Keywords: Semantic Document Classification, Clustering, Tagging, Seed Selection, k-means, k-C, Cosine Similarity.

Abstract: In this paper we analyze and discuss two methods that are based on the traditional k-means for document clustering and that feature integration of social tags in the process. The first one allows the integration of tags directly into a Vector Space Model, and the second one proposes the integration of tags in order to select the initial seeds. We created a predictive model for the impact of the tags' integration in both models, and compared the two methods using the traditional k-means++ and the novel k-C algorithm. To compare the results, we propose a new internal measure, allowing the computation of the cluster compactness. The experimental results indicate that the careful selection of seeds on the k-C algorithm present better results to those obtained with the k-means++, with and without integration of tags.

1 INTRODUCTION

As a result of an unsupervised text clustering process, the documents are distributed among a set of groups (the “clusters”). It is expected that similar documents are placed on the same cluster and dissimilar documents in different ones.

A clustering algorithm is expected to be both efficient (fast at execution time, even with a large input) and effective (creating coherent clusters). However, although there are several clustering algorithms (Theodoridis and Koutroumbas, 2009), their advantages and disadvantages won’t allow the finding of one which fulfills these two properties for any input type and size.

Our investigation intends to assess how social classification, namely by the use of social tags, may contribute to improve the effectiveness of automatic document grouping.

In this article we will revisit two tag integration methods previously proposed. Our starting base is the k-means algorithm, considered one of the “top 10 algorithms” in data mining (Wu et al., 2007), mainly because of its efficiency (Feldman and Sanger, 2007, Theodoridis and Koutroumbas, 2009).

The first tag integration model (Cunha and Figueira, 2012) allows their integration on the document vectors (document representation in a Vector Space Model) through a parameter called Social Slider (SS) which allows attributing different weights to tags accordingly to their occurrence in the document. In order to predict the integration impact, a theoretical model was created. We describe this model and the obtained results, which suggest that using cosine similarity approaches the documents that share the same tags and sets apart those which do not have tags in common.

The second integration model is based on Communities Detection in the network of tags, enabling a careful seed selection. This new algorithm was named k-Communities (Cunha et al., 2013) and is different from the k-means algorithm not only because of the initial seed selection but also because it introduces a new way to calculate the centroids in each iteration of the clustering process.

In this article we compare both tag integration methods. To perform this comparison we use external evaluation measures which allow comparing automatic clusters with manual clusters. Further on, we introduce an internal evaluation index that allows measuring compactness and separation among clusters. Separation is measured through the distance between centroids and compactness through the network of documents, where each document is linked to its closest one.

The k-means++ and k-Communities algorithms
are executed with and without integration of tags.

2 SOCIAL CLASSIFICATION

The evolution of the World Wide Web led to the rise and growth of new concepts like Web 2.0 and the Social Web, in which users have access to a set of applications that allow them to interact with each other by easily publishing, editing and sharing content (for example, blogs, wikis, video sharing systems, photo sharing systems, etc.).

However, the massive user participation creates a growing flow of information which again requires new ways to recover information (Lee et al., 2009). The dynamics which occur among Web 2.0 users are naturally providing interesting ways to help organize information by creating folksonomies. The term folksonomy (Wal, 2007) was created by Thomas Vander Wal and derives from the agglutination of the terms folk and taxonomy. Folksonomies naturally arise when a set of users, interested in some information, decide to describe it through comments, or by attributing tags (Snuderl, 2008), providing important elements to categorize that information. The power that resides in creating a folksonomy is visible in initiatives like the one carried out by the Library of Congress or at steve.museum research project (Trant, 2008).

The Library of Congress launched a pilot project on Flickr, a popular photo sharing website, which consisted of an open invitation to the general public to tag and describe two sets of approximately 3000 historical photographs (Springer et al., 2008). The initiative was a success, generating a massive growing movement, typical to the Web 2.0 communities.

steve.museum research project is another example which relies on cooperation between museum professionals and other entities who believe social tagging may provide new ways to describe and access cultural object collections, besides promoting visitor interaction.

