithm of Bini and Buttazzo (Bini and Buttazzo, 2005) adapted to generate task sets with total utilization greater than one as it happens in multiprocessor systems. The minimum time interval between arrivals were generated according to a log-uniform distribution with a factor of 1000 difference between the minimum and maximum values, from 1 ms to 1 second. The log-uniform distribution was used because it generates an equal number of tasks in each time band (e.g. 1-10ms, 10-100ms, etc).

Constrained deadlines were assigned according to a uniform random distribution, in the range \([C_i,T_i]\). Task execution times were set based on the utilization and the minimum time interval between arrivals selected: \(C_j = U_j \times T_j\).

In each experiment, the task set utilization (x-axis value) was varied from 0.025 to 0.975 times the number of processors. For each utilization value, 1000 valid task sets were generated and the schedulability of those task sets determined using the classic and the two adversary simulators. We also used the necessary feasibility test described in (Baker and Cirinei, 2006) as a baseline. We considered three system sizes: 20 tasks running on 4 processors, 80 tasks running on 16 processors and 160 tasks running on 32 processors. For each system size and each utilization, we are interested in the number of task sets that were approved by each test. The best necessary test is that one that approves the minimum number of task sets.

The lines in each graph give the total number of task sets at each utilization level that was approved by the respective algorithm. Scheduling is always based on global FP. Two priority assignment policies were studied. Deadline monotonic priority ordering (DMPO) was used because it is the most used order-
ing when \( D \leq T \). Deadline minus computation time monotonic priority ordering (DCMPO) was also used because, according to simulation studies, it is more effective than DMPO (Davis and Burns, 2009).

6.2 Simulation Results

Figure 1 shows the results for 160 tasks on 32 processors when DMPO is used. We can see that the new lazy-adversary simulator is a better necessary but not sufficient test than the previously existing simulators. All simulators are more effective than the necessary feasibility test for multiprocessors. Figure 2 also clearly shows that the lazy-adversary simulator is a better necessary test when deadline minus computation time monotonic priority ordering (DCMPO) is used to assign priorities to tasks.

Figure 3 shows the results for 80 tasks on 16 processors scheduled by fixed priority assigned by DMPO. Again the graph clearly shows that the lazy-adversary simulator provides tighter lower bounds for maximum response times than those generated by both the classic and the greedy-adversary simulators. Let’s consider for instance an utilization of 10.0. The classic simulator finds 43% of all task sets to be schedulable, the greedy-adversary finds 32% to be schedulable, while the lazy-adversary simulator proposed in this paper finds only 13% of all task sets to be schedulable. Figure 4 shows similar results for when DCMPO is used.

Figure 5 shows the results for 20 tasks on 4 processors and DMPO. The lazy-adversary and the greedy-adversary simulators are better tests than the classic simulator and the generic feasibility test. But the lazy adversary is not always better than the greedy adversary. While the lazy adversary is indeed better for low utilization, the greedy adversary is still better for small systems with high utilization. That is because fewer tasks generates less opportunities to form the big higher-priority task gangs that will prevent the execution of the victim task. In this scenario the greedy approach is capable of rejecting a larger fraction of task sets. We arrive at these same conclusions when DCMPO is used instead of DMPO to assign priorities to sets with 20 tasks (Figure 6).

All figures show that the necessary feasibility test rejects a small number of task sets when compared to any simulator. That can be explained in part because the necessary feasibility test only re proves task sets that can not be scheduled by any scheduler. While the result of the necessary feasibility test is more general, when one wants to consider a specific scheduling algorithm, simulators are better necessary schedulability tests, and the lazy-adversary simulator is the best one. Regarding the classic simulator, it is a better test than the feasibility test, but it is a worse test than both greedy-adversary and lazy-adversary simulators.

All figures also show that DCMPO always enhances the schedulability of the system comparing with DMPO. This is true regardless system size and adversary simulator used.

The time to run a simulation depends on whether a deadline is missed or not. When the system is not schedulable the simulation is stopped once a task misses its deadline so the execution time is very small. It takes longer to run the simulators when all deadlines are met. The classic simulator makes a single
7 CONCLUSIONS

In hard real-time systems, formal analysis provides guarantees for the deadlines, but these analyses are extremely pessimistic for complex architectures. In this case, a necessary but not sufficient test is used to evaluate the pessimism level of the formal analysis, by differentiating unschedulable task sets from task sets that can not be proved to be neither schedulable nor unschedulable.

In this paper we presented a new necessary but not sufficient schedulability test for this task model. The new test is based on the concept of an adversary simulator, but it improves on previously existing algorithms. Like any adversary simulator, it manipulates the non-determinism of load generation in order to increase the response time of a victim task. But the new simulator was called a lazy-adversary simulator because it delays the arrival of high-priority tasks in order to form gangs that will preclude the execution of the victim task for a longer time.

Experiments showed that the new lazy-adversary simulator is a much more effective necessary test than the previously existing ones when considering large systems (80 and 160 tasks). For small systems (20 tasks), the new lazy-adversary simulator is better than the classic simulator and the feasibility test, but it is not better than the previously existing greedy-adversary simulator for all system utilizations.

The complexity of real-time systems grows each day, which makes the formal analysis necessary to guarantee deadlines at design time every more pessimistic. We plan to expand the existing adversary simulators to deal with more complex task models.

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