Module Isolation for Efficient Model Checking and its Application to FMEA in Model-driven Engineering

Vladimir Estivill-Castro and René Hexel
School of Information and Communication Technology, Griffith University, Nathan, QLD, Australia

Keywords: Model-driven Engineering, Formal Methods, Software Modelling, Failure Mode Effects Analysis.

Abstract: Model-driven development results in directly runnable implementations, and therefore it is of utmost importance to formally verify and validate such models. However, model-checking usually faces the challenge of concurrent modules generating a state space equal to the Cartesian product of the state spaces of all modules. This is even more dramatic as recent trends in model-driven-engineering aim at not only modelling the software in question, but other components of the system as well, in order to perform Failure Mode Effects Analysis (FMEA). These additional components further enlarge the collective state space. We provide an algorithm that identifies the sections of the system that are independent, enabling verification of separate sections of the system. As a consequence, formal verification of the system as well as the corresponding FMEA can be performed much more efficiently.

1 INTRODUCTION

Model-driven engineering is proving to be a widely successful approach to developing software. Tools and techniques are resulting in faster and simpler (easier to maintain) products and applications than traditional language parser/compiler or interpreter approaches. Model-driven engineering ensures traceability, validation against requirements, and platform independence (Schmidt, 2006). Finite state machines in particular are ubiquitous, for instance those of executable UML (Mellor and Balcer, 2002), MathWorks®, StateFlow or StateWorks (Wagner et al., 2006). There are now several commercial tools and standards to represent and compose behaviours for software that will execute in embedded systems. Among others, these include SysML (Friedenthal et al., 2009) and MathWorks® StateFlow with Simulink. Penetration of these technologies includes large industrial sectors such as the automotive industry (SLSF, 2009; GMG, 2009).

The safety of such systems is critically linked to the verification of the models as models are directly implemented. However, model-checking of concurrent finite state machines (FSMs) (or analogous modelling approaches, such as decision trees and Requirement Refinement Modeling Diagrams (RRMDs) (Satpathy et al., 2013)) face the challenge that the number of possible state combinations of the system is the Cartesian product of the possible states of the components. This can significantly hamper the use of formal methods and model-checking to verify models. Moreover, showing that a model is correct is just the first step. Systems are also examined using fault injection and extensive Failure Mode Effects Analyses (FMEAs). These FMEAs provide confidence that the software robustly handles failures of subsystems and other components. But, the automation of such an analysis starts by complementing the software models with models representing the hardware (i.e., sensors, actuators, and effectors). Thus, FSMs are used to represent the possible states of buttons, levers, or even operators. The entire system (software plus modelled external components) is then submitted to exhaustive exploration. Fault injection is then used on each modelled component to generate FMEA tables that contain information about violations of requirements or safety properties (Grunske et al., 2011; Estivill-Castro et al., 2012b). This is achieved by simulation or through formal model-checking. However, these extra FSMs required to model the additional hardware components, contribute multiplicatively to the overall size of the system state space: this further explosion of the state space makes it prohibitively costly (or even impossible) to use standard model-checking tools.

We show that the process described above can be significantly improved by systematically identifying independent components or groups of components.
Module Isolation for Efficient Model Checking and its Application to FMEA in Model-driven Engineering

...that we can demonstrate can be verified separately. Thus, without loss of generality, model-checking of the system can be partitioned. Similarly, the same model-checking process that performs FMEA can also be completed on the independent partitions while still being able to provide the complete FMEA table for the system. That is, our approach enables complete validation of models as well as comprehensive failure analysis in scenarios that would otherwise be too complex or costly to formally verify.

There is a further aspect where our approach offers a significant improvement on previous work. Estivill-Castro, Hexel and Rosenblueth (Estivill-Castro et al., 2012c) reduced the challenge of model-checking concurrent executable models by prescribing a deterministic sequential schedule on a single CPU. That approach reduced all possible permutations of states of computation to only those that were derived from the schedule. Similarly, the RRMDs (Satpathy et al., 2013) approach removes all parallelism, and converts the program into a totally deterministic behavior. Deterministic scheduling facilitates model-checking but prevents truly parallel execution of the system. If such software is to execute on hardware that supports more than one CPU (or a multi-core CPU, which is becoming increasingly common now, even on mobile or embedded systems), then such a sequential approach is not able to not take advantage of the true parallelism available on these systems. With our approach here, we can identify groups of modules that can be scheduled in parallel and still have completely verified models under consequential parallel schedules.