According to Trant (Trant, 2008), when implementing the steve.museum project prototype, the analyses of the tags attributed by common museum users showed they did not match the terms used by museum professionals. To minimize the gap between professional language and common language, social tagging was used as a promising addition to museum records as its terminology is usable in some kind of searches (although this possibility stills has to be verified by a large scale study) (Trant, 2008).

In fact, “[i]t is still uncertain that [a] new folksonomy will replace traditional hierarchy but now that all users have the power to classify according to their own language, research will never be the same” (Dye, 2006).

Still, in Trant (Trant, 2008) it is said that the museum professionals general opinion is that the tags attributed by users may be interesting even though its pertinence may require validation.

However, self-normalization theories state that folksonomic tags will self regulate, the collective vocabulary will become more consistent in time and all without need for an external imposed control (Trant, 2009).

The initiatives conducted in these two projects demonstrate an awareness of the potentialities emerging from using the collective intelligence generated from a folksonomy.

3 k-means ALGORITHM

The k-means algorithm was the starting point for this investigation specially because of its simplicity and efficiency (Feldman and Sanger, 2007, Theodoridis and Koutroumbas, 2009). Its time complexity by iteration is, in the worst case, $O(kn)$ but the number of iterations is generally quite small.

The k-means algorithm (MacQueen, 1967) allows the partition of an initial set of documents (each document is represented as a vector) in $k$ clusters. The algorithm starts by selecting $k$ random seeds and then calculates the distance from each document to every seed, grouping each document to its nearest seed. When all clusters are formed, the new centroids become the mean of the document vectors on each cluster. Each document is then associated to the nearest centroid. The process ends when convergence is achieved, or in other words, when there are no more changes.

Despite the efficiency, the random choice of seeds may lead to bad clustering examples. In this sense, Arthur e Sergei Vasilvitskii (Arthur and Vassilvitskii, 2007) proposed the k-means++ algorithm to overcome that fault, which chooses the seeds according to specific probabilities. Its complexity is $O(\log k)$ and the experimental results show a shrinkage on the number of iterations until convergence is achieved. However, the number of clusters is still unknown, a parameter which greatly influences the quality of the formed clusters.
4 INTEGRATION MODEL

In this section we revisit two proposed tag integration methods. The first method allows, through a parameter called Social Slider, the attribution of weights to tags accordingly to their occurrence in the document (Cunha and Figueira, 2012). The second approach consists in using a network of tags to determine the seeds that allow initializing the k-C algorithm (Cunha et al., 2013) (which, such as the k-means algorithm, initiates with k seeds).

4.1 Tags in Vector Space Model

The tag integration model (Cunha and Figueira, 2012) is based on the occurrence of tags on the content of the document, weighted according to a parameter called SS (Social Slider). Let \( P = \{p_1, p_2, ..., p_m\} \) be a set of \( n \) documents; \( W = \{w_1, w_2, ..., w_r\} \) and \( T = \{t_1, t_2, ..., t_q\} \) be respectively the bag of words and tags which may appear in the documents. There are several possibilities for the occurrence of a tag in a document: the tag does not appear in the document; the tag appears only once; the tag appears more than once. Each case is attributed a different weight as shown on Fig. 1. Every tag vector \( V_t \) is changed: to each vector coordinate is added the number of times the tag occurs in the document and, finally each coordinate is multiplied by the SS parameter accordingly to the tags occurrence in the document. The calculation ends with the replacement of the coordinates on the document vectors \( V_d \) by their respective coordinates on the tag vector.

4.2 Similarity Measures

The tag integration model was based on the construction of a prediction model that relies on the similarity measures, most commonly used to implement the k-means algorithm, which are the Euclidean distance and the Cosine Similarity.

When intending to weight tags accordingly to their occurrence in the document, it emerges the need to predict its impact: if documents get closer when using common tags or if they get more distant when they are not sharing any tags.

