GREEDY APPROACH FOR DOCUMENT CLUSTERING

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Abstract: A Greedy Algorithm for Document Clustering (Greedy Clustering) is proposed in this paper. Various cluster validity indices (DB, CH, SD, AS) are used to find the most appropriate optimization function for Greedy Clustering. The clustering algorithms are tested and compared on Reuter-21578. The results show that AS Index shows the best performance and the fastest running time among cluster indices in various experiments. Also Greedy Clustering with AS Index has 15~20% better performance than traditional clustering algorithms (K-means, Group Average).

1 INTRODUCTION

The document clustering is to group the documents which are similar in a set of documents without prior information(Christopher, 2008, Croft, 2009). The researches of document clustering are actively progressing for analysis amount of information in internet.

One of the main issues in document clustering is cluster validity index(Halkidi, 2001). Cluster validity index measure the clustering result is good or not. Document clustering is unsupervised classification technique, thus cluster validity index is very important.

Document clustering is optimization problem about the cluster validity index(Maulik, 2002). In recent years, some optimization algorithms such as the genetic algorithm(Song and Park, 2009) and the particle swarm optimization algorithm(Cui and Potok, 2005) are applied document clustering. These algorithms show good performance but have long running time.

Greedy algorithm is one of the fast optimization algorithms(Richard, 2011). And greedy algorithm sometimes works well for optimization problems. In this paper, we proposed the greedy algorithm for document clustering to make a fast and good performance clustering algorithm.

This paper is organized as follows. The next section introduces some cluster indices. Section 3, presents the principle of proposed algorithm. Section 4, explains experiment setting, results, evaluation approaches and analysis. Section 5, concludes and discusses future work.

2 CLUSTER VALIDITY INDICES

Cluster validity indices are used for measuring a result of clustering(D.L and D.W, 1979). In this section, the four cluster validity indices have been introduced. Table 1 shows the used notation in cluster validity indices.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>$n_c$</td>
<td>number of cluster</td>
</tr>
<tr>
<td>$nc_i$</td>
<td>number of document in $i$th cluster</td>
</tr>
<tr>
<td>$c_i$</td>
<td>$i$th cluster</td>
</tr>
<tr>
<td>$cv_i$</td>
<td>centroid vector of $i$th cluster</td>
</tr>
<tr>
<td>$N$</td>
<td>number of document</td>
</tr>
<tr>
<td>$x_i$</td>
<td>$i$th document</td>
</tr>
<tr>
<td>$d(x_i,x_j)$</td>
<td>similarity between $x_i,x_j$ (cosine similarity)</td>
</tr>
</tbody>
</table>

2.1 Davies - Bouldin (DB) Index

DB Index (D.L and D.W, 1979) based on the similarity of two clusters($R_{ij}$). The $R_{ij}$ calculated by the within cluster scatter and the between cluster separation.

Usually $R_{ij}$ is defined as
\[ R_j = \frac{s_i + s_j}{d_{ij}} \]

\[ d_{ij} = d(cv_i, cv_j), s_i = \sum_{x \in cv_i} d(x, cv_i) \]

where \( s_i \) means scatter within \( i \)th cluster, \( d_{ij} \) means similarity between \( i \)th cluster and \( j \)th cluster.

Then the DB Index is defined as

\[ DB = \frac{1}{n_c} \sum_{i=1}^{n_c} R_j, R_j = \max_{i \neq j} R_{ij}, i = 1, \ldots, n_c \]

The lower value of DB Index means better result of clustering.

### 2.2 Calinski Harabasz (CH) Index

The CH Index(Maulik, 2002) based on the between cluster scatter matrices(\( \text{trace} B \)) and within cluster scatter matrices(\( \text{trace} W \)).

The \( \text{trace} B \) defined as

\[ \text{trace} B = \sum_{k=1}^{n_c} n c_k \| n c_k - z \|^2 \]

where \( z \) means centroid of the entire data set.

The \( \text{trace} W \) defined as

\[ \text{trace} W = \sum_{k=1}^{n_c} \| x_k - n c_k \|^2 \]

The CH Index is defined as follow Equation 3 and Equation 4.

\[ CH = \frac{\text{trace} B (n_c - 1)}{\text{trace} W (N - n_c)} \]

The upper value of CH Index means better result of clustering.

### 2.3 SD Validity Index

The SD Index(Halkidi, 2001) based on the average scattering of clusters and total separation of clusters.

The scattering is calculated by variance of the clusters and variance of the dataset.

The average scattering for clusters is defined as

\[ \text{Scatt} = \frac{1}{n_c} \sum_{i=1}^{n_c} \left( \frac{\sigma(c_i)}{\sigma(X)} \right) \]

where \( \sigma(X) \) means the variance of the dataset, \( \sigma(c_i) \) means the variance of the \( i \)th cluster. So the average scattering calculated by variance of the dataset and variance of the each cluster.

The total separation of cluster is calculated by distance between each cluster.

The total separation of cluster is defined as

\[ \text{Dis} = \frac{D_{\max}}{D_{\min}} \sum_{k=1}^{n_c} \sum_{i=1}^{n_c} \| cv_k - cv_i \|^{-1} \]

where the \( D_{\max} \) means the maximum distance between cluster centroids, the \( D_{\min} \) means the minimum distance between cluster centroids.

Then SD index defined as follow Equation 6 and Equation 7.

\[ SD = \alpha \times \text{Scat} + \text{Dis} \]

where \( \alpha \) is weighting factor that is equal to parameter in case of maximum number of cluster (Csaba, 2006).