We will use two case studies to support the argument. Both examples are a widely used example in the literature of model-checking, model-driven development and safety: the one-minute microwave and the mine pump. The one-minute microwave has analogies for safety with well-publicised cases such as the failure of the Therac-25 X-Ray machine.

<table>
<thead>
<tr>
<th>Req.</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>R 1</td>
<td>There is a single control button available for the use of the oven.</td>
</tr>
<tr>
<td>R 2</td>
<td>If the oven is closed and you push the button, the oven will start cooking (that is, energise the power-tube) for one minute.</td>
</tr>
<tr>
<td>R 3</td>
<td>Pushing the button when the door is open has no effect.</td>
</tr>
<tr>
<td>R 4</td>
<td>When the oven is cooking, the light in the oven will be on.</td>
</tr>
<tr>
<td>R 5</td>
<td>Opening the door stops the cooking.</td>
</tr>
<tr>
<td>R 6</td>
<td>Closing the door turns off the light. This is the normal idle state, prior to cooking when the user has placed food in the oven.</td>
</tr>
<tr>
<td>R 7</td>
<td>If the oven times out, the light and the power-tube are turned off and then a beeper emits a warning beep to indicate that the cooking has finished.</td>
</tr>
</tbody>
</table>

2 TACKLING COMPLEXITY

The one minute microwave is a good case study for modelling requirements. Scholars discussing this example typically present a series of requirements in natural language like those in Table 1. Techniques such as behavior-trees, Petri Nets, plain finite-state machines (Wagner et al., 2006) and logic-labeled finite state machines (Estivill-Castro et al., 2012b) have been used to model this case study.

Fig. 1 shows the model that uses logic-labeled finite state machines (Estivill-Castro et al., 2012b) for the microwave controller (Estivill-Castro et al., 2012a). It consists of four finite state machines that are executed in a round robin fashion. Through such sequential execution, all possible state combinations that can occur in the system can be derived (Estivill-Castro et al., 2012c).

The sequential program corresponds to a Kripke structure by standard transformation techniques (Clarke et al., 2001, Chap. 2), and thus, standard model-checking tools such as NuSMV can be applied to establish that this software controller fulfills safety properties. For the microwave, safety
We can then build the FMEA table of failures and their consequences. Removal or modification of behaviour are indeed explored in detail. Each transition (arrow), state, or any value assignments in the corresponding sections of the states can be modified or removed. One such modification/removal consists of a single fault injection from the table (level 1). If we perform two such operations, we inject a level 2 fault. (Generally, the likelihood of higher level independent faults occurring quickly becomes infinitesimally small; consequently fault-tolerant systems aim at tolerating at least every possible level 1 fault, while only being able to handle some, clearly defined level 2 faults (Hixel, 2003)). After each fault-injection operation, we have a (faulty) model for which NuSMV is executed to determine the affected properties. The faults injected constitute the rows of the FMEA table while the columns constitute the properties. Note that automatic completion of the table requires the execution of a model checker. And therefore, there are as many entries in the FMEA table as properties and possible modifications/removals to/from the model.

If execution a model checker is already a costly exercise, completing the FMEA table multiplies this further by a large factor.

The useful set of modelling tools (such as logic-labeled finite-state machines or behavior trees), enables extending models to also represent hardware components. So the second type of fault injection concerns the simulation of hardware faults through software (Hixel, 2003)). For example, in the case of the microwave, we could model the actual bulb that produces the light. This example is for illustration only, but the point is that Fig. 1b) is a model, in software, of that hardware component. The variable int light models the belief of the software (along with the current state identifier) of whether the light has been asked to be on or off. A separate finite state machine as per Fig. 3 models the actual light bulb hardware (and any other connections and communications that turn the light on or off). In this particular illustration, the modelling of the hardware components of the system may not seem add much to the original analysis, but in other examples (such as the industrial press example (Grunske et al., 2011)) it is common to model hardware components that may be faulty in different ways, or sometimes even possible behaviour by people, e.g. mistakes made by a human operator.

These additional components (beyond the software model) enable simulation of the system as a whole, allowing validation of that system. Naturally, to actually perform verification and to carry out the analysis of building an FMEA table, the next step is to systematically inject faults into the model. For in-

---

**Figure 2:** NuSMV coding of the property that the cooking must stop if the door is held open.

properties include the following

Property-1 “Necessarily, the oven stops (after several steps, i.e. a small, finite number of transitions in the Kripke structure) after the door opens.”