4.2.1 Euclidean Distance and Cosine Similarity

Using Euclidian distance it is easy to conclude that the Social Slider parameter must vary between 0 and 1 in order to allow shortening the distance between documents sharing tags.

On the other hand, the idea to predict the impact of cosine similarity is to analyze the influence of tag integration through the cosine of the angle formed between documents after tag integration (cos(\(\alpha\))).

So, considering the cosine of angle \(\alpha\) between two documents before tag integration we have:

\[
\cos(\alpha) = \frac{\sum_{i=1}^{n} x_i y_i}{\|X\| \times \|Y\|}
\]

Where \(X = (x_1, x_2, ..., x_n)\) and \(Y = (y_1, y_2, ..., y_n)\)

Therefore, by writing the new angle cosine using the initial coordinates it is possible to change the value of the SS parameter and verify how the cosine of the angle varies after tag integration (cos(\(a\))).

Using the integration model, and without losing generality, we will assume that coordinates \(x_j\) and \(y_j\) correspond to the frequency of the same tag, coincident with the tag associated with both documents. Therefore, the coordinates which have tags associated are updated providing, through algebraic manipulation, the angle cosine formed by the new vectors \(\cos(a)\) can be expressed using the parameters present in equation (1):

\[
\cos(a) = \frac{(SS^2 - 1)x_j y_j + SS^2 x_j + SS^2}{\|X\| \times \|Y\| \times L \times M} + \cos(\alpha)
\]

(2)

Where:

\[
L = \sqrt{1 + \frac{(SS^2 - 1)x_j^2 + 2SS^2 x_j + SS^2}{\sum_{i=1}^{n} x_i^2}}
\]

\[
M = \sqrt{1 + \frac{(SS^2 - 1)y_j^2 + 2SS^2 y_j + SS^2}{\sum_{i=1}^{n} y_i^2}}
\]

In order to show the impact of tags integration we elaborated several graphs, considering documents with norms close to 10, 30 and 100, as seen in fig. 2. When the SS increases (or, in other
words, when tags are given a greater importance),
the cosine similarity tends to approach 1,
independently of documents being close or far
before integration. This means the angle formed
between documents tends to become zero.

Similarly, we analyzed the tag integration impact
on all other situations which result in tag
differentiation (whether they exist or not in the
document) and it showed a positive impact even
though it depended on the weight given to each
situation described in the model.

On the other hand, it is important to understand
what happens between documents which do not
share tags. The new angle cosine is given by (3):
\[
\cos(a) = \frac{(SS - 1)x_1y_1 + SSx_2y_2 + \cos(x) \times 1}{R}
\]
\[
R = \sqrt{1 + (SS^2 - 1)y_1^2 + 2SS^2y_2 + SS^2 - \sum_{i=1}^{\infty}y_i^2}
\]

For example, analyzing the specific case where
two documents don’t share the same tag but it
appears once in the document to which it is not
associated, we can observe, looking at fig. 3, that
when SS increases, the angle cosine decreases, i.e.,
the angle between documents becomes bigger.
However, as the vectors norm increases, the angle
cosine only starts to change on increasingly larger
SS values.

When analyzing all the other situations between
documents which did not share tags, it showed the
angle between documents increased when
documents don’t share tags.

Accordingly to this prediction model, it was
expected for documents sharing the same tags to be
closer and documents not sharing tags to be further
apart.

4.3 k-Communities Algorithm

The second approach is still based on k-means
algorithm but uses community detection, for a
network of tags, for the initial seed selection (recall
this is one of the main problems of the k-means).

We use cosine similarity as the similarity
measure because of its independence from document
length, allowing the pattern identification between
documents that share the same words but not exactly
with the same frequencies, and also because the
prediction model expects a positive impact among
documents sharing the same tags, whenever the
integration occurs, directly on the document’s
vectors (as described on Section 4.1). Note that in
traditional k-means when cosine similarity is chosen
to implement the k-means algorithm the new
centroid selection is still made through Euclidean
distance since the new centroid is calculated
throughout the mean of the vectors in each cluster.

