EDEX: Entity Preserving Data Exchange

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Abstract: Data Exchange creates an instance of a target schema from an instance of a source such that source data is reflected in the target instance. The prevailing approach for data exchange is based on generating and using schema mapping expressions representing high level relations between source and target. We show such class level schema mappings cannot resolve some ambiguous cases. We propose an Entity Preserving Data Exchange (EDEX) method that reflects source entities in the target independent of classification of entities. We show EDEX can reconcile such ambiguities while generates a core solution as an efficient solution.

1 INTRODUCTION

Data exchange is the process of taking data structured under a source schema, and generating an instance that adheres to the structure of a target schema. The prevailing approach for this process is based on schema mappings – high level specifications describing relationships between database schemas (Bonifati et al., 2005); (Popa et al., 2002). These specifications are usually represented in a logical formalism capturing relationships between database schemas independent of implementations details. Many leading projects, such as Clio (e.g., Fagin et al., 2009) have adopted the schema mapping approach. Nevertheless, because of semantic heterogeneities among data sources, some ambiguous cases cannot be handled using schema mappings.

We contend the problems of schema mapping based approaches emerge from the assumption of inherent classification (Parsons and Wand, 2000) in information system design, by which every thing modelled in a domain of interest is treated as an instance of a class or entity (e.g., in an object-oriented model or Entity Relationship model). Although classification organizes knowledge about things, real world objects do not inherently belong to classes. According to ontological foundations about the nature of things in the real world (Bunge, 1977), things (specified in terms of a set of properties) exist prior to and independent of their classification.

At the data level, there has been research on data-centric heterogeneity reconciliation in data exchange called entity resolution (Talburt, 2011). Generally, entity resolution is used to clean data and create a consistent view of data from heterogeneous and conflicting representations by identifying entities referring to the same real world object.

In spite of progress in schema level and data level approaches for data exchange, semantic heterogeneities are not completely resolved, resulting in ambiguous cases in schema mappings that lead to improper data exchange. Human intervention is usually required to resolve these ambiguities. We claim that, as schema mapping expressions are bounded in class definitions, they do not convey the whole semantics of data exchange. Although data exchange based on schema mapping has advantages in data exchange, neglecting entity and data level heterogeneities can be problematic. To address this gap, we suggest an entity preserving approach that focuses on preserving source entities in the target independent of classification. More specifically, given a set of entities in the source, we search for the best host relations that can reside source entities as accurately as possible.

In conventional data exchange through schema mapping, value correspondences as well as integrity constraints are used to generate schema mapping expressions. Then, such mappings are used to generate target instances. However, in the entity preserving approach, value correspondences are directly used to find best relations that can reside source entities without generating schema mappings.
The entity preserving approach proposed here addresses this problem by considering property correspondences and data level relations.

Parsons and Wand (2013) proposed a preliminary schema mapping algorithm in which conceptual models are used to semantically enhance schema mappings for the sake of resolving ambiguity. Although the results of experiments were promising, the quality of final result depends strongly on the quality of conceptual models. However, EDEX does not rely on extra knowledge to exchange data. In particular, the contributions of this paper are as follows: (1) we show how data exchange techniques based on schema mapping are not capable of handling ambiguous cases; (2) we propose the entity preserving approach for data exchange which is a hybrid of data level and schema level approach; (3) we propose a set of algorithms to demonstrate the feasibility of implementing this approach; and (4) we show the proposed approach generates a core solution (Fagin et al., 2005) in data exchange as the most efficient solution.

2 CLASS-BASED APPROACH

In practice, usually human intervention is required to analyze and validate ambiguous schema mappings. A mapping expression denotes an ambiguous case when it can be interpreted more than one way, and as a result, there is no unique way to generate the target instance based on it (Alexe et al., 2008). One important ambiguous case in data exchange occurs when a generalization structure is implemented using different techniques in source and target schemas. A generalization can be realized by: 1) allocating separate tables for super class and subclasses, 2) allocating a separate table for each subclass, and repeating the properties of the super class in each subclass, 3) a single table including all attributes of subclasses by an additional property indicating the subclass. A generalization relation can result in ambiguity in data exchange through schema mapping because other relations including functional dependencies and self-reference can also realized through the same technique (i.e., key/foreign key).

