An Improved Approach for Depth Data based Face Pose Estimation using Particle Swarm Optimization

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Keywords: Template Matching, Nose Tip Localization, Face Orientation Computation.

Abstract: This paper presents an improved approach for face pose estimation based on depth data using particle swarm optimization (PSO). In this approach, the frontal face of the system-user is first initialized and its depth image is taken as a person-specific template. Each query face of that user is rotated and translated with respect to its centroid using PSO to match with the template. Since the centroid of each query face always changes with the face pose changing, a common reference point has to be defined to measure the exact transformation of the query face. Thus, the nose tips of the optimal transformed face and the query face are localized to recompute the transformation from the query face to the optimal transformed face that matched with the template. Using the recomputed rotation and translation information, finally, the pose of the query face can be approximated by the relative pose between the query face and the template face. Experiments on public database show that the accuracy of this new method is more than 99%, which is much higher than the best performance (< 91%) of existing work.

1 INTRODUCTION

Face pose estimation or head pose estimation is an important and challenging task for many real life applications, such as human-computer interfaces (e.g., monitoring drivers attention in a car), preprocessing for face registration and face recognition, and visual gaze estimation, in which face pose provides an important supplementary information. Thus, numerous research (Murphy-Chutorian and Trivedi, 2009) concentrated on the issue of face pose estimation have emerged prominently in the last few years.

Recently, with the development of 3D scanning technology, like real-time stereo-enhanced structured-light method (Weise et al., 2007), Microsoft Kinect, etc, 3D data with high resolution and accuracy can be obtained conveniently. Since 3D data is much less affected by illumination changing and partial occlusion of the face (e.g. hair, glasses) than 2D data (RGB image or intensity image), recent researches for face pose estimation based on 3D data demonstrated more accurate and robust results. In general, the methods for this 3D data based study can be grouped into three classes: models method, regression method and alignment method.

In models method, 3D face model is always constructed from the facial features, landmarks, surface, or point clouds. With the generated model, related mathematic methods are used to solve the face pose. For example, (Cai et al., 2010) constructed their 3D face model using the linear deformable model (Zhang et al., 2004), and the face pose is obtained by computing the rotation, translation and deformation parameters between the head model and the depth camera with a regularized maximum likelihood deformable model fitting algorithm. (Bleiweiss and Werman, 2010) combined the color data with the time-of-flight depth data to construct a textured mesh model, and then synthetic image was obtained by projecting the hypotheses mesh model to 2D image space. The head pose is finally derived by minimizing the difference between the synthetic image and input image. Moreover, A rigid body motion model (Horn and Harris, 1991) is applied in (Kondori et al., 2011) to measure the face rotation and translation between two consecutive depth frames. In (Tu et al., 2011), the pitch and yaw angles are estimated by fitting a plane to the 3D points around the detected nose tip, while the roll angle is coarsely computed by fitting an ellipse to the head boundary points. However, the accuracy of this method is limited by the robustness of nose tip detection or nose tip tracking.

The regression method is efficient to solve the problem of face pose estimation for the reason that...
features extracted from the depth image are discriminately enough and robust to illumination and partial occlusion. For instance, (Tang et al., 2011a; See- mann et al., 2004) employed neural network (NN) to train and test their 3D face pose estimators. (Rajwade and Levine, 2006) utilized support vector regression (SVR) based on 3D data to estimate facial pose. Furthermore, random regression forests (RBF) is utilized in (Fanelli et al., 2011a; Fanelli et al., 2011b; Tang et al., 2011b) to solve depth data based face pose estimation problem. However, a large database has to be collected for training in the regression method.