Using two measures simultaneously may provide
inconsistent results. Therefore, we propose the k-
Communities (k-C) algorithm (Cunha et al., 2013)
which is described below:

Listing 1: K-C algorithm.
1. Select k seeds using community detection in a
   network of tags (where documents are nodes and
each edge is the connection between documents that
share a tag): each seed is the document that has the
greater degree inside its community.
2. Compute the cosine similarity between each
document and all seeds.
   (a) If the cosine similarity between a document
and all centroids is zero then stop calculating.
   Go to step 1 and add this document to the
   seeds set.
   (b) Else if generates clustering by assigning each
document to its closest seed.
3. Compute the new centroid for each cluster, the
   chosen document is the one who gets maximum sum
   as shown in Equation (4)
\[
max \sum_{j=1}^{n} \cos(d_i, d_j)
\]
4. Go to step 2. The process ends when convergence is
   achieved, i.e., no more changes occur.
5 EVALUATION MEASURES

It is a standard procedure to use internal and external evaluation measures in order to assess an algorithm’s quality. The internal ones intend to measure compactness and separation. I.e., whether the groups are well separated and simultaneously the documents inside the clusters are close together. However, it all depends on the documents on a determined dataset because we may find documents which are apparently far apart inside its cluster, however, this may only mean that they belong to the same area but are semantically unrelated with the other documents in the cluster. Therefore, we may have an internal evaluation measure which indicates the documents are too far apart within the cluster but that might be the only organization that makes sense.

Despite human judging being subjective, it is also important to consider external evaluation measures when intending to measure the coincidence degree between the automatically formed clusters and the manually formed ones.

In this article we propose a new internal evaluation measure and revisit some of the external evaluation measures most commonly used in literature.

5.1 Maximum Cosine Index

There are several internal evaluation measures found in literature. The way compactness and separation are measured often varies. For example, on the Dunn Index (Dunn, 1974), compactness is calculated using the square root of the maximum distance between any two points in the same cluster, therefore using the documents diameter. On the other hand, the DB Index (Davies and Bouldin, 1979) calculates compactness based on the similarities between each cluster and all other clusters, measuring the sum of two clusters dispersion.

We consider that, more than the distance between documents in each cluster, it is important to find out if each document and its nearest document belong in the same cluster. Therefore, our proposal intends to measure the compactness according to this principle, and separation through the distance between each cluster’s centroid. For each cluster is chosen the distance to the closest cluster, building the measure on the worst case as on the DB index (Davies and Bouldin, 1979).

To perform the Maximum Cosine Index (MCI), we need to build a network of documents where each document is connected to its nearest document (according to cosine similarity). It is intended to measure the distance from each cluster to its nearest cluster and assess how many times it is superior to the mean of the distances between each document and its nearest document within each cluster.

In fig. 4 we can see the documents belonging to each cluster. The dashed arrows indicate the distance from each cluster to its closest cluster and the other arrows indicate the distance between each document to its closest document.

In every cluster the connected documents are identified with a different color. The process gives different weights to the distances inside each cluster according to their connected component (each connected component will have the same weight as the number of its documents).

Figure 4: Representation of the closest document to each document and the distance between each cluster and its closest cluster.

The proportion between the clusters compactness and separation is given by the equation (5):

$$X_i = \frac{R_i}{d_i}$$  \hspace{1cm} (5)

Where:

- $R_i$ - weighted average of the observed distances to the nearest document inside each cluster
- $d_i$ – distance to the closest cluster.

Then the weighted average of the several clusters is determined. The weight of each cluster depends on the proportion of documents which have their closest document inside the cluster as shown by equation (6):

$$\frac{\sum_{i=1}^{n} X_i P_i}{\sum_{i=1}^{n} P_i}$$  \hspace{1cm} (6)
Where:

\[ p_i = \frac{s_i}{t_i} \]

\( s_i \) – total number of documents on cluster \( i \) that have the nearest document inside the cluster

\( t_i \) – number of documents on cluster \( i \)

In the example shown on fig. 4, we see that, on average, the distance between clusters is 13.8 times superior to the average of distances seen in the inside of each cluster.

