Shape Segmentation using Medial Point Clouds with Applications to Dental Cast Analysis

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Abstract: We present an automatic surface segmentation method for dental cast scans based on the point density properties of the surface skeleton of such shapes. We produce quasi-flat segments separated by soft ridges, in contrast to classical surface segmentation methods that require sharp ridges. We compute the surface skeleton by a fast 3D skeletonization technique followed by its regularization using surface geodesics. We segment the resulting skeleton by a mean-shift approach and transfer the segmentation results back to the surface. We demonstrate our results on an industrial dental-cast segmentation application and several generic 3D shape models.

1 INTRODUCTION

Segmenting 3D surfaces into their natural components has many applications in shape analysis, computer vision, shape compression, and medical imaging. Segmentation requirements strongly depend on the target application, so many segmentation methods exist. One can distinguish between patch-type and part-type segmentation methods (Shamir, 2004). Patch-type methods use local shape information such as surface curvature to produce quasi-flat segments separated by high-curvature creases or ridges. Part-type methods are more semantically-oriented, i.e., try to find segments that a human user would intuitively see as distinct logical shape parts. Such segments are not always separated by high-curvature ridges.

For some shapes, both patch-type and patch-type methods do not yield the desired result. Consider for example the dental cast model in Fig. 2 a, where we want to find the separate teeth as individual segments, and also separate them from the gums. Part-based methods fail here, since the teeth are not clear protrusions from the shape’s rump, as would be, e.g., the limbs sticking out of an articulated body model. Patch-based methods also fail, since ridges separating teeth from each other and from the gums are quite shallow. Detecting a compact, closed, and thin separation region between the segments based on curvature is quite hard. Fig. 2 b illustrates this by showing the surface’s curvature (concave=blue, convex=red).

The main motivation of this work is the need to segment dental casts, which are tools used to create orthodontic treatment plans for dental patients. Advances in range imaging and 3D scanning allow capturing dental scans directly from a patient (Atron, Inc., 2013), and next to digitize such shapes into 3D surface meshes of the teeth-and-gum structure. Digital casts allow the automatic assessment of several orthodontic metrics, such as the arch length discrepancy, and new opportunities towards teeth alignment treatment planning and simulation. However, all such analyses require a prior segmentation of the scan into individual teeth and the gums. Typical dental scans do not exhibit sharp creases between individual teeth (due to scanning resolution limitations or actual teeth touching), nor between teeth and gums. Hence, existing patch-based segmentation cannot be directly used.

For the motivating use-case of segmenting dental casts, we present here a new method to compute patch-based segmentations of 3D shapes which do not exhibit strong creases between segments. Instead of using local information such as curvature, we take a global approach, based on the shape’s surface skeleton. Key to our method is the observation that surface skeletons capture all input shape creases, regardless of their sharpness. To compute a high-resolution surface skeleton, we use a GPU-based method which delivers point-cloud skeletons for models of hundreds of thousands of polygons in a few seconds. Next, we regularize the surface skeleton, to eliminate small
manifolds that do not correspond to segments large enough to be of interest. Next, rather than segmenting the surface (as virtually all patch-based methods do), we segment its regularized surface skeleton, by a mean-shift approach. Finally, we project back the found skeletal segments onto the input surface, and use a nearest-neighbor approach to yield a segmentation that entirely covers the input shape (Figure 1).

The structure of this paper is as follows. Section 2 reviews related work on skeletonization and dental cast segmentation. Section 3 details our method. Section 4 presents our results. Section 5 discusses our method. Section 6 concludes the paper.

2 RELATED WORK

Related work can be organized into three areas:

Surface Segmentation. Patch-based segmentation subdivides a 3D shape into non-overlapping, compact, segments or patches which (a) respect desirable properties such as minimal size and boundary smoothness, and (b) are separated by local surface features, typically sharp creases. By construction, segments are much flatter than creases between them. Many methods exist in this area. (Garland et al., 2001) hierarchically clusters the input mesh faces to yield a segmentation consisting of planar segments. (Clarenz et al., 2004) propose a fuzzy multiscale segmentation based on surface curvature. This method often creates noisy segment boundaries in low-curvature regions. (Borgefors et al., 2009) compute local thickness in combination with a multisolution structure to hierarchically segment 3D voxel shapes. (Mangan and Whitaker, 1999) segment surfaces into similar-curvature patches by a watershed technique with curvature as the height function. (Zuckerberger et al., 2002) improved the watershed method and give many applications. (Provot and Debled-Rennesson, 2008) segment voxel shapes by detecting discrete planes with variable width.