One important type of ambiguous schema mapping occurs when a class in the source simultaneously refers to more than one class in the target where only one of them can be acceptable based on the properties of instances of that class in the source. For example, as shown in Figure 1, each course is taught by an instructor. On the other hand, in the target, a professor or a graduate student can be an instructor of a course (arrows represent value correspondence between properties and dashed lines show referential integrity constraints). Given the source and target schemas shown in Figure 1, the following schema mapping expressions $m_1$, $m_2$, and $m_3$ are generated by ++Spicy (Marnette et al., 2011).

![Figure 1: An example of a data exchange setting including source and target schemas in ++Spicy.](image)

$\textbf{m}_1$: for each $x_1, x_2, x_3$: Instructor (Name: $x_1$, STNo: $x_2$, EMPNo: $x_3$) → Grad (name: $x_1$, STNO: $x_2$).

$\textbf{m}_2$: for each $x_1, x_2, x_3$: Instructor (Name: $x_1$, STNo: $x_2$, EMPNo: $x_3$) → Prof (name: $x_1$, EMPNO: $x_3$).

$\textbf{m}_3$: for each $x_1, x_2, x_3, x_4$: Instructor (Name: $x_4$, STNo: $x_2$, EMPNo: $x_3$), Course (CName: $x_1$, Inst: $x_4$) → Course (CourseName: $x_1$, Instructor: $x_4$).

Using these mappings, given a source instance 
\{Instructor(I_1,st_1,null), Instructor(I_2,null,emp_1), Course(C_1, l_1), Course(C_2,l_2)\}, ++Spicy generates the target instance 
\{Grad(I_1, st_1), Grad(I_2, null), Prof(I_1, emp_1), Prof(I_2, emp_2), Course(C_1, l_1), Course(C_2, l_1)\}. One problem is that for each given tuple in Instructor, two different mappings are generated, but only one is acceptable according to STNo and EMPNo. Intuitively, when STNO exists for an instructor in the source, the corresponding record must be generated in the Grad table in the target, but when EMPNO exists for an instructor in the source, the corresponding record must be generated in the Prof table in the target. This ambiguity between $m_1$ and $m_2$ generates redundant information in the target while Grad($I_1, null$) and Prof($I_2, null$) are incorrect. We next show how EDEX handles such ambiguities.

3 ENTITY PRESERVATION

According to Bunge’s ontology (Bunge, 1977), a domain of interest includes a set of things each possessing at least one property. In (Chen, 1976) “entity” is defined as a “thing” which can be distinctly identified. A specific person, company, or event is an example of an entity. In relational

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database theory, a tuple (row) of a table can represent a particular entity where a primary key uniquely identifies tuples within a relation. In practice, a thing (physical object or a concept) can be represented using one or more tuples in the relational model. For example, characteristics of a student, his/her department and university can be stored all in a single student relation, where a tuple represents student, department and university entities. On the other hand, in a different database schema, there may exist three different relations where each tuple represents a particular entity. Different configurations of relationships between tuples and entities are a consequence of different classification structures used in various schemas. Such differences add complexity in data integration. (Parsons and Wand, 2000) attribute such problems to the assumption of inherent classification, wherein every thing in the domain is an instance of a class. To overcome the problem of different classifications in the source and target, we propose a solution that preserves entities in the source regardless of classification. Our technique identifies existing entities in the source and finds the best host(s) for these entities, with the goal of maximum information preservation and minimum redundancy.

Generally, a relational schema can be represented using a directed graph \( G=(V, E) \) where \( V=\{R_1, \ldots, R_n\} \) is a set of vertices representing relations (tables) and \( E \) is a set of edges where each edge shows a directed relation between the referencing table to the referenced table.

**Definition 1 (Schema Graph).** Given a schema \( S \), a schema graph \( G=(V, E) \) is a directed graph that defines relation joinability according to foreign key-primary key relationships in \( S \). It has a vertex \( R_i \) for each table \( R_i \in S \) and an edge from \( R_i \) to \( R_j \) for each foreign key-primary key relationship from \( R_i \) to \( R_j \).