5.1 Revisiting External Evaluation Measures

Some external evaluation measures are based on a direct comparison between manual and automatic groups, such as the purity measure (Feldman and Sanger, 2007), while other measures are based on the different relations which may exist in a collection of \( n \) documents between the \( n(n-1)/2 \) pairs of documents, such as the F1 measure, precision, recall e Rand Index (Manning et al., 2009).

Therefore, to calculate these measures it is necessary to know the various relations possible between the pairs of documents: True Positives (TP); True Negatives (TN); False Positives (FP); False Negatives (FN).

The Purity measure compares the clusters manually organized with the automatic clusters, selecting for each manual cluster the most similar automatic cluster. The percentage of common documents is given by (7), where \( L = \{L_1, L_2, \ldots, L_m\} \) is the set of classes and \( C = \{C_1, C_2, \ldots, C_m\} \) is the set of clusters.

\[ \text{Purity}(C, L) = \frac{1}{n} \sum_{x} \max_{y} |C_x L_y| \]  

(7)

F1 measure corresponds to the harmonic mean between Recall and Precision.

Precision is the percentage of pairs of documents which are correctly placed in the same cluster.

\[ \text{Precision} = \frac{TP}{TP + FP} \]  

(8)

Recall is the percentage of pairs of documents which are correctly placed in the same cluster among the pairs of documents that are or should be in the same cluster.

\[ \text{Recall} = \frac{TP}{TP + FN} \]  

(9)

Thus, F1 is computed as shown in equation (10).

\[ F_1 = \frac{2 \times \text{Recall} \times \text{Precision}}{\text{Precision} + \text{Recall}} \]  

(10)

Rand Index computes the percentage of correct decisions, pairs of documents that are correctly placed in the same cluster and the pairs of documents that are correctly placed in different clusters.

\[ R_I = \frac{TP + TN}{TP + TN + FN + FP} = 1 - \frac{2 \times (TP + TN)}{n^2 - n} \]  

(11)

6 Experimental Results

In this article we describe 3 case studies where we used the k-means++ algorithm and the k-C algorithm, with and without integration of tags. The tag integration was made using the parameter Social Slider (SS) for SS=0, SS=5 and SS=30. According to the documents norm, this parameter provides a general view of the process from 0 (no tag integration) to 30 (huge impact on documents distances).

The datasets (each one with approximately 50 documents) were created using documents from our personal library and from our University’s Digital Library. Since this is hierarchically organized collection, we chose some Faculties and then picked papers from specific scientific areas. Each dataset has documents from six different areas as shown in Table 1 and we considered as tags the key-words given by the authors of each scientific paper.

The evaluation was made using internal measure proposed in this paper and the external measures described in the same section.

Table 1: Manual classes of each data set.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Classes</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td>Clustering, statistics, Mathematics, History, Sport and Biology</td>
</tr>
<tr>
<td>D2</td>
<td>Clustering, statistics, Health, Sport, Biology and Mathematics</td>
</tr>
<tr>
<td>D3</td>
<td>Clustering, usability, Health, Sport, Biology and Mathematics</td>
</tr>
</tbody>
</table>

6.1 Internal Evaluation

As seen in Table 2, the k-C algorithm obtains better results than the k-means++ algorithm in almost every performed test. The only case where the k-means++ algorithm had better results was on dataset D2 with SS=5, even though the difference isn’t particularly significant.

We may also see that as the SS parameter increases it also increases the average distance to the nearest cluster, in comparison to the distances.
Table 2: MCI results.