Dental Segmentation. Dental cast segmentation has been widely explored recently due to the increasing availability of digital models. Manual segmentation is prohibitively slow for current orthodontic practice. Several methods have been proposed instead, ranging from fully automated methods (Kondor et al., 2004) to methods needing minimal user interaction (Kondo et al., 2010; Zhao et al., 2005; Hirogaki et al., 2001). (Kondo et al., 2004) avoids the 3D mesh processing complexity by first transforming the 3D data into a plan-view range image which is next segmented.

Recently, a snake-based approach for teeth segmentation has been proposed (Kronfeld et al., 2010). Here, a snake is iteratively fit to the surface curvature until it reaches local minima. However, such methods have problems in low curvature regions, i.e., where creases separating teeth are shallow. Also, such methods assume a way to find the positions and amount of teeth prior to segmentation, e.g., using the dental arch metric. In our proposal, we do not rely on such priors.

Skeletonization. Skeletons of medial axes contain the loci of maximally inscribed circles (in 2D) or spheres (in 3D) (Blum, 1967). 2D medial axes are collections of curves. 3D shapes admit two skeletons: Surface skeletons are sets of curved manifolds containing the loci of maximally inscribed spheres. They fully describe the shape, i.e., the shape can be reconstructed from the skeleton. Curve skeletons are sets of 1D curves locally centered in the shape, according to various heuristics. They cannot fully capture the geometry of the input shape, and are most useful for tubular objects (Cornea et al., 2007). Given these, we next focus on surface skeletons. Several methods compute surface skeletons either from a meshed surface or a volumetric (voxel) model. Volumetric methods have significantly higher memory and speed costs and lower accuracy. Skeletonization methods can be divided into thinning (Pudney, 1998; Palagyi and Kuba, 1999), geometric (Amenta et al., 2001; Stolpner et al., 2009; Stolpner et al., 2011), and field-based (Siddiqi et al., 2002; Pizer et al., 2003; Bouix et al., 2005; Bouix et al., 2006; Reniers et al., 2008b). For a survey, we refer to (Siddiqi and Pizer, 2009).

Only few 3D segmentation methods use skeletons. (Reniers and Telea, 2008a) uses curve skeletons for part-type segmentations of tubular shapes. (Reniers and Telea, 2008b) use surface skeletons for part-type segmentation of shapes with sharp edges. The latter is of interest to us: Given a voxel shape, we compute its surface skeleton by (Reniers and Telea, 2008a), and next simplify it to remove small-scale details. Next, we detect the skeleton boundary and back-project it on the surface via the inverse feature transform. (Re-
niers and Telea, 2007). This robustly detects creases between quasi-flat patches, as skeleton boundaries correspond to the surface’s curvature maxima (Pizer et al., 2003). Finally, we fill surface areas between these creases to compute segments. (Reniers et al., 2008a) use a similar relation between the skeleton and surface to robustly find ridges of anatomical surfaces. However, they do not actually segment the surface. A main blocker in using surface skeletons for segmentation is the difficulty to efficiently compute accurate skeletons of complex models. Recently, this has been overcome by (Ma et al., 2012) and (Jalba et al., 2013) who compute point-cloud skeletons for meshes of millions of polygons in seconds on the GPU. However, these methods produce an unstructured cloud rather than a compact voxel model (as in e.g. (Reniers and Telea, 2008a)), so they cannot be used to segment surfaces along (Reniers and Telea, 2008b). We next propose a shape segmentation method combining the skeleton description power with its local point density properties when extracted from a uniformly sampled surface. This enables a meaningful shape segmentation based on both global and local properties.

3 METHOD

Our proposal first transforms the surface into its medial domain (see Fig. 2). We next exploit skeletal point density properties to do the segmentation in this domain. Finally, we project the medial segmentation back to the surface. We detail these steps next.