**Definition 3 (Relation Ancestor Tree).** A Relation Ancestors Tree (RAT) of relation \( r \) denoted \( RAT(r) \) is a sub graph of schema graph \( G \) with the root of \( r \) and all paths from \( r \) to \( N(r) \), all paths from each relation \( r_i \) in \( N(r) \) to \( N(r_i) \), and so on until adding a path does not result in a cycle. \( RAT(r) \) represents all ancestors of \( r \) that can be extracted using the breath-first-search technique and traversing from relation \( r \) to all ancestors of \( r \) where that node is not already visited. Relation Ancestor Tree for each relation of the schema and its schema graph in Figure 2 is shown in Figure 4.

We distinguish between class level (generic) and instance level (specific) properties. A relation in a data model is represented in terms of a set of generic properties while its tuples possess specific properties represented as a set of property and value pairs \( \langle p, v \rangle \). Possessing a specific property manifests possessing a generic property. For example, \((\text{gender}, \text{male})\) and \((\text{gender}, \text{female})\) are two manifestations of generic property \text{gender}. We use \( P(r) \) to show properties of relation \( r \) (i.e., a set of
generic properties) and \( P(t) \) to represent properties of tuple \( t \) (i.e., a set of specific properties \( \langle p_1, v_1 \rangle \)).

Drilling down a tuple from its foreign key(s) to corresponding tuples in referenced relations, it is possible to extract indirect properties in neighbour relations. For example, given the Student relation in Figure 3, \( \{ \langle \text{name}, s1 \rangle, \langle \text{program}, p1 \rangle, \langle \text{dep}, D1 \rangle, \langle \text{supervisor}, Prof1 \rangle \} \) is the set of properties of the first tuple of Student. On the other hand Student references Department through \( \langle \text{dep}, D1 \rangle \), where \( \{ \langle \text{idName}, D1 \rangle, \langle \text{building}, B1 \rangle \} \) can be considered indirect properties of this student. Accordingly, properties of supervisor \( \{ \langle \text{pName}, prof1 \rangle, \langle \text{degree}, deg1 \rangle, \langle \text{profDep}, D1 \rangle \} \) can also be considered as indirect properties of this student. In addition, each professor tuple references a particular department where properties of that department can be considered as indirect properties of that professor.

**Definition 4 (Tuple Ancestors Tree).** A Tuple Ancestors Tree of a tuple \( t \) denoted \( TAT(t) \) is a tree with the root of \( t \) and all paths from \( t \) to \( N(t) \), all paths from each \( i \) in \( N(t) \) to \( N(i) \) and so on until adding a path does not result in a cycle.

Using the concept of indirect properties, we introduce and define the concept of super entity.

**Definition 5.** A Super Entity of a tuple \( t \) from relation \( r \) (i.e., denoted \( SE(t) \)) is a set of specific properties of \( t \) as well as all indirect properties of that \( t \) that are accessible from \( TAT(t) \). Formally, \( SE(t) = P(t) \cup P(TAT(t)) \) where \( P(TAT(t)) \) is the set of all specific properties in \( TAT(t) \).

Intuitively, if \( t \) is a tuple of relation \( r \) with no referring relation, then super entity of \( t \) has the same set of properties as \( t \). A super entity shows complete information of a tuple including all direct and indirect properties regardless of the classification in a schema. Generating super entities can be considered as a declassification process that shows information content of a data source regardless of any structure and only through a set of properties. We argue that such flat structures can be used for data exchange without difficulties in handling the structure of classes in the source.

### 3.1 Entity-preserving Data Exchange

EDEX is performed in four steps: (1) extract all super entities in the source schema; (2) prune redundant entities; (3) select the best host relations for these entities in target; and (4) move the pruned super entities to their proper host tables.

**Step 1 (Super Entity Generation).** The first step towards data exchange in EDEX is extracting all super entities, as they hold complete information regarding source entities independent of classification. In a schema graph, an edge between nodes \( v_1 \) and \( v_2 \) is a foreign key from a column of \( v_1 \) to a primary key of \( v_2 \). Each foreign key of a tuple references at most one tuple of the referenced table (where more than one foreign key references the same table, the tree includes more than one edge with different labels between the nodes).