<table>
<thead>
<tr>
<th>SS</th>
<th>k-C</th>
<th>k-means++</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>13.746</td>
<td>3.731</td>
</tr>
<tr>
<td>5</td>
<td>74.923</td>
<td>8.589</td>
</tr>
<tr>
<td>30</td>
<td>400.047</td>
<td>80.630</td>
</tr>
<tr>
<td>D2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>4.359</td>
<td>1.701</td>
</tr>
<tr>
<td>5</td>
<td>13.621</td>
<td>14.521</td>
</tr>
<tr>
<td>30</td>
<td>181.874</td>
<td>101.966</td>
</tr>
<tr>
<td>D3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>19.673</td>
<td>5.189</td>
</tr>
<tr>
<td>5</td>
<td>157.450</td>
<td>3.993</td>
</tr>
<tr>
<td>30</td>
<td>1354.626</td>
<td>148.494</td>
</tr>
</tbody>
</table>

observed to the nearest document inside each cluster. This confirms that using cosine similarity and tag integration approaches the documents sharing the same tags are set apart from those who do not have those tags.

6.2 External Evaluation

Comparing the external evaluation measures to the k-C and the k-means++ algorithms (fig. 5 and fig. 6), we found out that if in the k-C algorithm the results vary between 0.5 and 1, on the k-means++ algorithm they vary between 0.3 and 0.9. This means there is a greater dispersion on the k-means++ algorithm.

It shows that tag integration has a greater impact on the k-means++ algorithm, more specifically on datasets D2 and D3 where parameter SS=5 and parameter SS=30 provide better results than when tags are not used.

In the k-C algorithm we only find better results on dataset D1 when using parameter SS=5.

The average Recall value shows that both algorithms have a close percentage of pairs of documents that belong to different clusters and that should be part of the same cluster. However, the average Precision value, indicates that the k-C algorithm presents an improvement of 36% in comparison with the k-means algorithm. Therefore, the k-C algorithm presents a greater number of pairs of documents that are correctly classified in the same cluster. Hence, the F1 measure, which is the harmonic mean between Recall and Precision, indicates that the k-C algorithm is the one that presents better results, 75% versus 54%.

The Rand Index shows that the k-C algorithm has in average more 11% of correct decision (True Positives and True Negatives) when compared to the
k-means++ algorithm.

Finally, the average purity also shows better results for the k-C algorithm, indicating that these clusters are more similar to those that are manually organized.

Comparing the results of these external evaluation measures with the results of the internal evaluation measures we can conclude that even when the Maximum Cosine Index indicates an improvement with the increase of the SS parameter, it does not necessarily means there is a corresponding improvement in grouping effectiveness.

7 CONCLUSIONS

In this paper we compared two methods of tag integration to perform the effectiveness of the automatic clustering.

Having the k-means as the base algorithm for both approaches, the first method builds on giving weights to tags according to their relevance in the documents' content through a parameter called Social Slider. To implement this method we constructed a model to predict the clustering results according to the selected similarity measure, showing that the use of the cosine similarity leveraged the approximation of documents with common tags, as well as the separation of documents with no common tags.

The second method uses the information provided by tags to select the seeds, originating a clustering algorithm called k-C algorithm, similar to the k-means algorithm but with a different method to find the centroids in each iteration.

To assess the results we used internal and external measures for the k-means and k-C clustering algorithms.

The integration of tags through the Social Slider Parameter shows that the distance between documents with common tags is reduced and the distance between those that do not share tags is increased. Note that, as the SS increased, the distance between clusters became bigger when compared to the distances between documents inside the clusters (regarding the distance between the documents and their closest documents).

The results of the internal measure also show that the k-C algorithm provides better results than the k-means++ algorithm. However, the effectiveness of the formed clusters is not proportional to the increase of the SS parameter.

The external measures show some improvements for the k-means++ algorithm but sometimes for SS=5 and others to the parameter SS=30. The same happens with the k-C algorithm but with a smaller impact. Even though, generically the k-C algorithm provided better results. Therefore, using the information provided by tags to select the initial seeds (second method) seems to produce better results.

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