3.1 Skeletonization Preliminaries

Given a shape $\Omega \subset \mathbb{R}^3$ with boundary $\partial \Omega$, we first define its distance transform $DT_{\partial \Omega} : \mathbb{R}^3 \rightarrow \mathbb{R}^+$

$$DT_{\partial \Omega}(x \in \Omega) = \arg\min_{y \in \partial \Omega} |x - y|.$$ 

(1)
The skeleton of $\Omega$ is next defined as

$$S_\Omega = \{ x \in \Omega \mid \exists f_1, f_2 \in \partial \Omega, f_1 \neq f_2, \| x - f_1 \| = \| x - f_2 \| = DT_{\partial \Omega}(x) \},$$

where $f_1$ and $f_2$ are two of the contact points with $\partial \Omega$ of the maximally inscribed ball in $\Omega$ centered at $x$, also called feature transform (FT) points (Strzodka and Telea, 2004; Reniers and Telea, 2007). The vectors $f_1 - x$ and $f_2 - x$ linking the skeleton points $x$ with their feature points are called feature vectors or spoke vectors (Stolpner et al., 2009). In some cases, a skeleton point can have more than two such feature points—consider e.g. the center of a ball whose feature points are the entire ball surface. For our purposes, we however need only two of these points, which are faster to compute and store than the full feature transform.

Given a densely sampled mesh surface $\partial \Omega$, we extract its densely sampled surface skeleton following (Jalba et al., 2013; Ma et al., 2012). In detail, for each point $p \in \partial \Omega$ having the surface normal $n$, we create a ball $B(s, r)$ of center $s = -rn + p$ and initial radius $r$ larger than the diameter of $\partial \Omega$. The ball is iteratively shrunk by searching the closest surface point to $s$ until it touches $\partial \Omega$ in exactly two points $f_1 = p$ and $f_2$. At this moment, the center $s$ is a newly found skeleton point with feature points $f_1$ and $f_2$. To remove small-scale skeleton details created by equally small-scale convexities (bumps) on $\partial \Omega$, we next regularize the skeleton. For this, we compute an importance metric $\rho : S \rightarrow \mathbb{R}^+$ for each skeleton point. $\rho(s \in S) equals the shortest-path distance on $\partial \Omega$ between the feature points $f_1$ and $f_2$ of $s$. As shown in (Reniers and Telea, 2008a; Jalba et al., 2013), $\rho$ monotonically increases from the skeleton boundary inwards. Thresholding it with a small value $\tau$ yields a simplified skeleton

$$S_\tau = \{ s \in S_\rho | \rho(s) > \tau \}$$

which captures all salient branches of $S_\Omega$ but removes those for surface details shorter than $\tau$. Figure 2 shows this: From a dental cast (a), we compute the skeleton cloud. Image (c) shows the simplified skeleton $S_\tau$ for a value $\tau = 3\%$ of the shape’s diameter, colored by $\rho$ (blue=low, red=high). We see how simplification removed many spurious skeletal points created by small surface wiggles. Image (d) shows, for comparison, the surface skeleton reconstructed from the skeletal cloud following (Telea and Jalba, 2012). Given the high resolution of the skeletal cloud, the reconstructed skeleton also has a very complex manifold structure. Robustly finding the boundaries of these manifolds, to further apply the patch-based segmentation of (Reniers and Telea, 2008b), is very challenging, as already noted in Sec. 2.

### 3.2 Surface Curvature vs Skeleton Density

To further segment our skeleton cloud, we use the following observations linking the curvature of $\partial \Omega$ and point density on $S_\Omega$. Consider a densely sampled $\partial \Omega$. For a positive-curvature region of $\partial \Omega$ (bump, or convexity), the ball-shrinking directions $rn$, identical to the feature vector directions, point inwards in a converging fashion. Hence, the density of the skeletal points for this region will be higher than the surface density. Conversely, for a region with negative curvature (a crease, or concave, region), the ball-shrinking directions will point inwards in a diverging fashion, so the density of the skeletal points for this region will be lower than the surface density. Figure 3 (top) illustrates this in 2D. Figure 3 (bottom) shows an actual example for a 3D skeletal cloud computed from a dental cast. We observe that skeletal parts enclosed in the front teeth present a high point density, since these teeth are indeed convex shape parts.

### 3.3 Mean Shift Clustering

We now show how to use the density-related observations in Sec. 3.2 to segment the skeleton cloud.