In alignment method, the query face image is first aligned with a fixed template face image, and then the pose of the query face is measured by the orientation difference between them. Iterative closest point (ICP) (Besl and McKay, 1992) is a commonly used approach for 3D point clouds alignment. Numerous papers (Ghorbel et al., 2010; Mora and Odobez, 2012) have applied ICP to solve the task of 3D face pose estimation. Nevertheless, ICP need a good initialization, and it is sensitive to facial expression changing and oblique face poses. These limitations invoke other methods to improve the robustness and reduce the limitations. (Breitenstein et al., 2008) proposed a real time face pose estimation system based on single range images. Nevertheless, several limitations exist in their work: 1) a huge database with face models of different reference poses should be prepared; 2) the space of face poses is discretized, which may reduce the accuracy; 3) the nose detection part is complicate and time consuming. Evolutionary algorithm (EA) (Back, 1996) for face pose estimation was first published in (Padeleris et al., 2012). In their work, particle swarm optimization (PSO) is used to register the resampled candidate face to the template face. Furthermore, (Wang and Ying, 2012) employed genetic algorithm (GA) to register two point clouds of partial faces to recover the whole face, and it showed better performance on this task than ICP.

Therefore, in the above literatures, either training is required or the accuracy is limited by large pose variations. Inspired by the work of (Padeleris et al., 2012) by Padeleris et al., this paper presents an improved approach for face pose estimation based on depth data. Unlike (Padeleris et al., 2012), in the proposed algorithm, we get rid of the processes of surface reconstruction and depth image resampling, but utilize the PSO algorithm on the original depth image directly for template matching, which results in two corresponding point clouds between the query face and the optimal transformed face. Moreover, the nose tips on the two corresponding point clouds can be localized precisely by the proposed method. Finally, with the obtained corresponding points and nose tips mentioned above, the relative rotation and translation matrices of the query face to the optimal transformed face or template face can be derived using the singular value decomposition (SVD) algorithm. Therefore, the estimated orientation of the query face can be obtained from the rotation and translation matrices by assuming the orientation angles of the template face are all zero degree. The proposed algorithm is expected to be faster and more accurate than the method proposed in (Padeleris et al., 2012). An overview of the proposed framework is shown in Figure 1.

The remainder of the paper is organized as follows: The proposed approach for face pose estimation is described in detail in Section 2; Experimental results are presented in Section 3 to verify the efficiency of the proposed approach; A conclusion is made and the future work for this study is discussed in Section 4.

2 PROPOSED APPROACH

In this paper, the face pose, \( P = [p, \eta, \gamma, x, y, z]^T \), is composed by the nose tip location \((x, y, z)\) and face orientation \((p, \eta, \gamma)\) (pitch, yaw, roll angles). Suppose the face is already segmented, the organized point cloud of the face whose pose needs to be estimated is named as query face denoted by \( Q \in \mathbb{R}^{m \times n} \). Denote that \( M \in \mathbb{R}^{m \times n} \) is the template face depth image (2D map of \( z \) values), and \( F_0 \in \mathbb{R}^{m \times n} \) is the optimal depth image transformed from \( Q \).

2.1 Template Matching

The first goal of the proposed algorithm is to align the depth image of query face \( Q \) to the template face depth image \( M \) and obtain the optimal transformed depth image \( F_0 \). To this end, as (Padeleris et al., 2012), this alignment process can be formulated by minimizing the Sum of Squared Differences (SSD) of pairwise pixel differences between the template \( M \) and the face depth image \( F_k \in \mathbb{R}^{m \times n} \), which is transformed from \( Q \) by several candidate parameters: scaling scalar \( c_k \in \mathbb{R}^+ \), rotation matrix \( R_k \in \mathbb{R}^{3 \times 3} \) and translation matrix \( T_k \in \mathbb{R}^{3 \times 1} \). Hence, this optimization problem can be formulated by

\[
\arg \min_{c_k, R_k, T_k} = \xi^{-1} \sum_{i=1}^{m} \sum_{j=1}^{n} H(i, j) [M(i, j) - F_k(i, j)]^2 ,
\]

where \( \xi = \sum_{i=1}^{m} \sum_{j=1}^{n} H(i, j) \) is a normalization factor and \( H(i, j) \) is a point matching indicator.
The translation along x, y, and z axes respectively; \( d_x, d_y, d_z \) denotes the translation along x, y, and z axes. Note that the origin of the coordinate system mentioned above is the centroid of the query face point cloud.

Assuming the optimal solution of (1) is found using PSO, the indicator \( k \) for all parameters mentioned above is replaced with \( o \). However, this optimal solution is not the accurate face pose, because the centroid of the query face is not the corresponding point of the centroid of the template face, which results in meaningless rotation Euler angles and translation values for face pose. Therefore, to compute accurate face pose, a reference point has to be defined.