A super entity regarding a tuple \( t \) is a flat structure that can be defined as a view over all ancestors of \( t \). The Relation Ancestor Tree \( RAT(r) \) is a structure showing how this view can be built regarding tuples of relation \( r \). In order to build \( RAT(r) \), node \( r \) is selected as the root. Then using the schema graph, all outgoing edges from \( r \) and their corresponding nodes \( R \) are connected to \( r \). For each node \( r_i \) in \( R \), their outgoing edges and corresponding nodes are added to \( r_i \) if they do not already exist in \( RAT(r) \). The process continues until there is no edge to add or adding an edge results in a loop in \( RAT(r) \).

Once Relation Ancestor Trees of all relations in a schema are extracted, super entities can be extracted using view statements generated by post-order traversing these trees. In each step, leaves are joined with parent nodes. The output of this traverse is a nested view statement representing how nodes are joined. A Relation Ancestor Tree is traversed in post-order manner such that in each step, a join between a child and its parent is formed. For the four relational ancestor trees shown in Figure 4, the following view statements are generated.

\[
\begin{align*}
\text{Dep}: & \text{Dep} \\
\text{Prof}: & \text{Prof} \bowtie \text{Dep} \\
\text{Student}: & \langle \text{Student} \bowtie \text{Dep} \rangle \bowtie \text{Prof} \\
\text{Registration}: & \text{Registration} \bowtie \langle \text{Student} \bowtie \text{Dep} \rangle \bowtie \text{Prof}
\end{align*}
\]

Applying these view statements on the source instance (shown in Figure 3) results in generating the set of super entities listed in Figure 5. In addition to \( \langle \text{property, value} \rangle \) pairs, the source of each entity is also indicated for each super entity.

**Step 2 (Pruning Redundant Information).**

The set of super entities must be pruned to eliminate repetitive information. To this end, we introduce and
use the concept of distinct super entity. A distinct super entity is a super entity possessing at least one property that does not exist in other super entities of an instance. To extract a list of distinct super entities, a pruner algorithm is proposed to check if all elements of a super entity (the set of property, value pairs specifying that super entity) exist in at least one other super entity.

To avoid brute force search, the pruner algorithm for a given super entity checks only super entities extracted from neighbours of the source relation of that super entity. As a result, given a schema graph, the algorithm searches for inclusion only among super entities tagged as neighbours of the source of that super entity. For example, for super entities extracted from Dep, only instances of Student and Prof are checked (these are the only relations referencing Dep). Accordingly, only super entities extracted from Registration are checked for each super entity extracted from Student. The order of checking super entities for inclusion can be problematic as different checking orders may result in different output. To address this problem, once an inclusion is found, instead of physical deleting, the item is marked as “deleted”. Actual deleting is performed once all inclusion tests are performed.

In our example, the Super Entity Pruner algorithm removes super entities $e_1$ as it is completely included in $e_2$. $e_2$ is removed because of inclusion in $e_3$ and $e_4$. Accordingly, $\{e_5, e_6, e_7\}$ are checked for inclusion in $\{e_8, e_9, e_{10}, e_{11}, e_{12}\}$. In the same way, $\{e_8, e_9, e_{10}\}$ are checked for inclusion in $\{e_6, e_7, e_{11}, e_{12}\}$. Nothing is checked for $e_5, e_6, e_7$ as their source (i.e., Registration) is not referenced by a relation in the schema graph.

**Algorithm 1: Super Entity Pruner.**

**Input:** a list of super entities $suprEnt$ 

a schema graph regarding a source schema $G=(V, E)$

**Output:** a pruned list of super entities

1. foreach super entity $e_i$ in $suprEnt$
2. src = the source of $e_i$
3. refNeighbors = a set of nodes in $G$ referencing src:
4. // there is no node $v_i$ in $f$ such that $v_i$ is referencing src:
5. if (refNeighbors == null)
6. continue;
7. foreach super entity $e_j$ in $suprEnt$
8. src = the source of $e_j$
9. if (refNeighbors contains src)
10. if ($e_i$ is included in $e_j$)
11. mark $e_i$ as “deleted”
12. foreach super entity $e_i$ in $suprEnt$
13. if (remove $e_i$ from $suprEnt$ if $e_i$ is marked as “deleted”)