Property-2 “It is necessary to pass through a state in which the door is closed to reach a state in which the motor is working and the machine has started.”

Property-3 “Necessarily, the oven stops (after several steps, i.e. again, a small, finite number of transitions in the Kripke structure) after the timer has expired.”

Property-4 “Cooking may go on for ever (e.g. if the user repeatedly keeps pressing the add button while the timer is still running).”

The NuSMV coding using a CTL (Computation-Tree Logic (Clarke and Emerson, 1981; Huth and Ryan, 2004)) formula for Property 1, for Property 2, and Property 3 appears in Fig. 2.

However, the next step is the Failure Mode Effects Analysis of these properties. For that, two types of fault injection are used. The first type consists on introducing a fault into one or more of the components of the software model. That is, we perturb the components displayed in Fig. 1. The suggested fault injection consist of the following operations (Grunske et al., 2011), loosely following the well-established original classification (Bondavalli and Simoncini, 1990):

1. to remove behaviour from the model (an omission failure) and test all properties, and
2. to modify (a value failure) behaviour and test all properties.
We propose a method to identify dependencies between components. We use the semantics and sequential scheduling (Estivill-Castro et al., 2012b; Estivill-Castro et al., 2012a) proposed for logic-based finite-state machines (FSMs). These FSMs consist of a set $S$ of states and a transition table $T : S \times E \rightarrow S$. There is an initial state $s_0 \in S$, and for each state, the transitions leading out of the state are ordered in a sequence. Transitions are labeled by an expression $e \in E$, and these expressions are evaluated in deterministic order (and time) by an expert system (the examples in the literature use Decisive Plausible Logic (DPL) (Estivill-Castro et al., 2012b; Estivill-Castro et al., 2012a), but the expressions can also be Boolean expressions of an imperative programming language such as C, C++, or Java (or any decidable logic, that provides an answer in predictable time). The point is that execution of an vector of these machines (such as the ones in Fig. 1 in the previous section) is sequenced deterministically by a pre-defined schedule. Each machine in the vector receives a pre-defined number of ringlets it executes before execution passes to the next machine in the vector. The execution token passes back to the first machine after the last machine completes its allocated ringlets. A ringlet consists of evaluating the $\text{OnEntry}$ section of the current state (if it is the first time control arrives to this state from another state in this machine), followed by evaluation of the expressions in the list of transitions until an expression evaluates to true. In this case, the $\text{OnExit}$ section is evaluated and the ringlet concludes. If the list of transitions is exhausted without any expression becoming true; then the $\text{Internal}$ section of the state completes and the ringlets also conclude. Thus a ringlet is the complete assessment of the current state.

The shared variables between the different modules (FSMs) are called external variables and are managed on a repository architecture named the whiteboard (Hayes-Roth, 1988). When the execution token arrives at a machine, it makes a local copy of any external variables it will use in the current state. We refer to this as the $\text{READ}$ footprint on the whiteboard. Before the execution token of an FSMs is handed back, the machine copies to the whiteboard any external variables it has modified locally. We refer to this as the $\text{WRITE}$ footprint of the state. This ensures there is never a race condition between the FSMs that are running concurrently under the predefined schedule (and thus, there is no need for further mechanisms to protect shared variables or synchronise FSMs).

For a FSM, the union of all the $\text{READ}$ footprints of its states is called the $\text{REQUIRES}$ set of the FSM. Similarly, the union of all the $\text{WRITE}$ footprints of its states is called the $\text{PROVIDES}$ set. Note that it has been shown that the $\text{REQUIRES}$ set and the $\text{PROVIDES}$ set of an FSM can be computed from the static analysis of the FSM description (Estivill-Castro and Haxel, 2011).

We can compute a dependency (impact) graph between the FSMs in a vector, given the $\text{REQUIRES}$ set and the $\text{PROVIDES}$ set of the FSMs in that vector. That is, we can find the dependency graph of the
modules that constitute the software. There, nodes of the graph are the modules (the FSMs), while there is a directed edge from FSM $M_1$ to FSM $M_2$ if the 	extit{REQUIRES} set of $M_2$ has a not empty intersection with the 	extit{PROVIDES} set of $M_1$.