### 2.2 Nose Tip Localization

Finding that nose tip is a good reference point which is invariant to the changes of face expression and easy to locate automatically, we measure the query face orientation around its nose tip (face location). In this part, a simple hybrid method for nose tip localization is proposed.

**Method 1.** Normally, the nose tip of a frontal face point cloud is the nearest point to the camera. Thus, one method of localizing the nose tip is to find the point with smallest depth value in the optimal transformed face depth image \( F_o \), and then use the optimal transformed face point cloud \( F'_o \) to obtain the 3D nose tip point \( \Delta_f \) in it. Meanwhile, the 3D nose tip point \( \Delta_f \) in the query face point cloud \( Q \) can be obtained by finding the corresponding points of \( F'_o \) in its corresponding points matrix \( Q'_o \). However, finding only one point with smallest depth value in the point cloud may produce wrongly located nose tip caused by noisy points, and it may need a large number of computing time when the searching space is the whole face image. To solve the problems mentioned above, a constrained nose region is predefined for nose tip searching. First, the nose of the template face is detected on its RGB image using object de-
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projection method (e.g., Viola-Jones method); If the RGB image is not available (suppose the depth image or 3D point cloud of the template face is already segmented), the nose region can be roughly defined by computing the center of the point cloud, which means the 2D location of the point cloud center is the same with the center of the nose region. After defining the nose tip searching region on the template face, this region is fixed and applied to all the transformed frontal faces, since the relative 2D locations of the template image and the optimal transformed image are identical. Rather than only selecting only one point in the predefined searching region, \( N_{m1} \) points in \( F'_{f} \) with smallest depth values are selected and taken the average of these 3D points, which results in the nose tip \( \Delta_f \) of the optimal transformed face. Accordingly, with \( Q'_{o} \), the nose tip \( \Delta_q \) of the query face can be derived by computing the average of the corresponding points of the selected \( N_{m2} \) points in \( F'_{q} \). The procedure of Method 1 is depicted in Figure 2.

Method 2. Another method for nose tip localization is similar to Method 1, but more time saving and more insensitive to noise. In this method, the nose tip of the template face is localized using the same means of Method 1. However, instead of searching points with smallest depth value in the predefined nose region, the 2D location of the nose tip on the template face image is considered as the 2D location of the nose tip on the optimal transformed face image. In this way, the nose tips of the transformed face and the query face are localized by averaging the \( N_{m2} \times N_{m2} \) neighborhood 3D points of the pre-computed 2D nose tip location in \( F'_{f} \) and \( Q'_{q} \), respectively. Nevertheless, for some large rotation angles, the \( N_{m2} \times N_{m2} \) neighborhood 3D points may contain no information, and this method will not detect any nose tip in such case. Figure 3 illustrates this method. Note that in Figure 3, \( h_{i,j} \) is greater than 0; Otherwise, \( h_{i,j} = 0 \). This means the neighborhood points to be averaged in this method should have depth values greater than zero.

Method 3. In our work, to combine the advantages of the above two methods for nose tip localization, we propose to apply Method 2 first, and if no nose tip was detected, Method 1 is used to detect the nose tip. In this hybrid method, both the nose tip and nose region of the template face need to be found and retained before estimating the pose of the query face, while this process is fully automatic and fast. Since the case of very large face rotation is rare, the hybrid method not only reduces the computation complexity (avoiding the point searching procedure for most cases), but also improves the robustness of nose tip localization (reducing the influence of noise).

Thus, with \( F'_{f} \) and \( Q'_{q} \), the nose tip \( \Delta_f \in \mathbb{R}^{3 \times 1} \) of the optimal transformed face \( F'_{f} \) and the nose tip \( \Delta_q \in \mathbb{R}^{3 \times 1} \) of the query face \( Q \) can be localized respectively.