**Step 3 (Host Relation Selection).** Selecting target host relations requires considering several issues. First, the same concepts may be shown using different representations and as a result, two different properties can represent the same concept in the source and target. To connect source and target, we use property correspondences in form of $p_1, p_2 \rightarrow$ representing correspondence between property $p_1$ in source and property $p_2$ in the target. Each correspondence shows that an attribute of the target is semantically related to an attribute in the source. In our approach, value correspondences are directly used to select best hosts regarding source
entities regardless of schema mapping expression. We consider conditions for selecting best host for source entities: (1) Completeness means the residing hosts must be able to recover properties of source entities in the target as complete as possible; (2) Non-redundancy means no repetitive information is transferred to the target. To satisfy these conditions, we propose a host selection algorithm (Algorithm II). We use the target schema in Figure 6 and the following value correspondences (name ↔ sName, program ↔ prog, dName ↔ dpt, supervisor ↔ supervisor, course ↔ courseName, regDate ↔ date) between this schema and source schema in Figure 2 to explain the host selection algorithm.

![Figure 6: The target schema residing the source instance.](image)

To select the best hosts for source entities, we consider Relation Ancestor Trees in the target as structures that can reside super entities of the source. Then, a RAT correspondence to each relation in the target must be extracted. We need to check which structure can properly reside super entities of source. For the target shown in Figure 6, the RATs constructed for each relation are shown in Figure 7.

![Figure 7: RATs constructed for each relation in Figure 5.](image)

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We assume existence of a unique property name for each property (as each property can be named using the triple (dbName, tableName, propertyName)). We form a hash table from value correspondences where, for each correspondence (p1, p2), the corresponding property of a given property is accessible. The best Relation Ancestor Tree to reside given super entity would be the one that has the maximum number of properties (class-level properties) matching the properties (specific properties) of that super entity. Among those RATs with maximum number of matching properties, a RAT with minimum number of total properties is selected as this RAT holds minimum number of unrelated properties (see Algorithm II).

Algorithm 2: Host RAT selector.

**Input:** A list of source super entities suprEnt

Schema graph regarding the target schema GT=(V_T, E_T)

Hash Table htCorr with target properties as keys and source properties as values

**Output:** The list of super entities marked with host names

1: tgt_RAT_collection ← the set of RATs for each relation in GT
2: tgt_property_collection ← a collection holding a set of properties for each RAT(r)
3: foreach super entity e in suprEnt
4: matchingCount = new HashTable();
5: foreach property p in e
6: foreach RAT r in tgt_RAT_collection
7: if htCorr[p] in tgt_property_collection[r]
8: matchingCnt[r]++; //values are initialized with 0
9: if there is a single maximum value in matchingCnt
10: assign RAT (r) corresponding to this value to e
11: else if more than one r exists with max matchingCnt
12: select RAT (r) with minimum number of properties and assign it to e
13: return suprEnt

When no TRV with any matching property is found, this indicates the target schema is not capable of hosting this super entity. Otherwise, matching at least one property ensures residing that super entity. Given the set of super entities extracted in Step 2, the following host RATs are selected for each super entity as follows:

\[ e_1 \rightarrow ST, e_2 \rightarrow ST, e_3 \rightarrow ST, e_4 \rightarrow Reg, e_5 \rightarrow Reg, e_6 \rightarrow Reg, e_7 \rightarrow Reg, e_8 \rightarrow Reg, e_9 \rightarrow Reg, e_{10} \rightarrow Reg, e_{11} \rightarrow ST, e_{12} \rightarrow ST, e_{13} \rightarrow ST \]

**Step 4 (Entity Residing).** The final step of EDEX is residing super entities extracted from the source in host RATs. Although super entities completely included in other super entities are removed by the pruner algorithm in step 2, there still may exist super entities containing information about the same entity. For example, \( e_1 \) and \( e_2 \) may contain information about the same department. In data exchange, such information should refer to the same entity in the target to avoid entity redundancy. To address this problem, we use target edgs to encode primary key constraints in the target. We use these constraints to avoid inserting the same entities with different identifications by checking primary keys. When a request to insert in target relations is made, the algorithm checks if information about the unique properties already exists. If so, the insertion is aborted. Otherwise the insertion is performed.