It is clear that in this graph, if we find several disjoint, connected components, then these are completely independent, and any model-checking of the entire system is equivalent to performing model-checking of each connected component separately. Simply put, none of the external variables of the connected components are shared. That is, there is no communication whatsoever between FSMs in one connected component and another. They can actually be scheduled in parallel and not sequentially, and each would have no impact on the other. This is an extreme case that would rarely appear in practice as it indicates that a system is made of completely independent systems without communication between them. However, this is an important precursor to the principle we shall discuss next, as such partitioning illustrates that the model-checker no longer has to explore a Kripke structure for the entire system, but indeed we can get away with exploring essentially separate spaces, but indeed we can get away with exploring essentially separate spaces, only adding their number of states (rather than multiplying them).

This directed graph can now be analysed by traditional digraph algorithms. Consider the following procedure. Let $v_1$ be a node with a non-zero indegree. We can find an ancestor (as $v_1$ has an in-degree larger or equal to 1). If the ancestor has an in-degree larger than 0, we find an ancestor of the ancestor. In fact, we conduct a depth-first search considering the edges in reverse orientation from $v_1$. We call this graph $A_{v_1}$ (and although we refer to it as the ancestors of $v_1$, we consider $v_1 \in A_{v_1}$).

**Lemma 3.1.** For any vertex $u_1 \in A_{v_1}$, there is a directed path from $u_1$ to $v_1$ in $G$; and therefore the WRITE set of $u_1$ may influence the READ set of $v_1$.

**Proof.** This follows by induction and transitivity on the length of the path from $u_1$ to $v_1$. 

We refer to the construction of $A_{v_1}$ for a vertex $v_1$ as the ancestor exploration step with focus $v_1$.

As a consequence of Lemma 3.1 we have the following observation.

**Observation 3.2.** If there is a directed path from a node $v_1$ to a node $v_2$, then $v_1$ and $v_2$ must be analysed jointly.

Conversely, if there are two nodes $v$ and $u$, and there is no directed path from $v$ to $u$ and there is no directed path in the other direction either (from $u$ to $v$), then nodes $u$ and $v$ can be analysed separately.

Thus, what we are aiming for is a decomposition of the graph $G = (V, E)$ of dependencies into a cover $\hat{C} = \{C_1, \ldots, C_t\}$ so that

1. every node is included; that is $\bigcup_{C \in \hat{C}} C = V$,
2. each component $C \in \hat{C}$ of this cover has the property that if $u$ and $v$ are vertices in $C$, then there is a path in $C$ from $u$ to $v$ or a path in $C$ from $v$ to $u$,
3. each component is ancestor-maximal, that is, there is no vertex $v \notin C$ so that there is a path from $v$ to some vertex $u \in C$.

Moreover, we aim for a cover with minimum number of components. For illustration, consider the graph in Fig. 4a). This graph’s cover is shown by the 3 components in Fig. 4b). Note that there is no further ancestor to any vertex that belongs to a component outside the component. Also, vertex 1 and vertex 2 are in different components, as in the graph itself, there is no directed path in either direction.

To compute this cover we recall the classical description (Aho et al., 1974) of depth-first search (both for a directed graph and an undirected graph). We reduce the problem to connected components by applying depth-first search to the undirected version of the graph. Thus, in what follows, we assume that the undirected version of the graph is connected. Then, we can take any vertex $v_1$ with a non-zero in-degree and find its ancestors by using directed depth first search (but following the directed edges in reverse direction). Moreover, the depth directed depth first search produces (Aho et al., 1974, page 188) tree edges which lead to new vertices during the search and form the topological-sort tree, forward edges which go from ancestors to proper descendants but are no tree edges back edges which go from descendants to ancestors, cross edges which go between vertices that are neither ancestors not descendants of one another.

Thus, the depth-first search in reverse direction from $v_1$ has leave nodes of the topological-sort tree. Let $u$ be a leave node. If such a leave $u$ does not have a back edge, then $u$ is a maximal ancestor. The starting set of

![Figure 4: A dependency graph, and b) its cover into 3 components.](image-url)
ancestors consist of \( u \) alone. If \( u \) has a back edge, then \( u \) is in a cycle and we take all the vertices in all the cycles involving \( u \) as the starting set of ancestors.

The next step consists of performing a directed depth first search from each vertex in the set of ancestors. We obtain the same classification as before of all the edges of the graph. However, we find components every time

1. there is a node \( v \) that has two or more children in the topological-sort tree,
2. there is no back edge from any descendant of \( v \) in the topological-sort to an ancestor of \( v \)
3. there is no forward edge from an ancestor of \( v \) to a descendant of \( v \).

