Forecasting Price Movement of SOFIX Index on the Bulgarian Stock Exchange – Sofia using an Artificial Neural Network Model

Veselin L. Shahpazov, Vladimir B. Velev and Lyubka A. Doukovska

Institute of Information and Communication Technologies, Bulgarian Academy of Sciences,
Acad. G. Bonchev str., bl. 2, 1113 Sofia, Bulgaria
veselin.georgiev@abv.bg, vladimir.velev@allianz.bg, doukovska@iit.bas.bg

Keywords: Forecasting, SOFIX Index, Artificial Neural Network, Business, Predicting Stock Prices, Supervised Learning.

Abstract: The Bulgarian capital market is characterized by its relatively short history and its low liquidity, SOFIX is the first index of BSE-Sofia based on the market capitalization of the included issues of common shares, adjusted with the free-float of each of them. The authors intend to use a model implying an Artificial Neural Network to predict the future price of the index. A neural network has the ability to extract useful information from large sets of data, which often is required for a satisfying description of a financial time series. Capital markets are known for their complexity and unpredictability and are best described as chaotic systems. Artificial Neural Networks can be used to find relationship in large sets of data which have some unknown relationship between input and output. Once that relationship is found, the neural network can be used to compute the output for similar (but usually different) input.

1 INTRODUCTION

The Bulgarian capital market is characterized by its relatively short history and its low liquidity, especially in recent years. Yet the companies listed represent different economic segments from the heavy production industry to pharmaceuticals and local banking. SOFIX is the best known and the first index of BSE-Sofia, which calculation started on October 20, 2000. SOFIX is based on the market capitalization of the included issues of common shares, adjusted with the free-float of each of them. SOFIX is the most successful index calculated by BSE-Sofia and is the first one on which structured products are based on. The index covers the 15 issues of shares complying with the general requirements for selection of constituent issues that have the greatest market value of the free-float.

Artificial Neural Networks are flexible computing frameworks and universal approximators that can be applied to a wide range of time series forecasting problems with a high degree of accuracy, (Atsalakis, 2009). They are an artificial intelligence method for modeling complex target functions. For certain types of problems, such as learning to interpret complex realworld sensor data, Artificial Neural Networks are among the most effective learning methods currently know. During the last decade they have been widely applied to the domain of financial time series prediction and their importance in this field is growing. The ability of neural networks to closely approximate unknown functions to any degree of desired accuracy has generated considerable demand for Neural Network research in Business. The attractiveness of neural network research stems from researchers need to approximate models within the business environment without having a priori knowledge about the true underlying function, (Sexton, 1998). However, despite all advantages cited for artificial neural networks, their performance for some real time series is not satisfactory.

Predicting stock prices with traditional time series analysis has proven to be difficult. An artificial neural network may be more suitable for the task. Primarily because no assumption about a suitable mathematical model has to be made prior to forecasting. Furthermore, a neural network has the ability to extract useful information from large sets of data, which often is required for a satisfying description of a financial time series, (Nygren, 2004). In recent years, neural networks have received an increasing amount of attention as a very
popular forecasting and data mining tool. Their origin stems from the attempt to model the human thought process as an algorithm which can be efficiently run on a computer. Software is developed to mimic this thought process. A neural network can be used to find relationships in large sets of data which have some unknown relationship between input and output. Once that relationship is found, the neural network can be used to compute the output for similar (but usually different) input, (Choong, 2009). One of the advantages include automatic learning of dependencies only from measured data without any need to add further information (such as type of dependency like with the regression). The neural network is trained from the historical data with the hope that it will discover hidden dependencies and that it will be able to use them for predicting into future.


2 PROBLEM FORMULATION

The neural network that the authors intend to use for predicting the price of Sofix index will be trained with supervised learning. The network that will be used will be a feed forward, multi-layer perceptron network with very fast learning and an advanced mechanism to prevent overfitting. The Multi-layer perceptron (MLP) networks trained using backpropagation (BP) algorithm are the most popular choice in neural network applications in finance, (Atsalakis, 2009 and Atanasova, 2006). The MLP networks are feed forward neural networks with one or more hidden layers which is capable to approximate any continuous function up to certain accuracy just with one hidden layer (Cybenko, 1989).

The MLP consists of three types of layers. The first layer is the input layer and corresponds to the problem input variables with one node for each input variable. The second layer is the hidden layer used to capture non-linear relationships among variables. The third layer is the output layer used to provide predicted values.

The data used for the study is from the Bulgarian stock exchange official website, and consists of the following: last price, open, high, low and volume traded, as well as five of the most commonly used technical indicators (according to study conducted by bightrends.com): the 30 day moving average, 60 day moving average, 200 day moving average, the 14 day relative strength index and the 30 day relative strength index. The training data covers a period of two years and two months or from 04.01.2011 until 08.03.2013. We find the period appropriate because it consists of an uptrend and a downtrend in the first couple of months than the price of SOFIX consolidates and in the last months of the observed period enters into an uptrend. This we believe will permit us to train the network in a better way and produce results with a minimal error.