2.3 Face Orientation Computation

At last, the orientation of the query face can be derived by finding the rotation and translation relationship with respect to the face location (nose tip) between \( F'_{f} \) and \( Q'_{q} \), which is formulated by the following least square problem.

\[
\arg \min_{R,T} \frac{1}{N} \sum_{i=1}^{N} \left\| (f'_i - \Delta_f) - [R(q'_i - \Delta_q) + T] \right\|^2, \tag{4}
\]

where \( f'_i \in \mathbb{R}^{3 \times 1} \) and \( q'_i \in \mathbb{R}^{3 \times 1} \) are corresponding points in \( F'_{f} \) and \( Q'_{q} \), respectively; \( N \) is the number of points with depth value greater than zero.
The minimization problem in (4) can be easily solved using SVD. Note that \( R \) and \( T \) obtained in (4) represent the rotation and translation from the query face \( d_q \) to the optimal transformed face \( F_t \). Because the optimal transformed face has been already aligned with the template face based on depth data (\( z \) value) using PSO, it can be approximated that \( R \) and \( T \) are also the motion parameters from the query face to the template face. Assume that the reference rotation matrix \( R_0 \) and translation vector \( T_0 \) of the initialized template face are \( R_0 = A_{3 \times 3} \) (3 \( \times \) 3 identity matrix) and \( T_0 = [0 \ 0 \ 0]^T \), respectively. Therefore, take the forward direction vector of the template face as \( \bar{d}_0 \in \mathbb{R}^{3 \times 1} \), then the forward direction vector \( \bar{d}_q \in \mathbb{R}^{3 \times 1} \) of the query face can be obtained by taking the inverse translation and rotation. That is

\[
\bar{d}_q = R^T (\bar{d}_0 - T) \tag{5}
\]

In the end, the desired pitch and yaw angles of the query face \( d_q \) can be easily derived by the obtained direction vector \( \bar{d}_q \). Similarly, the roll angle can also be derived with the same method by defining a vertical direction vector that is perpendicular to \( d_q \). In other words, if the forward direction vector parallels to \( z \) axis, the vertical direction vector to compute roll angle should parallel to \( y \) axis.

3 EXPERIMENTS

In order to assess the efficiency of the proposed algorithm for face pose estimation based on 3D data, the ETH Face Pose Range Image Data Set (Breitenstein et al., 2008) is used. In this database, more than 10,000 range images (i.e. images with per-pixel depth, also known as depth images) of 20 persons (3 female, 6 persons of them recorded twice for the situations with and without glasses) are included. The range images were captured at 28 fps with a scanner using the real-time stereo-enhanced structured-light method (Weise et al., 2007) when each person first looked straight into the camera, and then freely turned her head. Each range image has a resolution of 640 \( \times \) 480 pixels, and a face typically consists of about 150 \( \times \) 200 depth values. The face pose range covers about \( \pm 90^\circ \) for yaw rotation and \( \pm 45^\circ \) for pitch rotation. Nose position and face direction (vector through nose) in a left-handed coordinate system of each range image were provided as ground truth. All the experiments in this section are performed on a PC equipped with i5 3.10GHz CPU.

Throughout our experiments, the size of each face range image is set to 200 \( \times \) 260 pixels. In the part of face alignment using PSO, the following parameters are predefined: Since the first range image in each sequence was taken when the person looked straight into the camera, we take this image as the person-specific initialization, where the person-specific template face depth image with assumed face direction \( \bar{n} = [0, 0, -1] \) is obtained. The number of particles is set to \( S = 25 \), and the maximum running generations are tested by \( G = 10, 20, 30, 40 \) separately. For simplification, the scaling factor \( c \) in the first dimension of each particle is taken as \( c = 1 \), because there is little scaling variation in the sequence of each person, who was asked to just rotate her head but not to move forward or back when recording the database.