Since the skeletal cloud exhibits strong density variations, it should be possible to segment it into point clusters representing the dense regions based on a method which exploits such density variations. An ideal such method is mean shift clustering (Comaniciu and Meer, 2002), which we extend to our segmentation needs, as follows. We start by selecting a set of seed points $P \subset S_\tau$ from the simplified skeleton. The seed point selection is discussed separately.
in Sec. 3.4. Each seed point \( x \in P \) is assigned a unique ‘segment id’. For each seed point \( x \in P \), we aim to find its so-called convergence point \( c(x) \in \mathbb{R}^3 \). For this, we first find all neighbors \( N^\varepsilon_x \subset S \) of \( x \) within a small fixed radius \( \varepsilon \) and determine the centroid of \( N^\varepsilon_x \)

\[
\mathbf{m}(x) = \frac{\sum_{y \in N^\varepsilon_x} K(||x - y||)}{\sum_{y \in N^\varepsilon_x} K(||x - y||)}
\]

(4)

where \( K \) is a Gaussian kernel

\[
K(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2\sigma^2}}
\]

(5)

following the kernel density estimation idea in (Comaniciu and Meer, 2002). \( \varepsilon \) is set to a small fraction (about 5%) of the model size. We next iteratively shift the seed points \( x \) to their centroids \( \mathbf{m}(x) \) following Eqn. 4 (see also Fig. 4 a) until these stabilize, i.e., move at one iteration less than a small threshold \( \lambda = ||\mathbf{m}(x) - x|| \), set in practice to \( 10^{-4} \). Also, for each non-seed point (which is not shifted), we define a voting weight \( v(y) \), initialized to zero at the beginning of the algorithm. At every mean-shift iteration, we add a value \( K(||y - \mathbf{m}(x)||) \) to \( v(y) \) for each non-seed point \( y \in N^\varepsilon_x \), and also add a pointer from \( y \) to \( \mathbf{m}(x) \), to indicate that \( y \) was in the neighborhood of \( \mathbf{m}(x) \). When \( \mathbf{m}(x) \) has converged, we search its neighborhood for other existing convergence points \( c' \) than itself. If one exists, we merge the ids of \( \mathbf{m}(x) \) and \( c' \). Otherwise, we create a new convergence point \( c = \mathbf{m}(x) \).

At the end of the mean shift, all seed points have thus converged to a set \( C \) of convergence points (see Fig. 4 b). The ids of the points \( c \in C \) give us the final segments. Finally, to assign each non-seed point \( y \in S \) to a segment, is done by assigning to \( y \) the id of the convergence point that it is linked to and which has the highest amount of votes within the \( k \) last iterations (Fig. 4 c). Different segmentation levels can be achieved by considering the voting of only the last \( k \) iterations of the mean shift process. This way, only the areas around the skeleton-cloud density peaks are considered. This is illustrated by the dental cast models, where the gum areas remain mostly unsegmented (Fig. 5 a–c), for which we used a value \( k = 20 \). In contrast, for the other shapes in Fig. 5 f–k, the full mean-shift path has been considered for the voting, leading to the full surface being segmented into patches.

### 3.4 Seed Point Detection

We find the initial seed points \( P \) used in mean shift clustering by using the specific geometry of our dental casts. We want at least one seed point in each relevant segment (that is, inside each high-density cluster such as the ones in Fig. 3): we do not want seed points outside such segments. We allow more seed points in a segment, so that finding seed points is not parameter-critical. The definition of segment relevance is application-dependent: For our dental cast use-case, we only want the teeth segments and the gum, i.e., we don’t want to over-segment the gum. To achieve this, we use as seed points all skeleton points which (a) have a low distance \( DT_{\Omega}(s) \) to the original surface \( \partial\Omega \) and (b) have a high curvature, computed as the angle between the feature vectors \( f_1 - s, f_2 - s \).

### 3.5 Segmentation Transfer to Surface

In the last step, we transfer the skeleton segmentation to the input surface, as follows. For each point \( s \in S \), we copy the segment ID of \( s \) to its two feature points \( f_1 \) and \( f_2 \). However, this does not assign a segment ID to all points on \( \partial\Omega \), since we segmented the simplified skeleton \( S_f \) rather than the full skeleton \( S \). For all points \( p \in \partial\Omega \) which are not assigned a segment ID, we search the closest surface point \( p' \in \partial\Omega \) which has an ID \( ID(p') \) assigned, and mark \( p \) with the same \( ID(p') \). This fills the gaps between segments on \( \partial\Omega \) in distance order, yielding a full, non-overlapping, surface segmentation.
4 RESULTS