### 2.4 Average Similarity (AS) Index

The AS Index(Cutting, 1992) based on the average similarity. Average similarity of AS Index calculate similarity all documents in each cluster.

The AS Index defined as

\[ AS = \frac{1}{n_c} \sum_{i=1}^{n_c} \sum_{j \neq j}^{n_c} d(x_i, x_j) \]

where \( \alpha \) is weighting factor that is equal to parameter in case of maximum number of cluster (Csaba, 2006).

### 3 Greedy Approach for Document Clustering

A greedy algorithm is any algorithm that follows the problem solving heuristic of making the locally optimal choice at each stage with the hope of finding the global optimum(Zhang, 2000).

Document clustering is optimization problem about cluster index. An optimization problem is one in which you want to find, not just a solution, but the best solution. And greedy algorithm sometimes works well for optimization problems.

In this paper, we proposed a greedy algorithm for document clustering. In this paper our proposed algorithm is called Greedy Clustering(GC).

### 3.1 Data Structure

First of all we need to define a data structure for greedy algorithm applied to document clustering. The data structure of GC can express the
information of cluster number all documents belongs to. Figure 1 shows the data structure of GC.

![Data Structure of GC](image)

Figure 1: Data Structure of GC.

As shown the Figure 1, GC has N data. Index of data means a document number and value of data means a cluster number that document belongs to.

### 3.2 Greedy Clustering Operations

GC operations consist of Initialization and Greedy Searching. Figure 2 shows the progress of GC.

![Progress of GC](image)

Figure 2: Progress of GC.

As shown Figure 2, the progress of GC is simple. First initialize data in Initialization operation and then repeat the Greedy Searching operation until the algorithm can’t find better result.

#### 3.2.1 Initialization

In Initialization operation, all documents in data-set are randomly assigned to a cluster.

#### 3.2.2 Greedy Searching

In this operation, just one cluster number of document is changed. Therefore GC selects the cluster number of document that gives the biggest improvement in performance. The performance is measured by cluster validity indices.

In this paper, the GC use various cluster validity indices, so that GC is represented by
- GC(DB) : Greedy Clustering with DB Index
- GC(CH) : Greedy Clustering with CH Index
- GC(SD) : Greedy Clustering with SD Index
- GC(AS) : Greedy Clustering with AS Index

### 4 EXPERIMENT AND RESULT

This paper proposed a greedy approach for document clustering. For estimating its performance, the Reuter-21578 text collection set is used. Two Topic-Sets are experimented and four subjects were allocated to each Topic-Set. Each subject has 50 documents, so that a Topic-Set has 200 documents. Table 2 shows the subjects of Topic-Sets.

<table>
<thead>
<tr>
<th>Subjects</th>
<th>Topic-Set1</th>
<th>Topic-Set2</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>coffee, acq, trade, interest</td>
<td>earn, grain crude, ship</td>
</tr>
</tbody>
</table>

Documents in Topic-Set are represented by VSM. The term weight as follow (Christopher, 2008)

$$w_{ij} = tf_j \times \log \frac{N}{df_j}$$

$w_{ij}$ means $j$th term frequency in $i$th document, $tf_j$ means a document frequency of $j$th term, $N$ means the number of documents in Topic-Set.

To evaluate the clustering performances, F-measure is used. The F-measure defined as (Croft, 2009)

$$F-\text{measure} = \frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$$

Traditional clustering algorithms such as K-means (Shokri, 1984) and Group Average (Cutting, 1992) are compare with the GCs.

Figure 3 shows the performance of traditional clustering algorithms and GCs in Topic-Set1.

![F-measure of Clustering Algorithms(Topic-Set1)](image)

Figure 3: F-measure of Clustering Algorithms(Topic-Set1).

Figure 4 shows the performance of traditional clustering algorithms and GCs in Topic-Set2.
As shown in Figure 3 and Figure 4, AS index and DB index have better performance than traditional clustering algorithms (K-means, group average) in all topic-sets. But CH index and SA index show lower performance than traditional clustering algorithms.

Table 3: Running time of GC with Cluster Index.

<table>
<thead>
<tr>
<th>Cluster Index</th>
<th>time(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GC(DB Index)</td>
<td>2.549</td>
</tr>
<tr>
<td>GC(CH Index)</td>
<td>3.612</td>
</tr>
<tr>
<td>GC(SD Index)</td>
<td>3.892</td>
</tr>
<tr>
<td>GC(AS Index)</td>
<td>15</td>
</tr>
</tbody>
</table>

Table 3 shows a running time of GC with Cluster Index. As shown Table 3, AS Index has faster running time than other cluster indices. Consequently AS Index has the best performance and the fastest running time for Greedy Clustering.

5 CONCLUSIONS

In this paper, we propose the greedy algorithm for document clustering (Greedy Clustering). Main goal of this paper is find optimal function for Greedy Clustering (high performance, fast running time).

So various cluster indices are used to optimal function for Greedy Clustering. As the results of experiments in this paper, the Average Similarity index is the most suitable for the Greedy Clustering among cluster indices (DB, CH, SD, AS). Moreover Greedy Clustering with AS Index has 15~20% better performance than traditional clustering algorithms (K-means, Group Average Clustering).

But Greedy Clustering has weakness that is a long running time due to the complexity of calculation of cluster index compare with traditional clustering algorithms. We will fix this problem through the optimization of Greedy Clustering with AS Index.

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