In addition, the rotation angles and translation distance dimensions of each particle are initialized at the uniform distribution of the center of the searching space, while their velocities are set to zeros. Because each sequence in the database is continuous, i.e. the poses of every two consecutive images have relative small difference, the optimal solution of the previous image is taken as the searching center of current image, and the searching space around the center is defined as \( \pm 20^\circ \) for each rotation angle dimension \((\phi, \theta, \psi)\) and \( \pm 20 \text{mm}\) for each translation dimension \((d_x, d_y, d_z)\). This searching space constriction method both accelerates the searching speed for optimal solution and improve the face alignment accuracy. Furthermore, in the particle velocity update equation, we take the same parameters setting and constraints as (Padeleris et al., 2012). Moreover, the predefined threshold \( \tau \) for the fitness result of the fitness function (1) is \( \tau = 0.1 \). Finally, a matching ratio threshold

\[
\alpha = \frac{\sum_{i=1}^{m} \sum_{j=1}^{n} H(i, j)}{\text{No. of nonzero pixels in template } M} \tag{6}
\]

with \( H(i, j) \) defined in (1) between the candidate transformed depth image and the template depth image is defined to exclude the bad solutions that give small fitness value but wrongly aligned face (e.g. oblique poses or severe occlusions). If \( \alpha < \xi \), \( \xi \) is a threshold, the candidate solution is accepted; Otherwise, it is rejected. In our experiments, we use \( \xi = 0.1 \).

For the part of nose tip localization, the number of nearest points that are selected to compute the nose tip location is taken as \( N_{n1} = 5 \) in Method 1; \( 5 \times 5 \) neighborhood of the 2D location of the template face is used in Method 2 (i.e. \( N_{n2} = 5 \)).

Although the computing speed can be improved by using a subset pairs of corresponding points with SVD to compute the face orientation, this improvement is insignificant compared to the large number of computing in the process of face alignment. There-
fore, to ensure the robustness and high accuracy during computing the face orientation, we use all pairs of corresponding points for SVD.

We consider the ground truth of nose position of the database as the ground truth of nose tip location in our experiments, and since the rendered ground truth of face direction only encodes the yaw and pitch rotations while does not contain roll rotations, we convert the face direction of ground truth and the output face direction vector to their corresponding yaw and pitch angles respectively before the estimated yaw error and pitch error are computed. As (Padeleris et al., 2012) and (Fanelli et al., 2011a), we also take a frame as a successfully estimated frame if the L2 norm of its nose tip location error and face orientation error are less than their corresponding predefined thresholds.

Table 1 shows the mean errors of estimated face pose from the whole data set with different number of maximum generations in face alignment. It can be seen that the face pose estimation error decreases with the number of generations increasing, which means PSO convergent better with more generations. In addition, Figure 4 and Figure 5 compare the face pose estimation accuracy under different number of generations in PSO. One can observe that the face alignment cannot achieve optimal solution with small number of generations, like 10 generations, and the performances with 20, 30, and 40 generations are very similar, therefore, it can be concluded that we can achieve considerable with 20 generations in PSO. Though PSO with 40 generations gives slightly smaller pose error, using 20 generations will save almost half of the processing time for one frame in real time application.

Table 1: Face pose estimation error comparison with different number of generations in PSO. Mean error and standard deviation of nose tip location and face orientation (yaw and pitch) are shown.

<table>
<thead>
<tr>
<th>Itr(#)</th>
<th>Nose(mm)</th>
<th>Yaw(°)</th>
<th>Pitch(°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>5.16 ± 11.69</td>
<td>2.19 ± 4.89</td>
<td>1.20 ± 2.32</td>
</tr>
<tr>
<td>20</td>
<td>3.51 ± 3.83</td>
<td>1.33 ± 2.12</td>
<td>0.67 ± 0.88</td>
</tr>
<tr>
<td>30</td>
<td>3.32 ± 3.83</td>
<td>1.16 ± 1.83</td>
<td>0.56 ± 0.76</td>
</tr>
<tr>
<td>40</td>
<td>3.26 ± 3.29</td>
<td>1.12 ± 2.03</td>
<td>0.53 ± 1.17</td>
</tr>
</tbody>
</table>

The performance of the proposed algorithm is compared with other related work on the same database in Table 2. It can be seen that the proposed approach performs much better in both pose estimation error (the first three columns) and estimation accuracy (the last column) within 10° face orientation error than the latest work. Note that the errors reported in (Breitenstein et al., 2008) are computed with a threshold for a true positive rate of 80% and false positive rate of 3% (i.e. a high confidence for nose identification). In the system of (Fanelli et al., 2011a), 6.5% of the range images in ETH database were discarded before computing the errors, because these images failed to be estimated. In a word, more or less images were omitted when calculating the pose errors in the two literatures mentioned above. However, the pose estimation error in our work is calculated from all frames in the whole database except for the first frame in each sequence, which is taken as the template. Therefore, one can conclude that the proposed approach can handle more difficult situations and estimate face pose more accurately than the compared work in Table 2.