When such a node \( v \) is found, then we have a candidate component that consists of all the ancestors of \( v \) with the child branch \( B \) that has no back edges emanating and no forward edges arriving. The candidate components share \( v \) and the ancestor of \( v \). That is, they are of the form \( B \cup A \), and are as many as child branches \( B \) of \( v \) that have no back edges and no forward edges. However, candidate components may need to be extended to be ancestor closed. This is because, although we built the starting set of ancestors from \( v \), and because \( v \) is a descendant of \( v \), there may be nodes in \( B \) that have other ancestors. But completing each candidate component \( B \cup A \), to a component consist of a depth-first search (with edges considered in the reverse direction). This may actually result in fusing some candidate components.

If finding components from the starting set of ancestors of \( v \) covers the entire graph, then the process terminates. If not, then the process is repeated with a new vertex of in-degree larger than zero in the part not covered playing the role of \( v \) in the above algorithm.

Since depth-first search is linear on the number of edges and the number of vertices of a graph, and clearly, the process of identifying the decomposition only processes a vertex at most 3 times, the entire algorithm finds the decomposition into independent components for model-checking in linear time.

4 EVALUATION

To demonstrate our point we now review the situation with the Microwave Oven case study introduced earlier. We suggest that this case study is particularly illustrative of the situation where many actuators are controlled by combinations of a few sensors. This is perhaps where our approach has the highest impact in practice. Fig. 5 shows the dependencies of the microwave modules. Actuators are shown in dark boxes, while sensors appear in clear boxes. Software modules appear in shaded boxes. These dependencies can also be found by converting the logic-based FSMs to decision trees (Billington et al., 2010) and using tools such as BECCIE (Wen and Dromey, 2004).

Although all modules depend on the two sensors (the door and the button), there is a clear three-way split at the software module (the FSM in Fig. 1a) that acts as the timer. Thus, we can decompose the dependency graph into the modules shown in Fig. 6.

We now compare the resources required to perform traditional model checking (involving all the modules) with our approach here. The results in Table 2 show a clear improvement in both time and space when generating NuSMV data with gufsm compared to the explosion of considering all FSMs in combination. The Kripke structure for the complete model of the Microwave Oven is 2 orders of magnitude larger! As a result, the CPU time to process is 4 orders of magnitude larger. In this example, it is

<table>
<thead>
<tr>
<th>Component</th>
<th>CPU Time</th>
<th>Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>Combined graph</td>
<td>2,557.32 s</td>
<td>287,877,511 bytes</td>
</tr>
<tr>
<td>Bell subgraph</td>
<td>0.27 s</td>
<td>2,817,073 bytes</td>
</tr>
<tr>
<td>Engine subgraph</td>
<td>0.22 s</td>
<td>2,457,880 bytes</td>
</tr>
<tr>
<td>Light subgraph</td>
<td>0.22 s</td>
<td>2,458,762 bytes</td>
</tr>
</tbody>
</table>
The pump will not turn on if the methane sensor detects a high reading.

Another example is the mining pump. This case is also discussed prominently in the literature (Shrivastava et al., 1993; Sloman and Kramer, 1987; Grunske et al., 2011; Winter and Yatapanage, 2011). It is also linked to the literature of software controlling safety-critical systems (Kramer et al., 1983). It has been used to present model-driven engineering, for performing model checking, for performing failure modes and effect analysis. The requirements (Burns and Lister, 1991) are reproduced in Table 3.

Fig. 7 shows the logic-labeled finite-state machines that constitute the controlling software (Estivill-Castro et al., 2012a). The most interesting part in this example is that the dependency graph consists, in fact, of two disjoint, connected components (Fig. 8). Therefore, when we split independent subgraphs, we find the two connected components. The resulting differences in Table 4 are even more impressive (5 orders of magnitude in size 7 orders of magnitude in time for the alarm).

5 CONCLUSIONS

Formal verification by model checking and the con-
struction of FMEA tables had been reported to take CPU times of the order of days or weeks for some well-discussed case studies (Grunsk et al., 2011). We have shown here that for logic-labeled FSMs we can efficiently split the corresponding dependency graph and obtain components of the graph that can be analysed independently. Such components are found by simple depth-first search exploration, in linear time, which is negligible with respect to the time required to perform the model-checking. With decomposition, even only identifying two or three such components results in improvements in performance of several orders of magnitude for a single model-checking exercise (as demonstrated in two important case studies, that have received much attention in the literature). Consequently, Kripke structures in description languages of common tools such as NuSMV can be generated and verified much more efficiently.

REFERENCES