The training data is split into three parts, with the major part of 50% of the data is treated as actual training data, and the rest are treated as a testing data (25%) and validation data (25%).

The software used during this study is STATISTICA 7.0. The preferred Neural Network structure was a three layer perceptron.

The software operates using back-propagation and conjugate gradient descent algorithms for training the network. The Artificial Neural Networks implements the on-line version of back propagation; i.e. it calculates the local gradient of each weight with respect to each case during training. Weights are updated once per training case.

The update formula is:

$$\Delta \omega_i(t) = \eta \delta_i + \alpha \Delta \omega_i(t-1)$$

(1)

where:

- $\eta$ - the learning rate;
- $\delta$ - the local error gradient;
- $\alpha$ - the momentum coefficient;
- $o_i$ - the output of the i'th unit.

Thresholds are treated as weights with $o_i = -1$. The local error gradient calculation depends on whether the unit into which the weights feed is in the output layer or the hidden layers. Local gradients in output layers are the product of the derivatives of the network's error function and the units' activation functions. Local gradients in hidden layers are the weighted sum of the unit's outgoing weights and the local gradients of the units to which these weights connect.

The Conjugate gradient descent (Bishop, 1995; Shepherd, 1997) is an advanced method of training multilayer perceptron’s. It usually performs significantly better than back propagation, and can be used wherever back propagation can be. It is the recommended technique for any network with a large number of weights (more than a few hundred).
and/or multiple output units. Conjugate gradient descent is a batch update algorithm: whereas back propagation adjusts the network weights after each case, conjugate gradient descent works out the average gradient of the error surface across all cases before updating the weights once at the end of the epoch.

The most widely used activation function for the output layer are the sigmoid and hyperbolic functions. In this paper, the sigmoid transfer function is employed and is given by:

\[ E(t) = \frac{1}{1 + e^{-t}} \]  

(2)

The criteria which will evaluate the Neural Networks performance will be the error of the network on the subsets used during training (Root Mean Square-RMS).

\[ RMS = \sqrt{\frac{\sum_{i=1}^{n} (\hat{y}_i - y_i)^2}{n}} \]  

(3)

This is less interpretable than the performance measure, but is the figure actually optimized by the training algorithm (at least, for the training subset).

This is the RMS of the network errors on the individual cases, where the individual errors are generated by the network error function, which is either a function of the observed and expected output neuron activation levels (usually sum-squared or a cross-entropy measure); or Sum-squared. The error is the sum of the squared differences between the target and actual output values on each output unit. This is the standard error function used in regression problems.

The weights and biases of the network are automatically initialized to small random numbers by the software.

3 STUDY RESULTS

In order to achieve better results with training the Neural Network the authors decided to transform the input data from values to change. Since the period of time that the input data represents is limited to nearly two years the index fluctuates between a minimum value of 286.03 and a maximum value of 455.75.

The initial results showed that the networks that utilized all eight input parameters (last price, open, high, low and volume traded 30 day moving average, 60 day moving average, 200 day moving average, the 14 day relative strength index and the 30 day relative strength index) performed consistently much worse than the ones that isolated some of the input parameters. The networks that based their prognoses solely on the last price showed the best results in terms of test error.

The tests were conducted with different network architecture but the best result was obtained with a three layer perceptron, consisting of 1 input (43 time lagged steps) 7 nodes in the hidden layer and 1 output, training consisted of 100 epochs using back-propagation and 23 epochs using the conjugate gradient descent algorithm, the test error amounted to 0.119279. It is important to outline that the software stops the learning process when the minimum error is reached, that way it prevents the network from over-fitting.

After taking into consideration the specifics of the Bulgarian stock market (the extremely low traded volume, a problem that exposes the index to manipulation which will lead to distortion of the network results) the authors have found appropriate to conduct moving average smoothing to the input data commencing with 3 days smoothing (calculating the average value of the last three days).

As seen from the results shown in Table 1 this data manipulation managed to bring down the test error considerably. The table shows the effects of increasing the period that has been smoothed, the

<table>
<thead>
<tr>
<th>Network structure</th>
<th>Learning samples</th>
<th>Test error RMS</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 days smoothing</td>
<td>BP-100; CGD-115</td>
<td>0.076298</td>
</tr>
<tr>
<td>4 days smoothing</td>
<td>BP-100; CGD-58</td>
<td>0.089827</td>
</tr>
<tr>
<td>5 days smoothing</td>
<td>BP-100; CGD-48</td>
<td>0.067025</td>
</tr>
<tr>
<td>6 days smoothing</td>
<td>BP-100; CGD-76</td>
<td>0.075116</td>
</tr>
<tr>
<td>7 days smoothing</td>
<td>BP-100; CGD-34</td>
<td>0.057099</td>
</tr>
<tr>
<td>8 days smoothing</td>
<td>BP-100; CGD-68</td>
<td>0.057903</td>
</tr>
<tr>
<td>9 days smoothing</td>
<td>BP-100; CGD-67</td>
<td>0.064887</td>
</tr>
</tbody>
</table>
different network structures, learning samples and most importantly the resulted test error. The error reaches its minimum with 7 day smoothing and a structure of the network with 1 input (20 time lagged steps) 13 nodes in the hidden layer and 1 output, training consisted of 100 epochs using back-propagation and 34 epochs using the conjugate gradient descent algorithm, the test error amounted to 0.057903.