Furthermore, as shown in Table 3, the proposed approach renders higher face pose estimation accuracy than (Breitenstein et al., 2008) and (Fanelli et al., 2011a) within angle error thresholds of 10°, 15°, and 20°. The accuracy of the proposed approach within the most conservative threshold 10° is even higher than that of the other two within the less conservative threshold 20°.

Finally, some correctly estimated face depth images by the proposed approach from the ETH Face Pose Range Image Data Set (Breitenstein et al., 2008) were sampled to further prove its efficiency. As
Table 2: Face pose estimation comparison using the ETH Face Pose Range Image Data Set (Breitenstein et al., 2008). The first three columns show mean error and standard deviation for nose tip localization and face orientation estimation (Yaw, Pitch). The last column shows the percentage of successfully estimated frames for the predefined angle error threshold of 10°.

<table>
<thead>
<tr>
<th></th>
<th>Nose error (mm)</th>
<th>Yaw error (°)</th>
<th>Pitch error (°)</th>
<th>Accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Breitenstein et al., 2008)</td>
<td>9.00 ± 14.00</td>
<td>6.10 ± 10.30</td>
<td>4.20 ± 5.90</td>
<td>80.8</td>
</tr>
<tr>
<td>(Fanelli et al., 2011a)</td>
<td>13.40 ± 21.10</td>
<td>5.70 ± 15.20</td>
<td>5.10 ± 4.90</td>
<td>90.4</td>
</tr>
<tr>
<td>(Padeleris et al., 2012)</td>
<td>7.05 ± 6.46</td>
<td>1.62 ± 1.59</td>
<td>2.05 ± 1.87</td>
<td>90.1</td>
</tr>
<tr>
<td>Proposed Approach</td>
<td>3.26 ± 3.29</td>
<td>1.12 ± 2.03</td>
<td>0.53 ± 1.17</td>
<td>99.7</td>
</tr>
</tbody>
</table>

Table 3: Face pose estimation accuracy comparison with different angle error thresholds.

<table>
<thead>
<tr>
<th></th>
<th>10° accuracy (%)</th>
<th>15° accuracy (%)</th>
<th>20° accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Breitenstein et al., 2008)</td>
<td>80.8</td>
<td>97.8</td>
<td>98.4</td>
</tr>
<tr>
<td>(Fanelli et al., 2011a)</td>
<td>90.4</td>
<td>95.4</td>
<td>95.9</td>
</tr>
<tr>
<td>Proposed Approach</td>
<td>99.7</td>
<td>99.7</td>
<td>99.8</td>
</tr>
</tbody>
</table>

Figure 6: Some face pose estimation results from the ETH Face Pose Range Image Data Set (Breitenstein et al., 2008) with the proposed approach. In each image (a)-(f): The person-specific template face is shown in top right; The optimal transformed face is shown in top left; Dot represents nose tip location; Face direction is illustrated by a straight line originated from nose tip and paralleled to face direction vector. (Red: estimated pose; White: ground truth).

shown in Figure 6, one can see that the proposed algorithm can give high pose estimation accuracy for the situations of both large pose variation and partial occlusion (e.g., long hairs (a) and wearing glasses (b), (d)).

4 CONCLUSIONS

In conclusion, an improved algorithm for face pose estimation based on 3D data have been presented in detail in this paper. The contributions of this work include: 1) The proposed approach, which has no need of surface reconstruction and depth image resampling, improves the accuracy and computing speed for 3D face pose estimation. Comparing to the latest work of others, the proposed approach demonstrates the best performance in the public database; 2) A new hybrid method for nose tip localization has been proposed, and its efficiency and reliability have been proved by experimental results.

To further improve the proposed approach, in the future work, a genetic face model will be built to get rid of the initialization part and GPU programming will be studied to implement the proposed approach in real time.
REFERENCES