Figure 5 shows several results. Surface segments are colored differently, for illustration. For images (a-e), which show dental cast scans, we see that the method separates very well the incisives, canines, molars and pre-molars, both from each other, and also from the gums. We also see several problems. The molars are over-segmented (Fig. 5 a,b), and occasionally the gums are also oversegmented (Fig. 5 c,e). The gums oversegmentation is not problematic for the considered orthodontic application, since users are only interested to analyze the teeth, and not the gums. The molars oversegmentation is explained by the fact that they (a) have a more complex geometry than the other teeth (more internal creases) and also that, in our models, the input surface has less points here. Hence, the skeletal manifolds for these detail-rich areas are too poorly sampled to fully capture their features. We also segmented other shapes than dental casts, to get more insight in the method’s behavior (Figs. 5 f-k). Several observations can be made. For models having convex surface areas separated by well-delimited concave ridges, such as the hand or spider, we get the expected segmentation, just as for the dental casts. For the other models, segments are created around the most salient convex bumps of the shape. These segments meet along the model concavities, or creases – see e.g. the nose, eyes, and chin of the face model (Fig. 5 j); bunny years, tail, head, rump, and front paw (Fig. 5 h); and the convex bone components of the sacrum model (Fig. 5 k).

5 DISCUSSION

Several aspects are relevant for our method.

Simplicity and Novelty. A key asset of our method is its algorithmic simplicity. We use algorithms with proven accuracy, convergence, and complexity properties (Comaniciu and Meer, 2002; Reniers and Telea, 2008a; Jalba et al., 2013). Our method is the first we are aware of to use surface skeletons computed on mesh models to segment surfaces. Its only competitor, using more expensive and lower-resolution voxel models, is (Reniers and Telea, 2008b). This is also the first use of mean shift to cluster skeletons.

Robustness. The method is robust to different surface point-sampling densities, as the segmentation is performed based on the medial surface density properties. We tested our method on several dental cast models with the same parameter settings, and
Table 1: Segmentation timings.

<table>
<thead>
<tr>
<th>Model</th>
<th>dental 1</th>
<th>dental 2</th>
<th>dental 3</th>
<th>dog</th>
<th>bunny</th>
<th>bone</th>
<th>hand</th>
<th>spider</th>
<th>face</th>
</tr>
</thead>
<tbody>
<tr>
<td># points (surface)</td>
<td>119594</td>
<td>127578</td>
<td>82887</td>
<td>18114</td>
<td>34834</td>
<td>41035</td>
<td>327323</td>
<td>29741</td>
<td>35437</td>
</tr>
<tr>
<td># points (skeleton $S$)</td>
<td>6136</td>
<td>24339</td>
<td>11214</td>
<td>16823</td>
<td>10706</td>
<td>8271</td>
<td>128839</td>
<td>8389</td>
<td>8450</td>
</tr>
<tr>
<td># seed points</td>
<td>339</td>
<td>487</td>
<td>373</td>
<td>336</td>
<td>535</td>
<td>827</td>
<td>644</td>
<td>829</td>
<td>1041</td>
</tr>
<tr>
<td>CPU skeletonization (sec)</td>
<td>51.3</td>
<td>48.53</td>
<td>22.87</td>
<td>34.89</td>
<td>10.96</td>
<td>5.85</td>
<td>12.8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>GPU skeletonization (sec)</td>
<td>11.7</td>
<td>11.0</td>
<td>5.78</td>
<td>3.24</td>
<td>3.6</td>
<td>1.82</td>
<td>31.2</td>
<td>0.95</td>
<td>2.11</td>
</tr>
<tr>
<td>CPU segmentation (sec)</td>
<td>1.95</td>
<td>1.92</td>
<td>1.3</td>
<td>43.07</td>
<td>2.71</td>
<td>40.12</td>
<td>152.02</td>
<td>167.53</td>
<td>11.35</td>
</tr>
<tr>
<td>CPU total (sec)</td>
<td>53.25</td>
<td>50.45</td>
<td>24.17</td>
<td>77.96</td>
<td>13.67</td>
<td>50.38</td>
<td>303.7</td>
<td>173.38</td>
<td>24.15</td>
</tr>
<tr>
<td>GPU total (sec)</td>
<td>13.65</td>
<td>12.92</td>
<td>7.08</td>
<td>46.31</td>
<td>6.31</td>
<td>41.94</td>
<td>183.22</td>
<td>168.48</td>
<td>13.46</td>
</tr>
</tbody>
</table>

obtained identical results (cf. Figs. 2, 5).