Figure 1: Structure of Neural Network with 1 input (20 time lagged steps) 13 nodes in the hidden layer and 1 output.

Figures 1, 2, 3 and 4 show structure, predicted values versus observed plot, graphic of the predictions over the analysed period and the residual error diagram respectively.

As we can see from Figure 4, the error tends to increase in the beginning and the end of the analysed period of time. This can be explained from an economic perspective with the fact that during both periods the Bulgarian stock market is in a trend situation usually characterized with higher volatility in the prices of stocks, especially in downtrends. This leads the authors to believe that predictive abilities of a neural network are better suited for markets that find themselves in a period of consolidation.

The Networks that were fed with the same pre-processed data but trained with all 10 input parameters showed worse results. In the case with the best results (7 days smoothing) in terms of test error, the value of RMS 0.068935, the network structure produced by the software was 9 input (15 time lagged steps) 21 nodes in the hidden layer and 1 output, training consisted of 100 epochs using back-propagation and 81 epochs using the conjugate gradient descent algorithm.
4 CONCLUSIONS

In this paper, the problem of predicting the price of Bulgarian Stock Exchange’s Sofix index using neural networks is considered. The analyzed period is of two years and two months or from 04.01.2011 until 08.03.2013. Data used for the case consists of the daily values of last price, open, high, low and volume traded 30 day moving average, 60 day moving average, 200 day moving average, the 14 day relative strength index and the 30 day relative strength index.

The criteria which was used to evaluate the Neural Networks performance was the error of the network on the subsets used during training (Root Mean Square)

The input data was preprocessed and transformed from values into daily changes. Initial readings showed that better results would be achieved if the input is one compared to using all or fragments of the initial data set.

Smoothing ranging from 3 to 9 days was performed in order to eliminate the effects of the low liquidity and higher volatility in the market.

Results showed that this data manipulation managed to bring down the test error considerably. The produced neural network was structured by 1 input (20 time lagged steps) 13 nodes in the hidden layer and 1 output, training consisted of 100 epochs using back-propagation and 34 epochs using the conjugate gradient descent algorithm, the test error amounted to 0.057903. In comparison the best performing network using all or partial input data managed an error of 0.068935.

The obtained result was found good but the authors see further room for improvement of the predicting capabilities of the model. The error margin is still considered big and attempts to bring it further down will be made, especially improving the predictive capabilities for trends. The low liquidity and high volatility environment of the Bulgarian stock market is a challenge that could be addressed more efficiently with similar neural networks that have different structure and learning algorithms.

Future work will involve different input data and data pre-processing, possibly other types of neural networks and algorithms.

ACKNOWLEDGEMENTS

The research work reported in the paper is partly supported by the project AComIn “Advanced Computing for Innovation”, grant 316087, funded by the FP7 Capacity Programme (Research Potential of Convergence Regions) and partially supported by the European Social Fund and Republic of Bulgaria, Operational Programme “Development of Human Resources” 2007-2013, Grant № BG051PO001-3.3.06-0048.

REFERENCES

Lawrence R., Using Neural Networks to Forecast Stock Market Prices, Department of Computer Science University of Manitoba, December 12, 1997.

Tilakaratne C. D., S. A. Morris, M. A. Mammadov, C. P. Hurst, Predicting Stock Market Index Trading Signals Using Neural Networks, Centre for Informatics and Applied Optimization School of Information Technology and Mathematical Sciences University of Ballarat, Ballarat, Victoria, Australia. 2008.

Alhaj Ali S. M., A. A. Abu Hammadb, M. S. Samhouriya, A. Al-Ghandoora, Modelling Stock Market Exchange Prices Using Artificial Neural Network: A Study of Amman Stock Exchange, Industrial Engineering, Department, Faculty of Engineering, Hashemite University, Jordan. JMJIE Volume 5, Number 5, 2011.


Skabar A., I. Cloete, Neural Networks, Financial Trading and the Efficient Markets Hypothesis, School of Information Technology International University in Germany, Twenty-Fifth Australasian Computer Science Conference (ACSC2002), 2002.


 Sexton R. S., B. Alidaee, R. E. Dorsey, J. D. Johnson, Global Optimization for Artificial Neural Networks: A Tabu Search Application, European Journal of
Choong J., Build Neural Network with MS Excel, Published by XLPer Enterprise by XLPer Enterprise, 2009.