One issue that must be considered in residing of super entities is that information regarding each ancestor must be inserted before information of its descendants, as each child has at least one property referring to the primary key of its parent. In particular, the structure of host RAT can provide the
This structure shows the order of inserting properties given properties of a super entity. To generate insertion statements, we start from greatest ancestors. In our example, ex prescribes three insertion statements with the order of ST, Course and Reg. First, two set of properties P1 = (ST, stuName, prog, dpt, supervisor) and P2 = (Course: courseName, credit) are inserted as two nested set of properties. For example, for a super entity e3 (ex3): (stuName, S1), (name, S1), (program, P1), (dept, D1), (dName, D1), (building, B1), (supervisor, Prof1), (pName, Prof1), (degree, deg1), (profDep, D1), (course, C1), (regDate, dt1)) with Reg as a target host, the algorithm first checks if there is a common property between properties of e3 and P1. In this case {stuName, prog, dpt, supervisor} are selected as common properties. Value correspondences are taken into account in finding common properties (e.g., dName in source corresponds to dpt in target). Then, regarding the primary key of the corresponding target relation ST (i.e., stuName), the ST relation is checked to see if information related to this student is already inserted in this table. If not, a tuple covering these properties is inserted and the primary key of this tuple is returned as a reference. If this tuple is already inserted, no insertion is generated and stuName is returned as a reference. In the same way, for the second nested set of properties (Course: courseName, credit), courseName is identified as common property between e3 and ex3. Then, Course table is checked to find if information regarding courseName = C2 is already inserted to Course. Finally, since there is no other nested statement, an insertion statement for Reg is generated.

Applying target egd may result in losing entities of source because inserting a tuple into a table may not be possible due to integrity constraints. For example, since information about students and departments is stored in the same table with stuName as a primary key, existence of a department depends on existence of a student. In our example, e2 cannot be inserted to ST because there is no student who is assigned to this department. This is a trade-off between data consistency and data completeness where a designer may relax some target egds to gain complete data exchange. However, the algorithm we propose prioritises integrity constraints and does not allow breaking any target egd constraint. An important benefit of this feature is ensuring generation of the core solution as the most efficient solution in data exchange, as discussed next.

Algorithm 3: Entity Residing.

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>ex = the nested expression generated from the post-order traversal of RAT(r)</td>
</tr>
<tr>
<td>2</td>
<td>Seq = the order of relations from ex for insertion such that inner parentheses come before outer parenthesis</td>
</tr>
<tr>
<td>3</td>
<td>foreach relation r in Seq</td>
</tr>
<tr>
<td>4</td>
<td>if CP is null then</td>
</tr>
<tr>
<td>5</td>
<td>insert the tuple related to e in r, add the reference to HtReferences, and return this reference</td>
</tr>
<tr>
<td>6</td>
<td>continue</td>
</tr>
<tr>
<td>7</td>
<td>Else If information regarding CP is already inserted in r</td>
</tr>
<tr>
<td>8</td>
<td>return related reference from HtReferences</td>
</tr>
</tbody>
</table>

4 EDEX AND CORE SOLUTION

(Bonifati et al., 2011) define a desirable target instance as a legal instance satisfying correspondences between source and target and integrity constraints in the target. Such an instance contains all source information while no information is reported twice. In the schema mapping based data exchange, a mapping scenario is denoted \( M = (S, T, \Sigma_s, \Sigma_t) \) where \( S \) is a source schema, \( T \) is a target schema, \( \Sigma_s \) is a set of s-t egds (i.e., source-to-target dependencies) and \( \Sigma_t \) is a set of target constraints. If \( I \) is an instance of \( S \) and \( J \) is an instance of \( T \), then \( J \) is called a solution for \( M \) if \( I \) and \( J \) satisfy \( \Sigma_w \) and \( J \) satisfies \( \Sigma_r \). Formally, this is shown in form of \( J \in \text{Sol}(M, I) \) if \( I, J \) satisfies dependencies in \( \Sigma_s \cup \Sigma_t \) (i.e., \( I, J \models (\Sigma_s \cup \Sigma_t) \)). Given \( M = (S, T, \Sigma_s, \Sigma_t) \), multiple solutions may exist given a source instance because each tgd only states an inclusion constraint without indicating the content of a target instance.