**Applicability.** Our method is, by construction, geared towards the segmentation of convex surface patches separated by shallow creases. In this sense, we stress that the skeleton simplification (Eqn. 3) only eliminates skeleton points corresponding to small-scale surface bumps (convexities), but no skeleton point corresponding to a concavity (crease). This makes our method principally more robust than many other curvature-based segmentation methods. Also, our method can handle non-watertight surfaces (such as our teeth scans, which are not closed at the base, or the face model in Fig. 5 j) with no problems.

**Performance.** We implemented our method in C++ using ANN (Mount and Arya, 2011) to find nearest neighbors and the GPU skeletonization in (Jalba et al., 2013). The latter also provides the needed distance transform, feature points, and importance metric (Sec. 3.1). For 3D surface supersampling, we used Yams (Frey, 2001). Tab. 1 shows timings on a Windows PC at 2.66 GHz with an Nvidia 690 GTX for several shapes. Skeletonization times include regularization (Eqn. 3); we show timings for (Jalba et al., 2013) on both GPU and CPU. Segmentation timings include mean shift, segment ID assignment, and transfer on the original surface, all done on the CPU. As expected, GPU skeletonization is much faster than its CPU counterpart. The segmentation cost varies in function of the actual model. For the dental casts, this cost is quite low. Indeed, for these models, we use only the last $k$ iterations (Sec. 3.3), whereas for the other models we use the full mean shift path. The segmentation (not optimized, unlike skeletonization) is dominated by the nearest neighbor searches. Such searches can be massively accelerated using GPUs, as shown in (Jalba et al., 2013), so a GPU mean shift implementation should massively accelerate this step.

**Dental Use-case.** For teeth segmentation, our method can segment all teeth whose medial surfaces converge to a point density maximum. Given the geometry of the incisives, canines, molars and pre-molars, we saw that these present the expected properties, so are robustly segmented. Molars have a slightly more complex geometry, including too shallow separation creases from gums. This creates some challenges (over-segmentation) when using the exact same mean-shift parameters as for the other teeth (see e.g. Fig. 2 a,b). Possible ways to overcome this are supersampling the input mesh, leading to a surface skeleton with better separated manifolds. However, we stress that, even with such limitations, our method is superior to existing alternatives in the orthodontic industry (see references in Sec. 2), as all such methods require a non-trivial amount of user input to produce their segmentations.

**Limitations.** As seen in Fig. 5, our method cannot be directly applied to any 3D shape. The method is geared towards segmenting shapes whose skeletal manifolds exhibit clearly separated high-density branches, each branch corresponding to one surface segment. These are surfaces with convex patches separated by concave ridges. As such, one should not attempt to compare our current method with other general-purpose surface segmentation methods. Still, the main added value of our technique for segmenting general shapes (apart from the segmentation of dental casts) is the proof that point-cloud skeletons can be used for segmenting complex 3D surfaces. To our knowledge, this result has not been shown so far in current literature. Future work is needed to study how this result can be extended to more general surfaces.

6 CONCLUSIONS

We have presented a method for segmenting compact convex patches of 3D polygonal surfaces from dental cast scans which are separated by shallow creases. For this, we use the properties of surface skeletons, in particular the sampling relationship between the skeleton and its original surface, and the correspondence relationship between the two surfaces given by the feature transform. To our knowledge, our method...
is the second existing technique able to use surface skeletons to segment 3D surfaces. In contrast to the first published technique in this area (Reniers and Telea, 2008b), we can directly handle meshed models without a costly voxelization step; we do not require the complex and sensitive detection of skeletal boundaries; and we can treat significantly more complex shapes than the earlier cited method in this class.

Our research is motivated by the need to create robust and fast segmentations of dental cast models, driven by a concrete industrial application at Philips Research, Eindhoven, the Netherlands. We foresee several possible extensions of our method towards a more general-purpose surface segmentation technique. Examples are the incorporation of surface differential properties, captured by the feature transform, in the analysis and segmentation of the surface skeleton, and application-adaptive skeleton simplification metrics that preserve or eliminate specific surface details for the purpose of more versatile segmentation.

REFERENCES