In (Fagin et al., 2005) the concept of universal solution is proposed that has with several good properties. To formalize the notion of universal solution, we need to introduce homomorphism.
among two solutions. Let \( \text{Const} \) the set of all constant values that may occur in source instances, and \( \text{Var} \) an infinite set of variables (called labeled nulls) such that \( \text{Var} \cap \text{Const} = \emptyset \). Each element of a tuple \( t = \{a_1, a_2, \ldots, a_n\} \) over a relation from an instance is a member of \( \text{Const} \cup \text{Var} \).

Given \( K_1 \) and \( K_2 \), two instances over a relational schema \( R \) with values in \( \text{Const} \cup \text{Var} \). A homomorphism \( h: K_1 \rightarrow K_2 \) is a mapping from \( \text{Const} \cup \text{Var} (K_1) \) to \( \text{Const} \cup \text{Var} (K_2) \) such that: (1) \( h(c) = c \) for every \( c \in \text{Const} \); (2) for every fact \( R(t) \) of \( K_1 \), we have that \( R(h(t)) \) is a fact of \( K_2 \) where, if \( t = (a_1, \ldots, a_n) \), then \( h(t) = (h(a_1), \ldots, h(a_n)) \).

A universal solution for \( I \) is a solution \( J \) such that for every solution \( J' \) for \( I \), there exists a homomorphism \( h: J \rightarrow J' \). Among universal solutions, the solution with smallest size is called the core solution (Fagin et al., 2005). Because of the minimality and uniqueness of the core solution among universal solutions, this solution is considered as an ideal solution for data exchange.

Formally, a target instance \( J \) among universal solutions is called a core solution if there is no proper subinstance \( J' \subseteq J \) such that there is a homomorphism \( h: J \rightarrow J' \). We claim that EDEX is a schema mapping independent technique that generates the core solution. Theorems 1, 2 and 3 elaborate hypotheses regarding this claim (Proof is available from authors upon request).

**Theorem 1:** Given a set of correspondences \( \Sigma \), EDEX generates a valid target solution.

**Theorem 2:** Given a source instance \( I \), EDEX generates a universal solution in the target.

**Theorem 3:** EDEX generates the core solution.

## 5 RELATED WORK

The prevailing approach in data exchange uses schema mapping to generate the target instance. Alongside studies on practical tools and algorithms for schema mapping generation, there have been theoretical studies on data exchange to provide a solid foundation for data exchange (Fagin et al., 2005). Generated by many schema mapping systems such as Clio (Fagin et al., 2009); (Popa et al., 2002) and HePToX (Bonifati et al., 2005) universal solutions are preferred as they are the most general solution covering the entire space of valid solutions. On the other hand, generating core solutions as a minimal universal solution is considered a natural requirement in data exchange (Gottlob and Nash, 2008); (Fagin et al., 2005). In pre-processing approaches such as ++Spicy (Marnette et al., 2011), schema mapping expressions are rewritten such that refined mappings directly generate the core solution.

To resolve ambiguous mappings, Muse (Alexe et al., 2008) allows a mapping designer to select desired mapping among alternative interpretations of an ambiguous mapping. As an alternative option, (Qian et al., 2012) proposed a sample-driven schema mapping based on the technique that automatically constructs schema mappings from sample target instances provided by users. In Eirene (Alexe et al., 2011) data examples are used to refine schema mappings rather than generating mapping expressions. (Sekhavat and Parsons, 2013) proposed a technique in which schema mapping expressions are enhanced using conceptual models. The main drawback of this approach is the difficulty of designing a global conceptual model.

## 6 CONCLUSIONS

In this paper, we showed that class based mapping expressions are not capable of handling many ambiguous cases in data exchange. We attributed this problem to the assumption of inherent classification in information systems. To address this problem, we proposed an entity preserving approach (EDEX) for data exchange in which the focus is on preserving source entities in the target no matter to what class they belong in the source. We introduced the concept of super entities to capture indirect properties of entities. We showed unlike many schema mapping based data exchange systems, EDEX can resolve ambiguous cases. In addition, EDEX can directly generate the core solution as the most efficient and accurate solution for data exchange. Several interesting issues remain open. Developing mapping language expressing relations between source and target independent of classification is of particular interest.

## REFERENCES

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